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Assessment of air gap membrane distillation for milk concentration

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Abstract

Multi-effect evaporation is the state of the art for concentration of liquid food products to high solid content. Membrane technology with reverse-osmosis and membrane distillation offer an alternative. For the concentration of milk, a reverse osmosis and air-gap membrane distillation network was modelled and optimized. Fouling dynamics and scheduling are taken into account. Reverse osmosis is favourable until its maximum achievable concentration. Air gap membrane distillation is, despite the low operational temperatures, energy intensive for the concentration of milk. A large recirculation flow to keep sufficient cross flow has to be heated and cooled, and the costs for heating and cooling dominate the total costs for product concentration. Moreover, fouling increases the energy requirements. The optimal system for air gap membrane distillation has only one stage operating at a high concentration and relative low flux. Applying multiple stages reduces the investment costs due to smaller units, but the heating and cooling costs increase. Major opportunities to improve the performance of air gap membrane distillation for concentration of milk are: 1) increase the cold and hot side temperatures to their maximum acceptable values, 2) develop spacers that allow lower linear flow velocities in the system and thus lower recirculation rates, and 3) make use of available waste heat.

Keywords: Membrane distillation, milk, reverse osmosis, network optimization, process design

1 Introduction

Increasing need to reduce energy consumption and to use sustainable energy resources result in a demand for alternative product processing methods in the food industry. Traditional multi-stage evaporators used to concentrate food products are energy intensive, and require around 300 kJ per kg water removed [1]. This energy efficiency has increased in last decades due to the introduction of thermal and mechanical vapor recompression. Concentration by pressure driven membrane filtration, however, only requires 14 – 36 kJ per kg water removed [1]. The drawback of pressure driven membrane filtration is the achievable product concentration, which is limited due concentration polarization. For dairy products a maximum of 18% solids in the product stream is considered as economical feasible for reverse osmosis (RO) [2]. Membrane distillation (MD) is an emerging technology with the potential to concentrate to high solid contents. MD was developed as a desalination process in the 60's, and with the further development of suitable membranes in the 80's, the interest in this technology increased [3]. In more recent years MD gained attention for the concentration of food products, especially fruit juices and dairy products [4–7].

In MD, a porous hydrophobic membrane separates the feed and permeate phases and allows only water vapour to diffuse through the membrane. The driving force for mass transport is the partial vapour pressure difference between feed and permeate, which is related to the temperature difference over the membrane. As a result, the retention rate is very high, and high-quality water is produced as permeate. These advantages are the reason for the interest of MD for desalination and waste water treatment [3]. In contrast to other membrane processes, like reverse osmosis, ultrafiltration etc., MD is thermally driven instead of pressure driven. MD is therefore less affected by concentration polarisation [8]. For the concentration of milk a final solids concentration up to 45 – 50% is feasible by MD, which makes it a promising alternative for traditional evaporation [4,9,10].

Direct contact membrane distillation (DCMD) and air gap membrane distillation (AGMD) are most used for desalination and food applications. In DCMD the hot feed is separated by a hydrophobic membrane from a cold permeate stream. Water evaporates at the feed-membrane interface, passes through the membrane, and condensates at the membrane-permeate interface. In an AGMD configuration, on the other hand, water vapour from the feed passes through the membrane into an air gap, which on the other side is separated by a plate from a coolant at which the vapour condensates.

Advantage of AGMD compared to DCMD is the possibility of internal heat recovery, which results in a higher energy efficiency [11]. Therefore, AGMD has potential to compete with multi-effect evaporation and is considered in this study. A drawback of AGMD, on the other hand, is the lower flux compared to DCMD due to the smaller vapour pressure gradient [3]. Both systems operate at low temperatures, around 60°C, which makes MD processes interesting for heat sensitive products like fruit juices and dairy products. The thermal energy consumption is, however high compared to RO and modern multi-stage evaporators, with an energy consumption of 400 – 1300 kJ per kg water removed [1,12–16]. The advantage of MD is in the low operating temperatures, which allow the usage of low-quality heat, for example waste heat of other processes. Several studies suggested and investigated the usage of waste heat for operating the MD process [14,17–19]. In presence of abundant waste heat with temperatures of at least 40 – 70°C, MD might be an interesting alternative for traditional concentration methods like multi-stage evaporation.

For industrial applications MD will be applied in a network with RO network for pre-concentration. Both the RO and MD network consists of some concentration stages in series and in each stage a number of modules in parallel. Not only operational conditions, but also the configuration of a RO and MD network is crucial to guarantee a constant production, product quality, and minimum energy consumption. Several studies showed results on optimal membrane network designs, in which most focus on the synthesis of RO networks [20–24]. González-Bravo et al. [25] published the first results for the synthesis of a membrane distillation network for sea water desalination and dextrose syrup concentration. For seawater desalination the membrane distillation system had several stages with a different number of membrane units in parallel, while for dextrose syrup concentration a single stage system satisfied. At the start of this work it was not a priori clear what type of network configuration is most suitable for milk processing to high solids content. Another aspect that influences the network design for food products, like milk, is that fouling plays a dominant role due a gradual decline of mass and heat transfer over

75 time. In pressure driven membrane application the flux decline can be compensated by an increase in operational
76 pressure, but this option is not available for MD. Several authors investigated the effect of fouling on the operation
77 of a single MD unit [8,9,26,27]. However, the effect of fouling on the design of a MD network is yet to be
78 investigated.

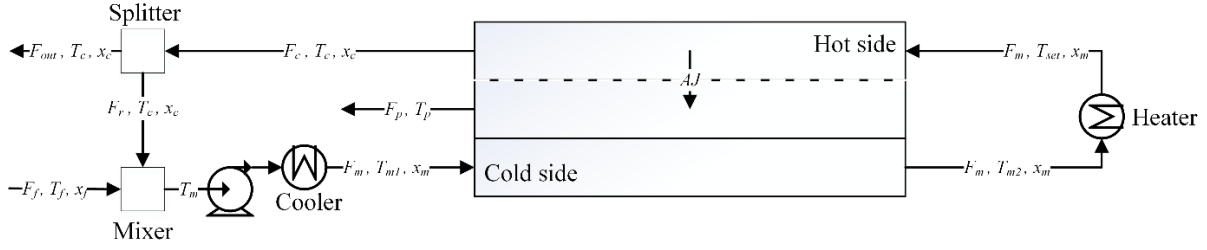
79 Network design implies decision making at two levels. First, the main task of the network is to reach the aimed
80 concentration. The number of stages in series and the concentration applied in each stage are decision variables to
81 reach this aim. Low concentrations in the stages imply a high flux and a lower fouling rate and thus increasing the
82 number of stages will be beneficial. However, a too high number of stages results in a larger membrane surface
83 (and thus investments) and higher energy costs for fluid recirculation over a stage, and therefore there is an
84 optimum in the number of stages. Secondly, fouling in the MD unit results in a serious decline of the product flow,
85 which is not accepted if the product is directly further processed in a dryer or other installation. To remove fouling
86 and to guarantee microbial safety, the installation must be cleaned at regular time intervals during which the
87 production is interrupted. To keep a constant product flow and to minimize the interruptions of the operation, the
88 parallel modules in each stage are operated in an operation-cleaning schedule. I.e. most modules are active in the
89 operation, while others are being cleaned. This approach needs extra membrane surface per stage which raises the
90 costs of the operation [28]. Also, due to the simultaneous stop and start of fouled and cleaned modules the product
91 flow and concentration vary. The challenge is to design a schedule that limits the variation in product flow and
92 concentration at low operational costs. To solve such complex problem a numerical simulation model is used. The
93 model is based on mass and energy balances, and the best available experimental results from literature.
94 Assumptions in the model are evaluated by variations in the main parameters and the role of process variables is
95 investigated by a sensitivity analysis. With the sensitivity analysis the strengths, weaknesses, and potential of the
96 system are qualified. Zhu et al. [22] approached this challenge for the design of a RO network and maintenance
97 schedule for sea water desalination. The main differences with the current MD network design is that the RO flux
98 was maintained constant over the operational period by increasing the pressure. Moreover, the operational window
99 for cleaning was in the order of 50-100 days instead of 8-12 hours, which is needed for concentrating liquid food
100 streams because of the stronger fouling rates and to prevent unacceptable growth of micro-organisms. This work
101 presents a two-step approach whereby first the number of stages and membrane surface with the resulting
102 concentrations in the succeeding RO and MD stages are obtained by mixed-integer non-linear optimization
103 (MINLP). Secondly the scheduling problem is solved, finding the optimal number of parallel modules in each
104 stage, by minimizing the total annual costs in combination with constrained variation of the product concentration
105 and flow rate.

106 **2 Process models**

107 **2.1 Membrane distillation**

108 Unlike the extensive literature available for RO process models, MD only recently gained more interest especially
109 as desalination technique. Most models are based on DCMD, however, because of the internal heat recovery the
110 AGMD system is investigated in this study. The overall schematic representation of the AGMD module is shown
111 in Figure 1. The membrane unit itself consists of a hot feed channel (hot side), hydrophobic membrane (dashed
112 line), air gap, condensation plate (solid line), and the cooling channel (cold side). Furthermore, the module consists
113 of a mixer, splitter, two heat exchangers, and pumps.

114 Fresh product feed is mixed with the recirculation flow, and the mixture is cooled to a fixed temperature before
115 entering the cold side, in order to realize sufficient driving force over the membrane. On the other side the product
116 is heated to a set temperature. The product flow from the heater enters the feed channel (hot side) of the membrane
117 unit and water evaporates through the membrane, as depicted in Figure 1. The water vapour condenses at the wall
118 of the air gap (solid line) due to the lower temperature in the cooling channel. The released heat of condensation
119 results in an increase in product temperature in the cold side. The concentrated product from the membrane unit is
120 partly recirculated to obtain sufficient crossflow in the membrane unit, which enhances heat transfer and reduces
121 fouling. The other part of the concentrate is fed to next stage.



