

*Lecture for International Summer School on the Atmospheric Boundary Layer,  
Les Houches, France, June 18, 2008*

# Modeling clear atmospheric boundary layers

Some basics, evaluations and applications

Bert Holtslag

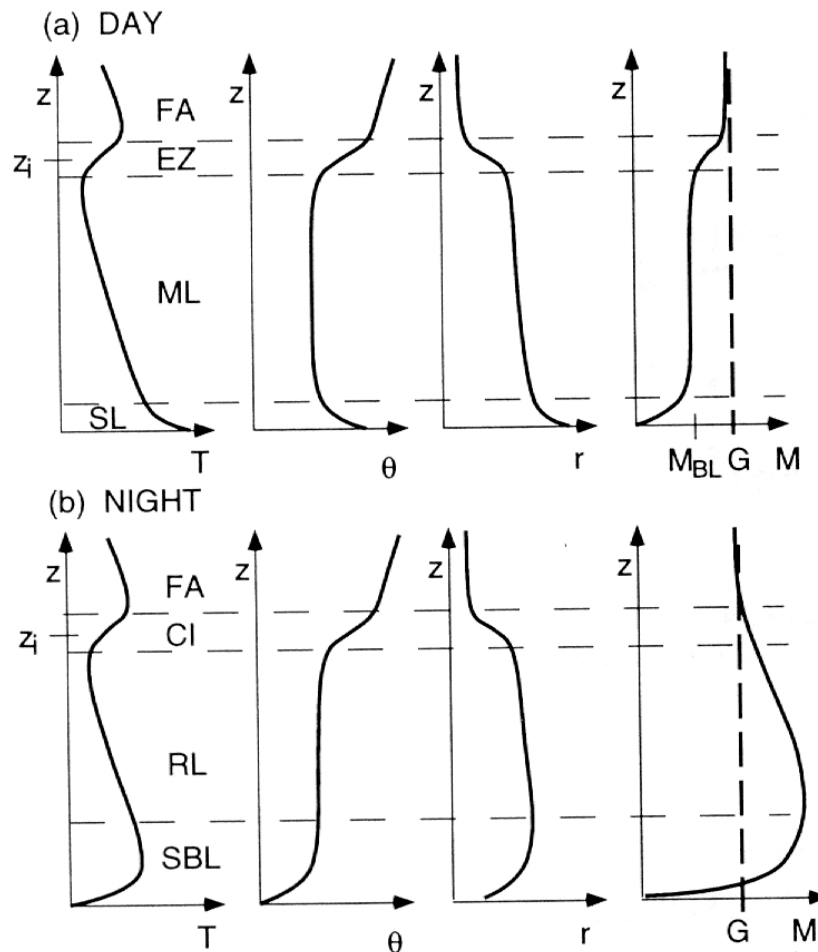
Thanks to all participants in the  
GEWEX Atmospheric Boundary Layer Study!



WAGENINGEN UNIVERSITY  
METEOROLOGY AND AIR QUALITY



## Typical boundary layer profiles over land without clouds



Model is needed to  
make forecasts  
in response to  
atmospheric forcings  
and surface conditions

Critical issues:  
Diurnal Cycle  
Mean Profiles and Fluxes

What is the status?

Figure adapted from Stull (1988)

## Basics of a boundary layer model after Reynolds decomposition

$$\frac{\partial C}{\partial t} + U \frac{\partial C}{\partial x} + V \frac{\partial C}{\partial y} + W \frac{\partial C}{\partial z} = - \frac{\partial \overline{wc}}{\partial z} \dots$$

$$\overline{wc} = -K \frac{\partial C}{\partial z} + \dots$$

Can be solved for given initial and surface conditions,  
and if the diffusivities are known

Valid for wind and any 'conserved' quantity  $C$   
(potential temperature, specific humidity, tracers,...)

# How to deal with turbulent mixing and eddy diffusivity?

$$K = f(\text{height, stability, ABL depth, ...})$$

## *Strategy*

Distinguish between stable and unstable conditions

Use theoretical concepts, observations and numerical simulations (LES and DNS) as a guidance

Compare model results with independent data

## Turbulent Kinetic Energy (TKE) closure scheme

(applied in many atmospheric models...)

$$\frac{\partial TKE}{\partial t} = S + B + T + P - \varepsilon$$

$$K = l\sqrt{TKE}$$

TKE represents the major characteristics of turbulence

How to do the length scale?

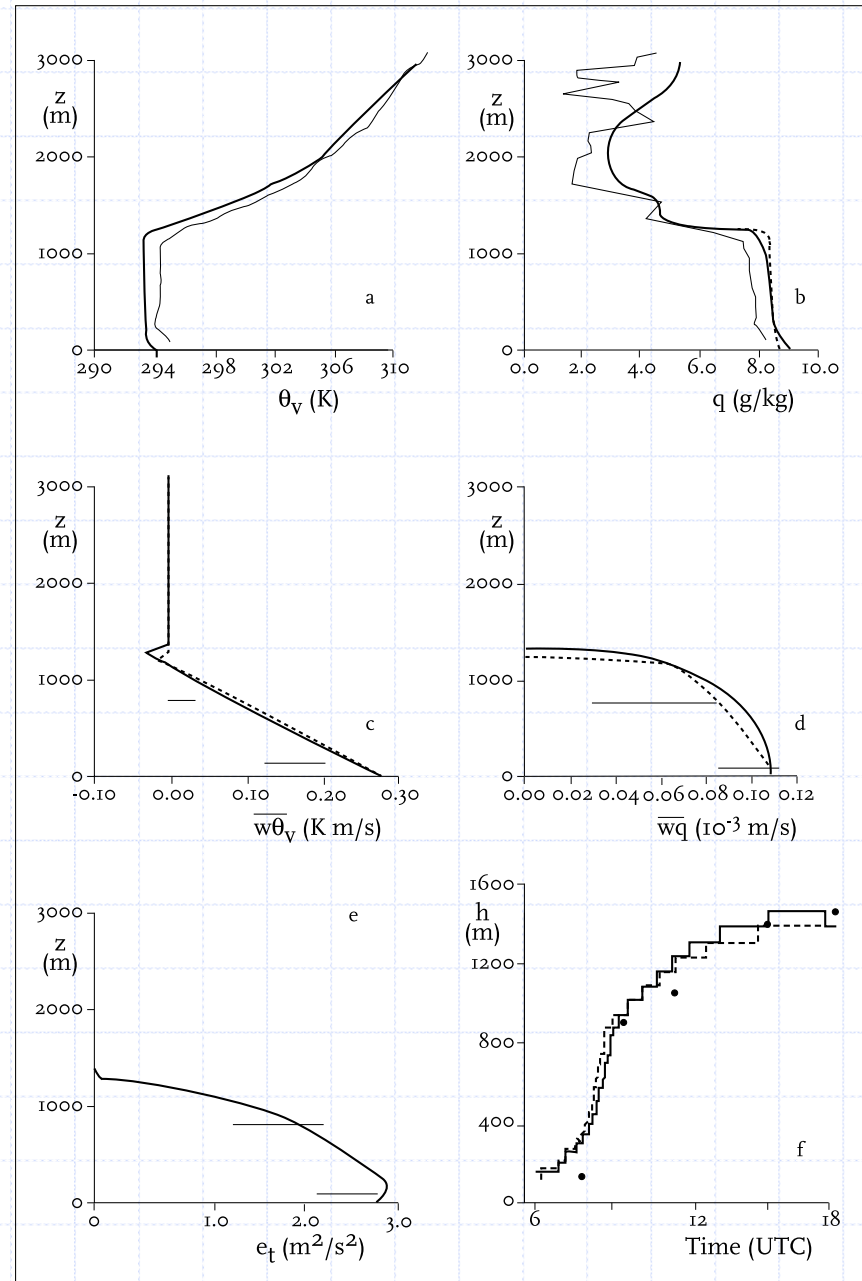
Is local gradient assumption valid?

