Timing the initiation of sex: Delay mechanisms alter fitness outcomes in a rotifer population model

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ABSTRACT

Species that inhabit variable environments have complex mechanisms to precisely time their life-history transitions as conditions change. One such mechanism in rotifers is a block on sexual reproduction that extends across multiple asexual generations after emergence from diapause. It has been hypothesized that this delay is advantageous in competitive and stochastic environments. Here, we develop a model of cyclically parthenogenic rotifer populations with a novel formulation of a "mictic block" that prevents sexual reproduction by females that are not sufficiently distant, generationally, from a stem ancestor that was produced sexually. We find that mictic blocks are indeed adaptive but that the most successful phenotypes have shorter blocks than previously reported and that the success of different delay phenotypes is highly dependent on the duration of the growing season. For a fixed environmental regime, coexistence of distinct mixis phenotypes is possible, wherein a phenotype with a longer block performs better in years with an average-length growing season, and a phenotype with a shorter block and lower mixis ratio performs better in years with an "extreme" growing season, whether short or long. Our model provides an eco-evolutionary framework for the study of *Brachionus* rotifers, a model system for non-genetic maternal effects and the evolution of sex.

1. Introduction

For species that live in variable environments, the timing of life history transitions is often subject to strong selection pressure. Mistiming activities such as metamorphosis, reproduction, or emergence from dormancy relative to changes in the environment can significantly reduce fitness. As a result, species living in variable environments have evolved precise, sometimes elaborate, mechanisms to control the timing of life-history transitions. Many species rely on a combination of external cues, such as photoperiod or food availability (Koch et al., 2009; Zhang and Baer, 2000), and internal timing mechanisms, or biological clocks (Simon et al., 2001). Although external cues may provide information about imminent changes in conditions, internal clocks can protect populations from unreliable cues or abrupt fluctuations.

Brachionus rotifers that live in ephemeral ponds are examples of organisms with carefully timed life-history transitions. At the beginning of the growing season, resting eggs in the sediment hatch into asexual

(amictic) females that live in the water column (Fig. 1). After a period of relatively rapid population growth fueled by asexual reproduction, amictic females begin producing mictic female offspring capable of sexual reproduction along with amictic female offspring. In the absence of fertilization by males, mictic females produce eggs that develop into males. Those males fertilize mictic females, who then produce resting eggs—stress-resistant, dormant embryos that can survive when the pond dries or freezes between growing seasons (García-Roger et al., 2019) .

This reproductive strategy, in which several rounds of clonal reproduction are followed by a sexual event, is called *cyclical parthenogenesis*. In animal species, cyclical parthenogenesis commonly occurs in trematode parasites, cladocerans (e.g., *Daphnia* spp.), aphids, cecidomyiids (gall midges) and cynipids (gall wasps), in addition to rotifers (Neiman et al., 2014). The strategy strikes a delicate balance between the contrasting benefits of sexual and asexual reproduction (Bogdan and Gilbert, 1982; Gilbert, 2020). Critical to the success of cyclical parthenogenesis is the *mictic delay*: the time between the start of each growing season and the initiation of mixis, which determines how large

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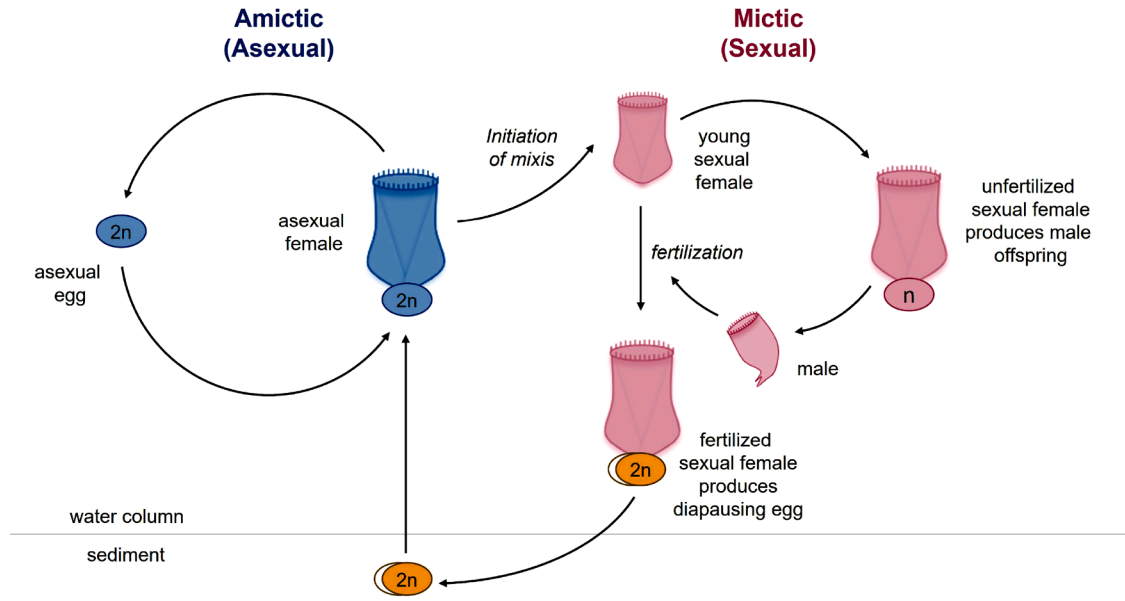 *E-mail address:* bstevens@ucsb.edu (B.L.F. Stevens).

Fig. 1. Life cycle of the rotifer *B. manjavacas*. Left (blue), the asexual (amictic) cycle, in which a female produces clonal diploid eggs by mitosis. Right (pink), the sexual (mictic) cycle, in which crowding conditions prompt a portion of females in the population to become mictic, producing haploid gametes via meiosis. If haploid gametes are not fertilized, they hatch into diminutive haploid males. Fertilized gametes develop into dormant resting eggs, able to desiccate and overwinter in the sediments. Upon hatching, resting egg restore the asexual cycle. Induction of the sexual phase is blocked for asexual females who are not sufficiently removed from their last sexual ancestor. Figure and caption adapted from Gribble (2021). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

the population becomes before sexual reproduction and the production of resting eggs begin.

