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Plasticity in colloidal gel strands

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Colloidal gels are space-spanning networks of aggregated particles. The mechanical response of colloidal gels is governed, to a large extent, by the properties of the individual gel strands. To study how colloidal gels respond to repeated deformations, we perform Brownian Dynamics simulations on single strands of aggregated colloidal particles. While current models assume that gel failure is due to the brittle rupture of gel strands, our simulations show that gel strands undergo large plastic deformations prior to breaking. Rearrangement of particles within the strands leads to plastic lengthening and softening of the strands, which may ultimately lead to strand necking and ductile failure. This failure mechanism occurs irrespective of the thickness and length of the strands and the range and strength of the interaction potential. Rupture of gel strands is more likely for long and thin strands and for a long-ranged interaction potential.

I. Introduction

Upon introducing an attractive interaction colloidal particles can aggregate and form a space-spanning network of dynamically arrested particles [1, 2]. Such a network, called a colloidal gel, behaves as an elastic solid that is able to withstand mechanical stress. Yet, when the applied stress exceeds the yield stress, the gel fluidizes and/or fractures and flows like a liquid [3–9]. This combination of properties makes colloidal gels interesting for a variety of applications, including food products, cosmetics, and scaffolds for tissue engineering [10–14].

The macroscopic properties of colloidal gels, such as their elasticity and yielding behaviour, are intimately linked to the structure and connectivity of the particle network at the microscale [15–17]. The main control parameters that determine the structure of a colloidal gel are the magnitude of the attraction strength between the particles [18–22], the particle volume fraction [18, 21, 22], and the shear history of the gel [23–25]. In the limit of very strong attraction and very low volume fraction, irreversible aggregation leads to the formation of dilute, diffusion-limited fractal gels [18]. In this regime, the mechanics and dynamics of the gel can be described using scaling approaches or by simulation models based on percolating networks of gel strands that ignore the internal structure of the strands [26–29]. However, when the attraction strength is only a few times the thermal energy $k_B T$, particle rearrangements can occur within the gel, leading to a much coarser gel structure formed by spinodal decomposition [19, 20]. The interplay between phase separation through spinodal decomposition and kinetic arrest then leads to very heterogeneous gels. As long as the volume fraction of particles is not too high (i.e. significantly below the colloidal glass transition), the microstructure of these gels consists of interconnected gel strands with a length and thickness that depends strongly on the interaction potential and the volume fraction [21, 22].

The linear elasticity of colloidal gels can be understood by considering the colloidal gel as a random network of gel strands, with an effective spring constant that depends on the thickness of the strands [30]. However, the non-linear response of colloidal gels remains much less clear. Fracture and yielding of colloidal gels have been attributed to the brittle-like rupture of individual gel strands due to force-activated breaking of inter particle bonds [30, 31]. However, several authors have shown evidence that this picture may not be very accurate, and that failure of colloidal gels is preceded by significant plastic particle rearrangements [32–34]. Recently we have shown, using a combination of rheological experiments and computer simulations, that these plastic rearrangements within gel strands lead to irreversible strand stretching and build-up of excess length, or slack, rather than strand rupture. [35]

Our results also suggested that the rheological response of colloidal gel networks can be understood by considering the mechanical and dynamic properties of the individual gel strands, which form the basic structural units of the gel (at least, at moderate volume fractions). To relate rheology to the structure of the colloidal gel, it is therefore necessary to know how the response of a gel strand depends on its thickness and length and on the interaction potential between the particles. Here, we will study this relation using computer simulations of gel strands under repeated deformation.

II. Method

We perform Brownian Dynamics simulation to study the effect of repeated deformation on individual gel strands. We consider colloidal particles that interact through a Morse potential [36]:

$$\beta u(r) = \beta \epsilon \exp(\rho_0[a - r]) (\exp[\rho_0(a - r)] - 2) \quad (1)$$

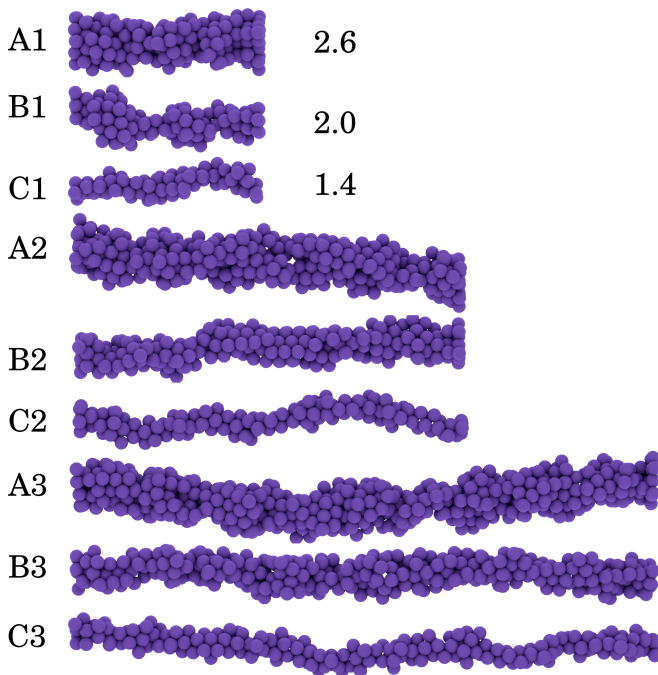


FIG. 1. Visual representation of A) thick, B) intermediate and C) thin strands before deformation. A_2, B_2 and C_2 , show strands that are 2x longer compared to A_1, B_1 and C_1 , whereas A_3, B_3 and A_3 are 3x longer compared to the shortest strands. The average thickness of the start configurations $\langle D_0 \rangle$ (expressed in particle diameters) is indicated next to the strands (see equation 4).

with $\beta = 1/k_B T$, ϵ the depth of the energy minimum and a the particle diameter. The parameter ρ_0 specifies the width of the interaction [37]. The different potentials used in the paper are shown in SI Fig. 1[†].

The motion of a particle i with position \mathbf{r}_i is obtained by solving the overdamped Langevin equation:

$$\dot{\mathbf{r}}_i(t) = \beta D_0 [-\nabla_i U(t)] + \sqrt{2D_0} \boldsymbol{\xi}_i(t) \quad (2)$$

where $\boldsymbol{\xi}_i(t)$ is random white noise, sampled with zero mean and unit variance, to model the thermal fluctuations of the particles. $D_0 = k_B T / \zeta_f$ is the short-time diffusion coefficient with ζ_f the friction coefficient, set to unity. The time step δt for the numerical integration is set to $\delta t = 1 \times 10^{-6} \tau_B$, where $\tau_B = a^2 / D_0$ is the Brownian time scale, which defines the unit of time in our simulations.

Gel strands are formed between two attractive flat walls. The parameters for the particle-wall interaction are the same as those for the particle-particle interactions, to make this interaction as inert as possible. The simulation box is periodic in the y- and z direction. The initial configuration of the gel strands is formed by placing a number of particles on a face centered cubic (fcc) lattice in a certain $H \times W \times L$, with H , W , and L the height, width, and length, respectively, expressed in numbers of particles. We consider nine types of gel strands

that vary in thickness and length. For a thick gel strand, $H = W = 5$ particles (type A), for intermediate gel strands, $H = W = 4$ (type B), and for thin gel strands, $H = W = 3$ (type C). For each strand thickness, we consider three different lengths (specified as 1, 2, and 3), which gives the following number of particles for the different configurations: $A_1 = 200$, $B_1 = 128$, $C_1 = 77$, $A_2 = 400$, $B_2 = 256$, $C_2 = 144$, $A_3 = 600$, $B_3 = 384$ and $C_3 = 216$. The equilibration time before applying oscillatory deformation is set to $t = 568 \tau_B$. As distances between particles in the initial configuration are larger than the range of the potential, particles aggregate randomly. Thus, the initial fcc lattice affects the approximate thickness of the gel strand but does not influence how particles are structured after equilibration. In Fig. 1 examples of these equilibrated gel strands are shown. The average thickness for each type of strand before deformation $\langle D_0 \rangle$ expressed in particle diameters equals 2.6, 2.0 and 1.4, respectively (see also equation 4 below).

