ELSEVIER

Contents lists available at ScienceDirect

## **Aquacultural Engineering**

journal homepage: www.elsevier.com/locate/aque



# Towards understanding the dynamic behaviour of bioflocs in a fish tank culture: Integration of fish growth and activated sludge modelling

Nurhayati Br Tarigan <sup>a,b,\*</sup>, Marc Verdegem <sup>b</sup>, Julie Ekasari <sup>c</sup>, Karel J. Keesman <sup>a,\*\*</sup>

- <sup>a</sup> Mathematical and Statistical Methods Biometris, Wageningen University and Research, Wageningen 6700AA, the Netherlands
- <sup>b</sup> Aquaculture and Fisheries, Animal Sciences Group, Wageningen University and Research, Wageningen 6700 AH, the Netherlands
- <sup>c</sup> Department of Aquaculture, Faculty of Fisheries and Marine Sciences, IPB University, Dramaga, Bogor, West Java 16128, Indonesia

## ARTICLE INFO

# Keywords: Activated sludge model Non-starch-polysaccharide Nile tilapia Biofloc Nitrogen Mathematical model

#### ABSTRACTS

Biofloc can improve the nutrient use efficiency of an aquaculture system. However, knowledge of the dynamic behaviour of biofloc related to the nutrient concentration in the water is limited. This study combined the fish growth model with the activated sludge model (ASM), later called fish-ASM, to understand the dynamic behaviour of biofloc in Nile tilapia culture. Fish were fed two types of diets that differ in fiber content. One of the diet contains three times higher fiber, which was formulated by incorporating more non-starch-polysaccharides (NSP). NSP is expected to increase carbon content in the water and promote more biofloc growth. Initial model parameter values were gained from experiments and ASM number 1. In fish-ASM, waste comes from uneaten feed, fish faeces, decay of heterotrophic and autotrophic biomass, and fish gill excretion (ammonia). Heterotrophic and autotrophic biomass then utilize the waste as substrates for their growth and part of the biomass is consumed by fish as natural food. The main model outputs in this study are hourly dynamics of fish, biofloc, and nitrogen in water. After trial and error calibration process, the model was fit to the fish, biofloc, and nitrogen dynamics of the lower fiber diet datasets with relative mean square error of 3 %-34 % to the corresponding average observations. However, future improvement was needed in the higher fiber diet simulation, especially related to biofloc and ammonia dynamics. The study shows that the development of biofloc was strongly influenced by organic matter availability.

## 1. Introduction

Inland aquaculture has been playing a crucial role in supplying animal protein, providing in 2022 74 % of the global production compared to 26 % produced in the marine environment (FAO, 2024). To minimize water and land use, aquaculture tends to intensify the system by increasing the stocking density which leads to a higher feed input per unit of aquaculture space (Verdegem et al., 2023). Although this strategy aims to increase fish production, it also increases waste production. Waste accumulation can eventually hamper fish growth and welfare due to poor water quality. Discharging the water without treatment will cause eutrophication of natural water bodies (Boyd et al., 2007). Hence, for sustainable development of aquaculture post or in-process treatment of the water is needed.

Biofloc technology (BFT) is a concept in aquaculture that utilizes microbiota to maintain water quality which enables a high-density culture with minimum water exchange. The main principle of BFT is to recycle nutrient waste into microbial biomass which can be later used as natural food for the culture animals (Avnimelech, 2009). Biofloc formation is mainly done by heterotrophic bacteria, and supported by algae and autotrophic bacteria (Ebeling et al., 2006). The growth of heterotrophs is stimulated by maintaining a high C/N ratio through direct addition of organic carbon in the water of by increasing the C/N ratio of the feed (Avnimelech, 2009; Bossier and Ekasari et al., 2017; Tinh et al., 2021; Vinasyiam et al., 2023). Hence, maintaining the C/N ratio is crucial in a biofloc system. On the one hand, insufficient amounts of carbon will inhibit biofloc formation and lead to poor water quality. On the other hand, carbon excess will lead to the accumulation of biofloc which eventually will hamper fish growth due to oxygen depletion and

Abbreviations: ASM, Activated sludge model; BFT, Biofloc technology; COD, Chemical oxygen demand; NSP, Non-starch pollysachharides; OM, Organic matter; RMSE, Relative mean square error; TAN, Total ammonia nitrogen.

E-mail addresses: nurhayati.brtarigan@wur.nl (N.B. Tarigan), karelkeesman@wur.nl (K.J. Keesman).

<sup>\*</sup> Corresponding author at: Mathematical and Statistical Methods - Biometris, Wageningen University and Research, Wageningen 6700AA, the Netherlands.

<sup>\*\*</sup> Corresponding author.

Symbols		$S_{co}$	Carbon dioxide (g CO <sub>2</sub> m <sup>-3</sup> )
		$S_{i}$	Soluble inert material (g COD m <sup>-3</sup> )
ADC <sub>OM</sub> Appar	rent digestibility coefficient of organic matter (-)	$S_{nd}$	Soluble organic nitrogen (g N $m^{-3}$ )
FCR <sub>Xba</sub> , FCR <sub>Xbh</sub> ,	FCR <sub>Xfeed</sub> Feed conversion ratio of autotrophic	$S_{nh}$	Ammonia nitrogen (g N m $^{-3}$ )
bioma	ass, heterotrophic biomass, and pelleted feed,	$S_{no}$	Nitrite and nitrate nitrogen (g N $m^{-3}$ )
respe	ctively (g dry weight $g^{-1}$ fresh weight)	$S_{o}$	Oxygen (g $O_2 m^{-3}$ )
N <sub>Xba</sub> , N <sub>Xbh</sub> , N <sub>Xfe</sub>	ed Total nitrogen content of autotrophic biomass,	$S_s$	Soluble organic matter (g COD m <sup>-3</sup> )
hetero	otrophic biomass, and pelleted feed, respectively (g N	$X_{ba}$	Autotrophic biomass (g COD m <sup>-3</sup> )
$kg^{-1}$ )		$X_{bh}$	Heterotrophic biomass (g COD m <sup>-3</sup> )
q <sub>GXf</sub> Fish g	rowth rate $(g h^{-1})$	$X_f$	Fish (g COD $m^{-3}$ )
QxfXnd, QxfXs, Qxf	Snh Waste production from fish in the form of	$X_{feed}$	Feed (g COD $m^{-3}$ )
nitrog	gen in faeces, organic matter in faeces, and ammonia,	$X_i$	Particulate inert material (g COD m <sup>-3</sup> )
respe	ctively (g h <sup>-1</sup> )	$X_{nd}$	Particulate organic nitrogen (g COD $m^{-3}$ )
qxbaxf, qxbhxf, q	KfeedXf, QXNXf Uptake rate by fish of autotrophic	$X_p$	Non-degradable organic matter (g COD $m^{-3}$ )
	ass, heterotrophic biomass, pelleted feed, and total	$X_{ph}$	Phytoplankton (g COD m $^{-3}$ )
nitrog	gen, respectively (g h <sup>-1</sup> )	$X_s$	Particulate organic matter (g COD $m^{-3}$ )
REN <sub>Xf</sub> Eaten	nitrogen feed content retained in fish body (%)	μ	Average value of observation data
S <sub>alk</sub> Alkali	nity (Molar)		

gill occlusion (Schveitzer et al., 2013).

Carbon can be introduced into the BFT system externally beside the feed or incorporated within the pelleted feed (Avnimelech, 2009; Bossier and Ekasari et al., 2017; Tinh et al., 2021; Vinasyiam et al., 2023). The latter has been done by the inclusion of non-starch polysaccharides (NSP) types of carbon into the diet (Kabir et al., 2020; Tarigan et al., 2025; Vinasyiam et al., 2023). Although there is a risk to lower fish production because a high dietary NSP content lowers the apparent digestibility of the feed, this diet-related approach can improve carbon use efficiency in a BFT system (Tarigan et al., 2025) and simplify carbon addition management (Vinasyiam et al., 2023).

To initiate optimum conditions for the growth of biofloc and fish, understanding the dynamic behaviour of biofloc is crucial. To date, knowledge of the dynamic behaviour of biofloc is still limited. Insight into different phenomena in a system can be obtained by mathematical models (Keesman, 2011), including aquaculture systems. Several models have been developed to understand the relationship between fish growth and nutrient dynamics in different aquaculture systems, including recirculated aquaculture system (RAS). (Jiménez-Montealegre et al., 2002; Serpa et al., 2013; Svirezhev et al., 1984), and RAS-hydroponics systems (de Korte et al., 2024; Goddek et al., 2016; Tarigan et al., 2021). However, only a few studies incorporate biofloc in pond aquaculture models due to the complexity of biofloc behaviour. To date, models that incorporate biofloc in aquaculture systems viewed biofloc as one aggregated component, and the change of biofloc biomass was described by an exponential function based on experimental observations (Pinho et al., 2023; Tarigan et al., 2024). This is a considerable simplification because biofloc is an aggregate of different types of microbial biomass, has various functions, and is affected by environmental conditions, such as nutrient availability, temperature, and light (De Schryver et al., 2008).

The family of activated sludge models (ASM), starting with the work of Henze et al. (1987) and known as ASM No 1, has been widely used, for instance treat pharmaceutical waste (Li et al., 2023) and micro-pollutants (Mohammadi et al., 2022) or to improve nitrogen and bioplastic recovery (Ribeiro et al., 2022). ASM has been advanced significantly compared to the first published version (Daigger, 2011). In the family of ASM, micro-organisms play a crucial role in transforming slowly biodegradable into readily organic matter, converting the waste into microbial biomass, and converting ammonia nitrogen (TAN) into NO<sub>3</sub>. The role of micro-organisms in activated sludge systems is similar to the role of biofloc in fish ponds, in which the waste comes from uneaten feed, faeces, and decaying organic matter (OM), the latter also including biofloc. The presence of cultured animals, e.g. Nile tilapia, in

the BFT system enables fish to recycle part of the waste nutrients resulting from applying pelleted feed by consuming biofloc (De Schryver et al., 2008).

This study is the first to merge an activated sludge model (ASM) and a fish growth model to evaluate fish and biofloc formation in a biofloc system (fish-ASM). The aim of this study is to predict biofloc growth or decay, as well as organic and inorganic waste accumulation and utilization in a fish-biofloc systems. In this study, the fish-ASM model was developed studying Nile tilapia (*Oreochromis niloticus*) culture performance in lined biofloc rearing tanks, fed diets with either a low or high NSP content.

## 2. Methodology

## 2.1. System description

In this study, the dynamic behaviour of biofloc, fish, carbon, and nitrogen of a fish-biofloc system was simulated. The operational data was based on the experimental data of Tarigan et al. (2025). Fish, Nile tilapia juveniles, were cultivated in ten experimental lined tanks with a diameter of 2 m for 56 days at IPB University, Bogor, Indonesia. Water depth ranged between 0.55 and 0.85 m depending on daily precipitation, evaporation, and water replacement. Originally, the water level was intended to be maintained during the experiment by compensating for evaporation loss. However, this became unnecessary due to the high precipitation during the experiment, with a total rainfall of 832.9 mm. Instead, some water was discharged to avoid overflow in the tank due to precipitation, with a total water replacement of 6.0-6.4 m<sup>3</sup>. Additionally, continuous aeration was applied to the rearing tank to maintain an oxygen level of at minimum 6 mg O2/L. The initial body weight and stocking density of the fish were 17.3  $\pm$  0.1 g and 15 fish/m³, respectively. The feeding ration was around 16 g/kg<sup>0.8</sup>/d and was administered equally twice a day, at 8.00 am and 4.00 pm. The average temperature during the culture period was 25  $\pm$  2.5 °C.