122
123 **Figure 1. Schematic overview of a single AGMD module.**

124 2.1.1 Mass transfer

125 The MD model is based on steady state mass and energy balances. These balances imply no loss of material and
126 energy to the environment. The mass and energy balances over the MD module are:

$$127 F_m = F_f + F_r \quad (1)$$

$$128 F_m x_m = F_f x_f + F_r x_c \quad (2)$$

$$129 F_m c_{p,m} T_m = F_f c_{p,f} T_f + F_r c_{p,r} T_c \quad (3)$$

$$130 F_r = N_{MD} A_{channel} v_{in} \rho \quad (4)$$

131 where F is the mass flowrate and x the concentration of solids, c_p the heat capacity of the flow, T the temperature
132 of the flow, and subscripts m, f, r are denoting mix, feed, and recirculation loop respectively. The recirculation
133 flow (F_r) is dependent on the linear flow velocity (v_{in}), the number of parallel membrane units (N_{MD}), the cross-
134 sectional area of the membrane channel ($A_{channel}$), and the density of the milk (ρ). The mass balance over the
135 membrane unit itself is given by:

$$136 F_m x_m = F_c x_c \quad (5)$$

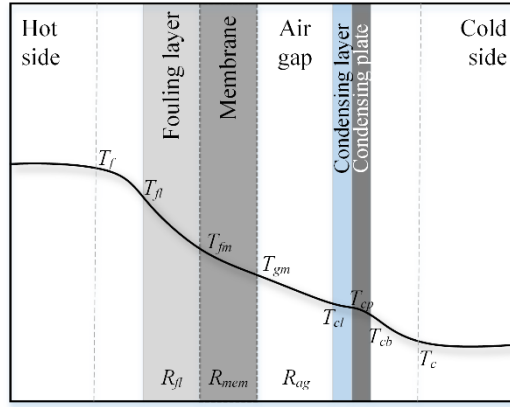
$$137 F_f = F_{out} + F_p = F_{out} + JA \quad (6)$$

138 where J is the water flux through the membrane and A the membrane surface area. According to Hausmann et al.
139 [29] the retention rate of MD for dairy components ranges from 99 to 100%, therefore no component losses via
140 the permeate are assumed in this work.

141 The water flux is based on the difference between the vapour pressures at the feed (P_f) and the condensing layer
142 (P_{cl}), and the overall resistance. The vapour pressure is calculated based on the saturated vapour pressure,
143 temperature and mole fraction of water.

$$144 J = \frac{P_f - P_{cl}}{R_{fl} + R_{mem} + R_{ag}} \quad (7)$$

145 The overall resistance consists of the resistance of the fouling layer (R_{fl}), the membrane (R_{mem}), and the air gap
146 (R_{ag}). Figure 2 gives an overview of the different layers. The fouling resistance is discussed in section 2.1.3.
147 Membrane resistance is described by the combined Knudsen and molecular diffusion model. The membrane and
148 air gap resistance are based on the work of Drioli et al. [30] and Hausmann [10]. The width of the air gap decreases
149 with the increase of the condensing layer towards the outlet of the module, however, in this work the condensing
150 layer is assumed to be equal over the whole length of the module.



144

145 **Figure 2. Schematic overview of the different resistance layers and temperature profile in the AGMD module.**

146 General characteristics of milk like viscosity, density and specific heat capacity are influenced by the concentration
 147 and temperature. Viscosity estimations are based on Fernández-Martín [31], equations for density and specific
 148 heat capacity are both taken from Choi et al. [32].

149 2.1.2 Heat transfer

150 The vapour pressure, and thus the flux, relies on the temperature (T_{fm}) at the membrane surface and condensing
 151 layer (T_{cl}) interface. The interfacial temperatures are calculated based on the overall heat transfer. Assuming the
 152 MD module operates at steady state without heat losses to the surroundings, the heat transfer equals:

$$\Delta Q = h_{bf}(T_f - T_{fl}) = \frac{\lambda_{fl}}{\delta_{fl}}(T_{fl} - T_{fm}) = J\Delta H_v + \frac{\lambda_{mem}}{\delta_{mem}}(T_{fm} - T_{gm}) = \frac{\lambda_{ag}}{\delta_{ag}}(T_{gm} - T_{cl}) + J\Delta H_v = \frac{\lambda_{cl}}{\delta_{cl}}(T_{cl} - T_{cp}) = \frac{\lambda_{cp}}{\delta_{cp}}(T_{cp} - T_{cb}) \quad (8)$$

153 in which ΔQ is the amount of transferred heat, T the temperatures at different locations, h is the heat transfer
 154 coefficient, δ the thickness, λ the conductivity of the specific layer, and ΔH_v the heat of evaporation. The different
 155 layers are visualised in Figure 2. The heat transfer coefficient of the membrane is given in Equation (9). Parameters
 156 and variables used are listed in Table A.1.

$$h_m = \frac{\left(\frac{\epsilon_m}{k_g} + \frac{1 - \epsilon_m}{k_m}\right)^{-1}}{\delta_m} \quad (9)$$

157 in which ϵ_m is the membrane porosity, k_m is the membrane material conductivity, and k_g is the thermal
 158 conductivity of air in the membrane pores.

159 Since both the flux and the interfacial temperatures depend on each other, an iterative model is used to calculate
 160 the interfacial temperatures. The vapour flux is from the feed channel to the air gap. The energy required in the
 161 heater (Q_{heat}) and the energy transferred in the cooler (Q_{cool}) is given by the following energy balances.

$$Q_{heat} = F_m c_{p,m}(T_{set} - T_{m2}) \quad (10)$$

$$Q_{cool} = F_m c_{p,m}(T_{m1} - T_m) \quad (11)$$

162 in which T_{set} is the set operating temperature of the membrane module at the inlet of the hot side, T_m is the
 163 temperature after the mixer, and T_{m1} and T_{m2} are the temperature of the product flow at the in- and outlet of the
 164 cold side, respectively. T_{set} and T_{m1} are controlling parameters and fixed in the operational conditions.

165 Electrical energy, required for the pumps, is based on the size of the stream (F_m), the pressure drop over the system
 166 (ΔP_{drop}), and the energy efficiency of the pump (η_{pump}).

$$E_{pump} = \frac{F_m \Delta P_{drop}}{\eta_{pump} \rho} \quad (12)$$

167

168 **2.1.3 Fouling model MD**

169 Deposition of product components on the membrane over time results in a gradual increase of resistance for mass
 170 and energy transfer over the membrane. According to Hausmann et al. [26] the fouling mechanism of skim milk
 171 in membrane distillation relies on the interaction between milk proteins, caseins, and salts, which form a gel like
 172 layer. However, Tijing et al. [8] pointed out, that the mechanism of fouling in membrane distillation is not yet
 173 extensively studied and as well understood as for pressure driven membrane processes. As fouling has a major
 174 impact on flux decline, and thus process performance, it is of importance to be included in process design and
 175 simulation.

176 A homogeneous fouling layer on top of the membrane is formed during the concentration of skim milk by MD,
 177 and to a lesser extent by adhesion inside the pores [26]. The formation of the fouling resistance can, therefore, be
 178 described by a cake filtration or gel layer model [33]. The linear relationship between the fouling resistance and
 179 the thickness of the fouling layer results in the following equation [34].

$$\frac{dR_{fl}}{dt} = \frac{\epsilon_{fl}c_b}{\rho} J - \frac{\epsilon_{fl}c_b k_f}{\rho} \ln\left(\frac{c_{fl}}{c_b}\right) \quad (13)$$

180 in which ϵ_{fl} is a constant for the resistance per unit of fouling layer thickness, c_b and c_{fl} are the concentration in
 181 the bulk and the fouling layer respectively, k_f is a mass transfer coefficient, and ρ the density. As we aim to study
 182 the effects of different levels of fouling on the organisation of the membrane system, and not to reveal the
 183 mechanism, the parameters in equation (13) are lumped, as suggested by van Boxtel et al. [35]. This results in the
 184 following semi-empirical equation:

$$\frac{dR_{fl}}{dt} = aJc_b - b \quad (14)$$

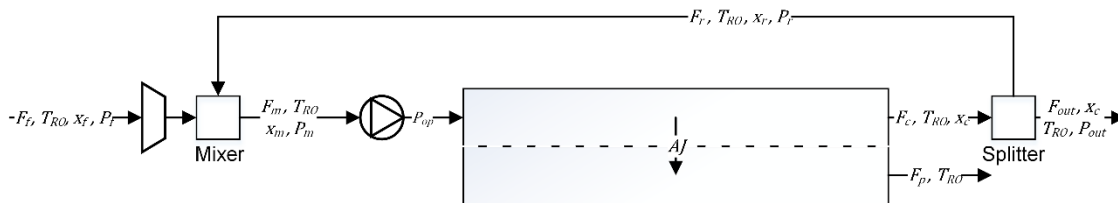
185 in which a and b are the lumped parameters and must be estimated from experimental data. Due to the lack of
 186 experimental data for the concentration of dairy or food products by AGMD, data for the concentration of skimmed
 187 milk by DCMD from Hausmann et al [10] was used to estimate these constants. Data validation is listed in
 188 Appendix A.2. The thickness of the fouling layer (δ_{fl}) is estimated by a linear relationship to the fouling resistance
 189 [35].

$$\delta_{fl} = \frac{R_{fl}(t)}{\epsilon_{fl}} \quad (15)$$

190

191 **2.2 Reverse osmosis**

192 The RO system (see Figure 3) consists of a high-pressure pump to pressurize the incoming feed to the desired
 193 operating pressure. Inside the apparatus the concentrate is to a large extent recirculated and mixed with the
 194 incoming feed to achieve high concentration factors and to have sufficient flow rate to prevent concentration
 195 polarization. After mixing the feed and recirculation flow a booster pump will provide the extra pressure that was
 196 lost over the module and to ensure operating pressure is maintained. After passing the module the concentrate is
 197 split into a recycle flow and a concentrate flow which is fed to the next stage.