After equilibration, the gel strand is deformed through 14 oscillations in which the distance between the two walls is varied in a cyclic manner by moving the position of the left wall outwards. This leads to a sawtooth strain profile with a maximum strain $\gamma_{max} = 0.04$ and a fixed strain rate $\dot{\gamma} = 0.00284 \tau_B^{-1}$. Data for different amplitudes and strain rates are shown in the SI (Fig. 6 and 7). To make sure that observations are statistically relevant, each data point contains simulation data for at least 30 different gel strands. Here, we only consider strands that stay intact during the entire deformation.

III. Results and discussion

We cyclically deform the gel strands at constant strain rate and measure the resulting force f exerted on the walls. For strain cycles at small amplitude ($\gamma_{max} = 0.005$), the force increases linearly with deformation, with a spring constant that increases with the strand thickness (SI Fig. 2). However, for larger amplitude ($\gamma_{max} = 0.04$), the force-strain curves are highly non-linear for all gel strands and show a pronounced hysteresis loop (Fig. 2a), which indicates significant energy dissipation during the deformation cycles. The dissipated energy is highest in the first deformation cycle (Fig. 2b), which is found to differ qualitatively from the subsequent cycles: the force first increases with increasing strain until a threshold value is reached, after which it levels off. This plateau in the force indicates plastic flow inside the gel strand due to irreversible particle rearrangements. The threshold force for plastic flow is proportional to the cross-section of the strands (SI, Fig. 3a), and increases with increasing strain rate (SI, Fig. 7), in agreement with models based on Kramers theory for force-activated dissociation of particle-particle bonds [38]. As we have shown pre-

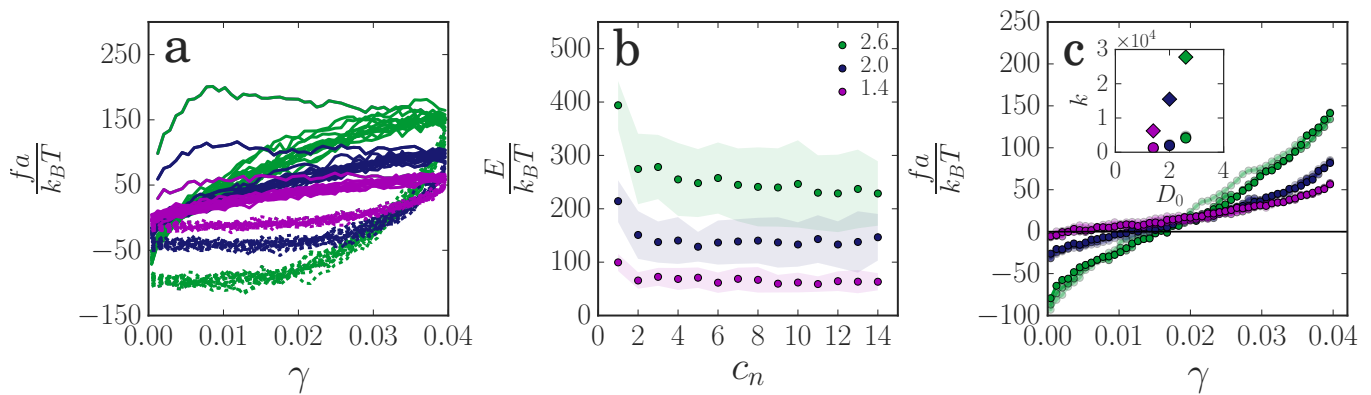


FIG. 2. (a) Force-strain curves upon 14 oscillatory expansions of gel strands of different diameter ($\gamma_{max} = 0.04$). The solid line indicates the loading- and the dotted line the unloading curve. (b) Dissipated energy per oscillation c_n , obtained by integration of the force-strain curves. The shaded area indicates the standard deviation. (a) and (b) contain data of the longest gel strands ($A_3 - C_3$) (c) Average elastic force of the 3th, 4th and 5th oscillation cycle for gel strands of different diameter and length ($\gamma_{max} = 0.04$). The color gradient indicates the length of the strands from short (light) to long (dark). The inset shows the spring constant k (units $k_B T a^{-1} \gamma^{-1}$) for the different strands at a deformation of $\gamma_{max} = 0.04$ (\circ) and $\gamma_{max} = 0.005$ (\diamond).

viously [35], the plastic rearrangements are associated with the irreversible stretching of the gel strand and the build-up of slack. Here, slack is defined as excess length that is created due to lengthening of the strands. This softens the gel strand, so that in subsequent cycles the observed force is lower than in the first cycle. The force-strain curve then quickly reaches a limit cycle, with an enclosed area that accounts for the viscoelastic dissipation due to reversible particle rearrangements. The dissipated energy is highest for the thick gel strands and lowest for the thin strands (Fig. 2b). As shown in SI Fig. 3b, the dissipated energy is roughly proportional to the cross-section A of the strands, with each particle contributing 3-4% of the interaction energy ϵ to the energy dissipation. Increasing the strain amplitude from $\gamma_{max} = 0.04$ to $\gamma_{max} = 0.06$ (SI, Fig. 6) results in a single particle contribution of 5-6% of ϵ to the dissipated energy. The total energy dissipation thus scales with the applied strain amplitude and with the interaction energy.

To analyze the softening of the gel strands in more detail, we disentangle the elastic and viscous contributions to the measured response by averaging the loading and unloading curve for each cycle [39]. This averages out the viscous contribution, so that only the elastic contribution remains. The resulting elastic force goes through zero at a finite strain (Fig. 2c), which reflects the increase in the rest length due to the expansion cycles. The relative increase in rest length is highest for the thick strands (approximately 1.7%) and smallest for the thin strands ($\sim 0.3\%$), indicating that thicker strands have more possibilities to deform plastically.

The plastic stretching of the gel strand leads to the build-up of slack. In subsequent deformation cycles, the slack induced in previous cycles is pulled out first, which results in little resistance and a strong decrease in the

effective spring constant. Indeed, the effective spring constants measured after deforming the gel at a strain $\gamma_{max} = 0.04$ is significantly smaller than those measured in the linear deformation regime ($\gamma_{max} = 0.005$) (inset Fig. 2c). When the strain amplitude of the cycles becomes larger, the accumulated slack increases so that the effective spring constant decreases even further [35] (see SI, Fig. 6). As expected, the spring constant increases with strand thickness and is approximately proportional to the cross-section of the strands (SI, Fig. 3c), indicating that each inter-particle bond contributes roughly equally to the spring constant.