Two diets, differing in the type of carbon, were tested, assigning five replicate tanks per diet. One diet was mainly rich in starch (Control-diet) and the other was rich in NSP (High-NSP diet). Both diets had a similar protein content, around 29 % on dry matter basis. However, the High-NSP-diet contained 3 times more fiber compared to the Control-diet (13.3 % vs 4.3 % on dry matter basis). The NSP-rich ingredients in the High-NSP-diet mainly came from palm kernel meal, rice bran, and corn gluten feed, which are fibrous ingredients. The High-NSP-diet was expected to boost the biofloc growth because it reduces fish digestibility, hence providing more fiber-rich organic matter for the biofloc through

fish faeces (Tarigan et al., 2025; Vinasyiam et al., 2023).

## 2.2. Conceptual model

In principle, the model followed concepts of ASM No 1 (Henze et al., 1987) and combined it with the fish growth model of Tarigan et al. (2024).

Components in the model are expressed as  $S_j$  or  $X_j$ , in which the terms S and X represent soluble and particulate forms, respectively, and the subscript j represents different component names. Components included in this study were inert material ( $S_i$  and  $X_i$ ), heterotrophic bacteria ( $X_{bh}$ ), autotrophic bacteria ( $X_{ba}$ ), phytoplankton ( $X_{ph}$ ), organic matter ( $S_s$  and  $X_s$ ), particulate matter arising from biofloc decay ( $X_p$ ), organic nitrogen ( $S_{nd}$  and  $S_{nd}$ ), ammonia nitrogen ( $S_{nh}$ ), nitrite nitrogen ( $S_{no}$ ), oxygen ( $S_o$ ), alkalinity ( $S_{alk}$ ), and carbon dioxide ( $S_{co}$ ). The initial value of each component is shown in Table A.1. Components related to organic matter ( $S_i$ ,  $S_i$ ,  $S_i$ ,  $S_i$ ,  $S_i$ ,  $S_i$ , and  $S_i$ ) were expressed in  $S_i$ 0 chemical oxygen demand (COD) per tank, nitrogen-related components ( $S_{nd}$ ,  $S_{nd}$ ,  $S_{nd}$ ,  $S_{no}$ ) were in  $S_i$ 1 nitrogen ( $S_i$ 2 per tank,  $S_i$ 3 nd molar concentration per tank, respectively.

Organic waste in the fish tank refers to the sum of uneaten feed, fish faeces, decayed  $X_{bh}$ , and decayed  $X_{ba}$ . Preliminary results showed that the amount of decayed  $X_{ph}$  was almost negligible compared to the aforementioned organic waste. Similarly, the amount of active  $X_{ph}$  is also insignificant compared to other feed sources for the fish. Hence, it is excluded from the model calculation. Conversion from g feed and g fish to g COD was calculated from the protein, fat, and carbohydrate content (Davis et al., 2021). The processes driving conversions between model components are depicted in Fig. 1.  $S_i$  and  $X_i$  were not shown in the figure because these are inert materials, which means no conversion occurs during the cultivation period (Henze et al., 1987). The mass balance equation of each component of the model can be found in Table A.2, which in general is written as:

Accumulation = Input - Output + Reaction

(1)

In this fish-ASM,  $X_{bh}$  plays a crucial role in maintaining water quality through hydrolysis (conversion from  $X_s$  into  $S_s$ ) and ammonification (conversion from  $S_{nd}$  into  $S_{nh}$ ) process while through nitrification, ammonia nitrogen ( $S_{nh}$ ) was converted into nitrite and nitrate nitrogen ( $S_{no}$ ).  $X_{bh}$  can also reduce  $S_s$  and  $S_{nh}$  concentrations in water through uptake into  $X_{bh}$  biomass. The growth of  $X_{bh}$  and  $X_{ba}$  is dependent on  $S_s$  and  $S_{nh}$ , respectively. Additionally, their growth is associated with oxygen ( $S_o$ ) utilization. In the case of anoxic conditions, the role of oxygen as a terminal electron acceptor in  $X_{bh}$  is replaced by nitrate ( $S_{no}$ ). In other words, the growth of  $X_{bh}$  is affected by  $S_s$  and  $S_o$  in aerobic conditions and by  $S_s$ ,  $S_o$ , and  $S_{no}$  in anoxic conditions. Compared to aerobic conditions, the hydrolysis rate of  $X_s$  into  $S_s$  is also lower under anoxic conditions. Additionally, part of  $X_{bh}$  and  $X_{ba}$  is grazed by fish, contributing to fish growth. Another part of the eaten  $X_{bh}$  and  $X_{ba}$  is excreted as faeces and ammonia, and kept in the nutrient cycle.

The organic waste (uneaten feed, fish faeces, and majority of decayed  $X_{bh}$  and  $X_{ba}$ ) are associated with the activated sludge subsystem as particulate organic matter ( $X_s$ ) which then is hydrolysed into soluble organic matter ( $S_s$ ). The hydrolysis process rate is linear with  $X_{bh}$  concentration in the water. Additionally, a part of decayed  $X_{bh}$  and  $X_{ba}$  is converted into degradable particulate ( $X_p$ ).

Besides organic matter, this study also examined nitrogen dynamics. The nitrogenous waste is divided into ammonia  $(S_{nh})$ , soluble organic nitrogen  $(S_{nd})$ , and particulate organic nitrogen  $(X_{nd})$ . Similar to  $X_s$  and  $S_s$ , the contributors of nitrogenous particulate organic waste  $(X_{nd})$  are fish faeces, uneaten feed, and the majority of  $X_{bh}$  and  $X_{ba}$  decay. Inert nitrogenous material is neglected in the model because it is usually small. In parallel with the hydrolysis of organic waste,  $X_{nd}$  is hydrolysed into  $S_{nd}$ , which subsequently is partially converted into  $S_{nh}$ . Besides the ammonification process, the input of  $S_{nh}$  also comes from gill excretion.

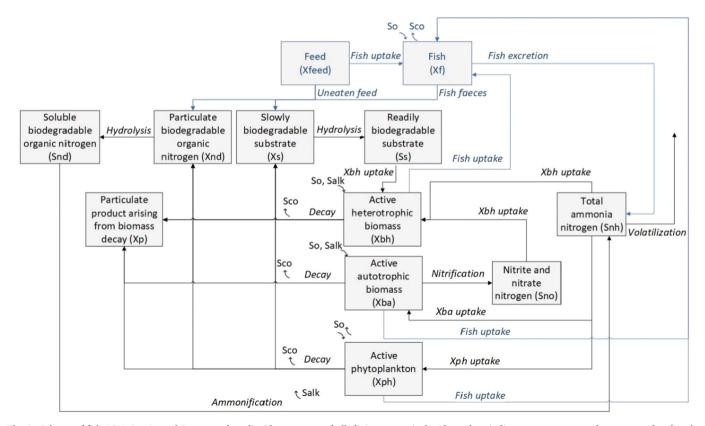


Fig. 1. Scheme of fish-ASM.  $S_{co}$ ,  $S_{o}$ , and  $S_{alk}$  are carbon dioxide, oxygen, and alkalinity, respectively. Blue colour indicates components and processes related to the fish growth model.

#### 2.3. Model equations

Mass balances expressing the dynamics or accumulation of each component are shown in Table A.2. Auxiliary equations of balance component (input, reaction, and output) in the mass balance are listed in Table A.3. Equations related to the ASM follow from Henze et al. (1987). Equations related to  $X_i$  and  $S_i$  are not shown because no reaction occurred in these components, they just enter the system through water inflow and leave through water replacement. Finally, parameter values used for the simulation can be found in Table A.4.

In terms the contribution to  $X_s$  and  $X_{nd}$ , it was assumed that 5 % of the feed given is uneaten.  $X_{bh}$  and  $X_{ba}$  decay is proportional to each of their biomass in a first-order manner (Henze et al., 1987; Svirezhev et al., 1984). The term fish faeces ( $q_{XfXs}$ ) was calculated based on the amount of eaten pelleted feed ( $q_{XfeedXf}$ ), eaten  $X_{bh}$  ( $q_{XbhdXf}$ ), and apparent digestibility coefficient of organic matter (ADC<sub>OM</sub>), which can be written as:

$$q_{XfXs} = (1 - ADC_{OM}) * (q_{XfeedXf} + q_{XbhXf} + q_{XbaXf})$$
 (2)

Calculation of N content in fish faeces  $(q_{XfXnd})$  is in line with  $q_{XfXs}$ , only the amount of eaten feed,  $X_{bh}$ , and  $X_{ba}$  is multiplied by each of their N content  $(N_{Xfeed}, N_{Xbh}, \text{ and } N_{Xba}, \text{ respectively})$ , and can be written as:

$$q_{XfXnd} = (1 - ADC_{OM}) * (N_{Xfeed} * q_{XfeedXf} + N_{Xbh} * q_{XbhXf} + N_{Xba} * q_{XbaXf})$$
(3)

Finally, the contribution to  $S_{nh}$  from fish  $(q_{XfSnh})$  was calculated based on total N consumed by fish from  $X_f$ ,  $X_{bh}$ , and  $X_{ba}$   $(q_{XNXf})$  minus total N retained by fish body minus total N ended up as fish faeces, which can be written as:

$$q_{XfSnh} = q_{XNXf} - REN_{Xf} + q_{XNXf} - q_{XfXnd}$$
 (4)

in which  $REN_{Xf}$  is the retention efficiency of N by the fish body and  $q_{XNXf}$  is defined as:

$$q_{XNXf} = N_{Xfeed} * q_{XfeedXf} + N_{Xbh} * q_{XbhXf} + N_{Xba} * q_{XbaXf}$$
 (5)

In terms of reactions, in ASM these are expressed as multiplication between stoichiometric coefficients and process rate, which contains the kinetics parameters. Equations related to the reaction of each component are shown in Table A.3. Stoichiometric coefficients and process rate related to  $X_{bh}$  and  $X_{ba}$  growth and decay, ammonification, and hydrolysis of  $X_s$  and  $X_{nd}$  follow from ASM No 1 (Henze et al., 1987, see Table A.3 and A.4). Reactions related to fish growth follow from Tarigan et al. (2024). The fish uptake rate of  $X_{bh}$  and  $X_{ba}$  was assumed to be proportional to fish biomass and maximum uptake rate in a first order-manner, and to  $X_{bh}$  biomass in a second-order manner (Svirezhev et al., 1984). Fish uptake of  $X_{bh}$  ( $q_{XbhXf}$ ) and  $q_{XbaXf}$ 0 contribute to fish growth ( $q_{GXf}$ ), together with pelleted feed ( $q_{XfeedXf}$ ), which can be written as:

$$q_{GXf} = q_{XfeedXf}/FCR_{Xfeed} + q_{XbhXf}/FCR_{Xbh} + q_{XbaXf}/FCR_{Xba}$$
 (6)

in which FCR<sub>Xfeed</sub>, FCR<sub>Xbh</sub>, and FCR<sub>Xba</sub> are feed conversion ratios of  $X_{feed}$ ,  $X_{bh}$ , and  $X_{ba}$ , respectively.

All components listed in Table A.2 leave the tank through water replacement, except for  $X_f$ ,  $S_{co}$ , and  $S_o$ . Each of the tanks was considered to be ideally mixed. Hence, the concentration of components leaving the tank is similar to the concentration in the tank.

The model was implemented in Ms Excel and solved using the Euler forward method with a simulation time of 56 days and a time steps of one hour.

## 2.4. Sensitivity analysis, calibration, and validation

Sensitivity analysis (SA) was conducted by increasing and decreasing the parameters listed in Table A.4 by 50 %. Parameters with the highest normalized sensitivity coefficient ( $S_{yx}$ ) (Tarigan et al., 2024) were prioritized in the calibration steps.