198

199 **Figure 3. Schematic overview of the reverse osmosis modules.**

200 **2.2.1 Mass and heat transfer**

201 The mathematical framework of the described system is based on the descriptions given in [22,36]. It is assumed
 202 that the feed flow (F_f) and the recirculation flow (F_r) are constant, and the recirculation flow is a fixed fraction
 203 (r_{RO}) of the feed flow.

$$F_m = F_f + F_r \quad (16)$$

$$F_m x_m = F_f x_f + F_r x_c \quad (17)$$

$$F_r = \frac{F_f}{1/r_{RO} - 1} \quad (18)$$

$$F_p = AJ = F_f - F_{out} \quad (19)$$

204 where A is the membrane area and J is the flux. The flux in a RO unit is based on the pressure difference over the
 205 membrane and the overall resistance (R_{ov}). In this study it is assumed that there are no losses through the
 206 membrane.

$$J = \frac{P_{op} - P_p - \pi}{R_{ov}} \quad (20)$$

207 where P_{op} , P_p and π are the feed pressure, the pressure at permeate side, and the osmotic pressure respectively. To
 208 guarantee a constant flux over time, the operating pressure is increased from 40 MPa to a maximum of 70 MPa to
 209 compensate for extra resistance due to fouling [20,22]. The osmotic pressure (π) is calculated as follows:

$$\pi = x_f R_{gas} (T_{RO} + 273) \quad (21)$$

210 where x_f is the molar concentration of the feed, R_{gas} the gas constant, and T the absolute temperature.

211 R_{ov} is the overall resistance consisting of the intrinsic membrane resistance (R_{mem}), the start-up resistance (R_p)
 212 and the fouling resistance (R_{fl}).

$$R_{ov} = R_{mem} + R_p + R_{fl} \quad (22)$$

$$R_{mem} = \frac{1}{D_w \gamma} \quad (23)$$

213 where D_w is the water permeability, and γ is a variable encompassing the membrane characteristics derived from
 214 Zhu [22].

215 The energy requirements for a RO unit are based on the electrical energy used by the pumps. The energy usage of
 216 the high-pressure pump is:

$$E_{hp,pump} = \frac{F}{\eta_{hp} \rho} (P_{op} - P_{in}) \quad (24)$$

217

218 2.2.2 Fouling model RO

219 The used fouling model for RO is the same as for MD (Equation (13)). The vapour pressure difference used in the
 220 MD model as driving force is, however, replaced by the pressure difference over the membrane ($\Delta P = P_{op} - P_p -$
 221 π). The constants in the model are estimated by fitting the model to published data [35,37]. The parameters used
 222 for the RO model are given in Table 1.

223 2.3 Overview of model assumptions

224 The presented models are based on mass and energy balances, and no loss of energy and material was assumed.
 225 For the flux in the MD system standard heat transfer equations are applied. Hausmann et al. presented the equations
 226 for DCMD [10] and a MD system with integrated heat exchange [17]. The equations for the AGMD correspond
 227 to those of the MD system with integrated heat exchange. The performance of the system calculated by the model
 228 depends on the applied constants in the model. Table 1 presents the applied constants and shows that the major
 229 part of these constants are derived from literature, or from specifications of membrane suppliers. Four constants
 230 from the table are less certain (membrane thickness, condensation layer thickness, thermal conductivity membrane,
 231 and membrane resistance) and in a sensitivity analysis the effect of these parameters is evaluated by changing the
 232 values $\pm 20\%$. For the RO model all constants are well defined by literature or equipment suppliers, and therefore
 233 assumed to give an accurate prediction of the systems performance.

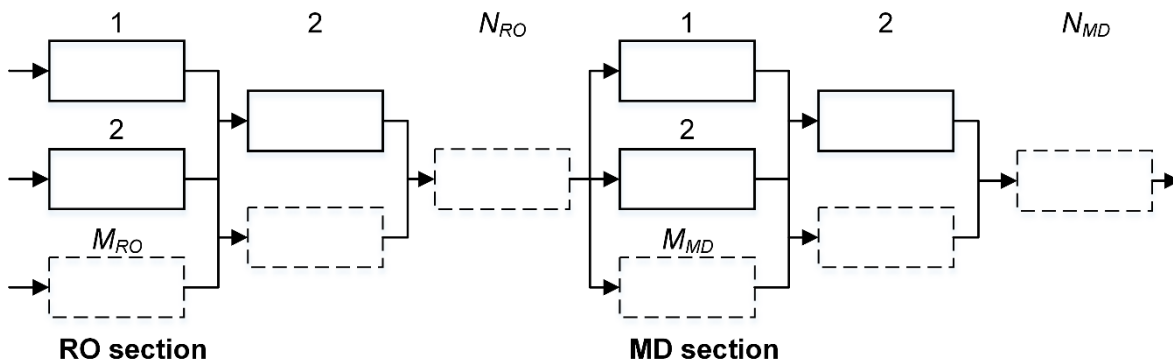
234 The flux decline due to membrane fouling can be caused by several mechanisms. Although a model proposed for
 235 cheese whey fouling on RO was used for MD, a realistic fouling pattern was simulated by fitting the model to
 236 experimental data published by Hausmann et al. [10]. The same model was also fitted to experimental data of RO
 237 [35,37]. In line with current practice the potential flux decline in RO was compensated by an increase of the
 238 operational pressure. Variations in the fouling behaviour in MD are evaluated by a sensitivity analysis of the
 239 fouling parameters.

240 **Table 1. Membrane specific process parameters**

Membrane specifications	Value	Reference
RO spiral wound		
Water permeability ($\text{kg s}^{-1} \text{N}$)	3×10^{-10}	[22]
Fixed recirculation fraction in RO module	0.95	equipment data
Membrane resistance (Pa s m^{-1})	1.27×10^{12}	[35,37]
Start-up resistance (Pa s m^{-1})	2.13×10^{10}	[35,37]
MD flat sheets		
Air gap width (m)	1×10^{-3}	[11]
Condensation layer thickness (m)	1×10^{-4}	10% of air gap
Membrane thickness (m)	6×10^{-5}	equipment data
Condensation plate thickness (m)	6×10^{-5}	equipment data
Cross sectional area channel (m^2)	1.5×10^{-3}	equipment data
Membrane porosity (-)	0.8	[11]
Resistance per unit of fouling layer (Pa s m^{-1})	8×10^{-11}	[35]
Membrane resistance (Pa s m^{-1})	1.6×10^5	[10]
Thermal conductivity condensation layer ($\text{W m}^{-1} \text{K}^{-1}$)	0.58	[38]
Thermal conductivity condensation plate ($\text{W m}^{-1} \text{K}^{-1}$)	24	[38]
Thermal conductivity membrane ($\text{W m}^{-1} \text{K}^{-1}$)	1.2	[11]
Thermal conductivity fouling layer ($\text{W m}^{-1} \text{K}^{-1}$)	0.23	[39]
Thermal conductivity air ($\text{W m}^{-1} \text{K}^{-1}$)	0.027	[38]
Latent heat of evaporation (kJ kg^{-1})	2257	[38]
Gas constant ($\text{J K}^{-1} \text{mol}^{-1}$)	8.314	[38]

241 3 Approach and problem formulation

242 The combined model equations of the membrane system (Eq. 1-22) are non-linear, and the number of units are
 243 integer variables. Therefore, the optimization of the network configuration of RO and MD is a mixed integer non-
 244 linear problem (MINLP). A downside of these problems is the complexity and the required computational time.
 245 The optimization problem is, therefore, split into two parts: 1) the estimation of the optimal number of RO and
 246 MD modules in series (N) and their respective total membrane surfaces, and 2) the scheduling problem where the
 247 optimal number of parallel units (M) and scheduling strategy is derived. Figure 4 gives an example of the possible
 248 membrane network.



249
 250 **Figure 4. Schematic representation of a RO and MD network. N_{RO} , and N_{MD} the number of membrane stages in series for RO and MD, and M_{RO} , and M_{MD} the number of membrane unit in parallel for each RO and MD stage.**
 251

252 3.1 Stage optimization

253 Each potential stage is considered as one large membrane module for which the total surface is estimated. The
 254 decision variable is the membrane surface in each stage, which results in a specific product concentration after
 255 each stage. The objective is to design a network with the lowest investment and operational costs that realizes a
 256 given final product concentration for a given feed rate. The objective function is formulated as:

$$\min \left(\sum_{n=1}^{N_{RO}} C_{RO,inv}^n + \sum_{n=1}^{N_{RO}} C_{RO,op}^n + \sum_{n=1}^{N_{MD}} C_{MD,inv}^n + \sum_{n=1}^{N_{MD}} C_{MD,op}^n \right) \quad (25)$$

$$\text{s.t. } c_{goal} \leq \bar{c}_{out,(n=N)}$$

Equations 1 – 23

257 where C_{inv} are the investment costs and C_{op} are the operational costs for each stage n for the total number of stages
 258 N for both RO and MD. The operational conditions and process boundaries are listed in Table A.2.

259 The investment costs for RO consist of the equipment costs of the pumps, and the RO module which consists of
 260 the module costs ($C_{RO,mod}$) and the membrane costs ($C_{RO,mem}$), which both are linearly related to the surface
 261 membrane surface (A). The installation costs are covered by a Lang factor (L_f). The total costs are annualised by
 262 the life time of the equipment (LF) and the life time of the membranes LF_m . Subsequently all costs are expressed
 263 in euro per m³ water removed.

$$C_{RO,inv} = \frac{\left(\frac{C_{pump,n}}{LF_{pump}} + \frac{A_n C_{RO,mod}}{LF_{mod}} \right) L_f + \frac{A_n C_{RO,mem}}{LF_{mem}}}{F_{p,a}} \quad (26)$$

264 The operational costs for RO contain the electrical cost for the pumps and the cleaning costs, both are annualized.
 265 Cleaning costs depend on the membrane surface (A_n) and the total cleaning time (t_{clean}).

$$C_{RO,op} = \frac{(E_{electric,n} C_e t_a + C_{clean} A_n)}{F_{p,a}} \quad (27)$$

266 Furthermore, the concentration of the last stage (\bar{c}_{out}) should not be lower than the set concentration (c_{goal}). The
 267 final concentration for RO is a decision variable but is limited to a final concentration of 18%. Output parameters
 268 (flow, concentration, and temperature) of the last stage of RO are the input parameters of the first stage of the MD
 269 section.