Many proposals have been made for various boundary layers

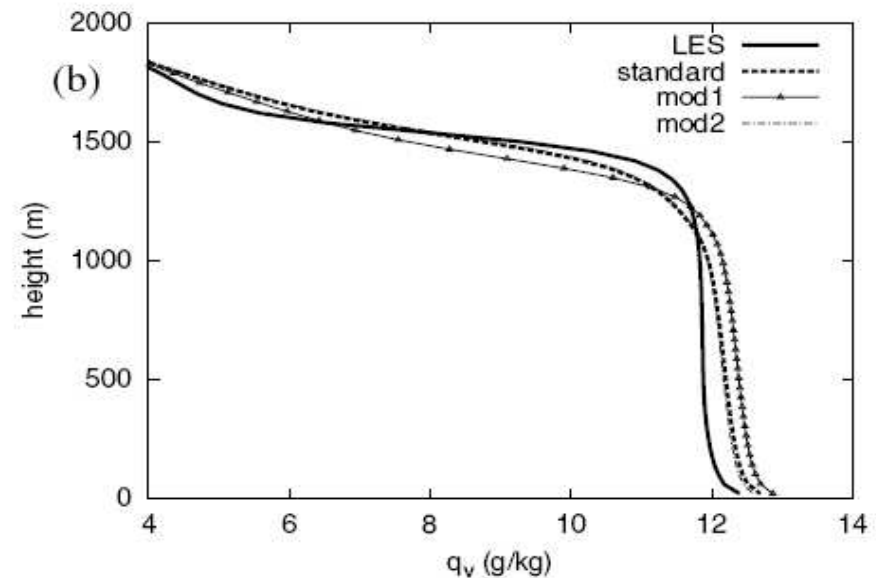
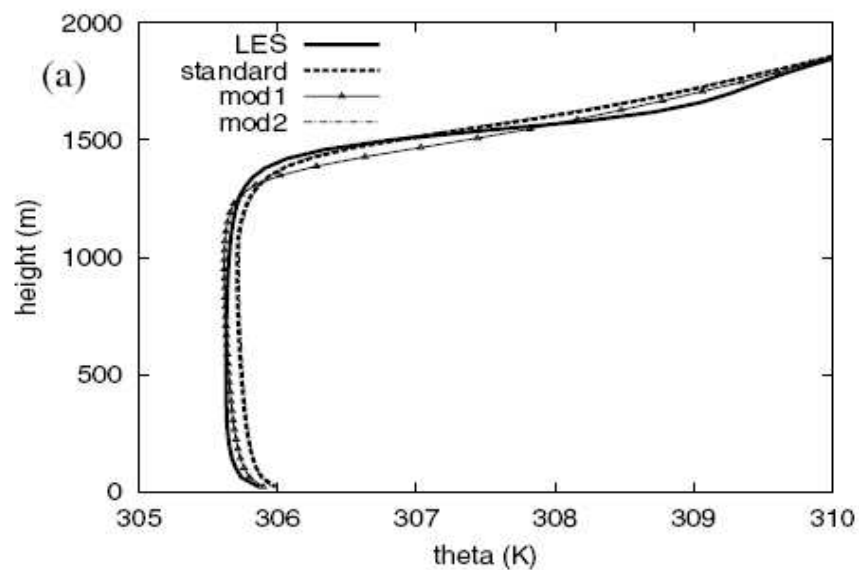
## Single column study

Example of ABL model results during daytime in comparison with observations of Hapex-Mobilhy, France, July 8, 1986 (Cuxart et al, 1994)

(using prescribed surface fluxes and advection terms neglected)



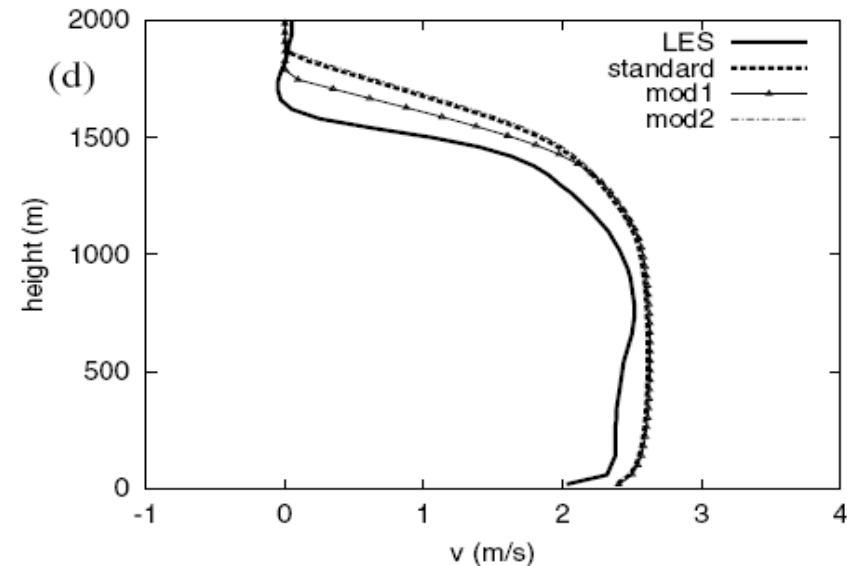
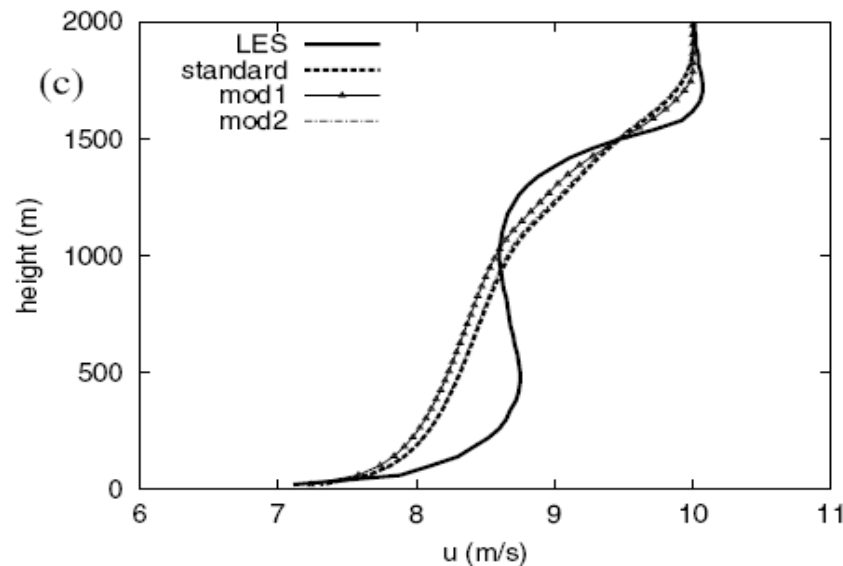
# Results with a TKE scheme for a convective boundary layer (using an updated length scale with a parcel method)



Results by Lenderink and Holtslag (QJRM, 2004)

# Momentum mixing

(these results by Lenderink and Holtslag, 2004)

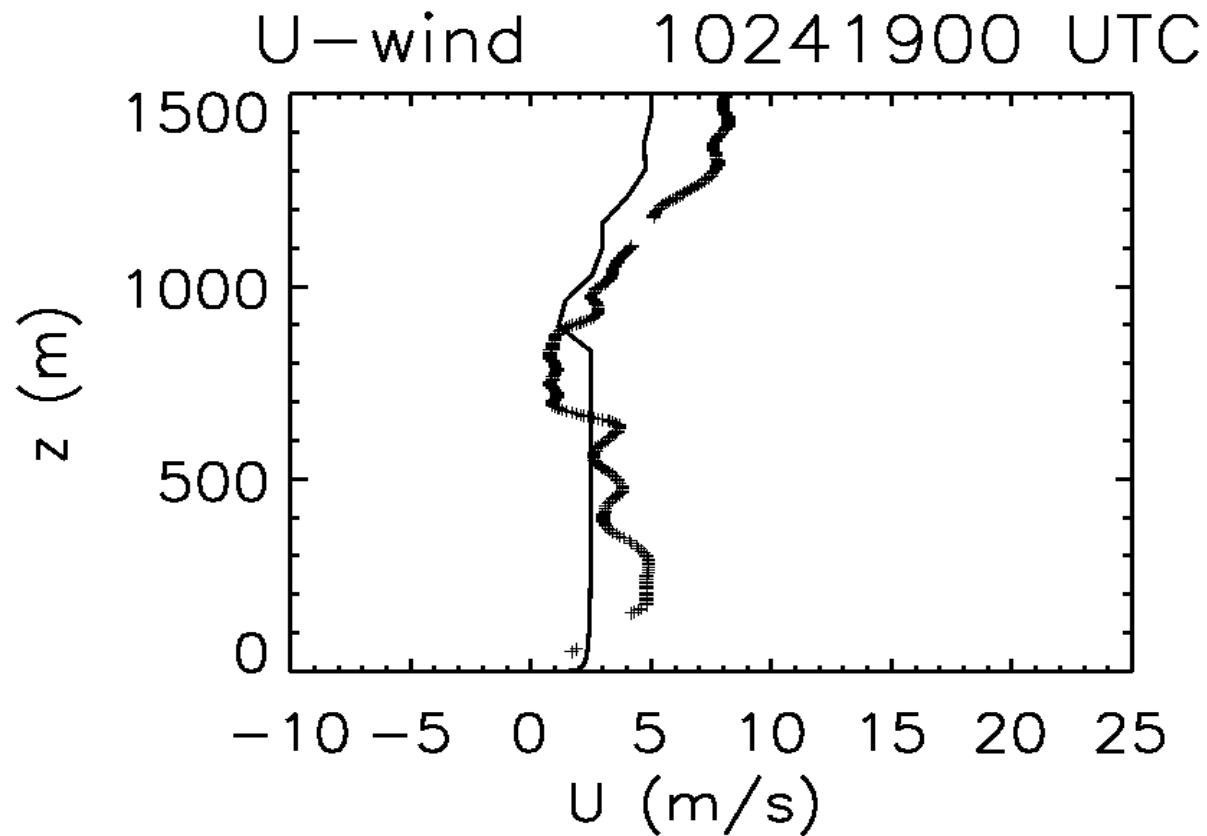


Nonlocal mixing for momentum is also needed, but often ignored  
Proposals are available in literature (e.g Frech and Mahrt, 1995;  
Brown and Grant, 1997, ...)