Calibration was done by fitting the corresponding model outputs to  $S_{nh}$ ,  $S_{no}$ ,  $S_{nd}$ , and biofloc data using a trial and error method. For the calibration the Control-diet dataset of Tarigan et al. (2025) was used. The fit is expressed in terms of as the ratio between the root mean square error (RMSE) to the average of observation data ( $\mu$ ) or RMSE/ $\mu$ , aiming to find the lowest RMSE/ $\mu$ . Further, RMSE/ $\mu$  is called as normalised RMSE (NRMSE). In the experiment of Tarigan et al. (2025), biofloc was defined as solid residue after tank water was filtered using Whatman paper. In the simulation, biofloc is defined as a combination of  $X_s$ ,  $X_p$ ,  $X_{bh}$ , and  $X_{ba}$  because solids residue can contain alive ( $X_{bh}$  and  $X_{ba}$ ) and dead ( $X_s$  and  $X_p$ ) particulate organic matters. The calibrated model was cross-validated using the High-NSP-diet dataset of Tarigan et al. (2025) to understand the model performance under different diet compositions.

In the cross-validation step, deliberately the same parameter value as in the calibration step were used, except for some parameters related to fish and feed characteristics, which are apparent digestibility of organic matter by the fish body (ADC $_{OM}$ ), the FCR, the nitrogen retention efficiency of the fish body (REN $_{Xf}$ ), and the nitrogen content of the feed (N $_{feed}$ ) (Table 1).

## 3. Results

## 3.1. Sensitivity analysis and parameterization

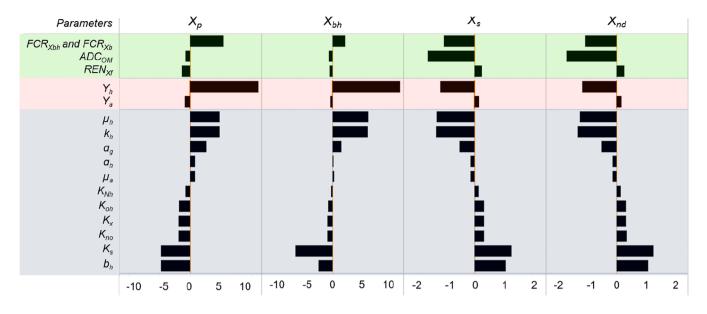
Compared to other components mentioned in Section 2.2,  $X_{bh}$  and  $X_p$  are the most sensitive model outputs, represented by a higher  $S_{yx}$  (Fig. 2). The maximum  $S_{yx}$  of  $X_{bh}$  and  $X_p$  are around 11, while the maximum  $S_{yx}$  of other model outputs is around 0.1–1.64. In general, parameters with the highest  $S_{yx}$  are related to  $X_{bh}$ , such as the  $X_{bh}$  yield  $(Y_h)$ , the maximum growth rate of  $X_{bh}$  ( $\mu_h$ ), the hydrolysis coefficient of  $X_{bh}$  ( $k_h$ ), and the decay rate of  $X_{bh}$  ( $b_h$ ). Parameters related to  $X_{ba}$  ( $Y_a$ ,  $\mu_a$ , and  $b_a$ ) had a relatively have lower  $S_{yx}$  than  $X_{bh}$ , which means that changing parameters related to  $X_{ba}$  have a lower effect on the model output. However, these parameters were considered in the calibration step of  $S_{no}$  as  $Y_a$  and  $\mu_a$  have the highest  $S_{vx}$  in  $S_{no}$ .

In terms of nitrogen balance,  $S_{nh}$  and  $S_{no}$  were mostly sensitive to fish-related parameters, which are the apparent digestibility of OM (ADC<sub>OM</sub>) and the retention efficiency of nitrogen in fish biomass (RENyr).

Based on the sensitivity analysis, five parameters with the highest  $S_{yx}$  were prioritized to be adjusted in the calibration step, namely  $Y_h,\,b_h,\,\mu_h,\,k_h,$  and  $\alpha_g.$  Another three parameters related to  $X_{ba}$  were also adjusted, which were  $i_{xb},\,b_a,\,$  and  $\mu_a.$  Although these parameters have low  $S_{yx}$  (-0.1–0.8), they are essential in determining the dynamics of  $S_{nh}$  and  $S_{no}$ . Finally, another parameter, which is  $k_a,$  was chosen for the sake of  $S_{nd}$  fitting.  $S_{yx}$  values of all parameters to  $S_{nd}$  were close to zero, and therefore not shown in Fig. 2. Consequently, fitting  $S_{nd}$  might include calibration of more than one parameter or more than 50 % adjustment compared to the initial value. Based on the sensitivity analysis, adjustment of  $b_h,\,\mu_h,$  and  $k_h$  can shift the dynamics of  $S_{nd}$ . However, it still resulted in NRMSE of  $S_{nd}$  and  $S_{no}$  of 74 % and 86 %, respectively. One of the highest  $S_{yx}$  values in  $S_{nd}$  (after  $b_h,\,\mu_h,$  and  $k_h$ ) was  $k_a$  ( $S_{yx}=-0.021$ ) and was chosen to be adjusted. The calibrated value of all

**Table 1**Diet-dependent parameter estimates value during calibration (Control-diet) and validation (High-NSP-diet) process.

Parameters	Control- diet	High-NSP- diet	Units
$ADC_{OM}$	0.60	0.48	-
FCR	1.42	1.64	g dry weight feed (g fresh weight fish) <sup>-1</sup>
$REN_{Xf}$	32.1	31.2	%
$N_{feed}$	0.047584	0.043748	g N (g dry weight feed) $^{-1}$



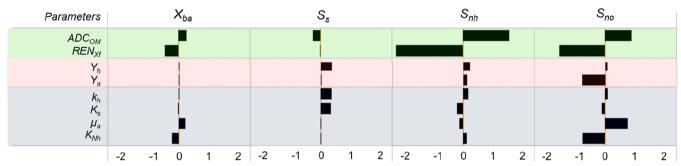


Fig. 2. Normalized sensitivity coefficients  $(S_{yx})$  of different parameters to model output of  $X_{bh}$ ,  $X_{ba}$ ,  $X_p$ ,  $X_s$ ,  $X_{nd}$ ,  $S_{nd}$ ,  $S_s$ ,  $S_{nh}$ , and  $S_{no.}$  Greenish, reddish, and bluish background colors indicate fish-related, stoichiometric, and kinetic parameters, respectively.

aforementioned parameters are shown in Table 2.

## 3.2. Model simulations

The parameters presented in Table 2 and Table A.4 were used to simulate components mentioned in Section 2.2. Model fitting was performed for  $X_f$ ,  $S_{nh}$ ,  $S_{no}$ ,  $S_{nd}$ , and VSS, in which VSS is the summation of  $X_s$ ,  $X_p$ ,  $X_{bh}$ , and  $X_{ba}$ . Using the calibrated parameters (Table 2 and Table A.4), the simulation fitted the value of the final harvested fish (X<sub>f</sub>) with a 3 %-5 % error (NRMSE) as shown in Table 3. In general, the simulation was able to depict the dynamics of S<sub>nh</sub>, S<sub>no</sub>, S<sub>nd</sub>, and VSS of the Control-diet datasets with NRMSE of 0.15-0.34. However, simulation with the calibrated parameters in tanks fed with the High-NSP-diet resulted in relatively higher error. The highest error was observed in VSS with NRMSE of 0.66, followed by  $S_{nh}$  and  $S_{no}$  with NRMSE of 0.64 and 0.36, respectively (Table 3). Since VSS consists of  $X_{bh}$  and  $X_{ba}$ , which have a direct relationship to X<sub>s</sub>, S<sub>s</sub>, S<sub>nh</sub>, and S<sub>no</sub>, a high error of VSS also leads to a higher error in  $S_{nh}$  and  $S_{no}$ . Therefore, more detail observation of the dynamics of VSS of the High-NSP-diet datasets is required to understand the reasons for the higher error compared to the Control-diet datasets (see 3.3.2 and 4.2).

## 3.3. Nutrient and biofloc dynamics

## 3.3.1. Control-diet

Hourly simulations data and biweekly observations of  $S_{nh}$ ,  $S_{no}$ ,  $S_{nd}$ , and VSS in tanks fed the Control-diet tank are depicted in Fig. 3. The effect of daily feeding, especially in the fluctuation of Snh and VSS are clearly visible in Figs. 3a and 3d, respectively. A relatively stable

behaviour of  $S_{nh}$  and increasing behaviour of  $S_{no}$  (Fig. 3a and Fig. 3b) is observed, indicating an active conversion of  $S_{nh}$  into  $S_{no}$ .  $S_{nh}$  was constantly added into the water via  $S_{nd}$  ammonification and fish digestion(Fig. 1). Accumulation of  $S_{nh}$  in the water was controlled by  $X_{bh}$  uptake and  $X_{ba}$  conversion during nitrification, causing  $S_{no}$  accumulation (Fig. 1). In terms of  $S_{nd}$ , the decreasing trend (Fig. 3c) was mainly due to water replacement and less due to ammonification. Since the tanks are assumed to be ideally mixed, a higher initial  $S_{nd}$  concentration (39 g/m³) means the loss of  $S_{nd}$  through water exchange when compared to the initial mass of  $S_{nh}$  and  $S_{no}$  (0.4 g/m³). Finally, the behaviour of VSS in the simulation aligned with the observation, increasing from day 0 to day 42 and decreasing slightly from day 42 to day 56 (Fig. 3d).

In the VSS, biofloc biomass was dominated by X<sub>s</sub> and X<sub>bh</sub> (Fig. 4a) and relatively a small amount of X<sub>p</sub> and X<sub>ba</sub> (Fig. 4b). The drop of VSS from day 42 to day 56 (Fig. 3d) was mainly caused by the drop of  $X_{\mbox{\scriptsize s}}$ (Fig. 4a). This drop was primarily driven by the drastic increase in X<sub>bh</sub> during this period. X<sub>bh</sub> plays a role in hydrolysing X<sub>s</sub> into S<sub>s</sub> in which the rate is linear to  $X_{bh}$  (Equation A.14). In other words, an increase of  $X_{bh}$ will eventually lower X<sub>s</sub> accumulation in the water when the input of X<sub>s</sub> is lower than the  $X_s$  hydrolysed into  $S_s$ . Regarding  $X_{ba}$ , the biomass concentration was relatively stable with 0.6–1 g COD/m<sup>3</sup> (Fig. 4b). Such amount of X<sub>ba</sub> contributes to 23 % of the S<sub>nh</sub> level with a maximum of 0.67 g/m $^3$  (Fig. 3a). Almost 75 % of the  $S_{nh}$  reduction was caused by  $X_{bh}$ uptake. Although the majority of S<sub>nh</sub> reduction was caused by X<sub>bh</sub> uptake, a change of 1 g of  $X_{ba}$  was 182 times higher than a change of 1 g of X<sub>bh</sub> in reducing S<sub>nh</sub> concentration in the water. Based on Table A.2 (Equation A.26 and A.27), 1 g of X<sub>ba</sub> growth consumed 4.19 g of S<sub>nb</sub>, while 1 g of X<sub>bh</sub> only consumed 0.023 g of S<sub>nh</sub>.

The increase of X<sub>bh</sub> will increase and decrease S<sub>nd</sub> simultaneously

**Table 2**Initial and final parameters estimates during the calibration process. Initial value was gained from ASM number 1 (Henze et al., 1987), which are parameters of domestic wastewater.