270 The MD investment costs and operational costs are formulated similar as for RO but contain additional
 271 components. In addition, the investment costs include the heat exchangers for heating and cooling. The membrane
 272 costs for MD are calculated in the same way as for RO. The operational costs also include the heating and cooling
 273 for every MD module, which results in the following equations.

$$C_{MD,inv} = \frac{\left(\frac{C_{pump,n} + C_{heater,n} + C_{cooler,n} + A_n C_{MD,mod}}{LF_{mod}} \right) L_f + \frac{A_n C_{MD,mem}}{LF_{mem}}}{F_{p,a}} \quad (28)$$

$$C_{MD,op} = \frac{(E_{electric,n} C_e + E_{heat,n} C_{heat} + E_{cool,n} C_{cool}) t_a + C_{clean} A_{tot} t_{clean}}{F_{p,a}} \quad (29)$$

274 MD is proposed as an alternative for multi-stage evaporation of milk, therefore, the final concentration of the last
 275 MD stage is fixed at 50% total solids. The resulting configuration is used as input for the scheduling optimization.
 276 Figure 5 illustrates the total optimization procedure, whereby Figure 5 part I represents the stage optimization. To
 277 solve the series problem the `fmincon` function of MATLAB R2017b with the interior point method algorithm was
 278 used.

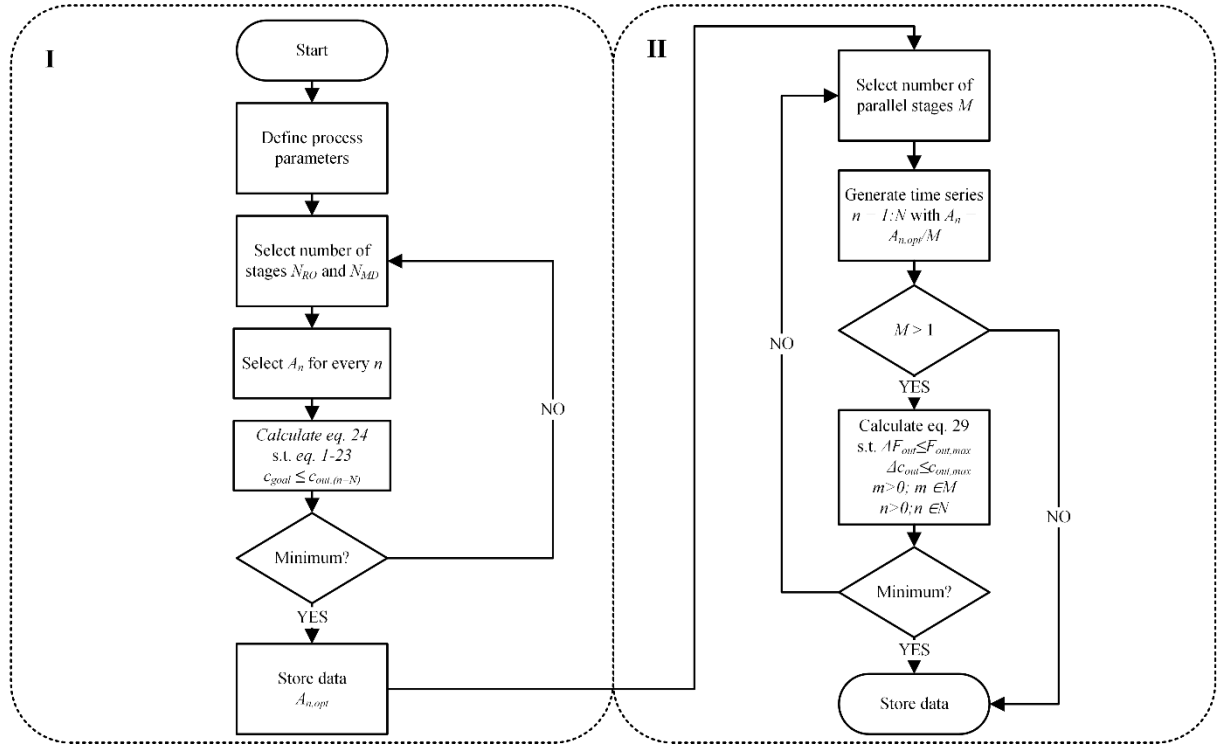


Figure 5. Solution strategy for an optimal membrane design. With I) the selection of the optimal number and area of RO and MD units in series, and II) the strategy for the scheduling problem and the selection of number of parallel units.

3.2 Scheduling strategy

The optimal scheduling strategy is based on the number of parallel units (M) and aims to guarantee a continuous production while minimizing the costs. For the economical evaluation of the different configurations the total costs are minimized. These consists of the annualized investment costs (C_{inv}) and the annual operational costs (C_{op}) of both the RO (C_{RO}) and the MD section (C_{md}). The operational conditions and process boundaries are listed in Table A.1.

$$\min \left(\sum_{n=1}^{N_{RO}} \sum_{m=1}^{M_{RO}} C_{RO,inv}^{n,m} + \sum_{n=1}^{N_{RO}} \sum_{m=1}^{M_{RO}} C_{RO,op}^{n,m} + \sum_{n=1}^{N_{MD}} \sum_{m=1}^{M_{MD}} C_{md,inv}^{n,m} + \sum_{n=1}^{N_{MD}} \sum_{m=1}^{M_{MD}} C_{md,op}^{n,m} \right) \quad (30)$$

s.t. $\Delta F_{out}^{n,m} \leq \Delta F_{out,max}$
 $\Delta C_{out,nm}^{n,m} \leq \Delta C_{out,max}$
 $m > 0; m \in M$
 $n > 0; n \in N$
 Equations 1 – 23

The next step in milk processing is spray drying, a unit operation that requires a constant feed rate and product concentration. Therefore, fluctuations in flow rate and concentrations have to be limited. For the RO section the deviation in outflow of every stage ($\Delta F_{out,max}$) may not be larger than 10%. In the MD section the final concentration will fluctuate due to the flux decline over time, therefore, the variation in final concentration ($\Delta C_{out,max}$) is restricted to 1.5% over the whole production period. These were set as constraints in the minimization problem.

The investments costs consist of the cost of the membrane units, pumps and heat exchangers, which depends on the number of stages (N) and parallel units (M). The investment costs are annualized and corrected with a Lang factor (L_f) [40].

$$C_{md,inv} = \frac{(C_{pump,mn} + C_{heater,mn} + C_{cooler,mn} + A_{mn}C_{md,mod})L_f + \frac{A_n C_{md,mem}}{LF_{mem}}}{F_{p,a}} \quad (31)$$

$$C_{RO,inv} = \frac{\left(\frac{(C_{pump,mn} + C_{md,mn} + A_{mn}C_{RO,mod})}{LF_{mod}} L_f + \frac{A_{mn}C_{RO,mem}}{LF_{mem}} \right)}{F_{p,a}} \quad (32)$$

297 The costs for the membrane distillation unit (C_{md}) consists of the membrane module (C_{mod}) and the membrane
 298 (C_{mem}) itself which all depend on the membrane area (A). The investment costs for the RO section are calculated
 299 in the same way, only without the heater.

300 The operational costs are based on the costs for electricity, heating, cooling, and cleaning. The cleaning consists
 301 of both thermal energy (E_{clean}) for cleaning and the material costs (C_{clean}), and depend on the number of
 302 operational hours (t_{op}).

$$C_{MD,op} = \frac{(E_{electric,mn}C_e + E_{clean,mn}C_{heat} + E_{heat,mn}C_{heat} + E_{cold,mn}C_{cold})t_{op} + C_{clean}A_{tot}t_{clean}}{F_{p,a}} \quad (33)$$

$$C_{RO,op} = \frac{(E_{electric,mn}C_e + E_{clean,mn}C_{heat})t_{op} + C_{clean}A_{tot}t_{clean}}{F_{p,a}} \quad (34)$$

303 Other auxiliary equipment, maintenance, and labour costs are not considered. To solve the scheduling problem the
 304 pattern search method of MATLAB R2017b was used.

305 For estimation of the number of parallel modules and the best scheduling strategy it was assumed that all modules
 306 have fixed production cycles of 7 hours followed by a 1 hour cleaning cycle, this to guarantee food safety.
 307 Furthermore, the membranes will operate at the same initial performance after every cleaning cycle, so fluxes are
 308 fully restored. Additionally, it was assumed that the modules operate after cleaning immediately at steady-state,
 309 and the operating conditions of each parallel unit in the same stage are identical. Figure 5 part II shows the solution
 310 strategy. Data generated in the series configuration section is used as input for generating the time series which
 311 are the input for the scheduling problem. All cost parameters are listed in Table A.2. The effect of the usage of
 312 waste heat on the total costs are evaluated in additional optimizations, as well as the effect of the operational
 313 conditions on the total performance.

314 4 Results and discussion

315 4.1 Process design

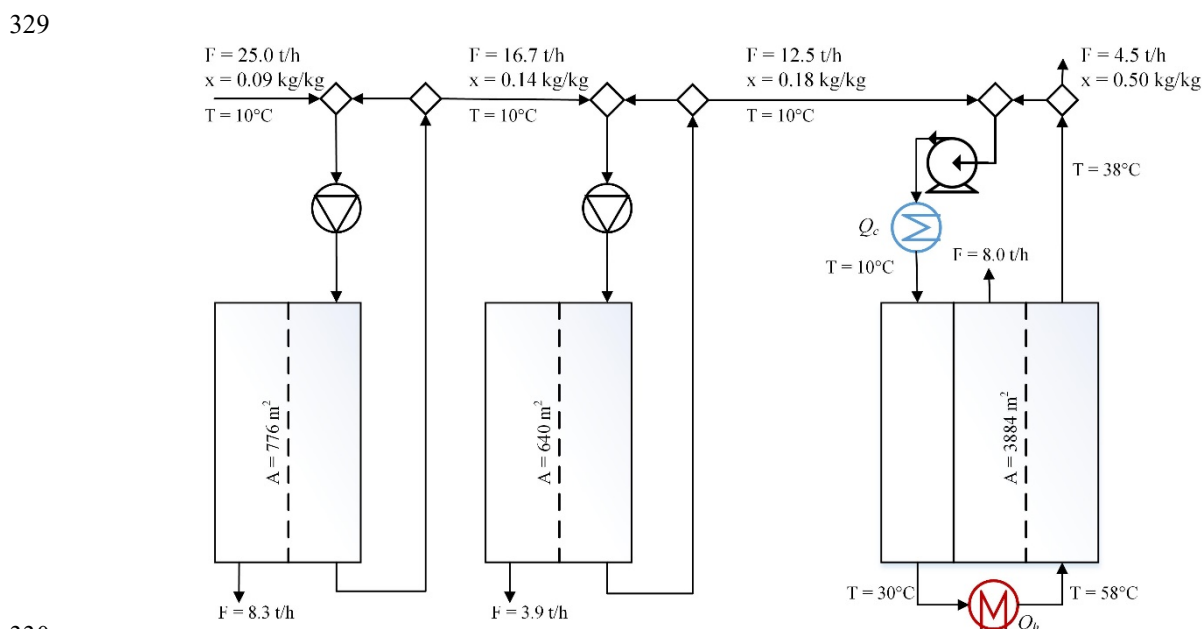
316 The optimal process configuration to concentrate milk from 0.09 kg kg⁻¹ to 0.5 kg kg⁻¹ solids is by a two-stage RO
 317 section and a single-stage MD section. The optimal process configurations for the RO and MD section are shown
 318 in Figure 6, and details are displayed in Table 2. RO proved to be more cost efficient compared to MD. Milk is,
 319 therefore, concentrated by RO to the upper boundary of 0.18 kg kg⁻¹ solids. A two-stage RO configuration is
 320 optimal for this case, which both consist of six parallel units. The energy consumption of the RO section resulted
 321 in 19 kJ per kg water removed, which is in line with reported values in literature [1].