As the rest length of the gel strands increases in the loading cycle, it must be compressed in the return cycle. This could lead to bending or buckling of the strand. To investigate this, we follow the contour of the gel strand during the deformation cycles. We do this by dividing the strand into equally sized bins ($\sigma = 0.9$) and calculating the average coordinates in each bin [40]. Since the ends of the strand are not fixed in our simulation, the strand fluctuates significantly, both during the deformation cycles and in rest (Fig. 3a). To analyze the shape of the strand and the amount of bending that occurs, we draw a line through the two ends of the strand and calculate the local distance of the contour from this straight line for each bin. The average distance over all bins α (Fig. 3b) is a measure for how much the shape of the gel strand deviates from a straight line, and indicates bending of the strand. For a gel strand that is not deformed, α does not change significantly, indicating that the shape of the gel strand remains more or less the same. However, when the gel strands are deformed α increases gradually with each deformation cycle, indicating that the strands must bend more to accommodate the increase in rest length. The increase in α is more pronounced for the

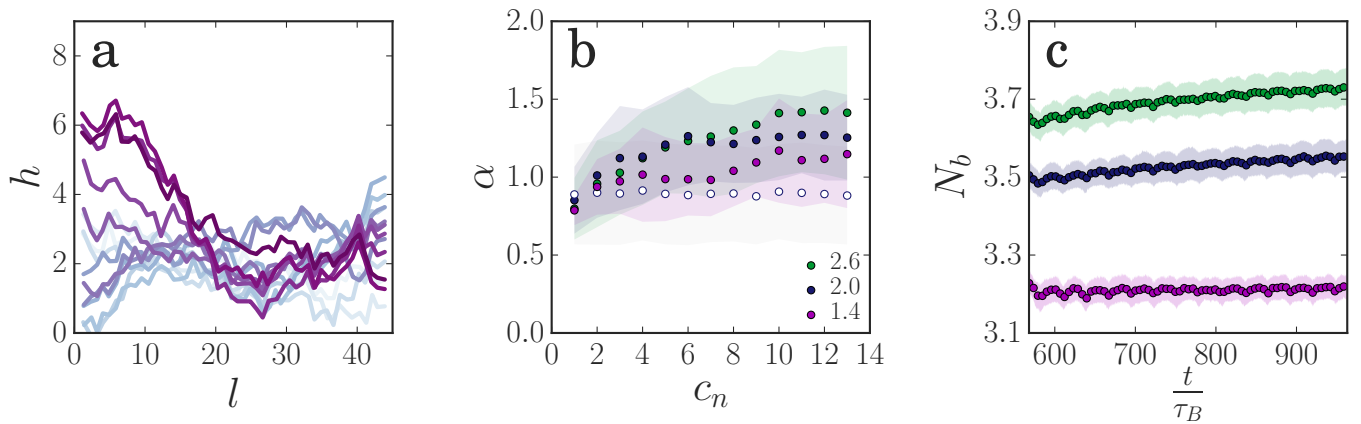


FIG. 3. (a) Projected 3D coordinates of a single gel strand (B_3 , $\gamma_{max} = 0.04$) at the start of each oscillation (cycle number increases from light blue to dark purple). The height (h) and length (l) of the strand are both represented in dimensions of particle diameter a . (b) The deviation from a straight configuration α as function of oscillation cycle c_n ($A_3 - C_3$). Open markers represent an undeformed gel strand (zero measurement). (c) Average number of bonds per particle in time ($A_2 - C_2$).

thicker gel strands, which is in agreement with our observation that the thick strands show a larger increase in rest length upon deformation [41]. Thus, thick strands are more prone to plastically elongate and develop slack, thereby contributing more strongly to this unusual non-linear response.

The internal rearrangements in the gel strands lead to the breaking and reformation of inter-particle bonds. Surprisingly, the average number of bonds per particle N_b increases as the strands are deformed and become longer (Fig. 3c). This suggests that the applied deformation leads to accelerated aging and coarsening of the gel strand, driving it gradually into a more favorable state by forming more inter-particle bonds [25, 42]. A similar strain-induced increase of the number of inter-particle bonds has been seen in computer simulations [43] and in experiments [24] on colloidal gel networks. We note that the strain-induced increase in the number of bonds is more pronounced and continues for a longer period as the gel strands get thicker (see also SI, Fig. 8b where data for even thicker gel strands are shown). This is further confirmed by the dissipated energy per cycle, which takes much longer to reach a plateau for thicker strands (SI, Fig. 8a). Again, this indicates that thick strands have more possibilities for local particle rearrangements and plastic deformation than thinner strands. The overall coarsening must imply that the deformation of the strands upon stretching occurs heterogeneously, so that thicker regions can form that are connected by thinner sections. This is reminiscent of the Rayleigh-Plateau instability in liquid jets (see Fig. 4b), and highlights the arrested liquid state of the colloidal gel. We further note that, even though the total number of bonds gradually increases, the force sustained by the strand does not increase. Our data suggests that this is because these newly formed bonds only stiffen the parts of the gel strand that

are already strong, while the overall stiffness is determined mainly by the weak regions. A similar conclusion was obtained in recent computer simulations on large gel networks [43].

We can further quantify the heterogeneity of the internal rearrangements by considering the displacement for each particle during a deformation cycle c_n :

$$m_i(c_n) = \frac{1}{\mathcal{N}_i a^2} \sum_{j=1}^{\mathcal{N}_i} \langle (\mathbf{r}_{ij}(0) - \mathbf{r}_{ij}(t))^2 \rangle_n \quad (3)$$

where $\mathbf{r}_{ij}(0)$ and $\mathbf{r}_{ij}(t)$ denote the separation vector between particle i and neighbouring particles j at the start of the cycle and after a time t , respectively, and \mathcal{N}_i is the number of nearest neighbours of particle i . Here, the average is taken over the entire oscillation.

As shown in Fig. 4, particles in thin strands on average rearrange over larger distances compared to particles in thick strands. Upon deformation, many particles in a thin strand participate in movement, whereas only a few particles in the thicker strands move. Note, that the displacements of the particles contain both the elastic and plastic contributions. From the rest length of the strands we know that thick strands lengthen more and have a higher plastic deformation. Here, we see that these plastic deformations are indeed very heterogeneous and strongly localized to certain regions in the gel strand. The same heterogeneity is seen in thin strands, but these strands are also largely elastically deformed. The strong strain localization leads to the formation of thin necks, where the strand will eventually rupture.

We also monitor strand rupture in our simulations and find that the percentage of broken gel strands increases strongly with increasing strand length and decreasing strand thickness (Fig. 5a). Long strands break more easily, because the probability that a weak spot forms

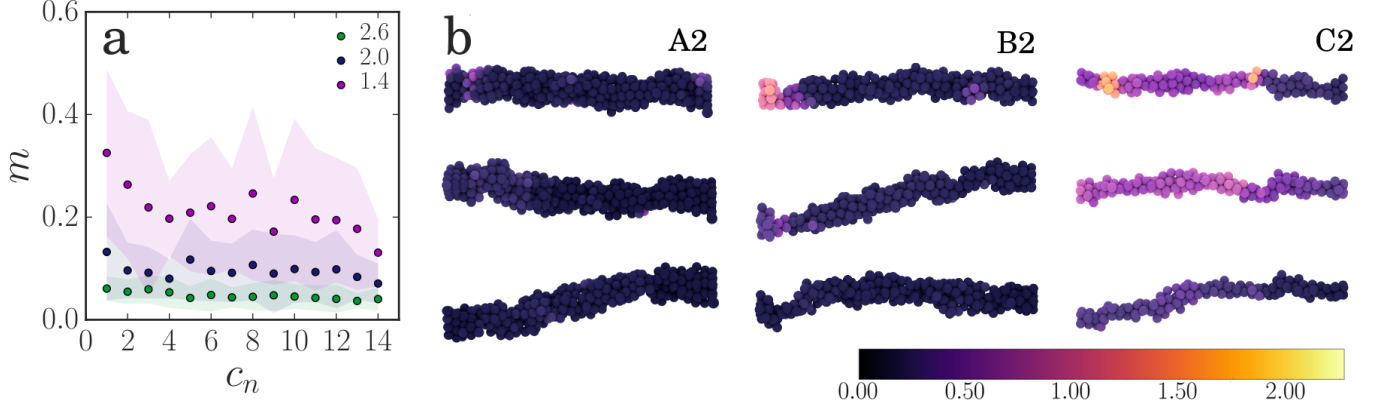


FIG. 4. (a) Average mobility of the particles per oscillation (for strand types $A_2 - C_2$). (b) Visual representation of particle displacements, highlighting the heterogeneity of the strain. The depicted strands are from oscillation cycle 1, 7 and 14 respectively.