Parameters	Description	Units	Initial value	Calibrated value
$Y_h$	Yield for heterotrophic biomass	g cell COD formed (g COD oxidized) <sup>-1</sup>	0.67	0.75
$b_h$	Decay coefficient for heterotrophic biomass	$h^{-1}$	0.0258	0.0019
$\mu_{h}$	Maximum specific growth rate for heterotrophic biomass	$h^{-1}$	0.25	0.0375
$k_h$	Maximum specific hydrolysis rate	g slowly biodegradable COD (g cell COD. h) $^{-1}$	0.125	0.0238
$\alpha_{g}$	Correction factor for $\mu_h$ under anoxic conditions	-	0.8	2
$i_{xb}$	Nitogen required per for the growth of $X_{bh}$ and $X_{ba}$	g N (g COD) <sup>-1</sup> in biomass	0.086	0.0234
b <sub>a</sub>	Decay coefficient for autotrophic biomass	$h^{-1}$	-	0.00014
$\mu_a$	Maximum specific growth rate for autotrophic biomass	$h^{-1}$	0.033	0.0027
k <sub>a</sub>	1/Ammonification rate	m <sup>3</sup> (g COD. h) <sup>-1</sup>	0.0033	0.00002

**Table 3** Normalized root mean square error (NRMSE) of the Control-diet and the High-NSP-diet dataset. NRMSE is the ratio of RMSE to average observation value (RMSE/ $\mu$ ).

		$X_f$	$S_{nh}$	Sno	$S_{nd}$	VSS
Control-diet	RMSE NRMSE	361.9 6 %	0.66 20 %	2.53 29 %	69.44 34 %	114.07 15 %
High-NSP- diet	RMSE	225.5	2.30	3.55	55.70	600.64
	NRMSE	4 %	64 %	36 %	23 %	66 %

through hydrolysis (conversion from  $X_{nd}$  into  $S_{nd}$ , see Equation A.14 and A.22) and ammonification (conversion from  $S_{nd}$  into  $S_{nh}$ , see Equation A.23), respectively. A higher kinetics parameter of hydrolysis than of ammonification caused a slight increase of  $S_{nd}$ . The increase of  $S_{nd}$  becomes more significant when  $X_{bh}$  increased more strongly from day 42 to day 56 (Fig. 3c and Fig. 4a).

## 3.3.2. High-NSP-diet

The highest NRMSE (66 %) in the High-NSP-diet is observed for VSS (Table 2). The discrepancy is particularly found on day 42 (Fig. 5a) in which total biofloc biomass was much higher than the predicted biomass (204 vs 302 g COD/m³). This discrepancy is most likely caused by  $X_s$  or  $X_{ba}$  which are the dominant components in the VSS (Fig. 5b). From day 37–42,  $X_s$  dropped from around 114 g COD/m³ to around 10 g COD/m³. This drastic drop was triggered by the increase in hydrolysis rate (conversion from  $X_s$  to  $S_s$ ), which was encouraged by the rise of  $X_{bh}$  over time from day 37 to day 42. A relatively high discrepancy is also observed in  $S_{nh}$  and  $S_{no}$  with NRMSE of 64 % and 36 % (Table 2), respectively, in which most of the error is caused by under-prediction and a sudden overprediction of  $S_{nh}$  on day 56 (Fig. 5c and Fig. 5d). Based on the simulation, some parameters related to  $X_{bh}$  and  $X_{ba}$  might need to be adjusted further to achieve a better fit in Hight-NSP-diet fed biofloc tanks, and will be discussed in Section 4.

#### 4. Discussion

#### 4.1. Feedback loop

This study presents the dynamic behaviour of biofloc in Nile tilapia culture. Interactions between different components in the fish-biofloc systems can be depicted in a causal loop diagram (Fig. 6). Two reinforcing feedback loops and nine balancing feedback (Barbrook-Johnson and Penn, 2022) loops were identified. More feedback loops might have occurred. These are not shown in this graph, for instance, a feedback loop between fish growth and fish mortality to fish biomass.

There is a balancing feedback loop interaction between X<sub>bh</sub> and X<sub>s</sub> as depicted in Fig. 6. Uneaten feed, fish faeces, and decay of microorganisms were introduced to the activated sludge system in the form of X<sub>s</sub>, which will subsequently be hydrolysed into S<sub>s</sub>. In turn, S<sub>s</sub> is incorporated into X<sub>bh</sub>, causing an increase in X<sub>bh</sub> biomass. In other words, an increase of X<sub>s</sub> leads to an increase of S<sub>s</sub> and possibly X<sub>bh</sub>. However, there are both a reinforcing and balancing feedback loop between X<sub>bh</sub> and X<sub>s</sub>. The reinforcing loop is triggered by the fact that more biomass will decay as more X<sub>bh</sub> becomes available in the water (R1 in Fig. 6), which is one of the inputs to X<sub>s</sub>. However, as more X<sub>bh</sub> is available in the water, it will increase the hydrolysis process, causing a faster drop of X<sub>s</sub> (B.1 in Fig. 6). In this study, the biomass decay rate was almost 10 times lower as compared to hydrolysis process rate, both in the Control-diet and High-NSP-diet tanks. Additionally, a balance occurred between the X<sub>bh</sub> and S<sub>s</sub> feedback loop. The increasing concentration of X<sub>bh</sub> means more S<sub>s</sub> is required for X<sub>bh</sub> growth, which eventually will decrease S<sub>s</sub> when the uptake rate is higher than the hydrolysis rate (q<sub>SsXbh</sub> (Equation A.15) and q<sub>XsSs</sub> (Equation A.14), respectively).

The balancing feedback loop in tanks fed the Control-diet was observed after day 42 when  $X_s$  started to decrease (Fig. 4a). The growth rate of  $X_{bh}$  overall increased until day 53. Since the simulation was only carried out until the end of the experiment on day 56, the decreasing growth rate was hardly seen (Fig. 4a). The late drop of  $X_{bh}$  growth rate was triggered by  $S_s$  that was still available before finally dropping on day 53 due to a limited supply through hydrolysis of  $X_s$  (see Fig. 5b and Figure B.1).

A similar feedback loop is also observed between  $X_{bh}$  and nitrogen components ( $X_{nd}$ ,  $S_{nd}$ , and  $S_{nh}$ ). A reinforcing feedback loop occurs due to  $X_{bh}$  decay (R2 in Fig. 6). Two balancing feedback loops occur, one between  $X_{bh}$  growth and  $S_{nh}$  uptake (B5 in Fig. 6), another one between  $X_{bh}$  and  $X_{nd}$  due to hydrolysis of  $X_{nd}$  into  $S_{nd}$  and ammonification of  $S_{nd}$  into  $S_{nh}$  (B3 in Fig. 6). Additionally,  $S_{nh}$  is not only balanced by  $X_{bh}$  uptake but also by  $X_{ba}$  uptake (B6 in Fig. 6). Finally, the relationship between fish and  $X_{bh}$  and  $X_{ba}$  is also expressed in a balancing feedback loop. A higher  $X_{bh}$  and  $X_{ba}$  lead to higher uptake by fish which will boost the fish growth. However, a higher consumption of  $X_{bh}$  and  $X_{ba}$  will reduce these micro-organism concentrations. In summary, several balancing feedbacks are observed in the fish-biofloc system. Understanding the balance will give insight on maintaining the continuity of the fed-batch fish-biofloc system.

## 4.2. Improving simulation of the High-NSP-diet

The fish-ASM shows a relatively high discrepancy of VSS,  $S_{nh}$ , and  $S_{no}$  in tanks fed the High-NSP-diet (Table 3). The error in VSS is mostly caused by  $X_s$  or  $X_{bh}$ , which are the dominant components in VSS (Fig. 5b). The error might be related to a temporal change in some of the parameter values, especially parameters related to the micro-organisms ( $X_{ba}$  and  $X_{bh}$ ). The High-NSP-diet dataset was used for cross-validation of the fish-ASM, which means using the same, except those mentioned in Table 1, parameter values as in the Control-diet simulation. A diet rich in NSP produces more fiber-rich faeces, which require more time to decompose as compared to starch-rich faeces (Avnimelech et al., 2009; Ekasari et al., 2014; Serra et al., 2015). This difference in the faeces

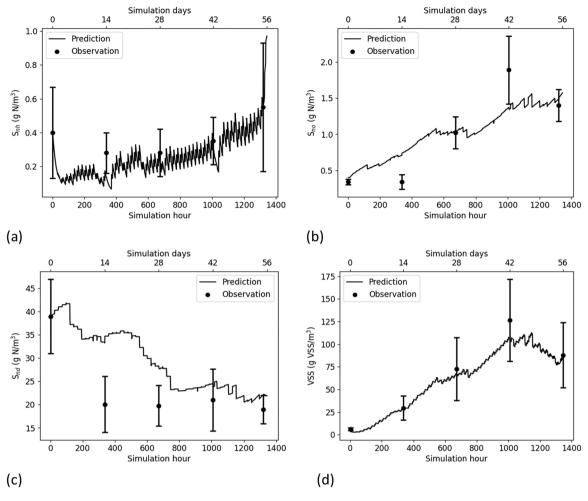


Fig. 3. Model predictions and observation data of (a) ammonia nitrogen  $(S_{nh})$ , (b) nitrate + nitrite nitrogen  $(S_{no})$ , (c) soluble organic nitrogen  $(S_{nd})$ , and (d) volatile suspended solide (VSS) or biofloc in the Control-diet case.

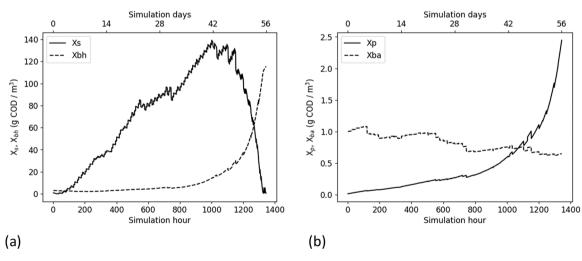


Fig. 4. Hourly simulation data of VSS based on its constituent components, which are (a) Xs, Xbh, and (b) Xp, and Xba, in Control-diet case in g COD/tank.

might cause a difference in hydrolysation rate between the between tanks fed the Control-diet or the High-NSP-diet. Slower hydrolysis in tanks fed the High-NSP-diet was not integrated in the model, and therefore not studied.

Improving the simulation-observation fit of the High-NSP-diet tanks by adjusting some parameters could be done based on the highest

sensitivity coefficient  $S_{yx}$  (Fig. 2). Additionally, the most interesting parameters might be related to  $X_{bh}$  and  $X_{ba}$  which have a direct relationship to VSS and  $S_{nh}$  which exhibited the highest NRMSE in tanks fed the High-NSP-diet. Changing the  $Y_h$ , parameters with the highest  $S_{yx}$  relative to  $X_{bh}$  (Fig. 2), from 0.75 to 0.71 improves the NRMSE of VSS from 66 % to 47 % (Table 3 and Table B.1). A lower  $Y_h$  means that less g

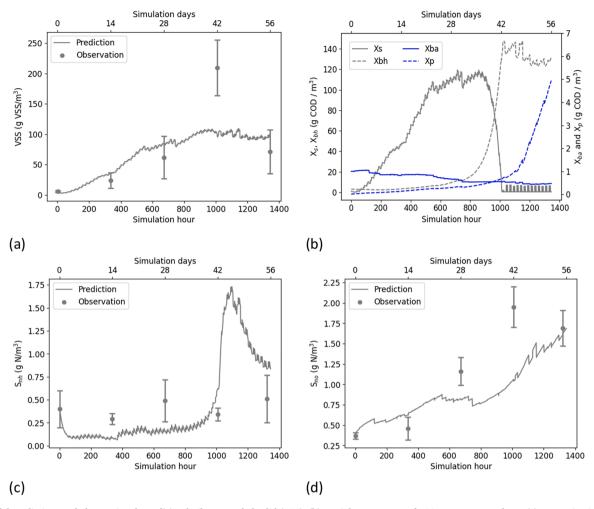


Fig. 5. Model predictions and observation data of(a) volatile suspended solid (VSS), (b) partial components of VSS:  $X_s$ ,  $X_{bh}$ ,  $X_p$ , and  $X_{ba}$ , (c) ammonia nitrogen ( $S_{nh}$ ), and (d) nitrate + nitrite nitrogen ( $S_{no}$ ) in the High-NSP-diet case.