Wind in CBL may also be influenced by inertial oscillation  
(e.g, Schröter et al, 18<sup>th</sup> BLT, Stockholm)



Wind profiles in reality are not that easy...



Example of CASES99 by Steeneveld et al, 2006

# Does more complexity help?

The Mellor-Yamada Level 2.5 turbulence closure model is governed by the equations

(MY82):

$$d(q^2/2)/dt - (\partial/\partial z)[\ell q S_q (\partial/\partial z)(q^2/2)] = P_s + P_b - \varepsilon \quad (2.1)$$

$$P_s = -\langle wu \rangle (\partial U/\partial z) - \langle wv \rangle (\partial V/\partial z), P_b = \beta g \langle w\theta_v \rangle, \varepsilon = q^3/(B_1 \ell) \quad (2.2)$$

$$-\langle wu \rangle = K_M \partial U/\partial z, -\langle wv \rangle = K_M \partial V/\partial z,$$

$$-\langle w\theta_v \rangle = K_H \partial \theta_v/\partial z, -\langle ws \rangle = K_H \partial S/\partial z, \quad (2.3)$$

$$K_M = \ell q S_M, K_H = \ell q S_H, \quad (2.4)$$

$$S_M (6 A_1 A_2 G_M) + S_H (1 - 3 A_2 B_2 G_H - 12 A_1 A_2 G_H) = A_2, \quad (2.5)$$

$$S_M (1 + 6 A_1^2 G_M - 9 A_1 A_2 G_H) - S_H (12 A_1^2 G_H + 9 A_1 A_2 G_H) = A_1 (1 - 3 C_1), \quad (2.6)$$

$$G_M = (\ell^2/q^2)[(\partial U/\partial z)^2 + (\partial V/\partial z)^2], G_H = -(\ell^2/q^2) \beta g \partial \theta_v/\partial z. \quad (2.7)$$

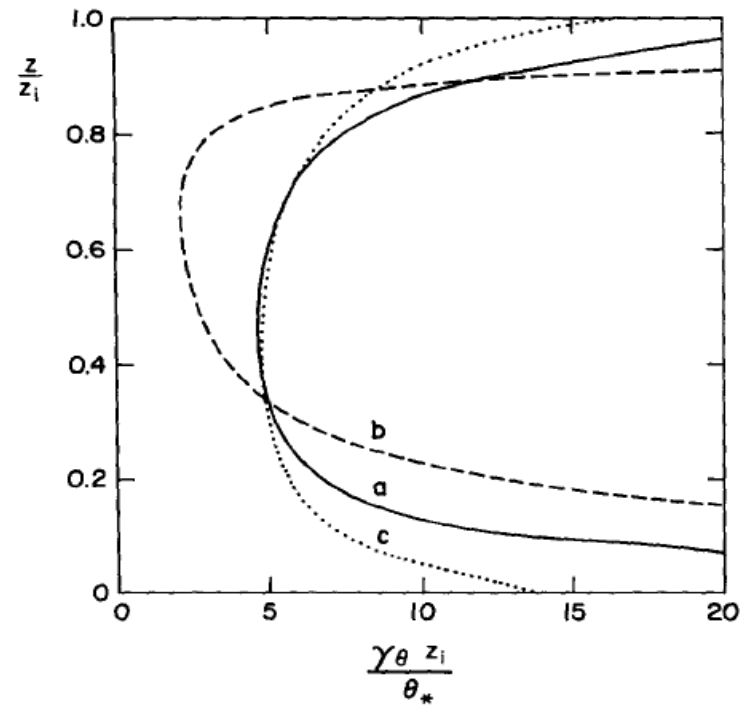
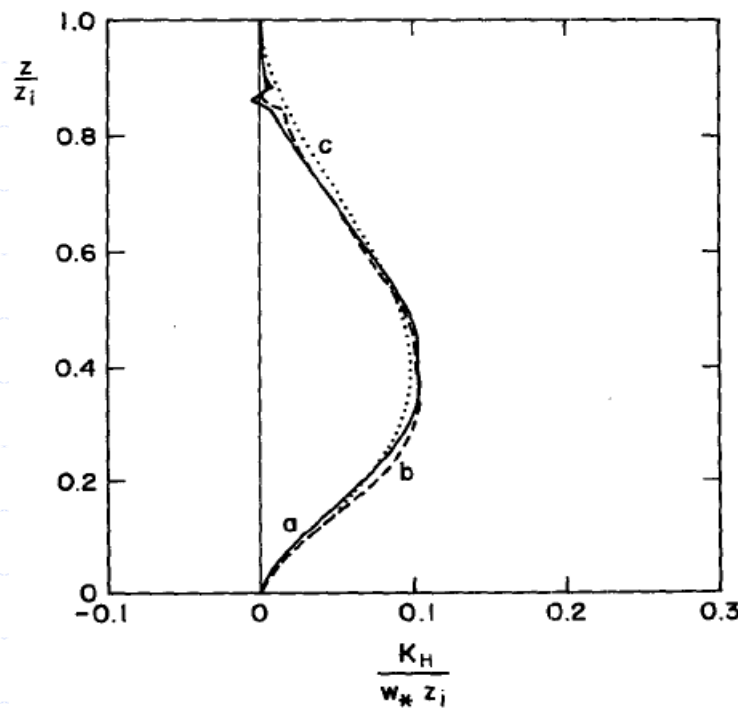
Or even more complexity?

$$\frac{D\overline{w'\psi'}}{Dt} = -\overline{w'^2} \frac{\partial \Psi}{\partial z} + \frac{g}{\Theta_{v0}} \overline{\theta'_v \psi'} - \frac{1}{\rho_0} \overline{\psi' \frac{\partial p'}{\partial z}} - \frac{\partial \overline{w'^2 \psi'}}{\partial z} + S_i$$

Attractive to simplify this,  
for instance by using LES results for flux budgets  
in convective boundary layer

(Deardorff, 1966, 1972; Holtslag and Moeng, 1991;  
Cuijpers and Holtslag, 1998 among others)

# Mixing in Convective boundary layers using results of simplified heat flux budget equation (a: LES; b: Deardorff, 1972; c: Holtslag and Moeng, 1991)



$$\theta_* \equiv \frac{\overline{w\theta_0}}{w_*}$$

$$\frac{K_H}{w_* z_i} = \left(\frac{z}{z_i}\right)^{4/3} \left(1 - \frac{z}{z_i}\right)^2$$

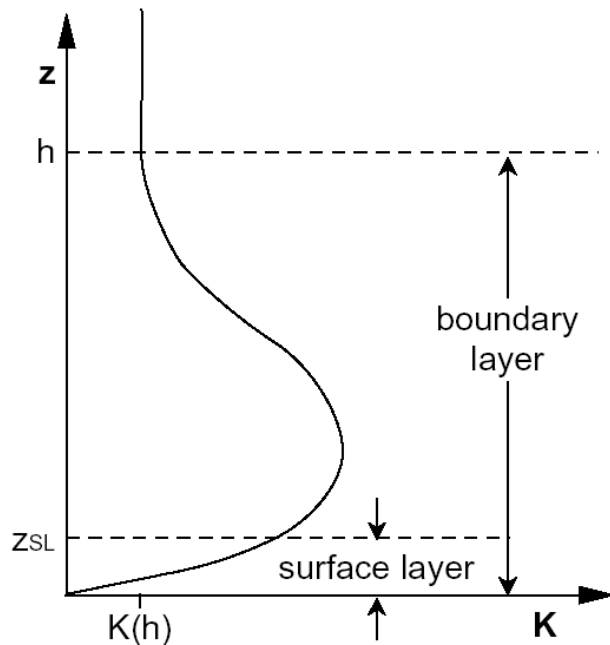
$$\gamma_\theta = c_4 \frac{\overline{w\theta_0}}{w_* z_i}$$

$$w_* \equiv (\beta g \overline{w\theta_0} z_i)^{1/3}$$

# Non-local mixing in convective boundary layers

Use profile function for eddy-diffusivity and non-local ('counter-gradient') corrections

$$\overline{w\theta} = -K \left( \frac{\partial \theta}{\partial z} - \gamma \right)$$