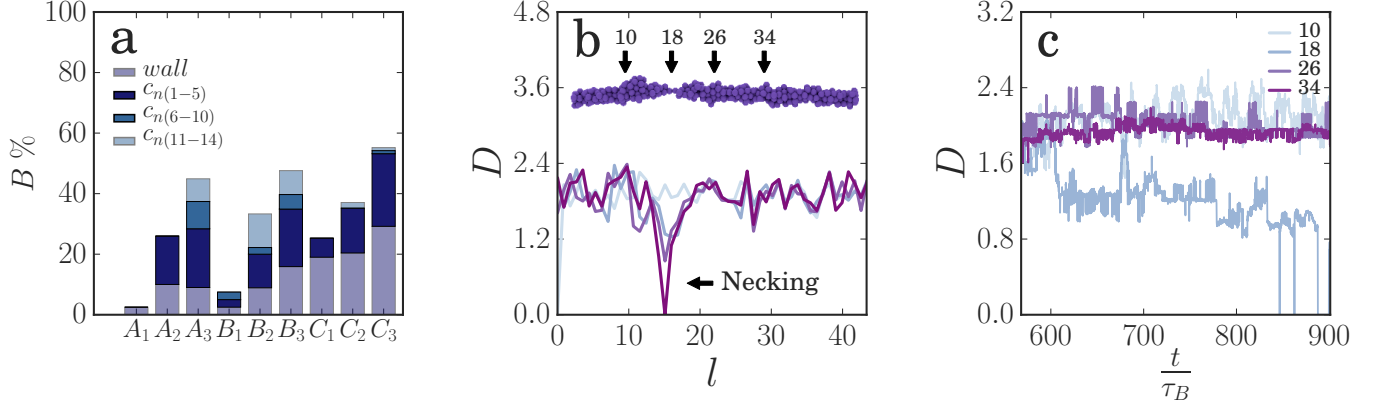


FIG. 5. (a) Breakage statistics for gel strands of different sizes ($\gamma = 0.04$), separated into strands that detach from the wall or break into clusters. To specify the moment of failure, breakage is categorized into oscillation cycle intervals. (b) Thickness D as a function of the length of a strand (B_3 , $\langle D_{start} \rangle = 2.0$, $\gamma_{max} = 0.04$) plotted in time (568-928 τ_B , colored from light to dark) (c) Thickness D in time for different segments of the strand in plot (b).

during the deformation increases as strands get longer. Thin strands are held together by fewer inter-particle bonds, making them more prone to breakage. For the longest gel strands, the moment of rupture appears to shift to longer times as the strands get thicker: most of the thin strands (C_3) rupture in the first cycles, while for the thicker strands (A_3) rupture occurs more frequently in the later cycles, probably because more plastic deformation is needed before a sufficiently weak spot is formed. For the shorter strands, we do not observe such a trend, but this could be due to poor statistics, as the number of broken strands is much smaller for short chains. The fraction of broken gel strands also increases strongly with increasing strain amplitude (SI, Fig. 6), and with increasing strain rate (SI, Fig. 7), the latter indicating a

transition to a more brittle response at higher rates due to fewer possibilities for plastic rearrangements [35]. In the breakage statistics we specifically show the amount of breakage at the walls. This breakage does not dominate. Only for thin gel strands we see that the connection with the wall becomes a weak spot. We note that failure at the walls of the container is also observed experimentally in the yielding of some colloidal gels [5, 6].

To follow the ductile deformation leading to strand rupture, we consider the local thickness of the gel strand by dividing the strand into a number of segments and calculating the root-mean square thickness in each seg-

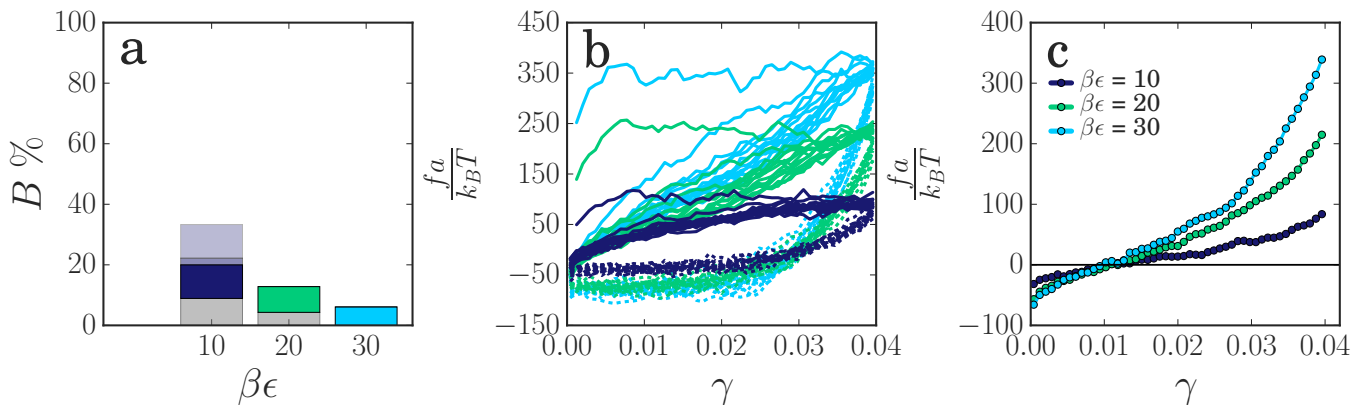


FIG. 6. (a) Breakage statistics for gel strands at different interaction energies. We distinguish breakage at the wall (gray) and breakage into clusters at oscillation cycles interval 1-5, 6-10 and 11-14 (dark till light) respectively. (b) Force-strain curves of 14 subsequent oscillatory deformations. (c) Average elastic force of the 3th, 4th and 5th oscillation cycle.

ment [44]:

$$D(x) = \frac{1}{N_x r_a} \sum_{k=1}^{N_x} \sqrt{(r_k(x) - r_{mean}(x))^2} \quad (4)$$

where r_{mean} is the average coordinate of the particles in a specific segment, r_k is the position of particle k in this segment (projected onto the xz -plane of the average coordinate), N_x equals the total number of particles per segment and r_a is the radius of the particles. We plot the local thickness along the gel strand for different times (Fig. 5b). Before the deformation cycles, the thickness is quite uniform along the strand. However, as the deformation cycles continue, a necking region arises locally. This necking region forms rather abruptly, as shown in Fig. 5c, where the thickness for a few locations along the gel strand (see arrows Fig. 5b) is plotted as a function of time. This rapid decrease in local thickness finally results in breakage of the gel strand.

The necking process leading to strand fracture raises the question whether strand rupture occurs at pre-existing defects in the gel strands, formed during gel formation as suggested previously [30], or at random locations along the strand where plastic deformations happen to localize during deformation of the gel. In other words, is there a correlation between the thinnest region of the gel strand before deformation and the location where the strand finally breaks? To test this, we deform the initial configurations of 15 strands multiple times and monitor the initial thickness at the location where the strand is found to break. We find that the strand is indeed more likely to break at a thin region: the average initial thickness at the location of rupture, normalized by the average strand thickness, $\langle D_{break} \rangle / \langle D_0 \rangle$ is 0.74, 0.82 and 0.82 for the thick, intermediate, and thin strands, respectively. Thus, strain localization and subsequent strand rupture tend to occur predominantly in low density regions of gel strands.

In 46 % of the cases, thick strands break at the thinnest part D_{min} of the start configuration. For intermediate and thin strands, this is only 37 % and 18 %, respectively. It can be concluded, therefore, that thick strands are more likely to break at a weak spot or defect in the original strand, while thin strands tend to break at more random locations. Previously, we noted that in thick strands only a few particles have large rearrangements at the weak spots. As a result, the initial structure of these strands is more likely to determine where failure will occur, in line with previous work [30].