322

323 **Table 2. Results for the optimal total system with specifications of the configuration and performance of the RO and MD sections.**
 324 **RO concentrates milk from 9% to 18% dry matter and MD from 18 to 50% dry matter.**

		Total system	RO section	MD section
Feed	tonne h ⁻¹	25	25	12.5
Total membrane area	m ²	5300	1416	3884
Number of series	-	2 – 1	2	1
Number of parallel units in subsequent stages	-	6 – 6 – 4	6 - 6	4
Heating costs	€ m ⁻³	3.2	-	8.3
Cooling costs	€ m ⁻³	2.3	-	6.0
Electrical costs	€ m ⁻³	1.1	0.6	1.7
Equipment costs	€ m ⁻³	0.9	0.2	2.1
Cleaning costs	€ m ⁻³	0.5	0.2	1.0
Total costs	€ m ⁻³	8.1	1.0	19.1

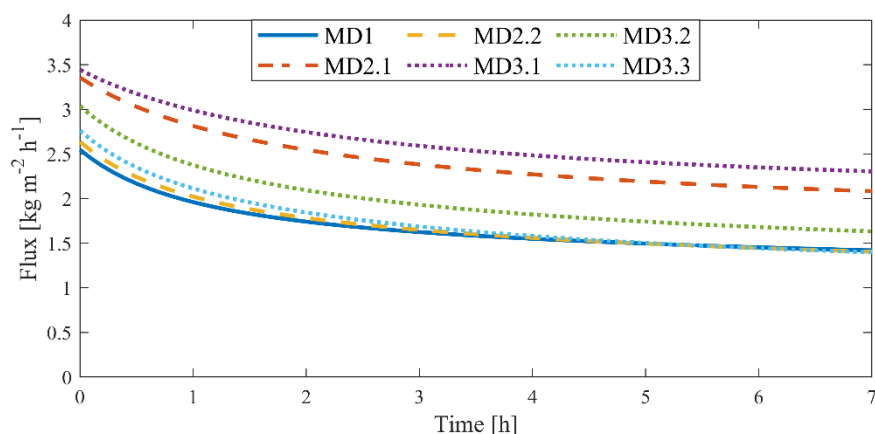
325
 326 Figure 6 shows the configuration for the RO and MD stages with operational conditions. In the figure the optimal
 327 MD configuration with one stage is given. Alternative, sub-optimal, MD configurations with operational
 328 conditions are given in appendix A.3.



330
 331 **Figure 6. Optimal process configurations for the combined RO (first 2 stages) and MD (3rd stage) system, including average flows,**
 332 **concentrations, and temperatures.**

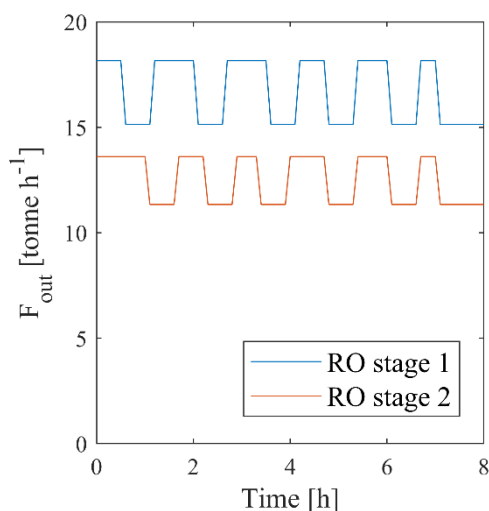
333 The costs for the optimal RO and MD configurations and the combination of the two (total system) are listed in
 334 Table 2. To reach the end concentration of 0.5 kg kg⁻¹ solids a single stage MD turned out to be best in terms of
 335 costs. Although the result corresponds to the work of González-Bravo et al. [25] for dextrose syrup concentration
 336 the result is counter-intuitive as the single stage AGMD system operates at a high concentration with a low flux
 337 and stronger fouling compared to a multi-stage system. No advantage is taken from the higher fluxes and lower
 338 fouling rate in the first stages of a multi-stage system (see Figure 7 for a specification of the fluxes in subsequent
 339 stages). The required membrane area and thus investment costs of this single-stage system are therefore higher
 340 than that of a multi-stage MD system. Details of multi-stage MD systems are listed in Appendix A.3. The
 341 membrane area proved, however, not to be the main cost driver, but the heating and cooling costs are (Table 2).
 342 Due to the required recirculation in each of the subsequent stages, to keep sufficient cross flow along the membrane
 343 surface, the increase of heating and cooling costs is larger than the reduction of the capital costs. Ignoring heating
 344 and cooling costs in the simulations resulted in a multi-stage system with low investment costs for membranes
 345 (like seawater desalination). Moreover, the flux decline over time plays an important role in the costs. Due to the
 346 flux decline the internal heat recovery decreases and as a consequence more heating and cooling is required in the

347 recirculation loop during operation. Altogether, the costs of a two-stage system are 16% above those of a single-
 348 stage MD system.



349
 350 **Figure 7. Flux profile over time in the different MD stages. Single stage: MD1, a two-stage: MD2 and a three-stage system: MD3.**

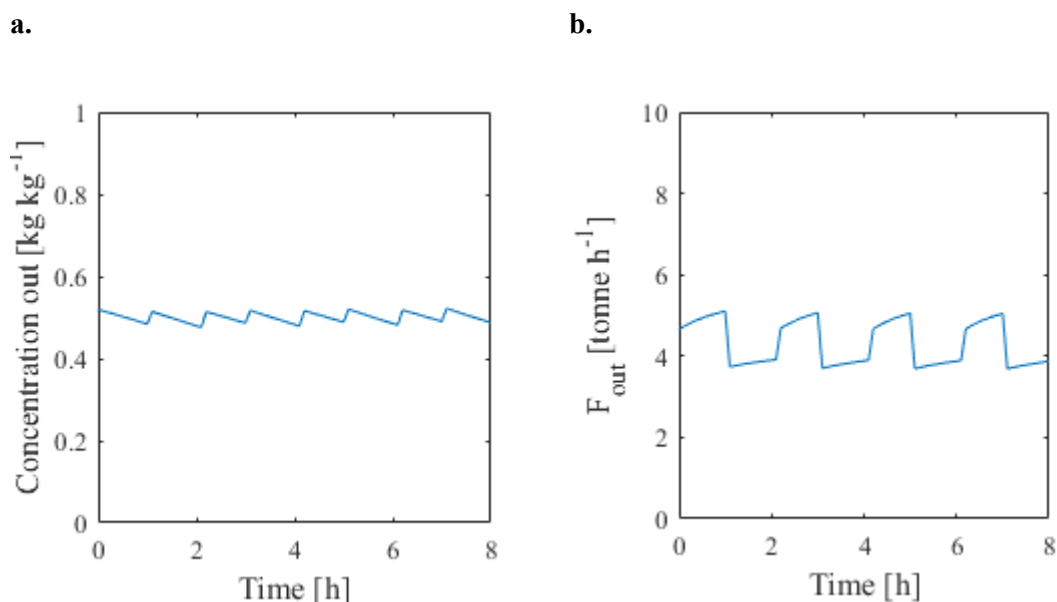
351 Concentration of food products like milk by MD has the advantage of reaching a high final concentration by using
 352 a membrane system. However, the energy consumption is high compared to concentration by RO. For milk
 353 concentration, besides heating also cooling of the recirculation loop is necessary in order to maintain the driving
 354 force. The energy required for a single stage system is 2.6 MJ for heating and 2.5 MJ per kilogram water removed
 355 for cooling, which is much higher compared to previously reported values for MD on desalination [12–16] and
 356 traditional multi-stage evaporator systems. Cooling is not required for desalination, as the permeate is the aimed
 357 product, and not the concentrate which is aimed for food products like milk. Reported costs values for desalination
 358 range between 0.3 and 5.1 euro per m³ water removed [18,25,41]. For milk the costs for MD are estimated at nearly
 359 20 euro per m³ water removed. However, when combining MD and RO the total costs are 8.1 euro per m³ water
 360 removed. This is still higher when compared to reported desalination values but does include the effect of fouling
 361 and the additional energy costs caused by the high recirculation and for cooling.



362
 363 **Figure 8. Effect of scheduling on the product out flow for a two stage RO system with 6 parallel units in each stage. At the high values**
 364 **all modules are in operation, at the low values one module is in the cleaning mode.**

365 In each stage a number of parallel membrane modules are operational. Each membrane unit is operational for 7
 366 hours, followed by a rinsing and cleaning period of one hour. With these intervals the flux and concentration
 367 would be constant if in each stage consisted of 8 parallel modules. If less modules prove to be optimal variation in
 368 outflow (RO and MD) and concentration (MD) will result.

369 In order to minimize fluctuation in flow to the next module, scheduling for the RO part is based on keeping the
 370 milk outflow within fixed boundaries of $\pm 10\%$. The flux, and thus milk concentration, is kept constant by
 371 increasing the operating pressure over time. Allowing a flow variation of $\pm 10\%$ from the RO system, the
 372 optimization resulted in 6 parallel modules in each stage. The use of 6 parallel modules in each stage implies that
 373 over the full scheduling period, during short times all parallel modules are operational, which causes the flow
 374 variations in Figure 8.