cell COD X<sub>bh</sub> formed per g S<sub>s</sub> uptake by X<sub>bh</sub>. Less X<sub>bh</sub> production means more X<sub>s</sub> will be accumulated due to the lower hydrolysis rate. Compared to the value of  $Y_h$  of 0.75, the updated value of 0.71 increases the VSS on day 42, which is caused by more X<sub>s</sub> accumulating (102 g VSS/m<sup>3</sup> vs 140 g VSS/m<sup>3</sup>) in the system. After day 42, X<sub>bh</sub> started to grow drastically, leading to faster hydrolysis, and eventually reduced Xs accumulation (Figure B.2a and Figure B.2b). The change of Y<sub>h</sub> also affects the dynamics of S<sub>nh</sub>, and eventually S<sub>no</sub> (Figure B.2c and Figure B.2d), in which more S<sub>nh</sub> will be accumulated at the end of the simulation due to higher ammonification of S<sub>nd</sub> into S<sub>nh</sub> by X<sub>bh</sub> from day 42 to day 56. Hence, after adjusting Yh, parameters related to Shh also need to be adjusted to improve the fit between simulation and observation, such as Ya (g cell COD of Xba formed per g N uptaken by Xba), ixb (g N required per g COD biomass of X<sub>bh</sub> and X<sub>ba</sub>), and 1/k<sub>a</sub> (g COD hydrolysed per h per m<sup>3</sup>). Adjusted parameters, NRMSE, and new simulation results of S<sub>no</sub> and S<sub>nh</sub> are depicted in Table B.1, Table B.2, Figure B.2e, and Figure B.2 f, respectively.

Changing the aforementioned parameters can reduce the NRMSE of VSS and  $S_{nh}$ , however, the error was still around 50 % (Table B.1). In terms of VSS, this updated strategy can improve  $X_s$  concentration on day 42, but not the  $X_{bh}$  concentration. The hydrolysis process of  $X_s$  might be slower due to its high fiber content as compared to the Control-diet. Consequently,  $S_s$  production, one of the limiting factors of  $X_{bh}$  growth, is also lower compared to the Control-diet. However, since the High-NSP-diet has lower ADC $_{OM}$  (Table 1), which means higher faeces production, the  $S_s$  production will eventually be higher than in tanks fed the Control-diet, which means a higher growth of  $X_{bh}$ . In this case, the

higher VSS on day 42 in the High-NSP-diet when compared to the Control-diet (127 g VSS/m³ vs 210 g VSS/m³) was probably caused by a higher accumulation of  $X_{s}$  and a higher  $X_{bh}$  concentration in the water. Further research might be needed to understand the mechanisms and dynamics of the hydrolysis process and its relationship to  $X_{bh}$  in biofloc systems fed a High-NSP or fiber-rich diet.

#### 5. Conclusion

To our knowledge, this is the first study that demonstrates the dynamics of nitrogen and biofloc in fish-biofloc systems. This study demonstrated the possibility of combining the ASM concept and nutrient-based fish growth modelling to understand the relationship between fish, organic matter, nitrogen, heterotrophic biomass, and autotrophic biomass in a fish-biofloc system. Simulation under Controldiet was considerably fit (NRMSE of around 15 %-34 %) to the field observation. However, improvement is needed in the simulation of the tank fed with the High-NSP-diet, especially in the biofloc and ammonia dynamics.

The High-NSP-diet datasets were simulated using a cross-validation technique, which means the simulation was performed based on calibrated parameters of Control-diet data. The inclusion of NSP was aimed to change fish faeces characteristics, which eventually will affect the hydrolysis rate and biofloc growth in the water. Further research might be focused on studying the mechanisms and dynamics of the hydrolysis of organic matter and its relationship to heterotrophic biomass in biofloc systems fed a high-NSP or fiber-rich diet.

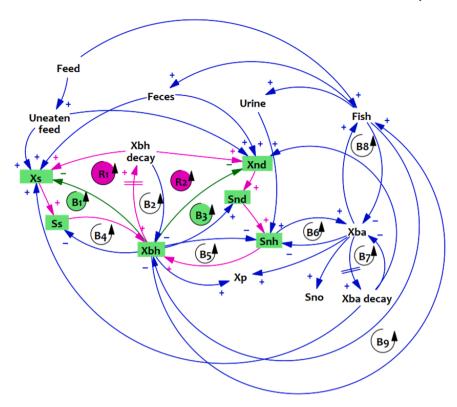


Fig. 6. Causal loop diagram of the fish-ASM.Bi = Balancing feedback loop i, Ri = Reinforcing feedback loop i, Ri = Particulate organic matter,  $S_s$  = Soluble organic matter,  $S_{hh}$  = Heterotrophic biomass,  $S_{hh}$  = Particulate organic nitrogen,  $S_{hh}$  = Ammonia nitrogen,  $S_{hh}$  = Autotrophic biomass,  $S_{hh}$  = Non-degradable organic matter. Pink arrows represent reinforcing feedback pathways of R1 and R2. Green arrows and colour represent balancing feedback pathways of B1 and B3.

## **Funding**

This work was supported by Interdisciplinary Research and Education Fund (INREF), Wageningen University & Research

## CRediT authorship contribution statement

Karel J Keesman: Writing – original draft, Validation, Supervision, Resources, Methodology, Funding acquisition, Data curation, Conceptualization. Julie Ekasari: Writing – review & editing. Marc Verdegem: Writing – review & editing, Validation, Supervision, Conceptualization.

Nurhayati Br Tarigan: Writing – review & editing, Writing – original draft, Visualization, Software, Resources, Project administration, Methodology, Investigation, Formal analysis, Data curation, Conceptualization.

## **Declaration of Competing Interest**

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

## Appendix A. Parameters and equations

**Table A.1**Initial values used in the calibration (Control-diet) and validation (High-NSP-diet) process

Parameter	Value	Units
S <sub>s</sub>	38.00	${ m g~COD~m^{-3}}$
$X_s$	9.00	$g COD m^{-3}$
$X_i$	17.00	$g COD m^{-3}$
$S_i$	36.00	$g COD m^{-3}$
$X_{bh}$	3	${ m g~COD~m^{-3}}$
$X_{ba}$	1	$ m g~COD~m^{-3}$
$X_p$	0.015	${ m g~COD~m^{-3}}$
$S_0$	6	${ m g~COD~m^{-3}}$
$S_{no}$	0.4	$ m g~N~m^{-3}$
$S_{nh}$	0.4	g N m <sup>-3</sup> g N m <sup>-3</sup>
$S_{nd}$	39	$g N m^{-3}$
X <sub>nd</sub>	0.5	${ m g~N~m}^{-3}$
$S_{alk}$	5	Molar

Table A.2
Mass balance equation of each compartment in the model

Compartment	Equation
Fish	$\frac{dX_f}{dt} = q_{\rm GXf} - q_{\rm MXf}$
Feed	$\frac{dt}{dt_{feed}} = \text{U(t)} - \text{q}_{\text{xfeedXf}} - \text{q}_{\text{xfeedXs}}$
Heterotrophic biomass	$\frac{dt}{dt} = q_{\text{GXbh}} - q_{\text{Xbhxs}} - q_{\text{Xbhxf}} - q_{\text{Xbhout}}$
Autotrophic biomass	$\frac{dt}{dt} = q_{\text{GXba}} - q_{\text{XbaXs}} - q_{\text{Xbaxt}} - q_{\text{Xbaout}}$
Organic matter	$\frac{dt}{dX_s} = \frac{q_{XDBAS}}{dt} + q_{XDBAS} + q_{XDBAS} - q_{XSSS} - q_{XSOUT}$
	$\frac{dS_s}{dt} = q_{SSS} - q_{SSMh} - q_{Sout}$
	$\frac{dX_p}{dt} = q_{XbhXp} + q_{XbaXp} - q_{Xpout}$
Nitrogen	$\frac{dX_{nd}}{dt} = q_{XfXnd} + q_{XfeedXnd} + q_{XbhXnd} + q_{XbaXnd} - q_{XndSnd} - q_{Xndout}$
	$rac{dS_{nd}}{dt} =  ext{q}_{ ext{NndSnd}}  ext{ -}  ext{q}_{ ext{Sndout}}$
	$rac{dS_{nh}}{dt}=q_{ m NfSnh}+q_{ m SndSnh}$ - $q_{ m SnhXbh}$ - $q_{ m SnhXba}$ - $q_{ m Snhvolat}$ - $q_{ m Snhout}$
	$rac{dS_{no}}{dt} =  ext{q}_{ ext{NbaSno}}  ext{-}  ext{q}_{ ext{Snooth}}  ext{-}  ext{q}_{ ext{Snoout}}$
Oxygen	$rac{dSo}{dt} =  ext{q}_{ ext{Sopump}} +  ext{q}_{ ext{Sosurface}}  ext{- }  ext{q}_{ ext{XfSo}}  ext{- }  ext{q}_{ ext{XbhSo}}  ext{- }  ext{q}_{ ext{XbaSo}}  ext{- }  ext{q}_{ ext{Soout}}$
Carbon dioxide	$\frac{dSco}{dt} = q_{ScoXf} + q_{ScoXbh} + q_{ScoXba} - q_{Scoout}$
Alkalinity	$\frac{dt}{dt} = q_{\text{SndSalk}} - q_{\text{SalkXbh}} - q_{\text{SalkXba}}$