Empirical work has identified both external and internal timing mechanisms that influence the length of the mictic delay in rotifer populations. Within the genus *Brachionus*, mixis is initiated in response to a density-dependent chemical signal (Carmona et al., 1993; Stelzer and Snell, 2003). In this case, the length of the mictic delay will depend on the time it takes for the rotifer population to exceed a given density, the *mixis threshold density* (Gilbert, 2017). Additionally, Gilbert (2002, 2003) showed that some strains exhibit a secondary, internal delay mechanism. In these populations, individuals do not become receptive to the density-dependent signal until many (8–12) generations after hatching from a resting egg. We refer to this second delay mechanism as a *mictic block*. Internally-timed mictic blocks are hypothesized to be particularly evolutionarily advantageous for late-hatching clones or when a strain is in competition with others that might interfere with its density-dependent chemical signal (Gilbert, 2017, 2020).

Serra et al. (2005) tested this hypothesis with a model of a cyclically parthenogenic rotifer population in a stochastic environment. In their model, females hatch from resting eggs and reproduce asexually until both a mixis threshold density has been met and a minimum number of days have passed since the resting eggs hatched. Serra et al. (2005) used this model to demonstrate that a rotifer phenotype with a mictic block could successfully invade a resident phenotype without such a block, by growing asexually to larger population sizes before transitioning to mixis.

Notably, there is a distinction between a block that lasts a fixed number of days (*temporal block*), as Serra et al. (2005) explored, and a block that lasts a fixed number of generations (*generational block*), as suggested by more recent observations (Colinas, unpublished; section S1; Fig. S2). In the first case, a single individual could become sensitive to the mixis signal over its lifespan, which is inconsistent with current understanding of the rotifer life cycle. Because the timing of the mictic delay is critical to fitness in this system, we must carefully consider how the mictic block is implemented, both biologically and in model formulations.

Here, we investigate how this difference in block implementation alters the fitness and eco-evolutionary dynamics of a cyclically parthenogenic species. We demonstrate that a phenotype with a temporal block produces resting eggs at a higher rate than a phenotype with a comparable generational block (S1). Then, inspired by Serra et al. (2005), we construct a model of a rotifer community with the capacity to delay mixis, in our case for a fixed number of generations. We explore how this new model alters the conclusions of the previous work, and identify fitness-maximizing and evolutionarily stable strategies for timing the onset of mixis.

2. Methods

2.1. A rotifer model with a generational mictic block

Following Serra and King (1999) and Serra et al. (2005), we model the dynamics of a population of rotifers over the course of sequential growing seasons of variable length (Fig. 2). We take the growing season to be the period of time in which a vernal pool provides viable habitat in the water column, after which the pool dries or freezes; only resting eggs survive to the following growing season. We model the changes in the population densities of females at each life stage over the course of each growing season as follows.

We begin with an initial density of resting eggs in the sediment that hatch daily in clutches of equal size at times $t = 0, 1, \ldots, H$ (Serra et al., 2005). Let ϕ_i be the density of eggs of each phenotype i divided by $H + 1$, such that every day in this hatching period, ϕ_i stem juvenile females of phenotype i are introduced into the water column. Assume that individuals die at rate q and that juveniles mature into adults after τ days. The population density of stem juveniles of phenotype i at time t, or $J_{i,0}(t)$, therefore changes as

$$\frac{dJ_{i,0}}{dt} = \sum_{k=0}^{H} \left[\delta(t-k)\phi_i - \delta(t-k-\tau)\phi_i e^{-q\tau} \right] - qJ_{i,0}, \quad (1)$$

where t is time measured in days since the start of the growing season and $\delta(t)$ is the Dirac delta function. The first term within the brackets
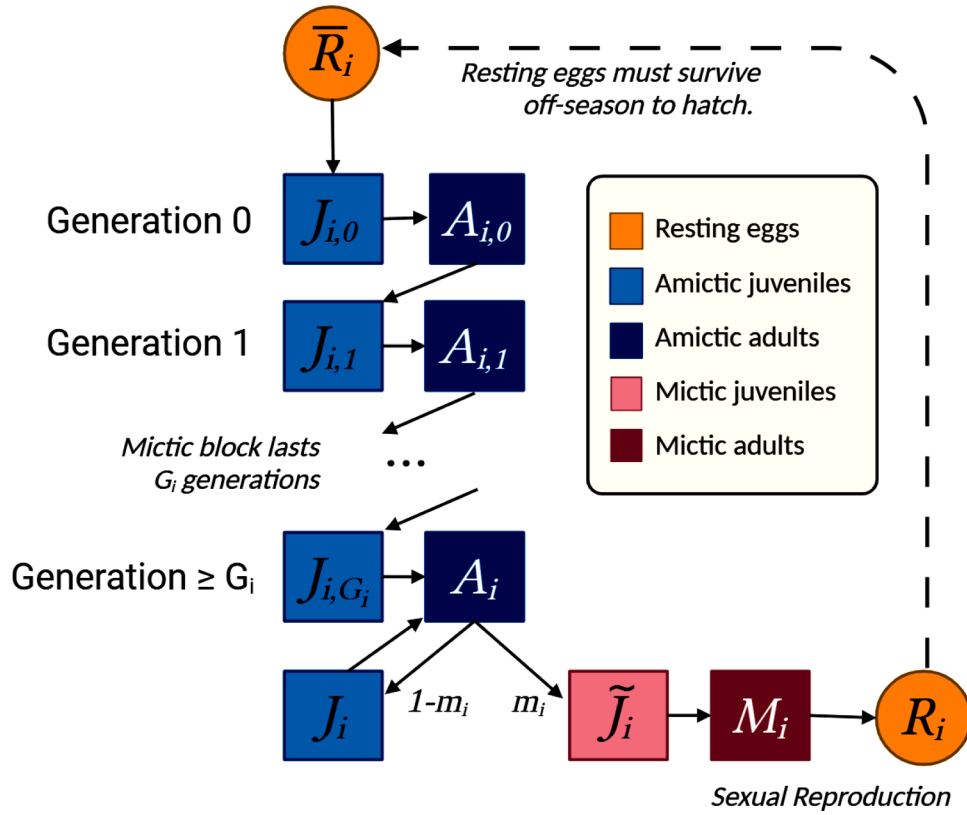
Fig. 2. Schematic of cyclically parthenogenic life cycle model with generational block. Resting eggs can only produce stem juveniles (generation 0). Juveniles become adults of the same generation. Amictic adults can subsequently reproduce asexually to create juveniles in the next generation. G_i is the first generation which might produce mictic offspring if other conditions for mixis are met (Eq. (5)). In this diagram, $G_i > 1$, but it could be any nonnegative integer (Fig. S2). Mictic adults only produce males (not included in the model) or resting eggs that will not hatch until the following season.