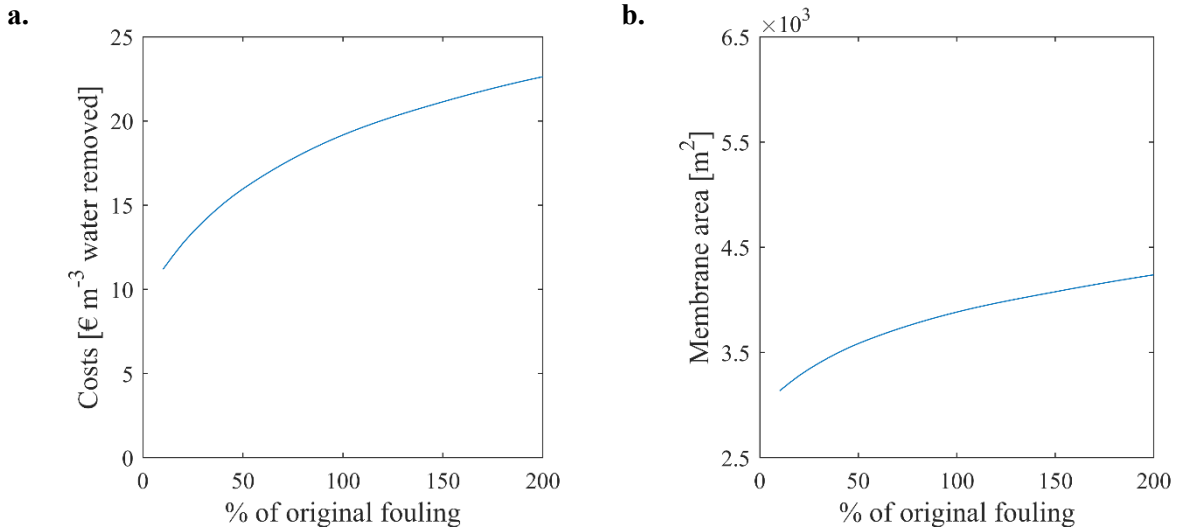


375 **Figure 9. Effect of scheduling on MD for the product concentration (a) and product flow (b) of 4 parallel units in a one-stage system.**
 376 **The gradual decline of concentration and increase of flow is result of the fouling.**

377 For MD, 4 parallel modules for the one-stage system are enough to keep the final concentration within the pre-
 378 defined operational boundaries (maximum fluctuation of 1.5% for the final concentration). In this scheduling
 379 system all 4 parallel units are used during 1.3 hours, then one unit is in the cleaning mode (Figure 9). These events
 380 cause the step variations in the graphs for concentration and flow. Moreover, during the operation of the membrane
 381 units, the flux declines gradually. As a result, the product outflow increases over time as the permeate flow
 382 decreases as a result of the flux decline until the next cleaning cycle. These gradual variations were absent for RO,
 383 where the flux reduction due to fouling is compensated by increasing the operational pressure.

384 **4.2 Effect of fouling rate**

385 Previous studies on MD featured a significantly lower fouling rate [40,42], or did not include the fouling dynamics
 386 at all [25]. Fouling, however, plays an important role in milk concentration by membrane processes. Although the
 387 fouling dynamics used in this study is based on assumptions, it gives an insight on the effect of fouling on the
 388 process configurations. To illustrate the effect of fouling, scenarios were simulated by varying the fouling rate
 389 (parameters a and b in Eq. (14)). The results for the one-stage MD system are given in Figure 10. All operating
 390 conditions were kept equal to previous simulations. At low fouling rates both the equipment costs and the utility
 391 costs decrease. There is no effect on the cleaning schedule.



392 **Figure 10. The effect of variation fouling for a one-stage MD system (100% standard fouling, 50% half of fouling rate, 200%**
 393 **doubled fouling rate) on the costs (a) and required membrane area (b).**

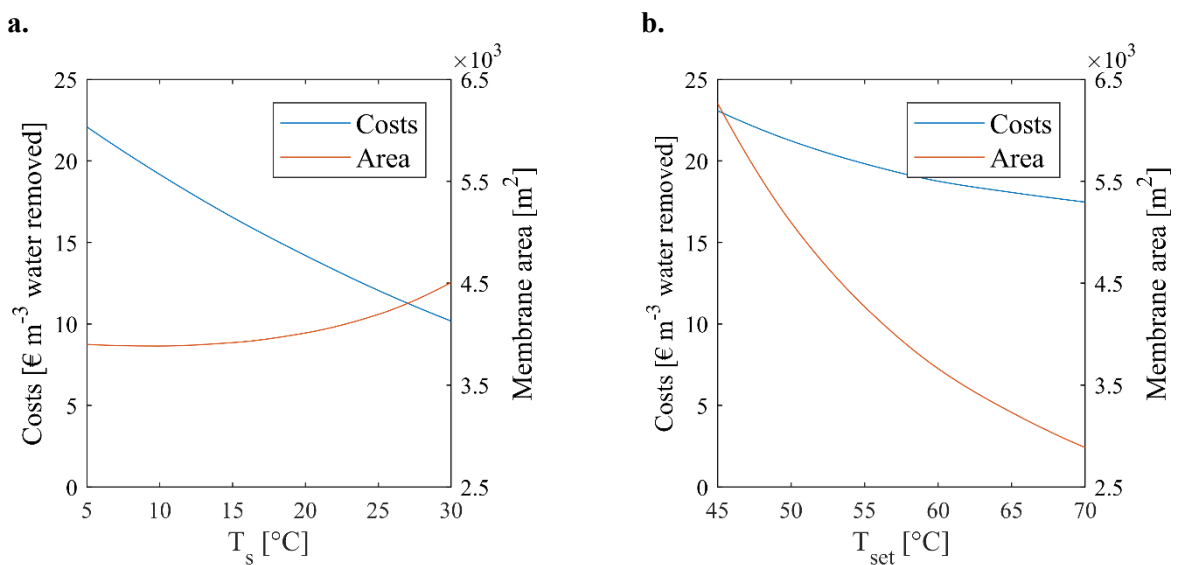
394 With flux decline over time, the temperature change of the product in both the hot and the cold side decreases. As
 395 a result, the heating and cooling duties, which are the main cost drivers, increase. The heating and cooling duties
 396 overshadow the capital related costs. Reduction of the heating and cooling costs by a low fouling rate and keeping
 397 high fluxes over time is therefore crucial to make membrane distillation viable.

398 **4.3 Influence of operational conditions and uncertain constants on MD performance**

399 Standard values for operational conditions were used for the discussed optimization of the RO and MD network.
 400 These conditions, however, affect the outcomes. Variations of the key operational conditions and membrane
 401 properties, like temperature and recirculation settings, give information on the role of the operational conditions
 402 for further system improvement.

403 **4.3.1 Effect of operating temperature**

404 Heating and cooling demand are the main cost contributors in MD usage for the concentrating milk. Unlike MD
 405 for desalination, where the permeate is the main product [41], cooling is required in the product recirculation. In
 406 previous calculations, the temperature of the cold side was set at 10°C and the hot side temperature was set to
 407 58°C. The effect of varying these temperatures on the costs and membrane surface is shown in Figure 11.



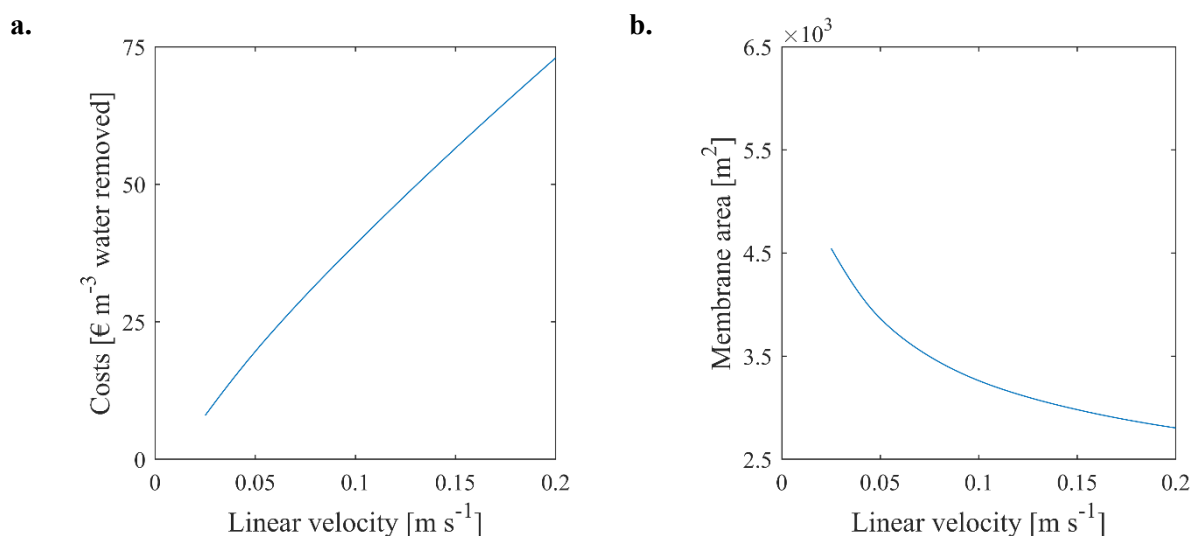
408 **Figure 11. Variation analysis of temperature setpoints for a single-stage MD system. a) Effect of the cold side temperature, T_s, on the**
 409 **processing costs (left axis) and membrane surface (right axis). b) Effect of the hot side temperature, T_{set}, at the processing costs (left**
 410 **axis) and membrane surface (right axis).**

411 Increasing the feed temperature (T_s) from 10 to 20°C reduces the cooling costs. The total membrane surface
 412 increases, due to the smaller temperature difference between the hot and cold side. Equipment costs have,
 413 compared to the heating and cooling, a small contribution to the costs. The costs decrease by 30% with a change
 414 of the feed temperature from 10 to 20°C on the cold side. It should be noted that raising the temperature may
 415 increase the risk of microbial contamination.