Now that we have shown how the thickness and length of colloidal gel strands affect their mechanical and plastic response, we consider the effect of the interaction potential between the particles (for potentials see SI Fig. 1). Increasing the attraction strength between the particles makes the strands more resistant to rupture, as indicated by a lower percentage of broken strands (Fig. 6a). The force-strain relations for the different interaction energies show a similar plastic flow regime in the first deformation cycle, with a threshold force for plastic flow that increases approximately proportionally to the attraction strength (Fig. 6b). These findings are in agreement with theoretical models based on Kramers theory for force-activated bond rupture, which predict a rupture probability that decreases exponentially with the interaction strength and a threshold force that, for a given strain rate, is proportional to the effective spring constant and thus to the attraction strength ϵ [4, 38, 45]. From the elastic contribution to the force, we observe that the change in rest length induced by the deformation cycles does not depend on the attraction strength (Fig. 6c). This indicates that the mechanism by which colloidal gels weaken due to local plasticity does not depend on the strength of the interaction, even when this attraction strength is as large as $30 k_B T$. This

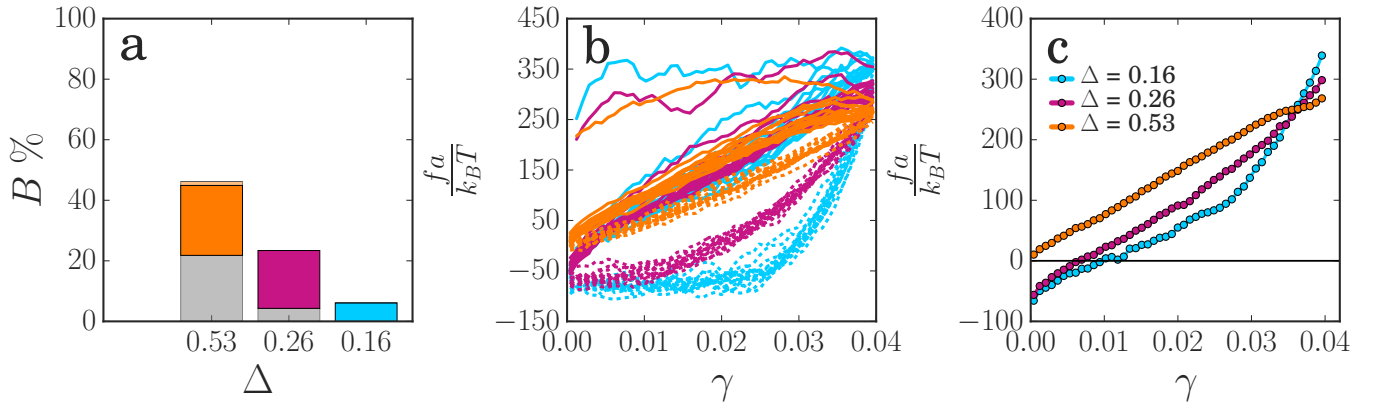


FIG. 7. (a) Breakage statistics for gel strands with different well widths $\Delta = 0.53, 0.26$ and 0.16 ($\beta\epsilon = 30$). (b) Force-strain curves of 14 subsequent oscillatory deformations. (c) Average elastic force of the 3th, 4th and 5th oscillation cycle.

is further confirmed by the amount of particle displacements, which is nearly independent of the attraction strength (SI Fig. 4a), and the total dissipated energy in the cycles, which is proportional to the attraction strength (SI Fig. 4b). The spring constant of the strands after the deformation cycles increases with increasing attraction energy (Fig. 6c), and after rescaling with ϵ , we find that the elastic contribution to the force is proportional to ϵ (SI Fig. 4c).

In addition to varying the strength of the interactions, we also change the range of the attraction by changing the range parameter ρ_0 , giving well widths of approximately $\Delta = 0.528 a, 0.264 a$, and $0.160 a$ (for $\rho_0 = 10, 20$, and 33 respectively) (see SI Fig. 1). This is an interesting property to vary as the range over which interactions are sticky influences the deformation of the strands. Note that for simulations of a full colloidal gel a given pair potential and volume fraction ϕ gives an average length and thickness distribution of the gel strands. Here, we try to uncouple these two, by looking at strands of a single length and thickness with different pair potentials. To a certain extent this gives some 'artificial' effects, as in real gels the potential width and network structure are coupled. Still, we can show some interesting observations.

We find that increasing the range of the attraction makes the strands more prone to rupture (Fig. 7a). However, note that due to a larger potential width strands are aged substantially more (see SI Fig. 5) and thus contain a higher number of weak spots.

The force-strain curves again look similar, showing a plastic flow regime in the first cycle. The threshold force for plastic deformation appears to be rather insensitive to the range of the attraction, while the amount of dissipated energy increases significantly as the attraction range decreases (SI Fig. 5), reflecting a higher number of broken bonds. When looking at the elastic component of the force-strain curve for the deformed strands (Fig. 7c),

we find a much larger increase in rest length for the shorter-ranged attraction. We thus conclude that plastic deformation, leading to strand stretching and softening, is more pronounced in gels with a short-ranged attraction, while a gel with long-ranged attraction only shows a linear deformation response at $\gamma_{max} = 0.04$.

Note also that the stiffness of the deformed gel strands, as indicated by the slope of the force-strain curves in Fig. 7c, becomes almost independent of the attraction range. This might seem surprising, as the stiffness of a single bond is given by the second derivative of the potential, $k \sim \epsilon \rho_0^2 \sim \epsilon / \Delta^2$, so that one would expect the highest stiffness for the smallest well width. Yet, we know that for small Δ the strand is plastically deformed and softening occurs, resulting in a decrease of the spring constant in the linear regime. The effective resulting stiffness is set by the threshold force f^* where the plastic flow regime starts, $k_{eff} \approx f^* / \gamma_{max}$.

Conclusions

Our results highlight how failure and yielding of colloidal gels result from plasticity at the scale of individual gel strands. While previous models for colloidal gel rheology and failure were based on the brittle rupture of gel strands, we show that this rupture is preceded by significant plastic deformations that cause irreversible lengthening and softening of gel strands. We observe this mechanism of failure for strands of different length and thickness and for interaction potentials of different strength and range, suggesting that it should be relevant for a wide range of experimental colloidal systems. Recently, we showed experimental results that support this finding [35]. Our findings are also in agreement with earlier experiments that showed a two-step yielding in colloidal gels under shear [32]; here, the first yielding

event was attributed to restructuring and effective lengthening of gel elements in the shear direction, while the second step was attributed to strand rupture. Our results underpin this hypothesis and provide a microscopic mechanism. Furthermore, our results indicate that the amount of plastic deformation that a gel can undergo before it ruptures is determined by the structure of the gel and by the interaction potential. Coarser gels, consisting of short and thick gel strands, will deform much more plastically than dilute gels with long and thin strands. Plasticity is also promoted by a large attraction strength and a short attraction range. Our simulations have focused on single gel strands. While our recent results have shown that the macroscopic rheological properties of a colloidal gel can indeed be linked to the properties of the individual strands that constitute the gel [35], it remains an open question how the network topology influences the non-linear response. Combining our results for single strands with a full characterization of the network structure may be a first step towards a fully predictive model for colloidal gel rheology.