describes the introduction of clutches that emerge from diapause, while the second term accounts for the maturation of individuals that survive to adulthood τ days after they emerge. Maturation leads to the production of mature, amictic stem females of phenotype i, which also die at rate q:

$$\frac{dA_{i,0}}{dt} = \sum_{k=0}^{H}\left[\delta(t-k-\tau)\phi_i e^{-q\tau}\right] - qA_{i,0}. \tag{2}$$

Juvenile females of subsequent generations ($j > 0$) are produced by amictic adults. Asexual reproduction in rotifers has been observed to depend on both crowding and resource availability, with individuals ceasing reproduction in order to survive under starvation conditions (Gatto et al., 1992; Kirk, 1997; Snell et al., 2001). We therefore model birth rate as dependent on the total rotifer density while mortality rate remains density-independent. Let $A_{i,j}(t)$ be the population density at time t of mature amictic females, with phenotype i, j generations removed from a stem female (for $j > 0$). These individuals will produce juveniles of generation $j + 1$ at a per capita birth rate, b, which is a function of total population density in the water column, $N(t)$:

$$b(N) = \max\left(b_{\max} - (b_{\max} - q)\left(\frac{N}{K}\right),\ 0\right), \tag{3}$$

where

$$N(t) = \sum_i \left\{ M_i(t) + \sum_j \left[A_{i,j}(t) + J_{i,j}(t)\right] \right\}. \tag{4}$$

Here, $b_{\max}$ is the intrinsic birth rate, K is the community-wide carrying capacity, and $M_i(t)$ is the population density at time t of mature mictic females of phenotype i. In this formulation, the birth rate equals

the death rate when $N(t) = K$, although note that if resting eggs continue to hatch, net population growth may not be zero.

In the model, all offspring inherit the phenotype of their mother. The phenotype of each individual comprises three traits: its mixis ratio, m_i; mixis threshold density, T_i; and the number of generations before mixis can occur, G_i. The mixis ratio is the proportion of female juveniles produced by amictic adults that will mature into mictic adults *when mixis is initiated*. The realized mixis ratio, $\overline{m}_{i,j}$, is a function of the individual's generation (j) the population density at the time of reproduction (not at the time of maturation), and the individual's phenotype (i):

$$\overline{m}_{i,j}(N) = \begin{cases} m_i, & \text{if } N \geq T_i \text{ and } j \geq G_i \\ 0, & \text{otherwise.} \end{cases} \tag{5}$$

While $\overline{m}_{i,j}$ and m_i are strictly proportions ($0 < m_i < 1$), we refer to these terms as mixis ratios, in keeping with the rotifer literature (e.g., Seudre et al., 2020). We explore evolutionary changes in all three dimensions of rotifer phenotype in our model through evolutionary invasion analysis (Section 3.2).

Let the total rate of asexual reproduction by phenotype i amictic adults of generation j at time t be expressed as $\Psi_{i,j}(t) = b(N(t))A_{i,j}(t)$. The dynamics of juvenile, amictic adult, and mictic adult females of all generations greater than 0 are then:

$$\frac{dJ_{i,j}}{dt} = \Psi_{i,j-1}(t) - \Psi_{i,j-1}(t-\tau)e^{-q\tau} - qJ_{i,j} \tag{6}$$

$$\frac{dA_{i,j}}{dt} = \Psi_{i,j-1}(t-\tau)e^{-q\tau}[1 - \overline{m}_{i,j}(N(t-\tau))] - qA_{i,j} \tag{7}$$

$$\frac{dM_i}{dt} = \sum_j \left[\Psi_{i,j-1}(t-\tau)e^{-q\tau}\overline{m}_{i,j}(N(t-\tau))\right] - qM_i. \tag{8}$$

Table 1

Model state variables and parameters. Daggers in descriptions indicate variables that were added to our model relative to Serra et al. (2005). All parameter values were chosen to match those in previous work, except $b_{\max}$ which was increased to exactly adjust for the lost reproduction from individuals that do not survive their maturation step in our model.

Symbol	Description	Value
State variables		
$J_{i,j}$	Juvenile females L^{-1} of phenotype i and generation j	–
$A_{i,j}$	Amictic adult females L^{-1} of phenotype i and generation j	–
M_i	Mictic adult females L^{-1} of phenotype i	–
R_i	Resting eggs L^{-1} of phenotype i	–
Environmental parameters		
S_α	Minimum growing season length (d)	10
S_ω	Maximum growing season length (d)	51
Biological parameters for all rotifers		
q	Intrinsic mortality rate (d^{-1})	0.5
$b_{\max}$	Intrinsic birth rate (d^{-1})	2.1
H	End of period for resting egg hatching (d)	31
τ	†Maturation time (d)	1
c	Cost of sexual reproduction	0.2
K	Water column carrying capacity (individuals L^{-1})	500
$B_{\max}$	Maximum density of resting egg pool (resting eggs L^{-1})	1
Phenotype-specific biological parameters		
m_i	Mixis ratio	0–1
T_i	Mixis threshold density (individuals L^{-1})	0–100
G_i	†First generation that may produce mictic offspring	0–10

The three terms in Eq. (6) account for births, maturation of juveniles that survive their juvenile period, and mortality. The first terms in Eqs. (7) and (8) represent the maturation of juveniles into amictic and mictic adults, respectively. We do not distinguish between generations of mictic adults, so the production of mictic adults by all generations is summed.

Finally, we simulate the number of resting eggs produced by mictic females over the course of each growing season. Let $R_i(t)$ be the population density of the resting eggs produced during the current growing season by phenotype i at time t. Resting eggs are produced at a reduced rate relative to the rate that amictic females produce juveniles. The rate is reduced by a factor, $0 < c < 1$, reflecting the costs of sexual reproduction, including the production of males and increased resource allocation to resting eggs. Resting egg production is therefore described by

$$\frac{\mathrm{d}R_i}{\mathrm{d}t} = c\,b(N(t))M_i. \tag{9}$$

As in Serra et al. (2005), we take the length of each season, S, to be a uniformly distributed random variable between S_α and S_ω. Thus, $R_i(S)$ is the density of eggs of phenotype i that had been produced by the end of a season. There is a maximum density, $B_{\max}$, of resting eggs across all phenotypes that can survive to hatch in the next growing season. Let $\overline{R}_i$ denote the density of eggs of phenotype i that survive to the next season. The between-season dynamics are then defined by

$$\overline{R}_i = \begin{cases} B_{\max}\frac{R_i(S)}{\sum_i R_i(S)}, & \text{if } \sum_i R_i(S) \geq B_{\max} \\ R_i(S), & \text{otherwise.} \end{cases} \tag{10}$$

All state variables except $\overline{R}_i$ reset to 0 between seasons (since no individuals in the water column survive past the growing season's end and no new eggs are laid until the next season begins). The first hatching in the new season will produce $\phi_i = \frac{\overline{R}_i}{H+1}$ individuals at time $t = 0$.