416 In previous calculations, the temperature of the hot side (T_{set}) was set to 58°C. Increasing the temperature results
 417 in a higher flux and reduces the required membrane area (Figure 11b). As a result, the costs drop due to the higher
 418 fluxes and increased heat transfer from the hot to the cold side. The hot side must be as warm as possible, the only
 419 limiting factor is the product quality. Temperatures over 60°C for a prolonged time are not desirable for milk due
 420 to protein denaturation [43].

421 4.3.2 Effect of linear flow velocity

422 The product is recirculated over each module to ensure sufficient crossflow along the membrane. In the system
 423 optimization the linear flow velocity was set to 0.05 ms^{-1} . To evaluate the effect on process performance the linear
 424 flow velocity was varied between 0.025 and 0.2 ms^{-1} . Increasing the velocity reduces the membrane surface due
 425 to higher fluxes (see Figure 12b). The same result was found by Hausmann et al. [10], by showing that higher flow
 426 velocities have a positive effect on the flux which results in a smaller membrane surface. An extra advantage of
 427 high flow velocities is a lower fouling rate and less flux decline over time. This aspect is also a factor to reduce
 428 the required membrane surface. In contrast, Figure 12a gives the effect of varying the linear velocity on the costs,
 429 which decrease almost linear towards lower velocities. Lowering the flow velocity also reduces the recirculation
 430 rate and consequently the cooling and heating costs. Although also the flux reduces and thus heat transfer from the
 431 hot to cold side, the increase in recirculation rate causes a higher energy increase. These calculations do not fully
 432 cover the turbulence properties at low velocities. This is a strong assumption, but the results point to the importance
 433 of spacer optimisation to reduce the operational costs. Additionally, at higher solids concentrations higher cross
 434 flows might be desired, because of the increased viscosity and the shear thinning behaviour of milk [44].

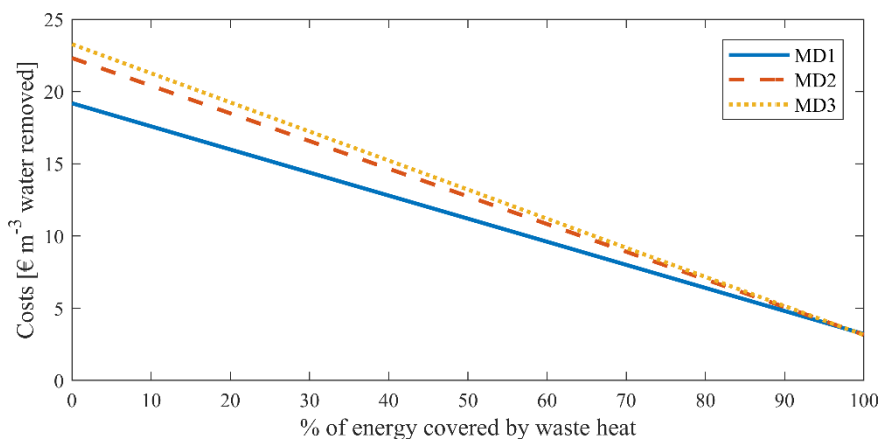


435 **Figure 12. Effect of linear velocity on the costs (a) and required membrane area (b) for a single-stage MD system.**

436 4.4 Use of waste heat

437 MD operates at a relative low operating temperature and, in contrast to multistage evaporators, MD can make use
 438 of low-quality energy streams. In food processing plants low-quality energy streams are often abundantly available
 439 [45]. The costs of the high heating demand for MD are reduced by using these low-quality energy streams. Several
 440 authors already exploited the potential of membrane distillation in combination with industrial waste heat
 441 [17,18,41]. Dow et al. [19] demonstrated the feasibility of operating a MD pilot plant by using waste heat from a
 442 gas fired power station. The temperature of the waste heat (less than 40°C was used) had a major influence on the
 443 flux of a direct contact membrane distillation unit. Also solar heat has potential as a heat source for membrane
 444 distillation [46]. Higher waste heat temperatures result, as expected, in higher fluxes. Figure 11b illustrates the

445 effect of varying set temperature on the required membrane surface and thus capital costs. More important is,
 446 however, the reduction of the costs for cooling and heating by using waste heat. Figure 13 gives the operational
 447 costs for water removal for different levels waste heat usage, ranging from zero to full replacement of the thermal
 448 energy demand by waste heat. Complete energy supply from waste heat, by heat integration with other processes,
 449 results in operational costs of 3.1 euro per m³ water removed. This makes membrane distillation competitive with
 450 current concentration techniques. To reach these benefits, additional capital costs are required for waste heat
 451 integration. These costs are very case dependent, and will therefore have to be assessed case by case.



452
 453 **Figure 13. Operational costs as a function of % of required energy for heating and cooling covered by waste heat for MD installations**
 454 **with 1, 2 and 3 stages.**

455 4.5 Membrane distillation system assumptions

456 Both the configuration of the membrane distillation, and the membrane specifications have influence on the
 457 performance. Simulations were based on literature values for physical constants (heat and mass transfer
 458 coefficients and condensation layer thickness, see Table 1). In the previous sections the effect of variation of the
 459 most important operational conditions (temperature, flow rate, fouling) was discussed. Membrane properties used
 460 in this study are based on reported literature or given by a membrane supplier. Experimental work is still required
 461 to confirm the findings, and to improve the used values for the membrane properties. The role of the most uncertain
 462 constants 1) the thickness of the condensation layer, 2) thickness of the membrane, and 3) thermal conductivity of
 463 the membrane were assessed in a sensitivity analysis by $\pm 20\%$ variation of the values given in Table 1. Despite
 464 these variations the optimal structure of the MD system was not altered. The most sensitive constant was the
 465 thermal conductivity of the membrane with a decrease of 17.6% on the total costs, when the thermal conductivity
 466 of the membrane decreases with 20%. The thickness of the condensation layer, and the thickness of the membrane
 467 only affects the total costs with 1 – 3%, at $\pm 20\%$ variation.

468 The membrane resistance was based on Hausmann et al. [10], but changes with the use of different membranes.
 469 Halving the membrane resistance (R_m) will increase the flux and reduces both the heating and cooling duties with
 470 18% for a one stage MD system. In order to achieve this advancement, development and testing of new membranes
 471 is required. The advantage of internal energy recovery in air gap membrane distillation (AGMD) was the reason
 472 to select this MD system for this work. Low fluxes and high recirculation rates proved to limit the internal heat
 473 recovery. In this light, direct contact membrane distillation (DCMD) could be a better option. In the AMGMD the
 474 average temperature difference over the hot side is for the one-stage system 20°C (milk cools down from 58 to
 475 38°C) while the temperature difference over the heater and cooler is 28°C (Figure 6). In this case it is more energy
 476 efficient to separate the heating and cooling circuited like in a DCMD. However, if the temperature difference of
 477 the hot side is larger compared to temperature difference over the heater, then the AGMD will be beneficial. These
 478 results point to the importance for higher fluxes to make the AGMD system viable for milk concentration.

479 Compared to permeate- or liquid gap membrane distillation (PGMD), the AMGMD has a smaller temperature
 480 difference as driving force and thus lower flux. According to Swaminathan et al. [47] the PGMD is 20% more
 481 energy efficient compared to AGMD. However, due to the liquid on the permeate side there is a higher chance of

482 pore wetting [30], which highly decreases the process performance and thus results in higher costs. Nonetheless,
483 exploring PGMD as option for the concentration of food products is of interest.

484 5 Conclusion

485 Membrane distillation (MD) is an emerging technology for product concentration. In this work the potential of
486 different process configurations for the concentration of milk by reverse osmosis (RO) and membrane distillation
487 was assessed and investigated. Although milk was considered as feed, the findings of this work give also important
488 information for application of MD for concentrating of other food products.

489 Due to the low costs, concentration of milk starts with RO to the maximal possible concentration of milk (18%
490 solids). RO is followed by membrane distillation to concentrate milk to the final 50% solids. The used air gap
491 membrane distillation (AGMD) has the advantage of internal heat recovery and is therefore often preferred over
492 direct contact membrane distillation. Nevertheless, due to the high product recirculation to achieve sufficient cross
493 flow along the membranes the energy costs of the AGMD unit are high. With the current available membranes
494 and energy prices membrane distillation cannot compete with a multi-stage evaporator.

495 Gradual fouling during the operation has a large influence on process cost of MD, as fluxes decline so does heat
496 transfer. Heating and cooling of product in each stage results in costs that overshadow the costs for membranes
497 and equipment. The optimal configuration of the membrane distillation unit is therefore a single-stage unit that
498 operates at high concentration and low flux. The effect analysis showed the following options for further
499 improvement of the system: 1) to increase the cold and hot side temperatures to their maximum acceptable values,
500 2) to develop spacers that allow lower cross flow velocities in the system and thus lower recirculation rates, and
501 3) make use of available waste heat.