**Table A.3**Auxiliary equations of each flow in the mass balance

MMF   Fish       AffeedXf   Feet       AffeedXf   Feet       AffeedXs   Feet       AffeedXs   Feet       AffeedXs   Feet       AffeedXs   Feet       AffeedXs   Aer       AffeedXs   Aer       AffeedXs   Arc       AffeedXs   Dec       AbbAXF   Het       Autotrophic bioma   Arc       Agoba   Gro       Autotrophic bioma       Autotrophic biom	robic growth of erotrophs oxic growth of heterotrophs tal growth of heterotrophs cay of heterotrophs terotrophs uptaken by fish ass owth of cotrophs cay of autotrophs tetrotrophs uptaken by fish something to the cotrophs totrophs uptaken by fish	$\begin{split} q_{XfeedXf}/FCR_{Xfeed} + q_{XbhXf}/FCR_{Xbh} + q_{XbaXf}/FCR_{Xba} \\ X_f * km \\ U(t) * (1-ku) \\ U(t) * ku \\ \mu_h * (S_s/(S_s+K_s)) * (S_o/(S_o+K_{oh})) * X_{bh} \\ q_{GXbh,aerobic} * (S_{no}/(S_{no}+K_{no})) * \alpha_g \\ q_{GXbh,aerobic} + q_{GXbh,anoxic} \\ b_h * X_{bh} \\ X_f * \mu_{XbhXf} * (X_{bh}/(K_{XbhXf}+X_{bh})) \\ \mu_a * (S_{nh}/(S_{nh}+K_{nh})) * (S_o/(S_o+K_{oa})) * X_{ba} \\ b_a * X_{ba} \\ X_f * \mu_{XbaXf} * (X_{ba}/(K_{XbaXf}+X_{ba})) \end{split}$	A.: A.: A.: A.: A.: A.: A.: A.:
MMF   Fish       AffeedXf   Feet       AffeedXf   Feet       AffeedXs   Feet       AffeedXs   Feet       AffeedXs   Feet       AffeedXs   Feet       AffeedXs   Aer       AffeedXs   Aer       AffeedXs   Arc       AffeedXs   Dec       AbbAXF   Het       Autotrophic bioma   Arc       Agoba   Gro       Autotrophic bioma       Autotrophic biom	h mortality ed uptaken by fish ed uptaken by fish ed uneaten mass robic growth of rerotrophs oxic growth of heterotrophs tal growth of heterotrophs cay of heterotrophs terotrophs uptaken by fish ass owth of totrophs cay of autotrophs totrophs uptaken by fish	$\begin{split} & X_f * km \\ & U(t) * (1-ku) \\ & U(t) * ku \\ & \mu_h * (S_s/(S_s+K_s)) * (S_o/(S_o+K_{oh})) * X_{bh} \\ & q_{GXbh,aerobic} * (S_{no}/(S_{no}+K_{no})) * \alpha_g \\ & q_{GXbh,aerobic} + q_{GXbh,anoxic} \\ & b_h * X_{bh} \\ & X_f * \mu_{XbhXf} * (X_{bh}/(K_{XbhXf}+X_{bh})) \\ & \mu_a * (S_{nh}/(S_{nh}+K_{nh})) * (S_o/(S_o+K_{oa})) * X_{ba} \\ & b_a * X_{ba} \end{split}$	A.: A.: A.: A.: A.: A.: A.: A.:
XfeedXf   Feet     XfeedXs   Feet     XfeedXs   Feet     XfeedXs   Feet     XfeedXs   Feet     XfeedXs   Feet     XfeedXs   Aer     Xfeet   Xfeet     Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet     Xfeet   Xfeet     Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet   Xfeet     Xfeet	ed uptaken by fish ed uneaten mass robic growth of rerotrophs oxic growth of heterotrophs tal growth of heterotrophs cay of heterotrophs terotrophs uptaken by fish ass owth of totrophs cay of autotrophs totrophs totrophs uptaken by fish	$\begin{split} &U(t) * (1-ku) \\ &U(t) * ku \\ &\mu_h * (S_s/(S_s+K_s)) * (S_o/(S_o+K_{oh})) * X_{bh} \\ &q_{GXbh,aerobic} * (S_{no}/(S_{no}+K_{no})) * \alpha_g \\ &q_{GXbh,aerobic} + q_{GXbh,anoxic} \\ &b_h * X_{bh} \\ &X_f * \mu_{XbhXf} * (X_{bh}/(K_{XbhXf}+X_{bh})) \\ &\mu_a * (S_{nh}/(S_{nh}+K_{nh})) * (S_o/(S_o+K_{oa})) * X_{ba} \\ &b_a * X_{ba} \end{split}$	A.: A.: A.: A.: A.: A.: A.:
ArkeedXf   Feet     ArkeedXf   Feet     ArkeedXs   Feet     ArkeedXs   Feet     ArkeedXs   Feet     ArkeedXs   Aer     ArkeedXs   Aer     ArkeedXs   Aer     ArkeedXs   ArkeedXs     ArkeedXs   Aer     ArkeedXs   Aer     ArkeedXs   Aer     ArkeedXs   Aer     ArkeedXs   Autorophic bioma     ArkeedXs   Gro     ArkeedXs   Gro     ArkeedXs   Autorophic matter     A	ed uneaten mass robic growth of erotrophs oxic growth of heterotrophs tal growth of heterotrophs cay of heterotrophs terotrophs uptaken by fish ass owth of otrophs cay of autotrophs terotrophs uptaken by fish	$\begin{split} &U(t) * ku \\ &\mu_h * (S_s/(S_s + K_s)) * (S_o/(S_o + K_{oh})) * X_{bh} \\ &q_{GXbh,aerobic} * (S_{no}/(S_{no} + K_{no})) * \alpha_g \\ &q_{GXbh,aerobic} + q_{GXbh,anoxic} \\ &b_h * X_{bh} \\ &X_f * \mu_{XbhXf} * (X_{bh}/(K_{XbhXf} + X_{bh})) \\ &\mu_a * (S_{nh}/(S_{nh} + K_{nh})) * (S_o/(S_o + K_{oa})) * X_{ba} \\ &b_a * X_{ba} \end{split}$	A.: A.: A.: A.: A.: A.:
Agreedxs Fees Heterotrophic bior Agxbh, Aer Agreedxs Aer Aer Aerobic hete Agxbh, Tota Agxbh Tota Agxbhx Het Autotrophic bioma Agxba Gro Autotrophic bioma Agxba Autotrophic bioma Agxba Gro Autotrophic bioma Agxba Gro Autotrophic bioma Agxba Gro Autotrophic bioma Agxba Gro Autotrophic bioma Agxba Autotrophic bioma Agxb	mass robic growth of rerotrophs oxic growth of heterotrophs tal growth of heterotrophs cay of heterotrophs terotrophs uptaken by fish ass owth of cotrophs cay of autotrophs totrophs uptaken by fish	$\begin{split} & \mu_h * (S_s/(S_s + K_s)) * (S_o/(S_o + K_{oh})) * X_{bh} \\ & q_{GXbh,aerobic} * (S_{no}/(S_{no} + K_{no})) * \alpha_g \\ & q_{GXbh,aerobic} + q_{GXbh,anoxic} \\ & b_h * X_{bh} \\ & X_f * \mu_{XbhXf} * (X_{bh}/(K_{XbhXf} + X_{bh})) \\ & \mu_a * (S_{nh}/(S_{nh} + K_{nh})) * (S_o/(S_o + K_{oa})) * X_{ba} \\ & b_a * X_{ba} \end{split}$	A. A. A. A. A.
Heterotrophic bior  IGXbh, Aer IGXbh, Aer IGXbh, Ance IGXbh, Ance IGXbh, Toti IXbhXs Dec IXbhXf Het Autotrophic bioma IGXba Gro IXbhXs Dec IXbhXs Dec IXbhXs Dec IXbhXs Hyt IXbhXs Dec IXbhXs Hyt IXSS Hyt IXSS Hyt ISSXbh Rea IXbhXp Het	robic growth of erotrophs oxic growth of heterotrophs tal growth of heterotrophs cay of heterotrophs terotrophs uptaken by fish ass owth of cotrophs cay of autotrophs tetrotrophs uptaken by fish something to the cotrophs totrophs uptaken by fish	$\begin{split} q_{GXbh,aerobic} * (S_{no}/(S_{no} + K_{no})) * \alpha_g \\ q_{GXbh,aerobic} + q_{GXbh,anoxic} \\ b_h * X_{bh} \\ X_f * \mu_{XbhXf} * (X_{bh}/(K_{XbhXf} + X_{bh})) \\ \mu_a * (S_{nh}/(S_{nh} + K_{nh})) * (S_o/(S_o + K_{oa})) * X_{ba} \\ b_a * X_{ba} \end{split}$	A. A. A. A.
erobic hete  GXbh,anoxic    GXbh   Tota  GXbh   Tota  IXbhXs   Dec  IxbhXs   Het  Autotrophic bioma  GXba   Gro  aute  IxbhXs   Dec  IxbaXf   Autorganic matter  IxrSs   Fish  IxsSs   Hyc  IxsSbh   Rea  IxbhXp   Het	cerotrophs oxic growth of heterotrophs tal growth of heterotrophs cay of heterotrophs terotrophs uptaken by fish ass owth of cotrophs cay of autotrophs totrophs uptaken by fish	$\begin{split} q_{GXbh,aerobic} * (S_{no}/(S_{no} + K_{no})) * \alpha_g \\ q_{GXbh,aerobic} + q_{GXbh,anoxic} \\ b_h * X_{bh} \\ X_f * \mu_{XbhXf} * (X_{bh}/(K_{XbhXf} + X_{bh})) \\ \mu_a * (S_{nh}/(S_{nh} + K_{nh})) * (S_o/(S_o + K_{oa})) * X_{ba} \\ b_a * X_{ba} \end{split}$	A. A. A. A.
erobic hete [GXbh,anoxic Anc [GXbh Tot: IXbhx Dec [Xbhx] Het Autotrophic bioma [GXba Gro aute [Xbhx Dec [Xbaxr Aut Drganic matter [Xxxx Fish [Xxss Hyc entr [3sxbh Rea [Xbhxp Het	oxic growth of heterotrophs tal growth of heterotrophs cay of heterotrophs terotrophs uptaken by fish ass owth of cotrophs cay of autotrophs totrophs uptaken by fish	$\begin{split} &q_{GXbh,aerobic} + q_{GXbh,anoxic} \\ &b_h * X_{bh} \\ &X_f * \mu_{XbhXf} * (X_{bh}/(K_{XbhXf} + X_{bh})) \\ &\mu_a * (S_{nh}/(S_{nh} + K_{nh})) * (S_o/(S_o + K_{oa})) * X_{ba} \\ &b_a * X_{ba} \end{split}$	A. A. A.
IGXbh,anoxic IGXbh IGXbh IXbhXs Dec IXbhXf Autotrophic bioma IGXba IGXba IGXba IGXba IGXba IGXba IGXba IGXba IGXba IXbhXs Dec IXbaXf Aut Organic matter IXXXS IXSS IXSS IXSS IXSS IXSS IXSS IX	tal growth of heterotrophs cay of heterotrophs terotrophs uptaken by fish ass owth of totrophs cay of autotrophs totrophs uptaken by fish	$\begin{split} &q_{GXbh,aerobic} + q_{GXbh,anoxic} \\ &b_h * X_{bh} \\ &X_f * \mu_{XbhXf} * (X_{bh}/(K_{XbhXf} + X_{bh})) \\ &\mu_a * (S_{nh}/(S_{nh} + K_{nh})) * (S_o/(S_o + K_{oa})) * X_{ba} \\ &b_a * X_{ba} \end{split}$	A. A. A.
GXbh Tota  Xbhxs Dec  Xbhxf Het  Xbhxf Het  Xbhxf Het  Xbhxf Gro  Xbaba Gro  Xbaxf Aut  Xbhxs Dec  Xbaxf Aut  Xganic matter  Xxxs Fish  Xxss Hyc  Xxss Hyc  Xxss Hyc  Xxsy Hyc	tal growth of heterotrophs cay of heterotrophs terotrophs uptaken by fish ass owth of totrophs cay of autotrophs totrophs uptaken by fish	$\begin{split} &q_{GXbh,aerobic} + q_{GXbh,anoxic} \\ &b_h * X_{bh} \\ &X_f * \mu_{XbhXf} * (X_{bh}/(K_{XbhXf} + X_{bh})) \\ &\mu_a * (S_{nh}/(S_{nh} + K_{nh})) * (S_o/(S_o + K_{oa})) * X_{ba} \\ &b_a * X_{ba} \end{split}$	A. A. A.
Xbhxs Dec  Xbhxf Het  Autotrophic bioma  GXba Gro  Xbhxs Dec  Xbaxf Aut  Drganic matter  XrXs Fish  Xxss Hyc  entil	terotrophs uptaken by fish ass owth of cotrophs cay of autotrophs totrophs uptaken by fish	$\begin{array}{l} b_h * X_{bh} \\ X_f * \mu_{XbhXf} * (X_{bh}/(K_{XbhXf} + X_{bh})) \\ \\ \mu_a * (S_{nh}/(S_{nh} + K_{nh})) * (S_o/(S_o + K_{oa})) * X_{ba} \\ \\ b_a * X_{ba} \end{array}$	A. A.
IXIADATÍ HET AUTOTOPHIC DIOMA IGXDA GRO AUTO IXIADATÍ AUTO Organic matter IXIXS FISH IXISS HYC ELSSS HYC ELSSADH REA IXISADH REA	terotrophs uptaken by fish ass owth of cotrophs cay of autotrophs totrophs uptaken by fish	$X_f^* \mu_{XbhXf}^* (X_{bh}/(K_{XbhXf}+X_{bh}))$ $\mu_a^* (S_{nh}/(S_{nh}+K_{nh}))^* (S_o/(S_o+K_{oa}))^* X_{ba}$ $b_a^* X_{ba}$	A.
Autotrophic bioma   GXba Gro	owth of cotrophs cay of autotrophs totrophs uptaken by fish	$\mu_a * (S_{nh}/(S_{nh}+K_{nh})) * (S_o/(S_o+K_{oa})) * X_{ba}$ $b_a * X_{ba}$	A
GXba	owth of cotrophs cay of autotrophs totrophs uptaken by fish	$b_a * X_{ba}$	A
autt	cotrophs cay of autotrophs totrophs uptaken by fish	$b_a * X_{ba}$	
Axbhxs Dec Axbaxf Aut Drganic matter Axfxs Fish Axss Hyc enti Assxbh Rea Axbhxp Het	cay of autotrophs totrophs uptaken by fish		
XbaXf Aut  Organic matter  XfXs Fish  XsSs Hyc entr  SsXbh Rea  XbhXp Het	totrophs uptaken by fish		
Organic matter   XfXs Fish  XsSs Hyc entr  SsXbh Rea  XbhXp Het	• •	PADANI (**Da/ (**Da/)	A
IXfXs Fish IXsSs Hyd entr ISsXbh Rea IXbhXp Het			
IXsSs Hyc entr ISsXbh Rea IXbhXp Het	h faeces production	$(1 - ADC_{OM}) * (q_{XfeedXf} + q_{XbhXf} + q_{XbaXf})$	Α
entr I <sub>SsXbh</sub> Rea I <sub>XbhXp</sub> Het	drolysis of	$k_h * [(X_s/X_{bh})/((X_s/X_{bh}) + K_x)] * [(S_o/(S_o+K_{oh})) + \alpha h * (K_{oh}/(S_o+K_{oh})) * (S_{no}/(S_o+K_{oh})) * (S_{$	A
lssxbh Rea lxbhxp Het	rapped organics	$(S_{no}+K_{no}))] * X_{bh}$	
l <sub>XbhXp</sub> Het	adily biodegradable substrate uptaken by heterotrophic biomass	1/Y <sub>h</sub> * q <sub>GXbh</sub>	Α
p	terotrophic biomass become non-degradable particulate organic	f <sub>p</sub> * q <sub>Xbh</sub> x <sub>s</sub>	Α.
XbaXp Aut	totrophic biomass become non-degradable particulate organic	f <sub>p</sub> * QxbaXs	Α.
Vitrogen	torropine biolitass become non-degradable particulate organic	тр чхрахѕ	11.
	rticulate organic nitrogen from fish faeces	$(1 - ADC_{OM}) * (N_{Xfeed} * q_{XfeedXf} + N_{Xbh} * q_{XbhXf} + N_{Xba} * q_{XbaXf})$	A.
	rticulate organic nitrogen from uneaten feed	N <sub>Xfeed</sub> * Q <sub>Xfeed</sub> Xs	A
	rticulate organic nitrogen from heterotrophics biomass decay	$(i_{xb} - f_p * i_{xp}) * q_{XbhXs}$	Α.
	ticulate organic nitrogen from autotrophics biomass decay	$(i_{xb} - f_p * i_{xp}) + q_{XbaXs}$	Α.
	drolysis of entrapped organic N	$q_{XSS} * X_{nd}/X_{S}$	A
inidona ,	amonification of soluble organic N	$ka * S_{nd} * X_{bh}$	A
	h total ammonia nitrogen (TAN) production	q <sub>XNXf</sub> - REN <sub>Xf</sub> *q <sub>XNXf</sub> - q <sub>XfXnd</sub>	A
	rogen from feed, heterotrophics, and autotrophics biomass taken up	Nxfeed*Qxfeedxf + Nxbh*Qxbhxf + Nxba*Qxbaxf	A
<sub>lxnxf</sub> Nitr by f		**Xfeed QXfeedXf + T*Xbh QXbhXf + T*Xba QXbaXf	Λ,
	N uptake by heterotrophics biomass	$i_{xb}$ * $q_{GXbh}$	A.
ISnhXba TAN	N uptake by autotrophics biomass	$(i_{xb} + 1/Y_a)^* q_{GXba}$	A.
Snhvolat TAN	N volatilization	$kv * S_{nh}$	Α
l <sub>XbaSno</sub> Nitr	rification by autotrophics biomass	$1/Y_a * q_{GXba}$	Α