In our simulations, we calculate the realized fitness of phenotype i within each season as the ratio of eggs produced to the number of eggs that initialized the population:

$$W_i = \frac{R_i(S)}{\overline{R}_i(0)}. \tag{11}$$

Because the season length S varies randomly, so do the ratios W_i across seasons. We also consider the expected number of resting eggs laid per season, which is the average value of $R_i(S)$ across all the seasons within a simulation.

A complete list of parameters and default values is included in Table 1. Serra et al. (2005) provide empirical justification for the values of each biological parameter except $B_{\max}$ and H. We therefore investigate sensitivity of fitness to these two parameters and to season length.

3. Analysis

3.1. Monomorphic populations

We begin our analysis by exploring the dynamics of populations with a single shared phenotype. For these populations, our model produces qualitatively similar dynamics to those of Serra et al. (2005) (Fig. 3A). Population growth starts slowly as resting eggs gradually hatch to produce stem juveniles and subsequently stem adults. The most rapid growth is achieved while these adults reproduce entirely asexually. Once their phenotype's mixis threshold density, T_i, is reached, all amictic adults that are of generation G_i or greater will begin producing some mictic adults which create resting eggs. The net growth of amictic individuals in the water column declines and the density of resting eggs increases.

In general, our simulated populations produce resting eggs more slowly than those presented in Serra et al. (2005). As demonstrated in section S1, the generational mictic block, compared to a temporal mictic block, results in a lower rate of resting egg production at the onset of mixis. This exacerbates the risks and reduces the benefits of waiting to initiate mixis. We therefore expect the optimal threshold and block traits to be lower in our analysis compared to those reported in the previous work.

To test this hypothesis, we analyzed our model for the same environmental regime as explored in Serra et al. (2005). That is, we ran
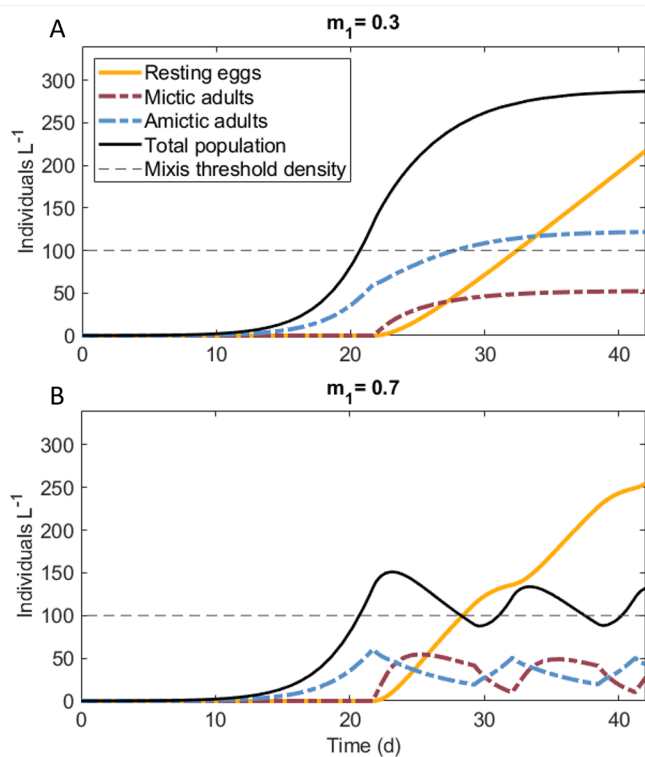
Fig. 3. Dynamics within a single season for populations with no generational mictic block ($G_i = 0$). Parameter values for these simulations are those indicated in Table 1, with initial resting egg density equal to B_{max}, mixis ratio (m_1) phenotypes indicated in the title to each panel, and mixis threshold density indicated by the horizontal dashed line ($T_1 = 100$). When the mixis ratio is high enough to lead to population decline (B), the total population can oscillate around the mixis threshold. See Fig. S4 for a close-up of hatching and maturation dynamics.

simulations for 40 consecutive seasons wherein each season length was randomly chosen from a uniform distribution between 10 and 51 days and assessed differences in average fitness between phenotypes (Fig. 4). Patterns in fitness across phenotypes appear to be insensitive to the values of H and B_{max} (Figs. S7 and S8). In the absence of a generational block, we find that the fitness-maximizing phenotype is a mixis ratio of 25 % and a threshold value of 0.4 rotifers L^{-1} (for $0 < m_i < 1$, $T_i < 100$ L^{-1}; Fig. S5). This contrasts with the values of 45 % and 82 rotifers L^{-1} reported in Serra et al. (2005). Looking at individual seasons (Fig. 5), we see that long seasons produce fitness patterns similar to those presented in Serra et al. (2005). When seasons are short, however, phenotypes with high threshold densities fail to produce any resting eggs, which leads to zero fitness. Because of the lower rates of resting egg production in our model, selection pressure favors much lower threshold densities than previously reported for the same environmental regime.

Phenotypes with low threshold densities have the highest fitness when paired with lower mixis ratios (Figs. 4A, 5C). A phenotype with a low threshold and low mixis ratio will have an early onset of mixis and low rates of sexual reproduction throughout the season. Compared to phenotypes with high mixis threshold densities, one with a low threshold density will have greater fitness in short seasons and lower fitness in long seasons. Without a generational block, surviving short seasons comes at the cost of reduced fitness in long seasons.

Generational blocks evidently reduce the trade-off between survival in short seasons and high fecundity in long seasons (Fig. 5). Compared to mixis threshold densities, which apply to all cohorts equally, generational blocks are more forgiving in very short seasons. The first cohort of eggs to hatch will lead to individuals of generation G_i after $\tau * G_i$ days, such that some resting eggs may be produced at that time, even if the cohort is small. At the other end of the spectrum, gener-

ational blocks are also successful at producing large numbers of resting eggs in long seasons. Phenotypes with generational blocks and low mixis threshold densities generate roughly the same number of resting eggs as those with higher mixis threshold densities (Fig. 5E, F). We expect this insensitivity to total population density to be particularly advantageous in a competitive context when the abundance of a competing phenotype would interfere with the density-dependent timing cue.