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Electronic Supplementary Information to "Plasticity in colloidal gel strands"

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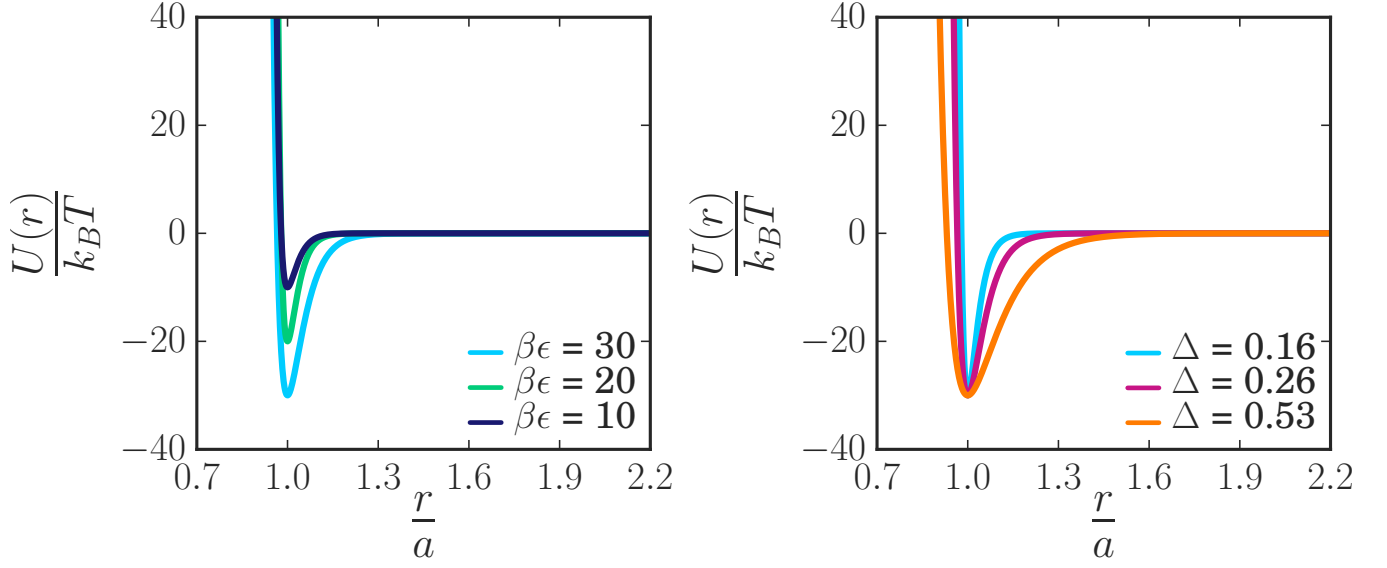


FIG. 1: (left) Morse potential with different depths of the potential, $\beta\epsilon = 10, 20$ and 30 respectively. (right) Morse potential ($\beta\epsilon = 30$) with different well widths corresponding to $\Delta = 0.16, 0.26$ and 0.53 a ($\rho_0 = 33, 20$ and 10).

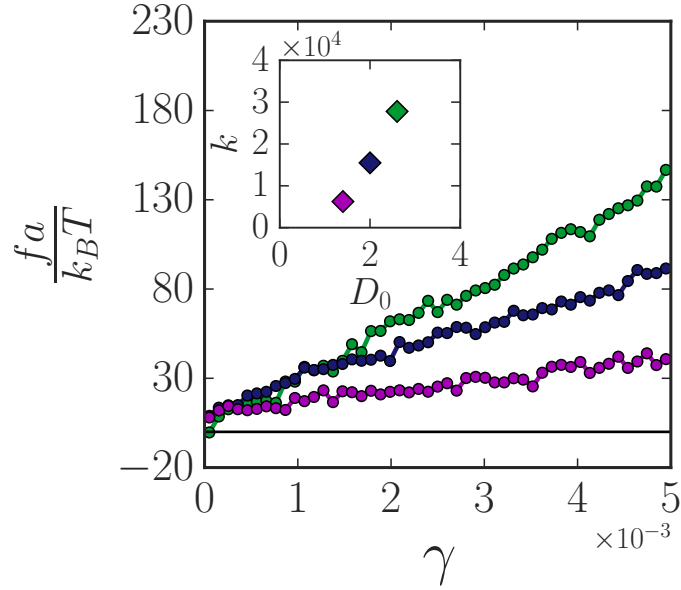


FIG. 2: Average elastic force of the 3th, 4th and 5th oscillation cycle for gel strands of different diameter ($A_3, B_3, C_3, \gamma_{max} = 0.005$). The inset shows the spring constant k (units $k_B T a^{-1} \gamma^{-1}$) for the different strands at a deformation of $\gamma_{max} = 0.005$ (\diamond).

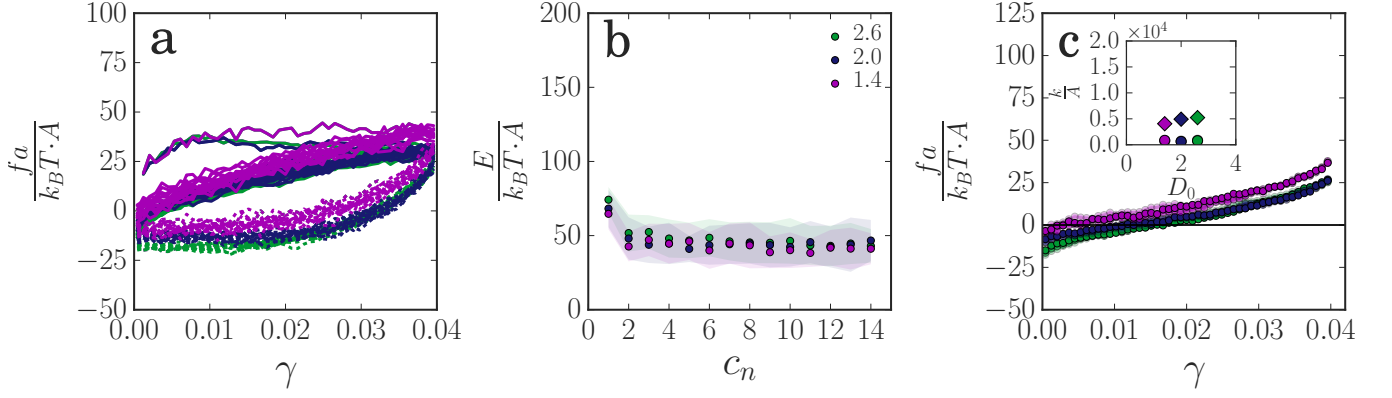


FIG. 3: All data is normalized by the cross-section $A = \pi \cdot (\frac{D_0}{2})^2$ of the strands. (a) Force-strain curves upon 14 oscillatory expansions of gel strands of different diameter ($\gamma_{max} = 0.04$). The solid line indicates the loading- and the dotted line the unloading curve. (b) Dissipated energy per oscillation c_n , obtained by integration of the force-strain curves. The shaded area indicates the standard deviation. (a) and (b) contain data of the longest gel strands ($A_3 - C_3$). (c) Average elastic force of the 3th, 4th and 5th oscillation cycle for gel strands of different diameter and length ($\gamma_{max} = 0.04$). The color gradient indicates the length of the strands from short (light) to long (dark). The inset shows the spring constant k (units $k_B T \cdot a^{-1} \cdot \gamma^{-1}$) for the different strands at a deformation of $\gamma_{max} = 0.04$ (\circ) and $\gamma_{max} = 0.005$ (\diamond).

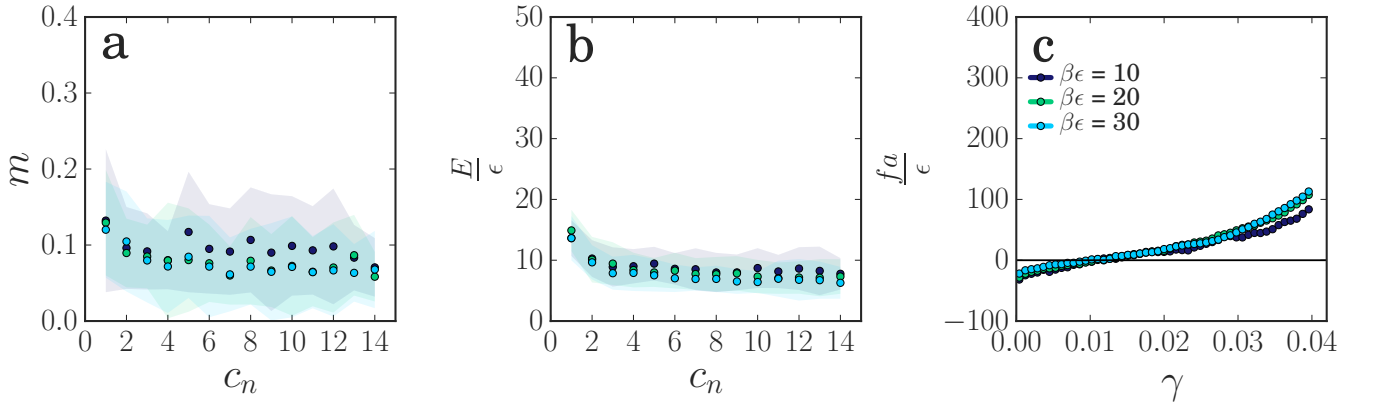


FIG. 4: $\gamma_{max} = 0.04$, gel strand B_2 (a) Average mobility of particles in successive oscillation cycles. (b) Dissipated energy per oscillation c_n , obtained by integration of the force-strain curves. The shaded area indicates the standard deviation. (c) Average elastic force of the 3th, 4th and 5th oscillation cycle. Plot (b) and (c) are scaled by $\beta\epsilon$.