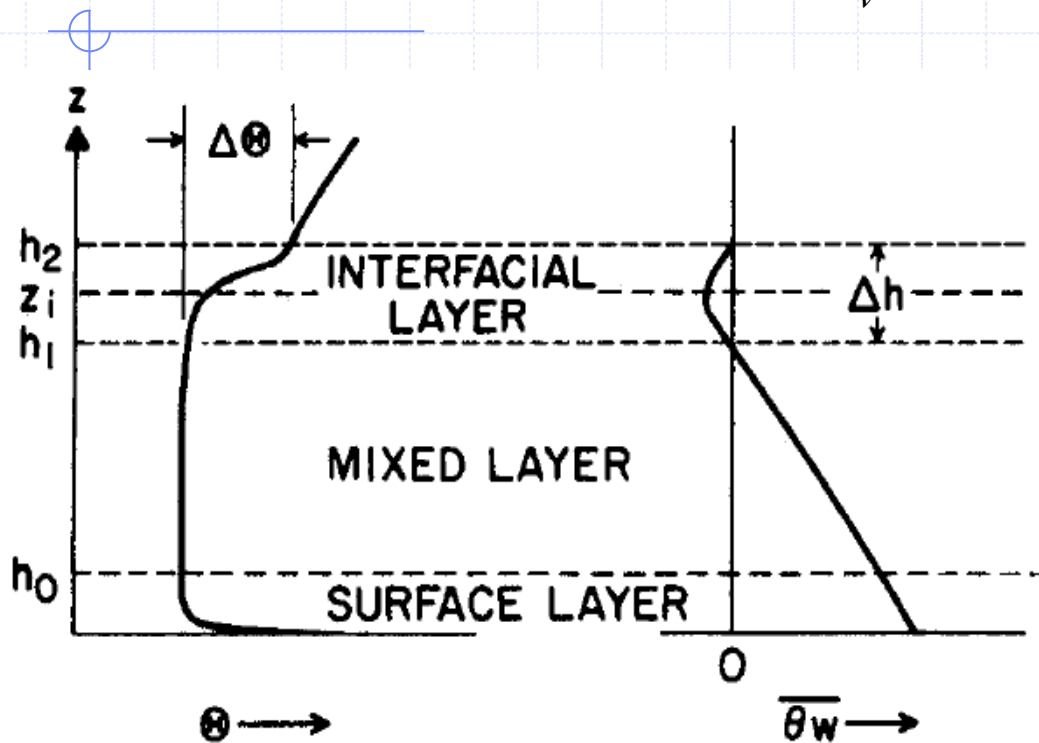


Deardorff (1966, 1972)  
Troen and Mahrt (1986)  
Holtslag and Boville (1993)  
Large et al (1994)  
Hong and Pan (1996)  
Beljaars and Viterbo (1998)  
Lock et al (2000)  
et cetera

This approach is now widely adopted (e.g., NCAR, NCEP, UKMO, ECMWF,...),  
but details differ...

# Entrainment

$$-\frac{g}{\theta_v} \left( \overline{w \theta_v} \right)_h = 0.2 \frac{g}{\theta_v} \left( \overline{w \theta_v} \right)_o + \frac{u_*^3}{h}$$



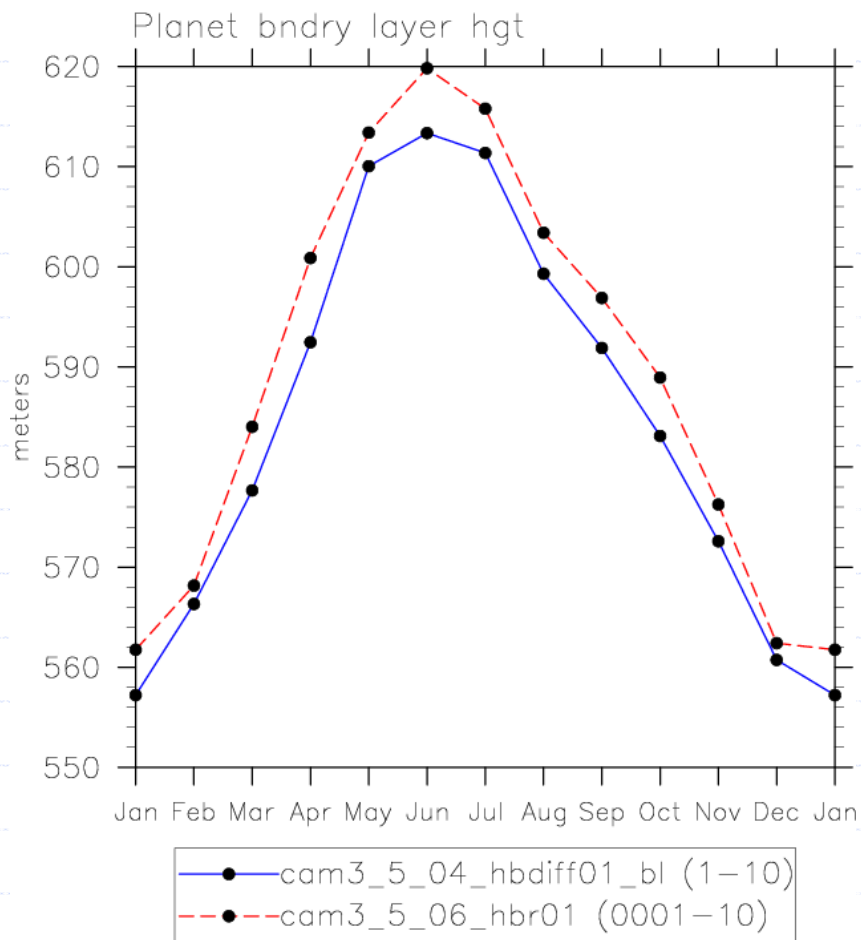
To avoid sensitivity for numerical details, prescribe entrainment **explicitly** using surface buoyancy flux and friction velocity (Moeng and Sullivan, 1994 among others)

Potential  
Temperature  
Profile

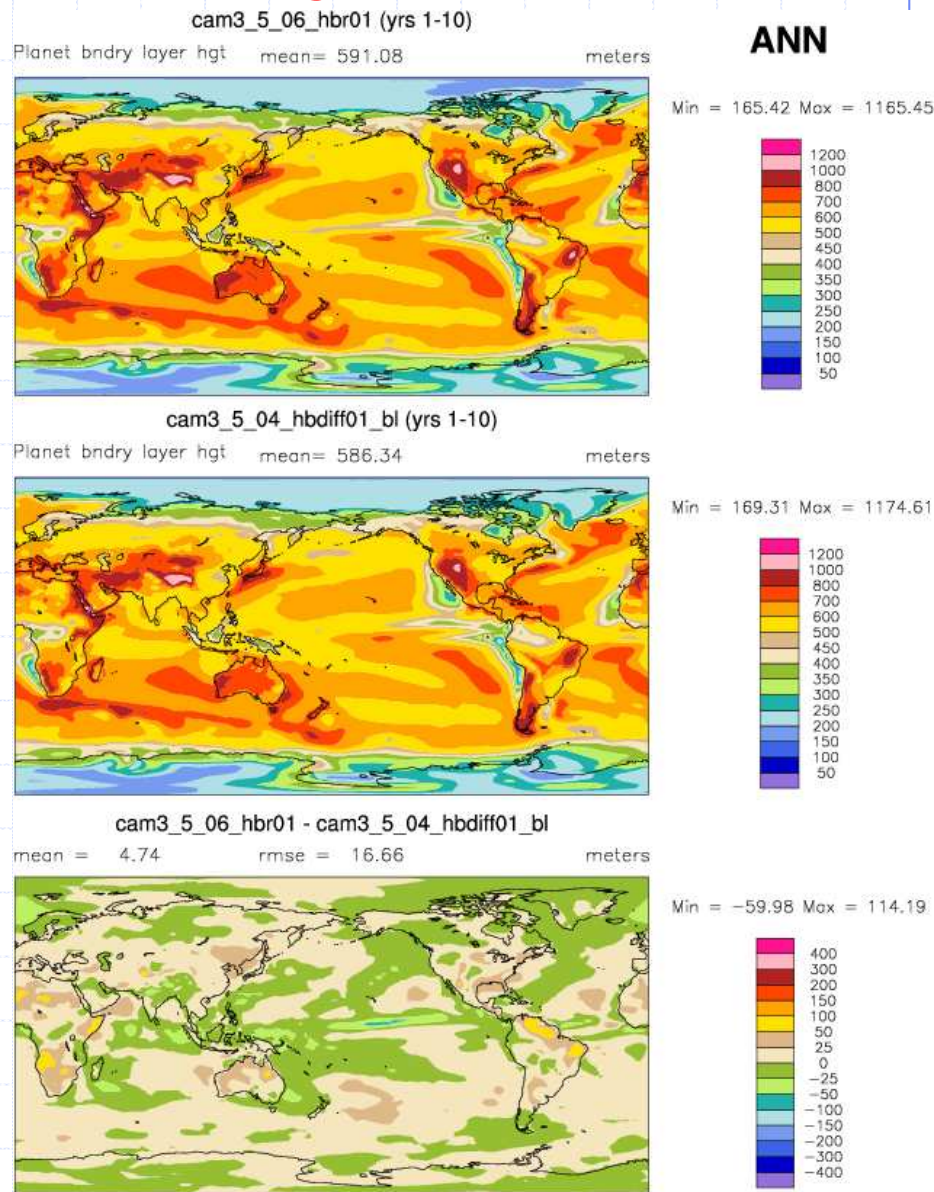
Heat Flux

# Some impact of entrainment on pbl height in NCAR Climate model (Holtlag, Svensson, Rasch and Large, 18<sup>th</sup> BLT)