3.2. Evolutionary invasion approach

We now consider competition between distinct rotifer phenotypes to ask whether a generational mictic block can be evolutionarily advantageous. To answer this question, we employ adaptive dynamics, also called evolutionary invasion analysis (Geritz et al., 1998). This approach explores the scenario in which a small mutation arises among a subset of individuals within a resident population at its asymptotic attractor (e.g., an equilibrium point or limit cycle). The mutant phenotype, or invader, will either increase in frequency in the population or will fail to invade, ultimately going extinct. In a deterministic model, these outcomes reflect high and low invasion fitness, respectively, and, in some simple cases, an analytical expression for invasion fitness can be written explicitly. Due to the high-dimensional stage structure, nonlinearities, and stochasticity in our model, we cannot attain an analytical expression for invasion fitness. Instead, we use a numerical estimate of invasion fitness. Note however, that stochasticity can lead to extinction even when a phenotype's invasion fitness is high. We therefore also conduct numerical invasion experiments in which the complete dynamics of two interacting phenotypes are simulated as in Serra et al. (2005).

We estimate invasion fitness by computing the relative fitness of an invader within a monomorphic resident population. More specifically, we simulate the dynamics of a resident population for a sequence of 1000 seasons, such that the number of eggs produced approaches a stable distribution. We calculate its fitness within each season according to Eq. (11) and consider the geometric mean across all seasons. We then simulate the addition of an invader at low frequencies at the start of each season. The invader frequency is assumed to be so low that it has no impact on the resident dynamics or the total rotifer density. We again compute fitness according to Eq. (11). The relative invasion fitness estimate is taken to be the ratio of the mean fitness of the invader to that of the resident.

To confirm that this estimate of relative invasion fitness corresponds to differences in realized invasion outcomes, we conduct simulated competitive invasion experiments. For each replicate of these experiments, we introduce an invader phenotype into a monomorphic resident population and simulate the competitive dynamics for 40 growing seasons. We initialize the population with B_{max} resting eggs and an invader frequency of 0.05, and, as in Serra et al. (2005), consider an invasion successful if the invader frequency increases on average over 20 experiments. We conduct invasion experiments across a range of values for both the resident and invader phenotypes, generating pairwise invasibility plots which indicate the long term evolutionary behavior of the model.

One of the pillars of adaptive dynamics is that mutations are assumed to be rare, such that the population reaches its equilibrium between each new mutation. By this logic, we initially assume that invaders differ from the residents in only one of the three dimensions of their phenotypes (G_i, T_i, and m_i) at a time. As in Serra et al. (2005), we first find a stable mixis strategy in the absence of a mictic block ($G_i = 0$), then allow the length of the mictic block to evolve. Next, we extend our analysis beyond that that of Serra et al. (2005) by considering competition between phenotypes with differences in any of the three distinct mixis traits (G_i, T_i, and m_i). We simulate a series of mutations by conducting invasion experiments in each of the dimensions of the phenotype, where the trait values of the resident are updated before each subsequent in-
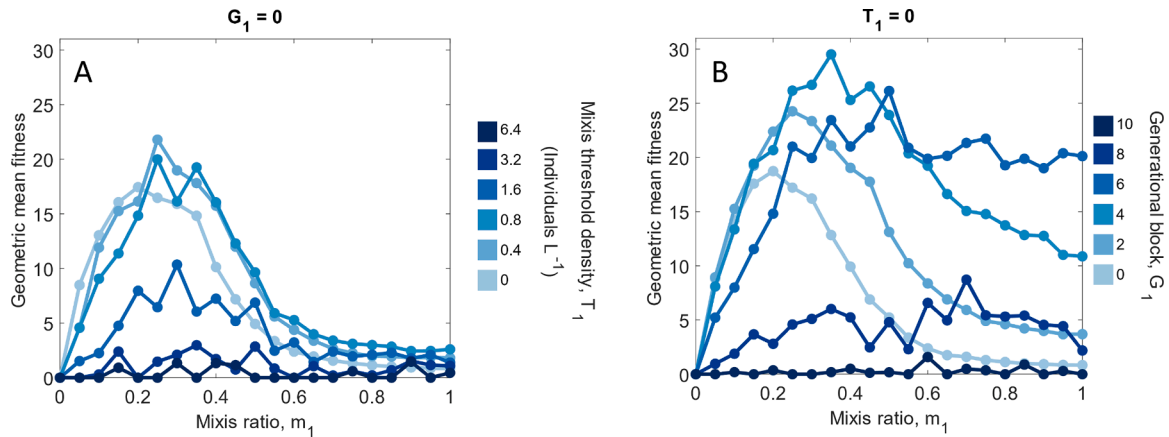
Fig. 4. Fitness of monomorphic populations of phenotypes without a generational mictic block (A) and without a mixis threshold density (B). Values plotted are the averages across 40 replicates. Generational mictic blocks of up to 6 generations generally increase fitness. In the absence of a mictic block, phenotypes with low mixis ratios and low mixis threshold densities have highest fitness. All parameters not indicated within the figure have values shown in Table 1. A close-up of panel (A) at a higher resolution is provided as Fig. S5, and a version of this figure with expected egg production per season is included as Fig. S6.

vasion. In this way, we arrive at a phenotype that cannot be invaded and replaced by any single trait mutation. Finally, we conduct pairwise invasion experiments between phenotypes that may differ in both m_i and G_i to further explore the stability of the system and the potential for polymorphism.