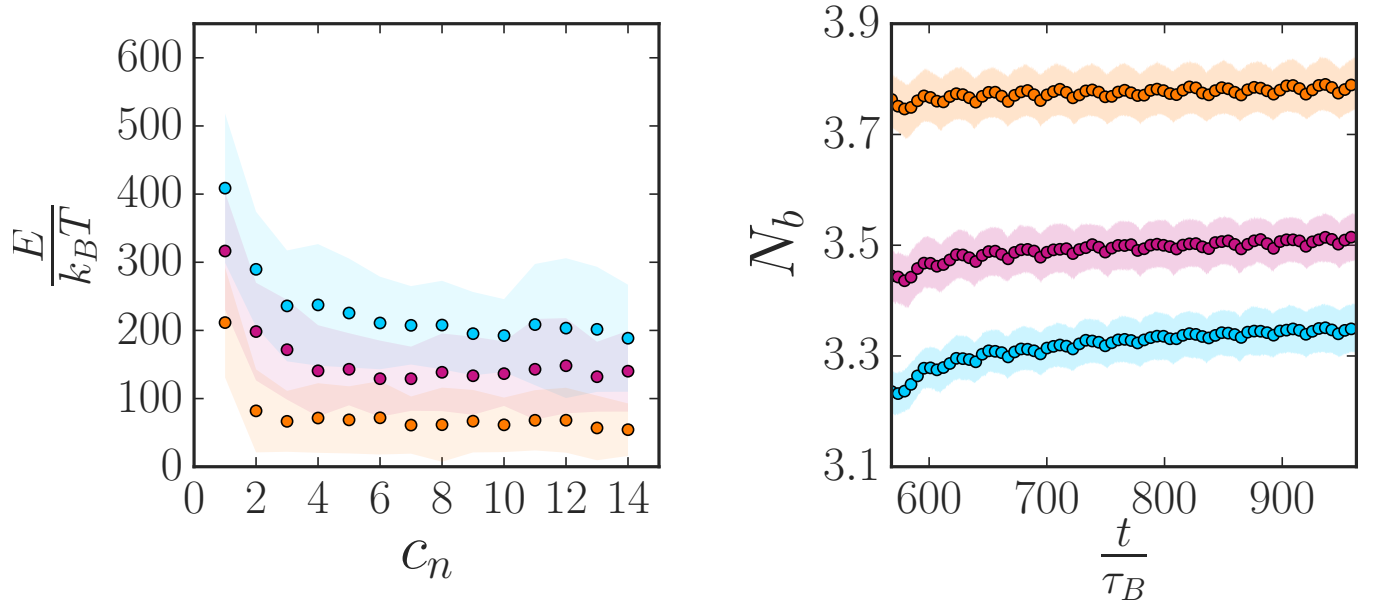


FIG. 5: $\gamma_{max} = 0.04$, gel strand B_2 (left) Dissipated energy per oscillation c_n , obtained by integration of the force-strain curves. The shaded area indicates the standard deviation. (right) Average number of bonds per particle in time. To compare the number of bonds of these strands we take the cut-off at the same position, 1.16 respectively.

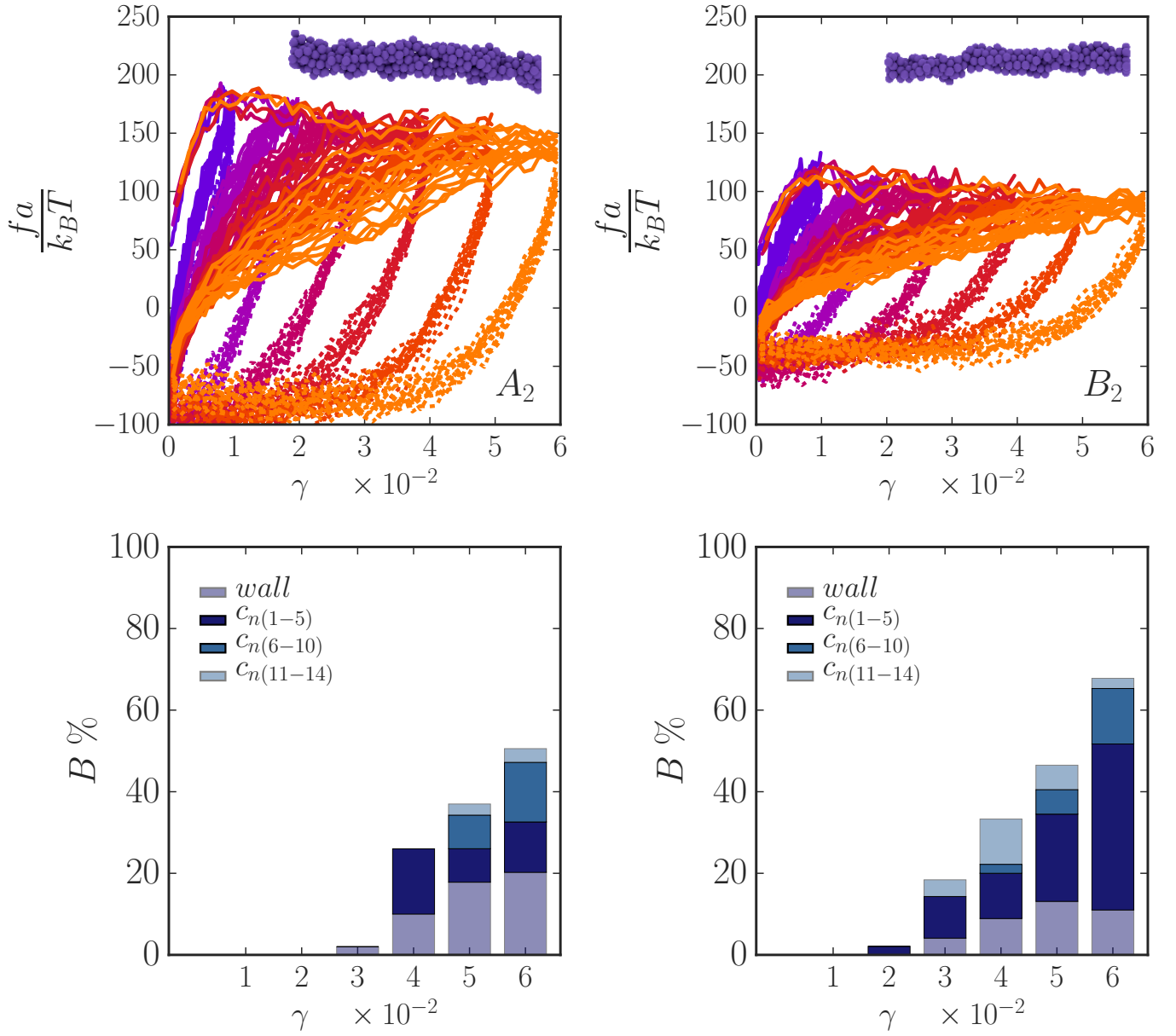


FIG. 6: (Up) Force-strain curves of 14 oscillatory expansions at a strain amplitude from $\gamma = 0.01$ (purple) till $\gamma = 0.06$ (orange) for strands with different aspect ratios (A_2 and B_2). (Down) Breakage statistics for oscillatory expansions at different strain amplitudes for strands A_2 and B_2