**Annual Cycle Global Mean Climatology**



**CAM 3.5 - 26 levels**



## A simple mixing scheme: Flux-Gradient Theory or First Order Closure

$$\overline{w'c'} = -K \frac{\partial C}{\partial z}$$

Turbulent Flux

$$K = \left| \frac{\partial U}{\partial z} \right| l^2 F_{m,h}(Ri)$$

Diffusivity K depends on  
characteristics of turbulent flow

*l* : length scale

$$Ri = \frac{g}{\theta} \frac{\partial \theta}{\partial z} / \left| \frac{\partial U}{\partial z} \right|^2$$

Richardson number  
(measure for local stability)

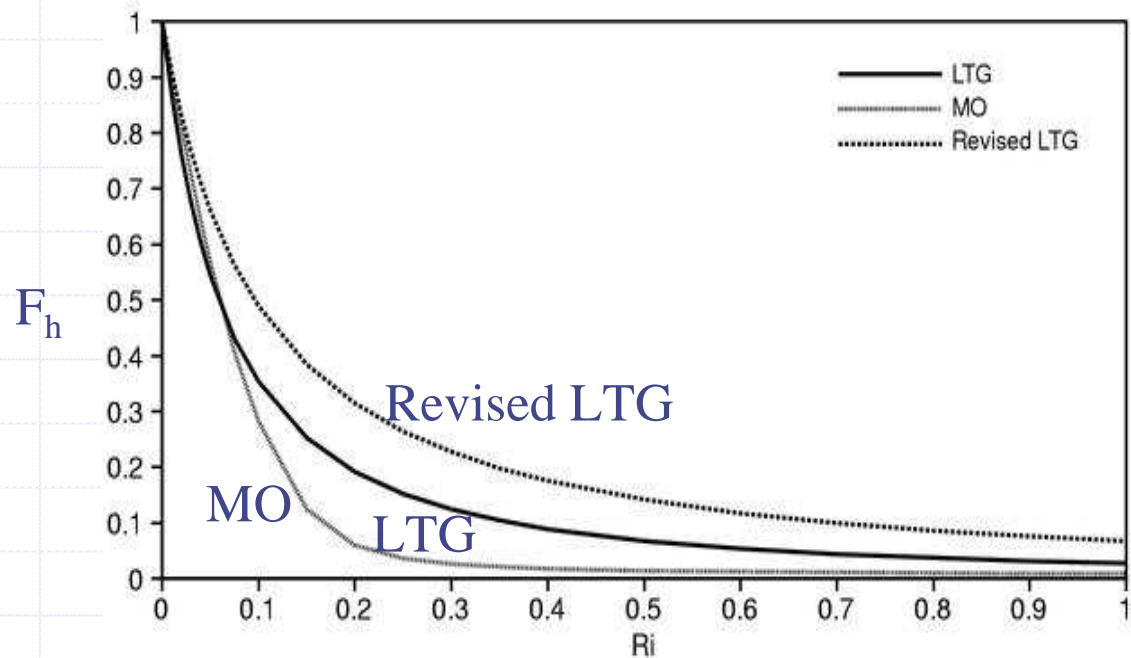
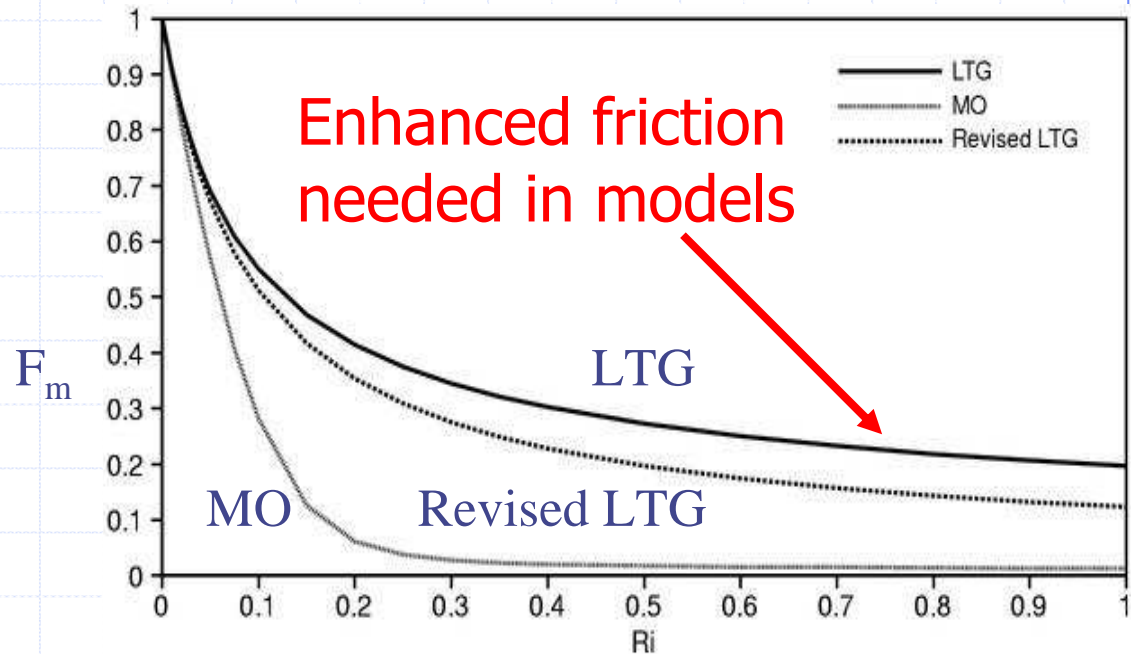


## *Stable boundary layer mixing*

Three alternatives for stability functions of heat and momentum

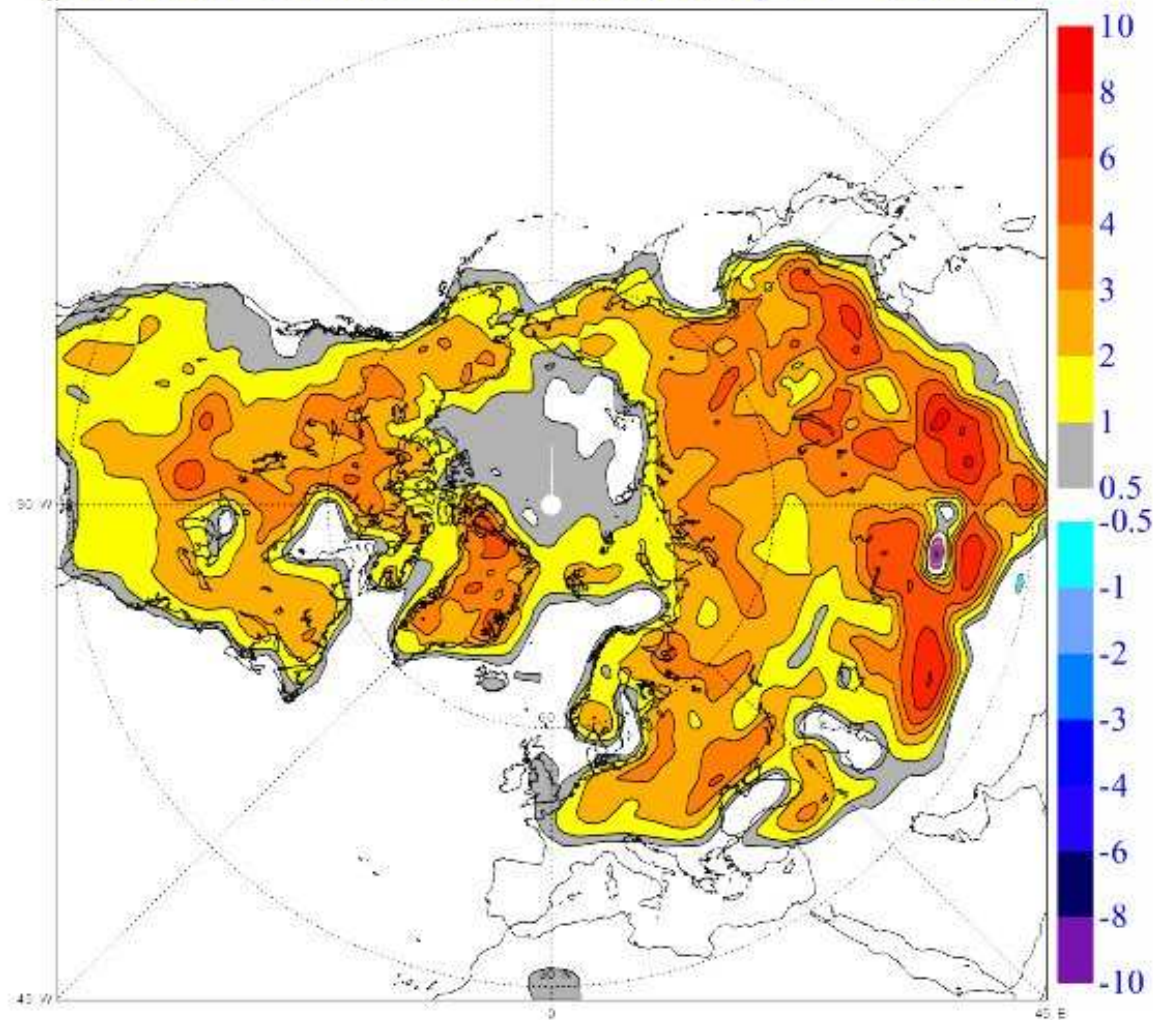
LTG: Louis et al (1982)