3.3. Results of evolutionary invasion analysis

We find that a mixis ratio of 0.11 is evolutionarily stable among phenotypes without a mictic block or mixis threshold density ($0 < m_i < 1$ at a resolution of 0.01; Fig. 6A). That is, this phenotype can successfully
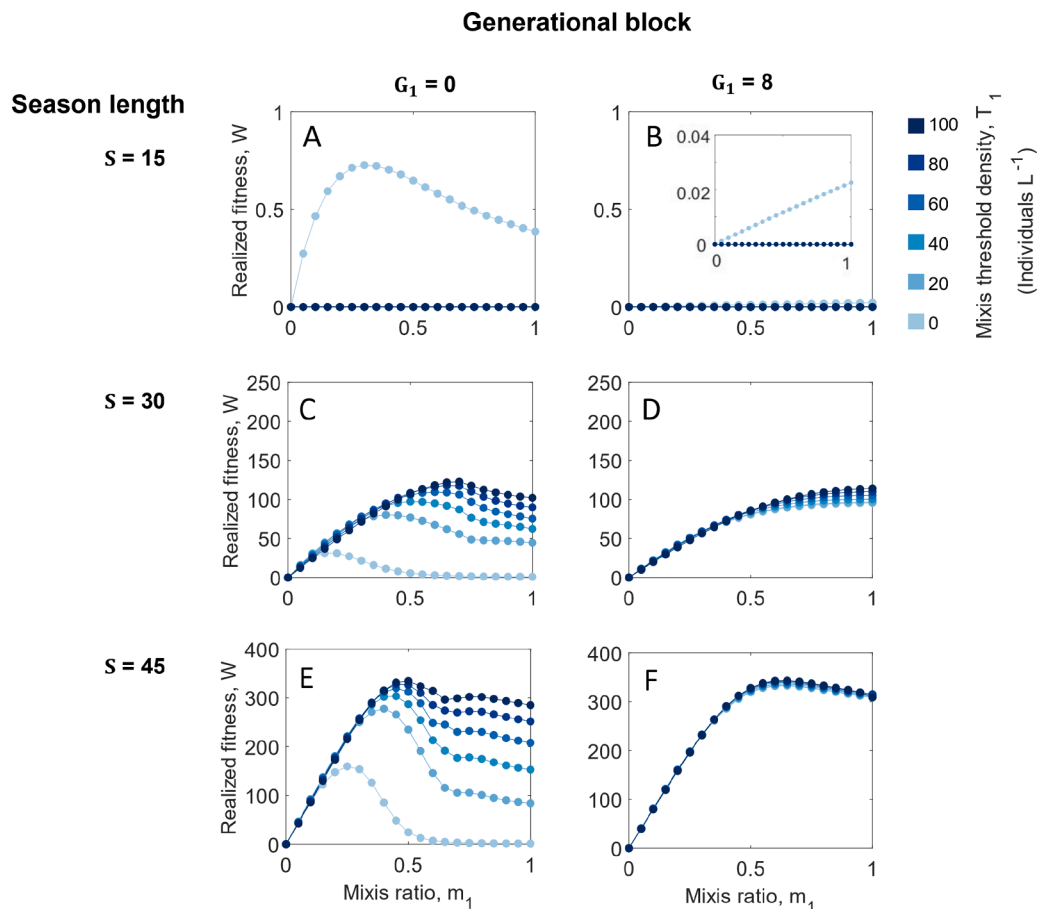
Generational block

Fig. 5. Realized fitness (resting eggs produced per egg hatched) of monomorphic populations within short (A, B), medium (C, D) and long (E, F) seasons of fixed length. Phenotypes with low mixis threshold densities have higher fitness in short seasons, and those with high threshold densities have higher fitness in long seasons. A long generational block (right column) does poorly in short seasons but can increase the fitness of phenotypes with low threshold densities in long seasons. Resting egg production in (B) is low but nonzero ($\sim 0.01 \ L^{-1}$) for phenotypes with $T_i = 0$. Note that the vertical scale changes between rows. Simulations were run with parameter values indicated in Table 1 and initial resting egg density, B_{max}.
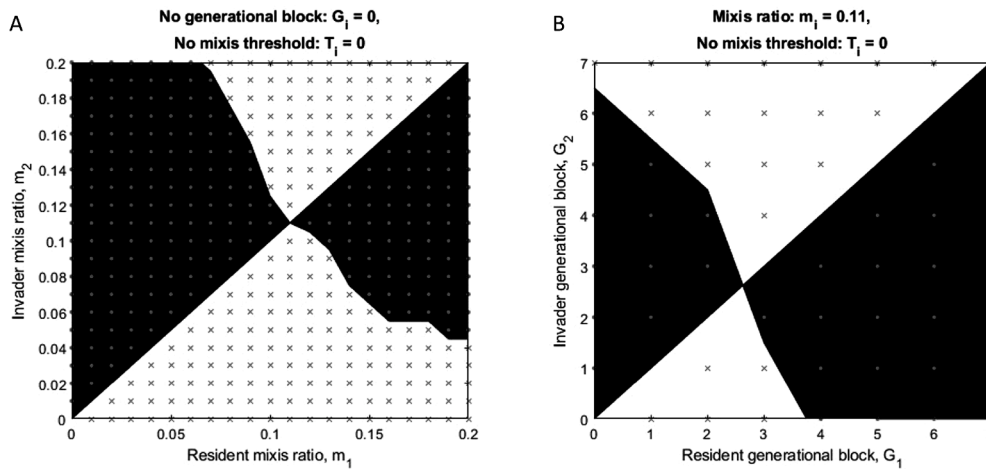
Fig. 6. Pairwise invasibility plot for rotifers with A) variable mixis ratio given no generational block or mixis threshold density ($G_i = 0$, $T_i = 0$). Invasion was deemed successful if, out of 20 simulations of 40 growing seasons each, the invader frequency increased on average from its initial frequency of 0.05. Gray crosses indicate unsuccessful invasions; circles indicate successful invasions. Black and white regions are interpolated regions of success and failure, respectively. Without a mixis block, a mixis ratio of 0.11 is the best invader and most resistant to invasion. B) Pairwise invasibility plot for rotifers with variable generational blocks given a mixis ratio of 0.11 and no mixis threshold density. Phenotypes with $G_i = 3$ are most resistant to invasion and can successfully invade all others. All parameters not indicated within the figure have values shown in Table 1.
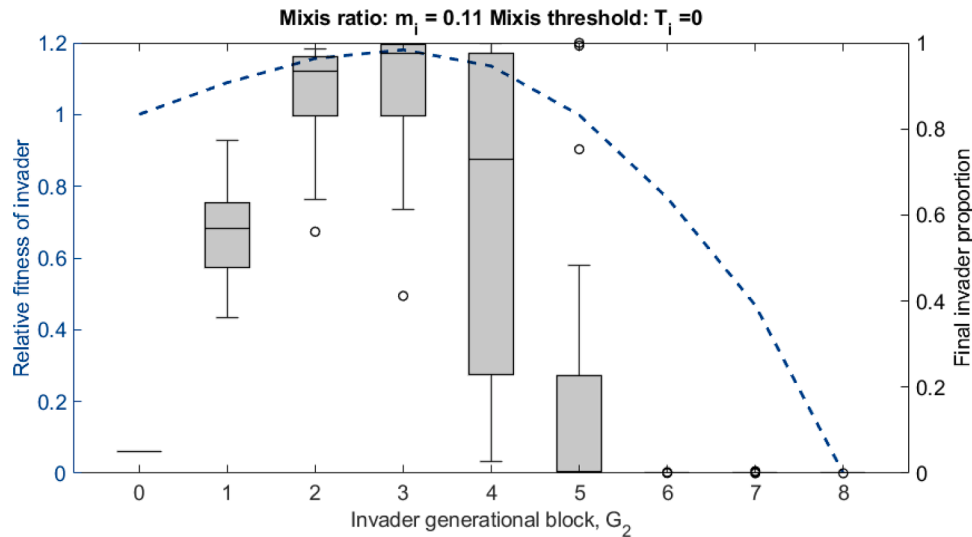