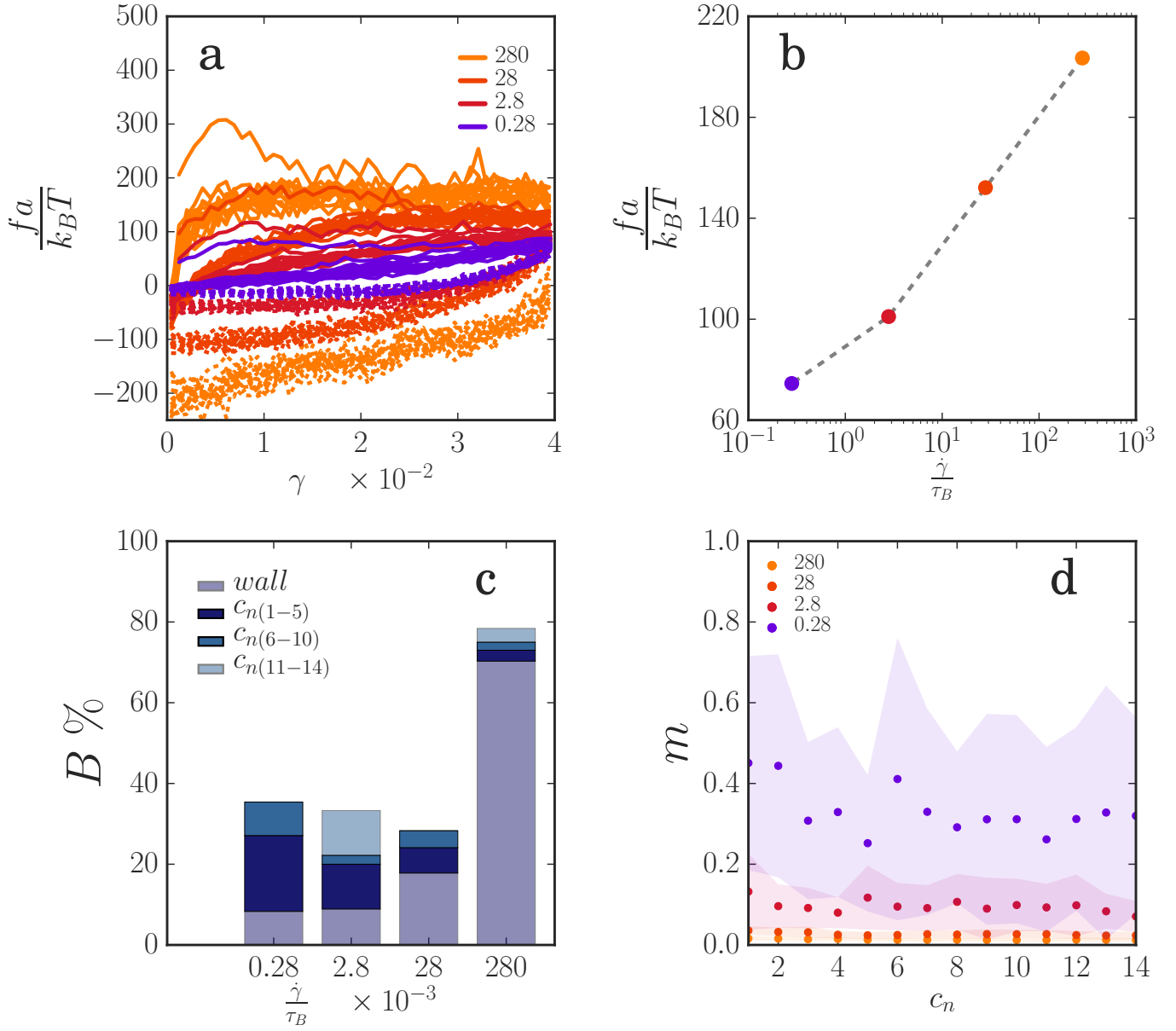


FIG. 7: (a) Force strain-curves upon 14 oscillatory expansions at different strain rates (b) The average plateau force of the first extension (between $\gamma = 0.01$ and 0.04) plotted versus strain rate. According to the force-activated Kramers model we expect the threshold force to scale logarithmic with the shear rate (Skrzeszewska et al., reference 37 main text). (c) Breakage statistics at different strain rates. (d) The mobility of particles in the strand as a function of the strain rate.

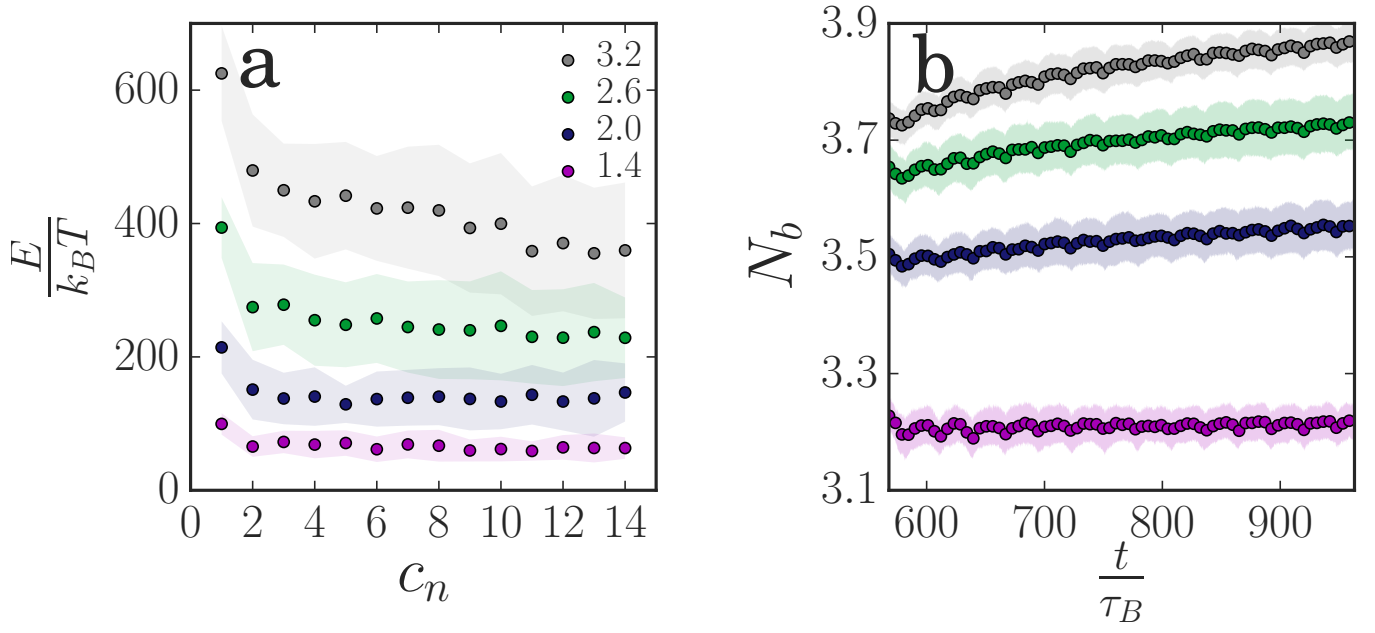


FIG. 8: strands $A_2 - C_2$ (a) Dissipated energy per oscillation cycle c_n (b) Average number of bonds per particle in time. In gray additional simulations -of even thicker strands- with a strand configuration of $H = W = 6$. The total number of particles in these strands is equal to $N = 864$.