MO: Extended Monin-Obukhov type, in agreement with Cabauw tower observations (Beljaars and Holtslag, 1991)



# Mean model difference in 2 meter temperature for January 1996 using two different stability functions in ECMWF model (Courtesy A. Beljaars)

Diff; 2t off 19951001 2184 to 2880 by 24 z12t-z11p



# DJF

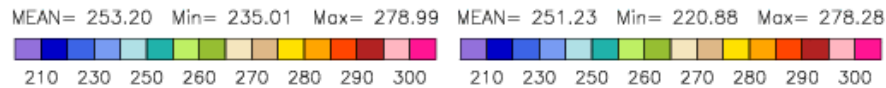
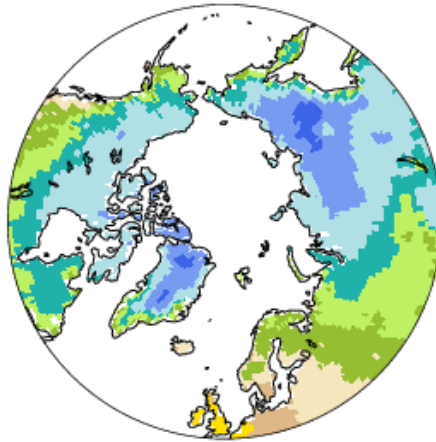
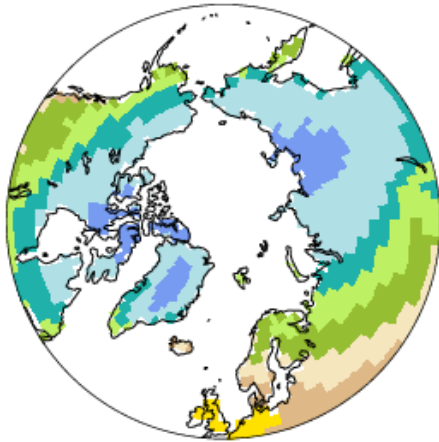
cam3\_5\_04 (yrs 1-10)

WILLMOTT

2-meter Temp (land)

K 2-meter Temp (land)

K

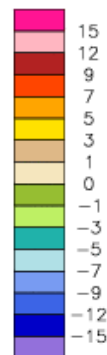
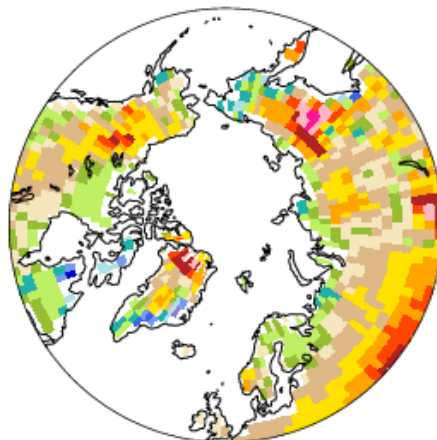


cam3\_5\_04 - WILLMOTT

2-meter Temp (land)

K

MIN = -15.90 MAX = 20.40



Comparison of climate models (such as NCAR-CAM) with observations for 2m temperature reveals large differences over land and ice in stratified conditions (here for HB scheme; 10 year winter averages)

Holtslag+Boville, J. Clim., 1993

DJF

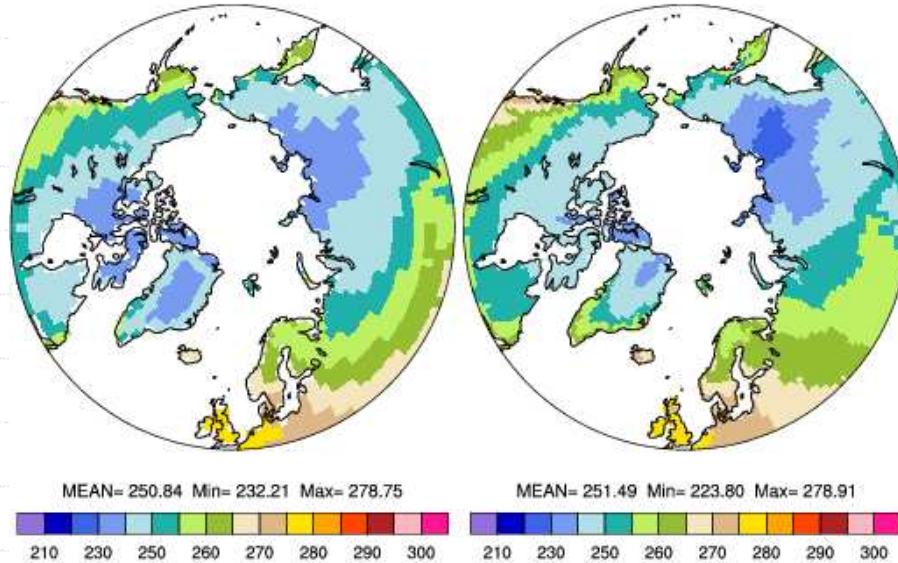
cam3\_5\_04\_uw00\_bl (yrs 1-10)

IPCC/CRU

2-meter Temp (land)

κ 2-meter Temp (land)

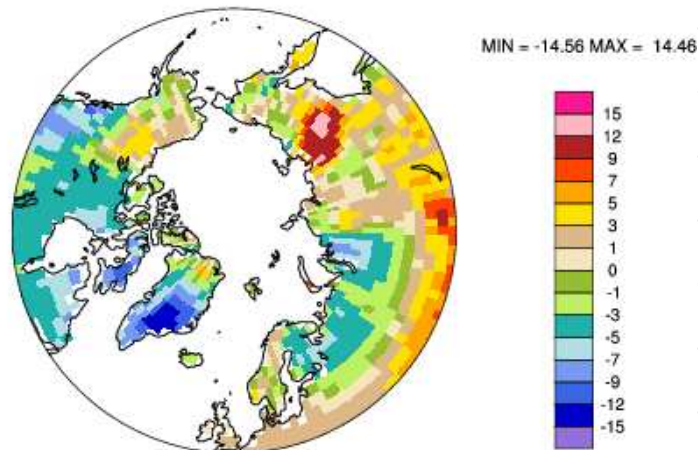
K



cam3\_5\_04\_uw00\_bl - IPCC/CRU

2-meter Temp (land)

K



Comparison of climate models (such as NCAR-CAM) with observations for 2m temperature reveals large differences over land and ice in stratified conditions (here for UW scheme; 10 year winter averages)

University of Washington scheme;  
Songsu Park and Chris Bretherton

## *State of art*

Larger scale atmospheric models have problems in representing stable boundary layers and typically allow for more mixing than can be seen in local observations