Fig. 7. Relative fitness and invasion success of phenotypes with generational mictic blocks. Invaders were introduced into a resident population with the most competitive mixis ratio and threshold phenotype in the absence of a mictic block ($m_i = 0.11$, $T_i = 0$). Strains with this mixis strategy and generational blocks of 3 generations have the highest relative fitness and can regularly invade and replace a resident without a block. Each box indicates the median and interquartile range (IQR) of 20 simulations of 40 seasons each per phenotype. Circles indicate values more than $1.5 * \text{IQR}$ away from the nearest box edge. All other parameters for these simulations are those indicated in Table 1.

invade and resist invasion by a strain with any other mixis ratio. Note that this value is less than the mixis ratio value that maximizes fitness or resting egg production in the absence of competition (Figs. 4, S6). This result is qualitatively comparable to that reported in Serra et al. (2005), in that the optimal mixis ratio is lower in competition than in isolation.

In general, we find that residents are susceptible to invasion by phenotypes with lower mixis threshold densities. Among phenotypes without a mictic block and with a mixis ratio of 0.11, phenotypes without a mixis threshold density can successfully invade strains with any other value of T_i (Fig. S9A). Competitive outcomes of phenotypes that differ in T_i, however, are sensitive to stochasticity in season length, creating noise in our pairwise invasibility plots. Nonetheless, phenotypes without mixis thresholds were successful invaders across all the phenotypes we tested.

We next ask whether a rotifer phenotype that delays mixis through a generational block can invade the strategy that would be evolutionarily stable in the absence of a block. That is, we allow G_i to mutate in a resident population with no block, a mixis threshold density of 0, and a mixis ratio of 0.11. We find that phenotypes with blocks that last 2 or 3 generations have high invasion fitness and can regularly invade and replace phenotypes without a block (Fig. 7). Phenotypes with blocks of 4 generations also have relatively high fitness, but their actual invasion success is much more sensitive to the stochasticity in season length. Blocks longer than 5 generations are mostly unsuccessful (Fig. 7).

Our results contrast quantitatively with the findings of Serra et al. (2005), which identified the optimal invader block timing as 8–12 days, substantially longer than the three days it would take to produce adults of generation 2. The difference is in line with our expectations described in section S1. The temporal block of Serra et al. (2005) results in a higher

per capita rate of egg production after the block is lifted, artificially favoring a longer delay and a higher mixis ratio. In contrast, our generational block implementation favors a shorter mictic delay to make up for the slower production of resting eggs. Even with the more realistic generational block model formulation, we find that a block phenotype is adaptive, validating the conclusions of Serra et al. (2005). We note that the invasion outcomes for any specific block length depends critically on the environmental regime and the relative chances of experiencing a short or a long season.

We now extend our invasion experiments to explore mutations in any of the three mixis traits. Starting with the phenotype that had the highest fitness in the absence of a generational block ($G_i = 0$, $T_i = 0.4$, $m_i = 0.25$), we conduct a series of pairwise invasibility experiments, each of which simulates evolution along a single phenotype dimension at a time. We update the default phenotype of the resident to reflect the strategy that is evolutionarily stable along that single dimension before conducting a new pairwise invasibility experiment along a different trait axis (Fig. S10). After eight iterations, we find that the simulated population has reached a phenotype ($m_i = 0.17$, $T_i = 0$, and $G_i = 3$) that cannot be replaced by phenotypes with mutations in any single trait.

Lastly, we conduct a collection of invasion experiments in which residents and invaders vary in both their values of G_i and m_i (Fig. S12). We find that for all phenotypes within the range of $0 \leq G_i \leq 5$ and $0.05 \leq m_i \leq 0.25$, two combinations of traits produce phenotypes that maximize both their invasion success and their resistance to invasion. The first is that which we identified by varying each trait in isolation: $G_i = 3$, $m_i = 0.17$. The second has a longer delay and a higher mixis ratio, $G_i = 4$, $m_i = 0.20$. When strains with phenotypes in each of these regions compete, each is able to invade the other when introduced at low abundances, indicating the potential for coexistence. The phenotype with the shorter mictic block and lower mixis ratio does well both in short seasons, due to its early transition to sexual reproduction, and in long seasons, due to its sustained high population densities. In contrast, a phenotype with a longer mictic block and higher mixis ratio can out-compete the first phenotype in seasons of roughly average length (Fig. S13). Competitive outcomes, in this case, depend on the duration of each growing season. Given the fixed environmental parameters on which we have focused in this work, we find these phenotypes can coexist across many seasons. Note, however, that a single population will not evolve divergently into these two strategies under the assumptions of rare and small mutations.

4. Discussion

Cyclic parthenogenesis occurs in at least seven groups of animals, including the best studied cases of rotifers, cladocerans, and aphids (Hebert, 1987). In these systems, there is strong selection pressure on the timing of sex, such that the onset of sex has evolved to be influenced by both internal and external cues (Koch et al., 2009; Simon et al., 2002; Zhang and Baer, 2000). Here, we have developed a model of the generational block observed in rotifers that delays the onset of mixis. This model allows us to investigate the fitness outcomes of rotifer phenotypes with distinct combinations of internal and external timing mechanisms, addressing questions about when different reproductive strategies are most advantageous.

We found that a phenotype with a generational mictic block can successfully invade a resident population that would be evolutionarily stable in the absence of a block (Fig. 6). This result supports the widespread hypothesis that generational blocks are adaptive and confirms the conclusions of Serra et al. (2005), despite the difference in the formulation of the mictic block between our model and theirs (highlighted in Section S1). Generational blocks increase the cumulative number of resting eggs produced in long seasons while still allowing for a minimal number of eggs in short seasons.