## Table A.3 (continued)

	Process name	Equations	Eqn
<b>Q</b> SnoXbh	Nitrate and nitrite nitrogen uptake by heterotrophics biomass in anoxic condition	$(1-Y_h)/(2.86 *Y_h) * q_{GXbh,anoxic}$	A.30
Oxygen			
$q_{XfSo}$	Oxygen uptake by fish	$2014.45 + 2.75 * X_f - 165.2 * T_w + 0.007 * X_f^2 + 3.93 * T_w^2 - 0.21 * X_f * T_w^4$	A.31
q <sub>XbhSo</sub>	Oxygen uptake by heterotrophics biomass	$(1-Y_h)/Y_h * q_{GXbh}$	A.32
q <sub>XbaSo</sub>	Oxygen uptake by autotrophics biomass	$(4.57-Y_a)/Y_a * q_{GXba}$	A.33
Carbon diox	ride		
q <sub>ScoXf</sub>	Fish CO <sub>2</sub> respiration	$kcoX_f * X_f$	A.34
<b>q</b> <sub>ScoXbh</sub>	CO <sub>2</sub> emission due to decay of heterotrophics biomass	$kcoX_{bh} * q_{XbhXs}$	A.35
q <sub>ScoXba</sub> Alkalinity	${\rm CO_2}$ emission due to decay of autotrophics biomass	$kcoX_{ba} * q_{XbaXs}$	A.36
QSndSalk	Alkalinity production due to ammonification of soluble organic N	1/14 * q <sub>SndSnh</sub>	A.37
<b>Q</b> SalkXbh	Alkalinity consumption due to growth of heterotrophics biomass	$(i_{xb}/14) * q_{GXbh,aerobic} + (i_{xb}/14 - (1-Y_h)/14 * 2.86Y_h) * q_{GXbh,anoxic}$	A.38
q <sub>SalkXba</sub>	Alkalinity consumption due to growth of autotrophics biomass	$(i_{xb}/14 + 1/7Y_a) * q_{GXba}$	A.39

**Table A.4** Parameter value used for the simulation

ription	Value	Unit	Reference
conversion ratio of pelleted feed	1.42	g dry weight g <sup>-1</sup> fresh weight	Tarigan et al., (2025)
conversion ratio of X <sub>bh</sub>	2	g dry weight $g^{-1}$ fresh weight	Stanley and Jones, (1976)
conversion ratio of X <sub>ba</sub>	2	g dry weight $g^{-1}$ fresh weight	Stanley and Jones, (1976)
ficient of mortality			See Figure C.2 of Tarigan et al.,
			(2024)
aten feed	5 %	-	Assumed
mum growth rate of X <sub>bh</sub>	0.0375	$h^{-1}$	Calibrated
saturation coefficient of S <sub>s</sub>	20	$g COD m^{-3}$	Henze et al., (1987)
saturation coefficient of So for the growth of Xbh	0.2	${ m g~O_2~m^{-3}}$	Henze et al., (1987)
saturation coefficient of S <sub>no</sub>	0.5	g NO <sub>3</sub> -N m <sup>-3</sup>	Henze et al., (1987)
ection factor for X <sub>bh</sub> growth in anoxic condition	2	-	Calibrated
y rate of X <sub>bh</sub>	0.0019	$h^{-1}$	Calibrated
mum uptake rate of X <sub>bh</sub> by fish (X <sub>f</sub> )	0.00042	$h^{-1}$	Calibrated
saturation coefficient of X <sub>bh</sub>	20	$g COD m^{-3}$	Svirezhev et al., (1984)
mum growth rate of X <sub>ba</sub>	0.003	$h^{-1}$	Calibrated
saturation coefficient of S <sub>nh</sub>	1	$g NH_3-N m^{-3}$	Henze et al., (1987)
saturation coefficient of S <sub>o</sub> for the growth of X <sub>ba</sub>	0.4	g O <sub>2</sub> m <sup>-3</sup>	Henze et al., (1987)
y rate of X <sub>bh</sub>	0.00014	$h^{-1}$	Calibrated
mum uptake rate of X <sub>bh</sub> by fish (X <sub>f</sub> )	0.00042	$h^{-1}$	Calibrated
saturation coefficient of X <sub>bh</sub>	20	$g COD m^{-3}$	Svirezhev et al., (1984)
arent digestibility coefficient of organic matter	0.6	-	Tarigan et al., (2025)
rolysis rate	0.0238	g slowly biodegradable COD (g cell COD. $h)^{-1}$	Calibrated
saturation coefficient of hydrolysis of X <sub>s</sub> by X <sub>bh</sub>	0.03	g slowly biodegradable COD (g cell COD) <sup>-1</sup>	Henze et al., (1987)
rield	0.75	g cell COD formed (g COD oxidized) <sup>-1</sup>	Calibrated
o of $X_{bh}$ and $X_{ba}$ decay become non-degradable particulate	0.08		Henze et al., (1987)
ogen content of feed	0.047584	g N (g feed) <sup>-1</sup>	Tarigan et al., (2025)
ogen content of X <sub>bh</sub>	0.0599	g N (g X <sub>bh</sub> COD) <sup>-1</sup>	Tarigan et al., (2025)
ogen content of X <sub>ba</sub>	0.0599	g N (g X <sub>bh</sub> COD) <sup>-1</sup>	Tarigan et al., (2025)
ogen requirement per g COD biomass synthesised	0.0234	g N (g COD) <sup>-1</sup> in biomass	Calibrated
ogen requirement per g COD endogenous biomass nesised	0.06	g N (g COD) <sup>-1</sup> in endogenous biomass	Henze et al., (1987)
nonification rate	0.00001	$m^3 (g COD. h)^{-1}$	Calibrated
ogen retention efficiency in fish body	0.321	-	Tarigan et al., (2025)
tilization coefficient	0.00319	$h^{-1}$	Wolfe et al., (1986)
rield	0.24	g cell COD formed (g N oxidized) <sup>-1</sup>	Henze et al., (1987)
er temperature		°C	See Figure C.1 of Tarigan et al., (2024)
emission	0.00026	$g CO_2 (g fish. h)^{-1}$	Muller and Bauer, (1994)
emission of X <sub>bh</sub> decay		g CO <sub>2</sub> (g biomass decay) <sup>-1</sup>	Snip, (2010)
*			Snip, (2010)
rield er te emi: emi:	mperature	mperature $\begin{array}{c} 0.24 \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$

## Appendix B. Simulation results

Table B.1
Root mean square error (RMSE) and normalise RMSE (NRMSE), which is ratio of RMSE to average observation value, of High-NSP-diet dataset after updating the parameters (see Table B2)

	$X_{\mathrm{f}}$	$S_{nh}$	S <sub>no</sub>	$S_{nd}$	VSS
RMSE	361.1	2.04	2.69	57.02	430.44
NRMSE	6 %	57 %	27 %	23 %	47 %

**Table B.2** Adjusted parameters in the High-NSP-diet tank

Parameters	Initial value	Adjusted value	Units
Y <sub>h</sub>	0.75	0.71	g cell COD formed (g COD oxidized) <sup>-1</sup>
$Y_a$	0.24	0.1	g cell COD formed (g N oxidized) $^{-1}$
$i_{xb}$	0.003	0.004	g N (g COD)-1 in biomass
k <sub>a</sub>	0.00002	0.000003	$m^3 (g COD. h)^{-1}$