Sensitivity to details in formulation, in particular over land and ice



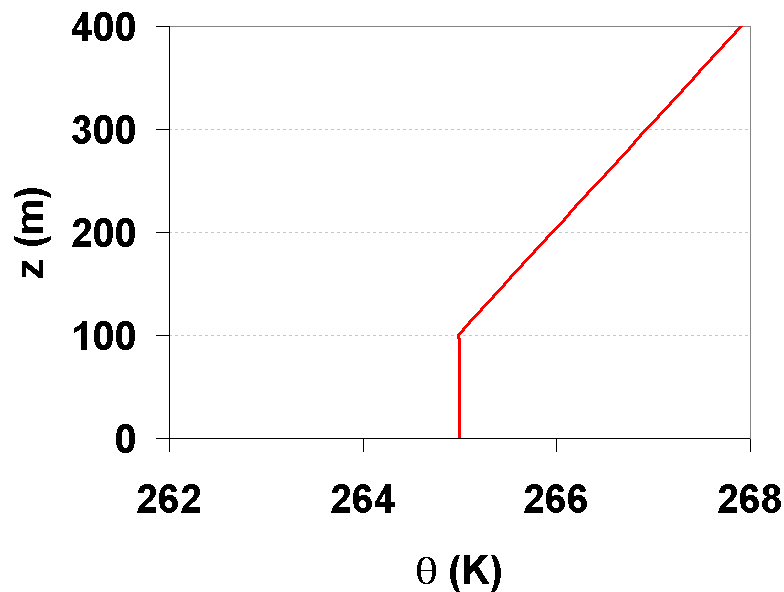
One of the motivations to organize the GEWEX Atmospheric Boundary Layer Study (see [www.gewex.org](http://www.gewex.org))

# ***GABLS first model inter-comparison case***

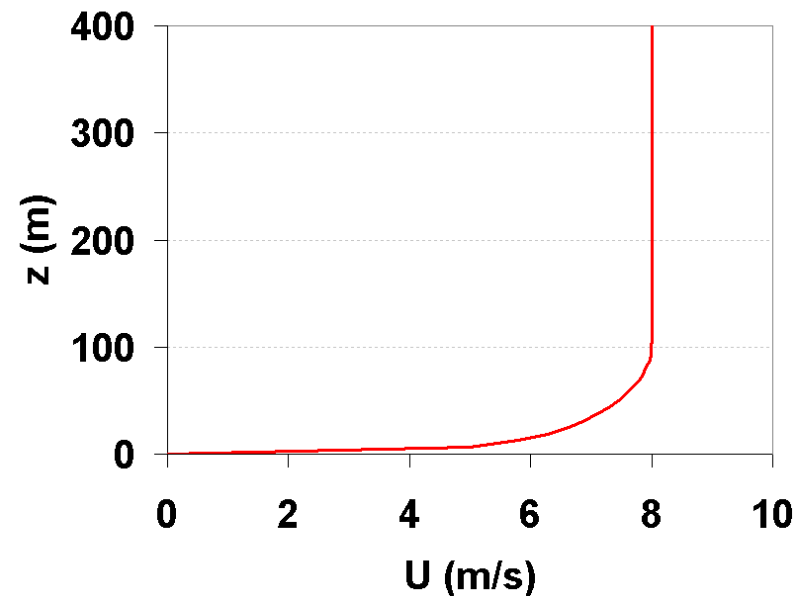
Simple shear driven case for a stable boundary layer over ice  
(after Kosovic and Curry, 2000)



Initial temperature profile GABLS case study



Initial wind profile GABLS case study



Prescribed surface cooling 0.25 K/h for 9 hours to quasi- equilibrium; no surface and radiation scheme

Geostrophic wind 8 m/s, latitude 73N

## List of 20 participating 1D models (Cuxart et al, 2006)

Model	Use	Type	Ref
ECMWF	operational	1st order	Beljaars and Viterbo, 1998
ECMWF-MO	operational-test	1st order	
NOAA-NCEP	operational	1st order	Hong and Pan, 1996
MeteoFrance	operational	1st order	Louis et al., 1982
JMA	operational	1st order	Mellor and Yamada, 1974
Met Office	operational	1st order	Louis, 1979
Met Office res	research	1st order	Williams, 2002
Wageningen U	research	1st order	Duynderke, 1991
Sandia Labs	research	ODT	Kerstein et al., 2001
MSC	operational	$e - l$	Belair et al., 1999
KNMI-RACMO	operational	$e - l$	Lenderink and Holtslag, 2004
UIB-UPC	research	$e - l$	Cuxart et al., 2000
	mesoscale model		
NASA	research	$e - l$	Xue et al, 2000
	mesoscale model		
WVU	research	$e - l$	Sykes and Henn, 1989
York U.	research	$e - l$	Weng and Taylor, 2003
Louvain U-L	research	$e - l$	Therry and Lacarrère, 1983
Louvain U-eps	research	$e - \epsilon$	Duynderke, 1988
Swedish MS	research	$e - \epsilon$	
Stockholm U	research	$e - l$	Andren, 1990
Stock.U-sim	research	$e - \theta^2$	Mauritsen et al., 2004

## List of 11 participating LES models (Beare et al, 2006)

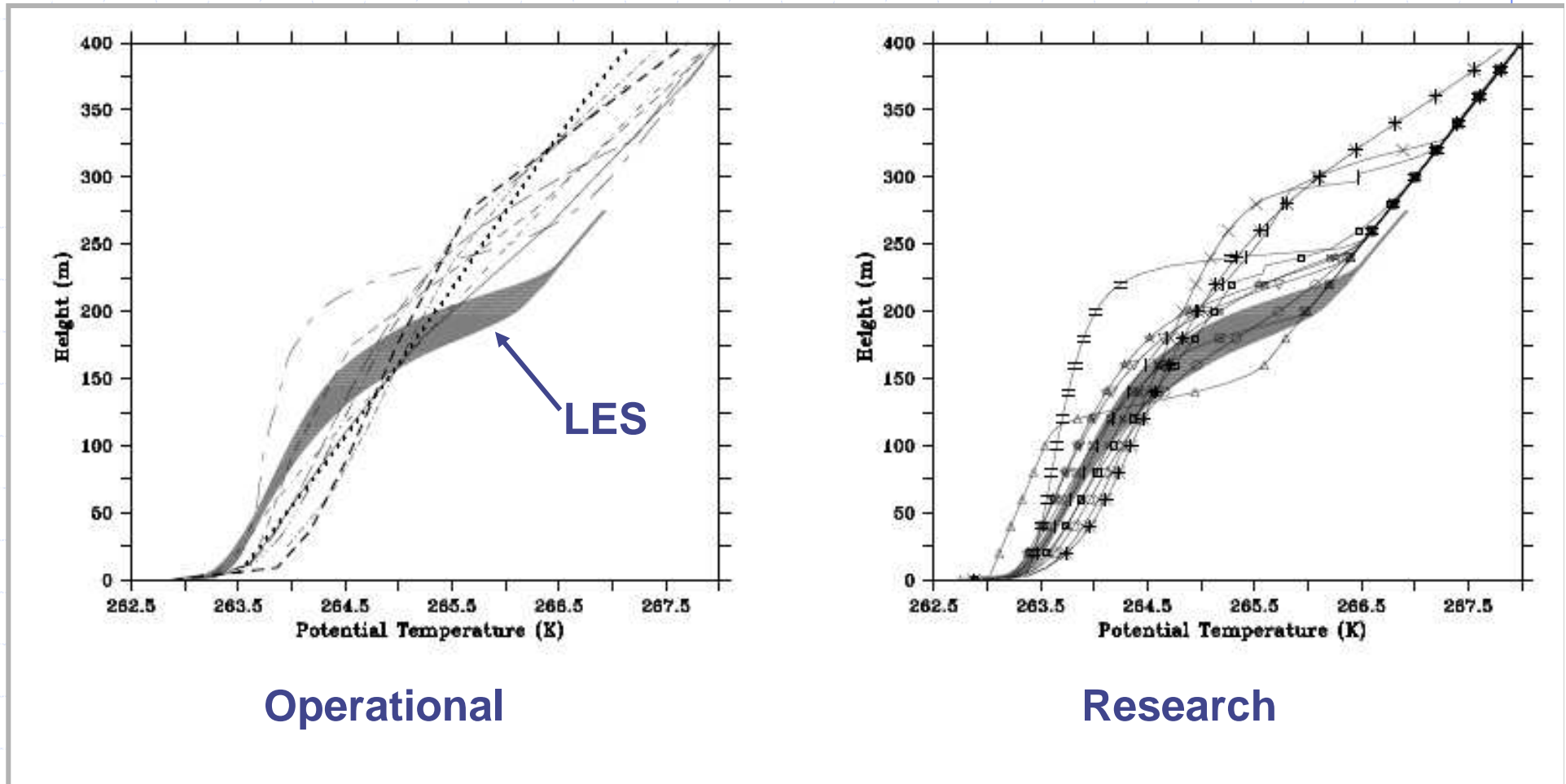
TABLE I  
A summary of the participants.