We found the optimal length of the mictic block in generations to be shorter than that reported in Serra et al. (2005), but we note that the success of phenotypes with generational blocks depends sensitively

on the distribution of season lengths. Long generational blocks offer a larger benefit in longer growing seasons and have a fitness cost when seasons are short. This is consistent with patterns in block phenotypes observed in natural populations, although there is variability among species (Schröder and Gilbert, 2004). Generational blocks are not evident in populations in the Chihuahuan desert, for example, where vernal ponds only last a few days (Schröder et al., 2007). Across eastern Spain, Colinas et al. (2023) found that ponds with longer hydroperiods are home to rotifer strains with longer generational blocks. Those authors and others have attributed the success of block phenotypes to the increased growth of late-hatching clones, though our model indicates that early-hatching clones also benefit from a mictic block in long seasons (Fig. S14). Phenotypes with high mixis ratios and a long mictic delay produce more eggs due to the prolonged period of asexual population growth.

Rotifer populations can exhibit a prolonged mictic delay as a result of either a high mixis threshold density or a generational block. In our model, the fitness of a phenotype with a long generational block is relatively insensitive to its mixis threshold density (Fig. 5), suggesting that either one of the two delay mechanisms is sufficient for high egg production in long seasons. Compared to phenotypes with high mixis threshold densities, those with generational blocks are stronger competitors and produce more resting eggs across a range of season lengths. Given these advantages, we expect generational blocks to be a more prevalent mechanism for timing the initiation of sex, yet empirical work has reported a wide range of mixis threshold densities (2.3 females L^{-1} King and Snell (1980); 6.6–22.9 individuals L^{-1} Carmona et al. (1995); 147 individuals L^{-1} Snell and Boyer (1988)). The prevalence of these mixis threshold densities suggests that they have benefits in addition to the associated delays in the initiation of sex.

Possible benefits of high threshold densities include an increased likelihood of sexual reproduction once high population densities have been reached. In this way, a high threshold density would be a strategy to avoid a mate-finding Allee effect, which is not typically seen in rotifers but has been shown to be relevant for other cyclically parthenogenic species (Drake, 2004). Alternatively, high densities may anticipate impending resource limitation (Gilbert, 1967). The transition to sexual reproduction would then occur before individuals are likely to experience starvation. While our model does not include any benefits of mixis threshold densities other than the resulting mictic delay, these benefits could be incorporated in models for future work.

Our results also contrast with observations from Seudre et al. (2020), who found that naturally occurring genotypes with the lowest mixis threshold densities also had the highest mixis ratios. This trend is the opposite of what we see in the model (Fig. 5C), reinforcing the hypothesis that high mixis threshold densities are not only a strategy for timing the onset of sex. Rather, they may reflect a difference in the overall investment of a phenotype in sexual versus asexual reproduction.

Because demographic and environmental parameters vary between specific rotifer strains and habitats, we consider the results of our analysis to be qualitative rather than quantitative. Additionally, we acknowledge that there are a number of simplifying assumptions in our model formulation. There may be demographic effects of population density other than negative density-dependent birth rate that we have overlooked. Maturation time, for example, may depend on resource availability, and under some conditions, rotifer survival has been reported to increase under crowding conditions, likely due to a tradeoff with reproduction (Gatto et al., 1992). More pertinent to our research questions, the density dependent mortality of resting eggs between seasons in our model is quite rigid. In real systems, there is unlikely to be a fixed maximum number of eggs that can survive, and resting eggs may be able to survive multiple off-seasons. Survival depends upon the length of the off-season, pond conditions, and predator dynamics, all excluded from our simulations (García-Roger et al., 2006; Jr et al., 1995).

That said, our model produces realistic within-season trajectories of both population size and the proportions of mictic females expected in

the population. We note that for certain parameter values, our model exhibits oscillatory dynamics that were not evident in previous model formulations (Fig. 3B). When birth rates are low and the mixis ratio is high, the initiation of mixis will lead to population decline. If the population then drops below the mixis threshold density, it will oscillate around T_i, toggling between producing mictic offspring and not. Evidence for such an oscillation has been reported in at least one natural population. While monitoring individual strains over time, Carmona et al. (1995) saw that the proportion of mictic females decreased during the growing season after an initial increase, leading to population growth and a second peak in population density in the latter half of the season. Our model indicates that this dynamic could be the result of the time lag between the conditions experienced by a female, which determine the mixis ratio of her offspring, and the contribution of those offspring to population growth once they mature. This is a non-genetic maternal effect, a phenomenon for which rotifers have become an important study system (Liguori et al., 2024; Seudre et al., 2020). Because our model tracks overlapping generations in the rotifer population, we expect it to be a valuable tool for future work on multigenerational maternal effects in this system.

Finally, we have used our model to confirm the conjecture of Serra et al. (2005) that a polymorphism is possible within the environmental regime considered in their work. We find that there exist distinct mixis phenotypes that may evolve allopatrically and that can mutually invade each other. Long-term coexistence would depend upon the distribution of growing season durations from year to year. In real systems, multiple strains of rotifers can exhibit different temporal mixis patterns within the same habitats, including some that are more continuous and others that are more periodic (Carmona et al., 1995). Our simulations suggest that a change in the distribution of season lengths, as would result from changes in rainfall or evaporation, would lead to changes in the relative fitness of these two strategies. We note that while environmental stochasticity (in the form of random growing season lengths) is critical for the coexistence of distinct phenotypes in the model we analyzed, life-history polymorphisms can also arise in constant environments (Landi et al., 2018).

We have argued in this manuscript for the careful consideration of the mechanisms by which life history transitions are timed. For cyclically parthenogenic rotifers, the success of a mictic delay strategy depends not only on the length of the delay, but also on how it is determined in a population. We and Serra et al. (2005) have explored two implementations, but some species may exhibit a mixture of timing mechanisms, including generational blocks as well as effects of birth order or time within the season. We have shown that a generational mictic block can be a robust and effective strategy for timing sexual reproduction in variable environments.

CRediT authorship contribution statement

Bethany L.F. Stevens: Writing – review & editing, Writing – original draft, Visualization, Software, Methodology, Investigation, Funding acquisition, Formal analysis, Conceptualization; **Silke F. van Daalen:** Writing – review & editing, Supervision, Software, Methodology, Investigation, Conceptualization; **Tirzah J. Blomquist:** Writing – review & editing, Methodology, Investigation, Conceptualization; **Kristin E. Gribble:** Writing – review & editing, Supervision, Methodology, Funding acquisition, Conceptualization; **Michael G. Neubert:** Writing – review & editing, Supervision, Software, Methodology, Investigation, Formal analysis, Conceptualization.

Data availability

The code used to carry out this research is publicly available in a GitHub repository and archived in Zenodo, https://doi.org/10.5281/zenodo.17993443.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Supplementary material

Supplementary material associated with this article can be found in the online version at 10.1016/j.jtbi.2025.112333.

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