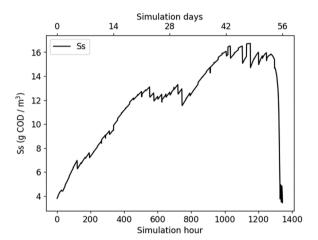


Fig. B.1. Simulation result of  $S_{\text{\tiny S}}$  in the Control-diet tank

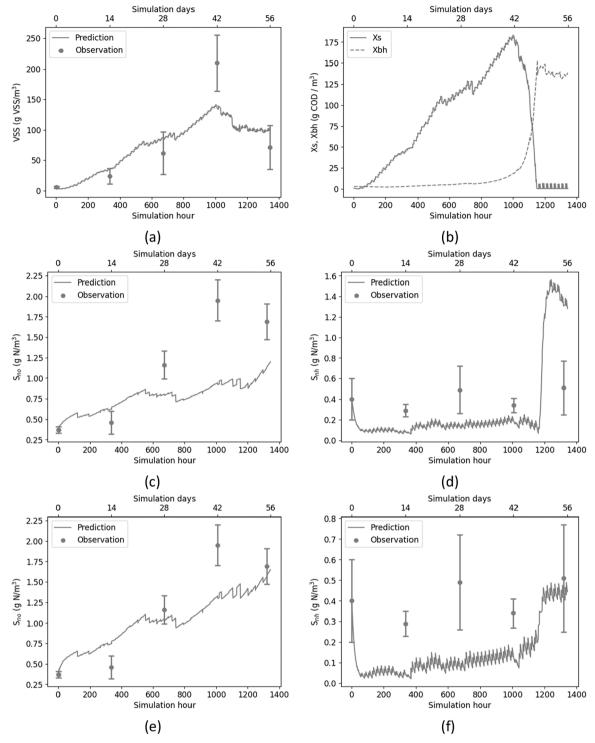


Fig. B.2. Updated model prediction and observation data when  $Y_h = 0.71$  (a. volatile suspended solid (VSS) or biofloc, b. detail component of VSS, c. nitrate + nitrite nitrogen  $(S_{no})$ , d. ammonia nitrogen when  $Y_h$  is 0.71), and when all parameters is adjusted as shown in Table B.2 (e.  $S_{no}$ , f.  $S_{nh}$ ) of the High-NSP-diet datasets

## Data availability

Data will be made available on request.

#### References

Avnimelech, Y., 2009. Biofloc technology: a practical guide book. World Aquaculture Society.

Barbrook-Johnson, P., Penn, A.S., 2022. Causal loop diagrams. In Systems Mapping: How to build and use causal models of systems. Springer International Publishing, Cham, pp. 47–59. https://doi.org/10.1007/978-3-031-01919-7\_4.

Bossier, P., Ekasari, J., 2017. Biofloc technology application in aquaculture to support sustainable development goals. Microb. Biotechnol. 10 (5), 1012–1016. https://doi. org/10.1111/1751-7915.12836.

Boyd, C.E., Tucker, C., McNevin, A., Bostick, K., Clay, J., 2007. Indicators of resource use efficiency and environmental performance in fish and crustacean aquaculture. Rev. Fish. Sci. 15, 327–360. https://doi.org/10.1080/10641260701624177.

- Daigger, G.T., 2011. A practitioner's perspective on the uses and future developments for wastewater treatment modelling. Water Sci. Technol. 63 (3), 516–526. https://doi. org/10.2166/wst.2011.252.
- Davis, T.L., Dirks, B., Carnero, E.A., Corbin, K.D., Krakoff, J., Parrington, S., Lee, D., Smith, S.R., Rittman, B.E., Krajmalnik-Brown, R., Marcus, A.K., 2021. Chemical oxygen demand can be converted to gross energy for food items using a linear regression model. J. Nutr. 151 (2), 445–453. https://doi.org/10.1093/jn/nxaa321.
- de Korte, M., Bergman, J., van Willigenburg, L.G., Keesman, K.J., 2024. Towards a zerowaste aquaponics-centered eco-industrial food park. J. Clean. Prod. 454, 142109. https://doi.org/10.1016/j.jclepro.2024.142109.
- De Schryver, P., Crab, R., Defoirdt, T., Boon, N., Verstraete, W., 2008. The basics of bioflocs technology: the added value for aquaculture. Aquaculture 277 (3-4), 125–137. https://doi.org/10.1016/j.aquaculture.2008.02.019.
- Ebeling, J.M., Timmons, M.B., Bisogni, J.J., 2006. Engineering analysis of the stoichiometry of photoautotrophic, autotrophic, and heterotrophic removal of ammonia-nitrogen in aquaculture systems. Aquaculture 257, 346–358. https://doi. org/10.1016/j.aquaculture.2006.03.019.
- Ekasari, J., Azhar, M.H., Surawidjaja, E.H., Nuryati, S., De Schryver, P., Bossier, P., 2014. Immune response and disease resistance of shrimp fed biofloc grown on different carbon sources. Fish. Shellfish Immunol. 41 (2), 332–339. https://doi.org/10.1016/ i.fsi.2014.09.004.
- FAO, 2024. FishStat: Glob. Prod. Prod. Source 1950–2022 (www.fao.org/fishery/en/statistics/software/fishstati).
- Goddek, S., Espinal, C.A., Delaide, B., Jijakli, M.H., Schmautz, Z., Wuertz, S., Keesman, K. J., 2016. Navigating towards decoupled aquaponic systems: a system dynamics design approach. Water 8 (7), 303. https://doi.org/10.3390/w8070303.
- Henze, M., Grady Jr, C.L., Gujer, W., Marais, G.V.R., Matsuo, T., 1987. A general model for single-sludge wastewater treatment systems. Water Res. 21 (5), 505–515. https://doi.org/10.1016/0043-1354(87)90058-3.
- Jiménez-Montealegre, R., Verdegem, M.C.J., Van Dam, A., Verreth, J.A.J., 2002. Conceptualization and validation of a dynamic model for the simulation of nitrogen transformations and fluxes in fish ponds. Ecol. Model. 147 (2), 123–152. https://doi. org/10.1016/S0304-3800(01)00403-3.
- Kabir, K.A., Verdegem, M.C.J., Verreth, J.A.J., Phillips, M.J., Schrama, J.W., 2020. Dietary non-starch polysaccharides influenced natural food web and fish production in semi-intensive pond culture of Nile tilapia. Aquaculture 528, 735506. https://doi. org/10.1016/j.aquaculture.2020.735506.
- Keesman, K.J., 2011. System identification: an introduction. Springer Science & Business Media
- Li, X., Lei, S., Wu, G., Yu, Q., Xu, K., Ren, H., Wang, Y., Geng, J., 2023. Prediction of pharmaceuticals removal in activated sludge system under different operational parameters using an extended ASM-PhACs model. Sci. Total Environ. 871, 162065. https://doi.org/10.1016/j.scitotenv.2023.162065.
- Mohammadi, F., Bina, B., Rahimi, S., Janati, M., 2022. Modelling of micropollutant fate in hybrid growth systems: model concepts, Peterson matrix, and application to a labscale pilot plant. Environ. Sci. Pollut. Res. 29 (45), 68707–68723. https://doi.org/ 10.1007/s11356-022-20668-2.
- Muller, M. S., & Bauer, C. F. (1994). Oxygen consumption of Tilapia and preliminary mass flows through a prototype closed aquaculture system (No. NASA-TM-111882).
- Pinho, S.M., de Lima, J.P., Tarigan, N.B., David, L.H., Portella, M.C., Keesman, K.J., 2023. Modelling FLOCponics systems: Towards improved water and nitrogen use

- efficiency in biofloc-based fish culture. Biosyst. Eng. 229, 96–115. https://doi.org/10.1016/j.biosystemseng.2023.03.022.
- Ribeiro, J.M., Conca, V., Santos, J.M., Dias, D.F., Sayi-Ucar, N., Frison, N., Oehmen, A., 2022. Expanding ASM models towards integrated processes for short-cut nitrogen removal and bioplastic recovery. Sci. Total Environ. 821, 153492. https://doi.org/ 10.1016/j.scitotenv.2022.15349.
- Schveitzer, R., Arantes, R., Costódio, P.F.S., do Espírito Santo, C.M., Arana, L.V., Seiffert, W.Q., Andreatta, E.R., 2013. Effect of different biofloc levels on microbial activity, water quality and performance of Litopenaeus vannamei in a tank system operated with no water exchange. Aquac. Eng. 56, 59–70. https://doi.org/10.1016/j.aquaeng.2013.04.006.
- Serpa, D., Pousão-Ferreira, P., Caetano, M., da Fonseca, L.C., Dinis, M.T., Duarte, P., 2013. A coupled biogeochemical-Dynamic Energy Budget model as a tool for managing fish production ponds. Sci. Total Environ. 463, 861–874. https://doi.org/10.1016/j.scitotenv.2013.06.090.
- Serra, F.P., Gaona, C.A., Furtado, P.S., Poersch, L.H., Wasielesky, W., 2015. Use of different carbon sources for the biofloc system adopted during the nursery and growout culture of Litopenaeus vannamei. Aquac. Int. 23, 1325–1339. https://doi.org/ 10.1007/s10499-015-9887-6.
- Snip, L., 2010. Quantifying the greenhouse gas emissions of wastewater treatment plants [MSc Thesis. Wageningen University & Research]. Wageningen University & Research Library. https://edepot.wur.nl/138115.
- Stanley, J.G., Jones, J.B., 1976. Feeding algae to fish. Aquaculture 7 (3), 219–223. https://doi.org/10.1016/0044-8486(76)90140-X.
- Svirezhev, Y.M., Krysanova, V.P., Voinov, A.A., 1984. Mathematical modelling of a fish pond ecosystem. Ecol. Model. 21 (4), 315–337. https://doi.org/10.1016/0304-3800 (84)90066-8.
- Tarigan, N.B., Amal, M.J. r, Ekasari, J., Keesman, K.J., Verdegem, M., 2025. Nitrogen, phosphorus, and carbon dynamics in biofloc system of Nile tilapia fed with high non-starch polysaccharides diet. Aquaculture 596. https://doi.org/10.1016/j.aquaculture.2024.741714.
- Tarigan, N.B., Goddek, S., Keesman, K.J., 2021. Explorative study of aquaponics systems in Indonesia. Sustainability 13 (22), 12685. https://doi.org/10.3390/su132212685.
- Tarigan, N.B., Verdegem, M., Ekasari, J., Keesman, K.J., 2024. Nutrient flows in biofloc-Nile tilapia culture: A semi-physical modelling approach. Biosyst. Eng. 248, 108–129. https://doi.org/10.1016/j.biosystemseng.2024.09.021.
- Tinh, T.H., Momoh, T.A., Kokou, F., Hai, T.N., Schrama, J.W., Verreth, J.A., Verdegem, M.C., 2021. Effects of carbohydrate addition methods on Pacific white shrimp (*Litopenaeus vannamei*). Aquaculture 543, 736890. https://doi.org/10.1016/ j.aquaculture.2021.736890.
- Verdegem, M., Buschmann, A.H., Latt, U.W., Dalsgaard, A.J., Lovatelli, A., 2023. The contribution of aquaculture systems to global aquaculture production. J. World Aquac. Soc. 54 (2), 206–250. https://doi.org/10.1111/jwas.12963.
- Vinasyiam, A., Kokou, F., Ekasari, J., Schrama, J.W., Verdegem, M.C., 2023. Effects of high wheat bran input on the performance of a biofloc system for Pacific white shrimp (*Litopenaeus vannamei*). Aquac. Rep. 33, 101853.
- Wolfe, J.R., Zweig, R.D., Engstrom, D.G., 1986. A computer simulation model of the solar-algae pond ecosystem. Ecological modelling 34 (1–2), 1–59. https://doi.org/ 10.1016/0304-3800(86)90078-5.