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507 Nomenclature

A	Area (m^2)
a, b	Fouling rate parameters
C	Costs (€ yr^{-1})
c	Concentration (kg kg^{-1})
c_p	Specific heat capacity ($\text{kJ kg}^{-1} \text{K}^{-1}$)
D_w	Membrane water permeability ($\text{kg s}^{-1} \text{N}$)
E	Energy requirement (kJ s^{-1})
F	Mass flow (kg s^{-1})
ΔH_v	Latent heat of evaporation (kJ kg^{-1})
h	Heat transfer coefficient ($\text{W m}^{-2} \text{K}^{-1}$)
J	Water flux ($\text{kg m}^{-2} \text{s}^{-1}$)
k_f	Mass transfer coefficient (m s^{-1})
k	Thermal conductivity ($\text{W m}^{-1} \text{K}^{-1}$)
L_f	Lang factor (-)
LF	Equipment life time (year)
M	Number of modules in parallel (-)
N	Number of membrane stages (-)
P	Pressure (Pa)
Q	Heat flow (kJ s^{-1})
R	Mass transfer resistance ($\text{Pa m}^2 \text{s kg}^{-1}$)
R_{gas}	Universal gas constant ($\text{J K}^{-1} \text{mol}^{-1}$)

r_{RO}	Fixed recirculation fraction in RO module (-)
T	Temperature (°C)
t	Time (s, h)
v_{lin}	Linear velocity (m s ⁻¹)
x	Weight fraction (-)
Greek letters	
η_{pump}	Energy efficiency of the pump (-)
γ	Variable encompassing the membrane characteristics (-)
δ	Thickness (m)
λ	Conductivity (W m ⁻¹ K ⁻¹)
π	Osmotic pressure (Pa)
ρ	Density (kg m ⁻³)
ϵ	Constant for the resistance per unit of fouling layer thickness (Pa m s kg ⁻¹)
ϵ_m	Membrane porosity (-)
μ	Viscosity (Pa s ⁻¹)
Subscripts	
a	Annual
ag	Air gap
b	Bulk
c	Concentrate
cb	Condensing plate – bulk
cl	Condensing layer
cp	Condensing plate
f	Feed
fl	Fouling layer
fm	Fouling – membrane
gm	Air gap – membrane
inv	Investment
m	Mix of feed and recirculated product
mem	Membrane
mod	Membrane module
op	Operational
ov	Overall
p	Permeate
r	Recirculation
s	Cold side variable
set	Hot side variable

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621

622 Appendix

623 A.1 Process data

624
625 **Table A.1 Operating and optimization conditions for both RO and MD process.**

Parameter	RO	MD
Starting temperature feed (°C)	10	10
Temperature permeate (°C)	10	-
Pressure feed (Pa)	40×10^5	10^5
Pressure drop over the module (Pa)	0.22×10^5	0.2×10^5
Pressure permeate (Pa)	10^5	-
Starting pressure feed (Pa)	10^5	-
Feed flow (kg h ⁻¹)	25000	25000 – 12500
Starting concentration (w/w)	0.09	≤ 0.18
Final concentration (w/w)	≤ 0.18	0.50
Linear velocity (m s ⁻¹)	2	0.049
Annual operating time (h)	8000	8000
Cleaning cycle time (h)	1	1
Operating cycle time (h)	7	7
Number of stages, <i>N</i> (-)	1 – 5	1 – 5
Equipment life time (year)	15	15
Membrane life time (year)	4	4

626

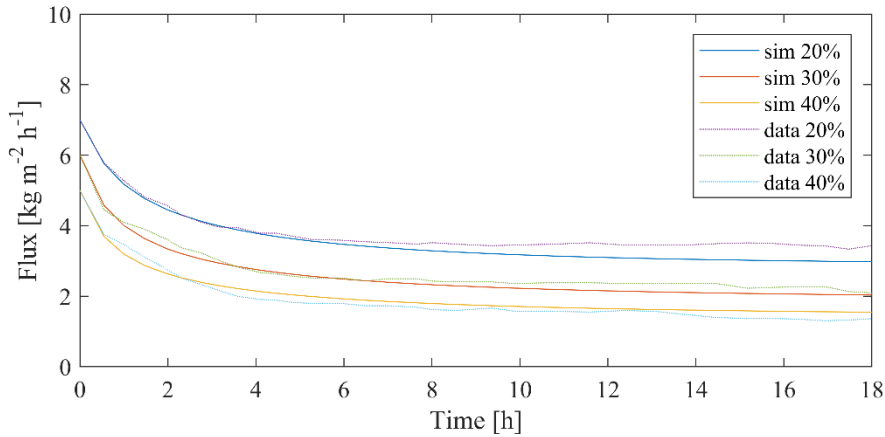
627 **Table A.2 Economic data (based on [22,25,40]).**

Parameter	Value
Investment cost pump (€)	$2590(P_{pump})^{0.79}$
Pump efficiency	0.85
Investment cost heater/cooler (€)	$1115F_{tot}$
Lang factor	1.4
Equipment lifetime (y)	15
MD module costs (€ m ⁻²)	58.5
MD membrane costs (€ m ⁻²)	100
RO module costs (€ m ⁻²)	58.5
RO membrane costs (€ m ⁻²)	17.75
Heating costs (€ GJ ⁻¹)	4.0
Cooling costs (€ GJ ⁻¹)	3.0
Electrical costs (€ kWh ⁻¹)	0.12
Cleaning cost (€ m ⁻² hour ⁻¹)	0.017

628

629 **A.2 MD fouling model validation**

630 In order to include fouling in the MD model, an estimate for the fouling resistance was made. Figure A.1 shows
 631 the fitting of the lumped parameters a and b for the estimation of the fouling resistance (R_f) as given in Eq. (14).
 632 Data from Hausmann et al [10] was used to estimate the lumped parameters a and b . Initial fouling build up is
 633 well fitted as can be seen in the comparison between the simulation and the data in the figure below. When the
 634 fouling layer build up stabilises (roughly after 8 hours) the flux is underestimated for low concentrations (20%)
 635 and overestimated at high concentrations (40%).



636

637 **Figure A.1. Result of the fitting of the flux at different concentrations 20, 30 and 40% dry matter. The dotted lines are the actual data**
 638 **(data) [10] and the solid lines are the fitted simulations (sim).**

639 The resistance over the air gap is based on the molecular diffusion model [30]:

$$R_{ag} = \left(\frac{\epsilon DP_t}{\delta_{ag} P_{ag,log} R (T_{ag,avg} + 273.15)} \frac{M_v}{R} \right)^{-1} \quad (A.1)$$

640 where $T_{ag,avg}$ is the mean temperature in the air gap, $P_{ag,log}$ is the log mean pressure in the gap, P_t is the total
 641 pressure, ϵ is the membrane porosity, M_v the molar mass of water molecules, D is the water vapour diffusion
 642 coefficient through air.

643 **A.3 Alternative MD configurations**

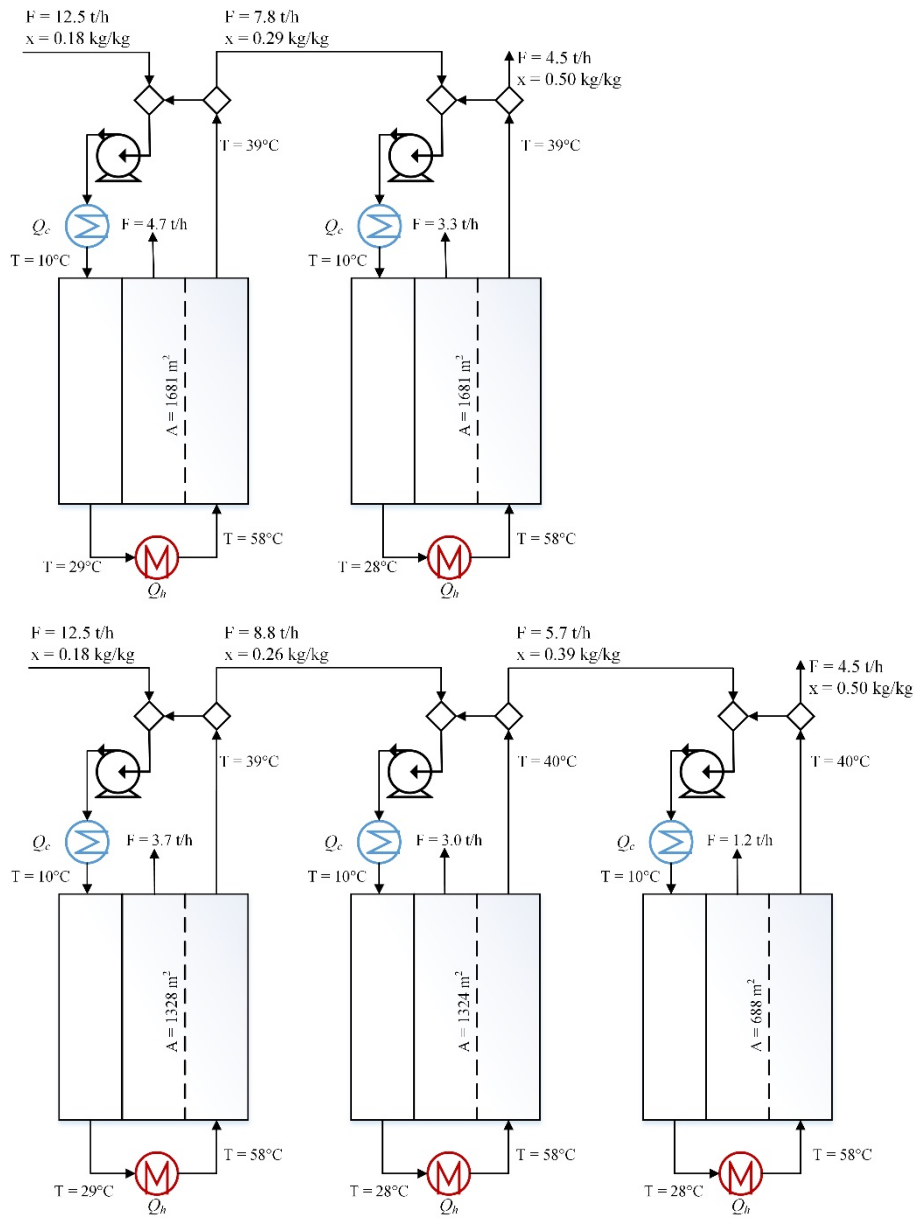
644 In this section the results are presented for the other membrane distillation configurations.

645 **Table A. 3. Results for other MD configurations with 2, 3, 4, or 5 stages in series.**

		MD 2	MD 3	MD 4	MD 5
Feed	tonne h ⁻¹	12.5	12.5	12.5	12.5
Total membrane area	m ²	3448	3340	3329	3299
Number of stages	-	2	3	4	5
Number of parallel units in subsequent stages	-	3-3	3-3-3	3-3-3-3	3-3-3-3-3
Heating costs	€ m ⁻³	10.3	10.9	10.9	10.8
Cooling costs	€ m ⁻³	7.2	7.5	7.3	7.1
Electrical costs	€ m ⁻³	2.0	2.2	2.2	2.3
Equipment costs	€ m ⁻³	1.9	1.9	1.9	1.9
Cleaning costs	€ m ⁻³	0.9	0.9	0.9	0.9
Total costs	€ m⁻³	22.3	23.3	23.2	23.0

646

647



648 **Figure A.2. Optimal process configurations for the MD configuration with 2 (a) and 3 (b) stages, including average flows,**
 649 **concentrations, and temperatures.**

650