Model	Institution (s)	Scientist (s)
MO	Met Office, UK	Beare, McCabe, MacVean
CSU	Colorado State University	Khairoutdinov
IMUK	University of Hannover, Yonsei University	Raasch, Noh
LLNL	Lawrence Livermore National Laboratory	Lundquist, Kosovic
NERSC	Nansen Environment and Remote Sensing Center	Esau
WVU	West Virginia University	Lewellen
NCAR	National Center for Atmospheric Research	Sullivan
UIB	Universitat de les Illes Balears	Jimenez, Cuxart
CORA	Colorado Research Associates	Lund
WU	Wageningen University	Moene, Holtslag
COAMPS™	Naval Research Laboratory	Golaz

LES: Large-Eddy Simulation model  
(e.g. fine-scale model resolving largest turbulent motions)  
Ensemble of LES results is taken as reference!

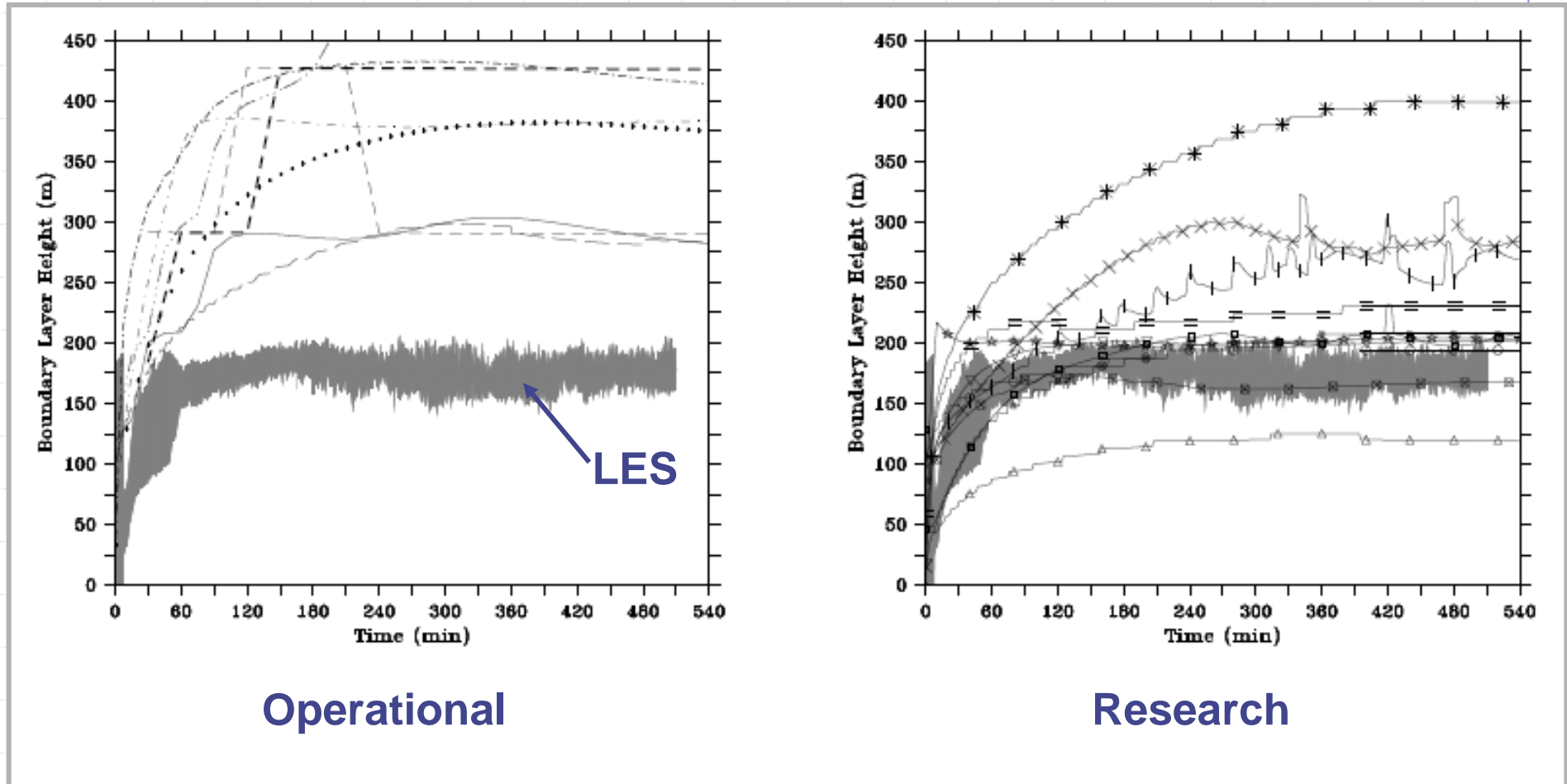


# Potential temperature



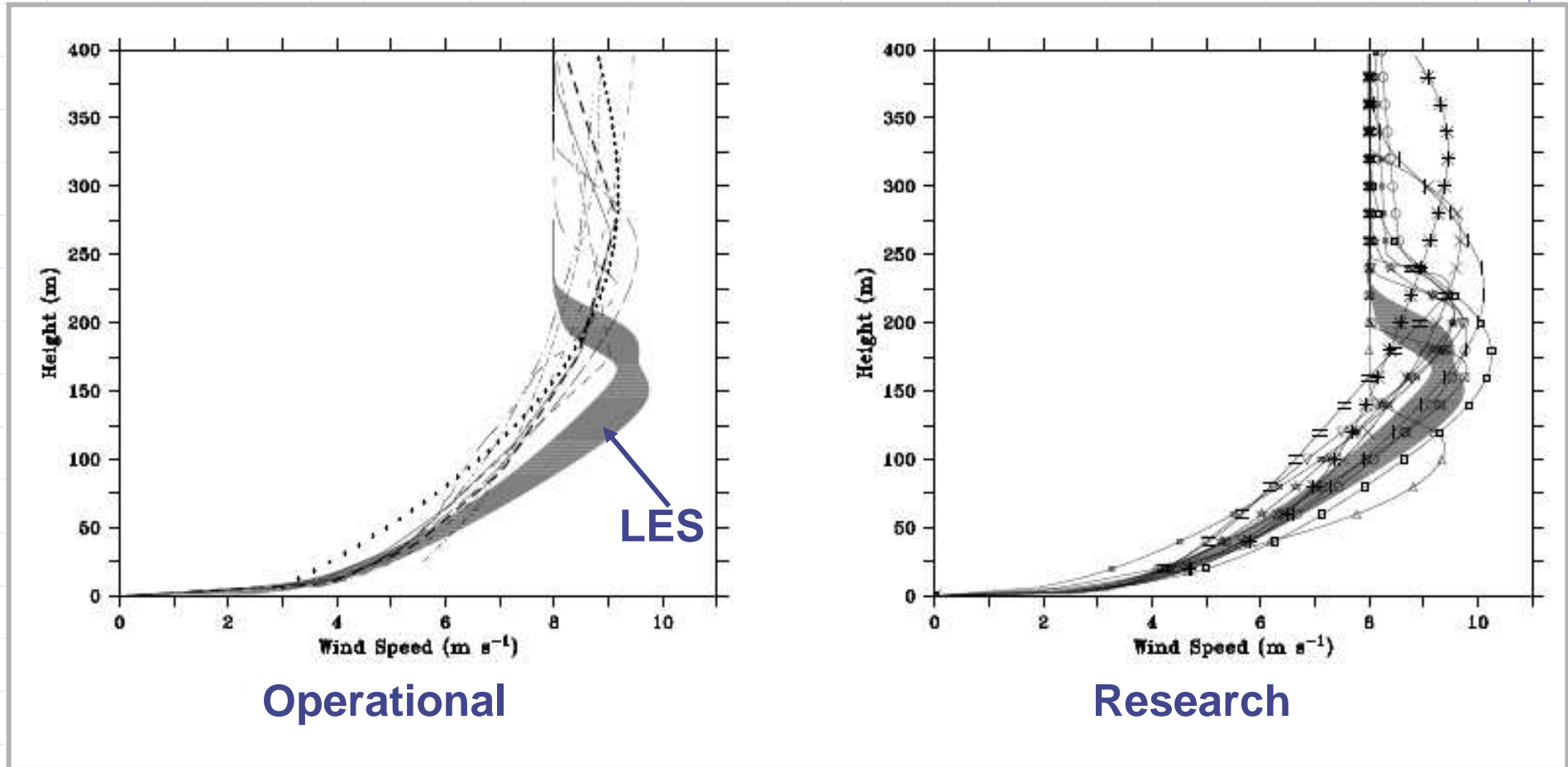
Comparison of Single-Column Models with Large Eddy Simulations (LES)  
(Beare et al, 2006; Cuxart et al, 2006)

# Boundary-Layer Height

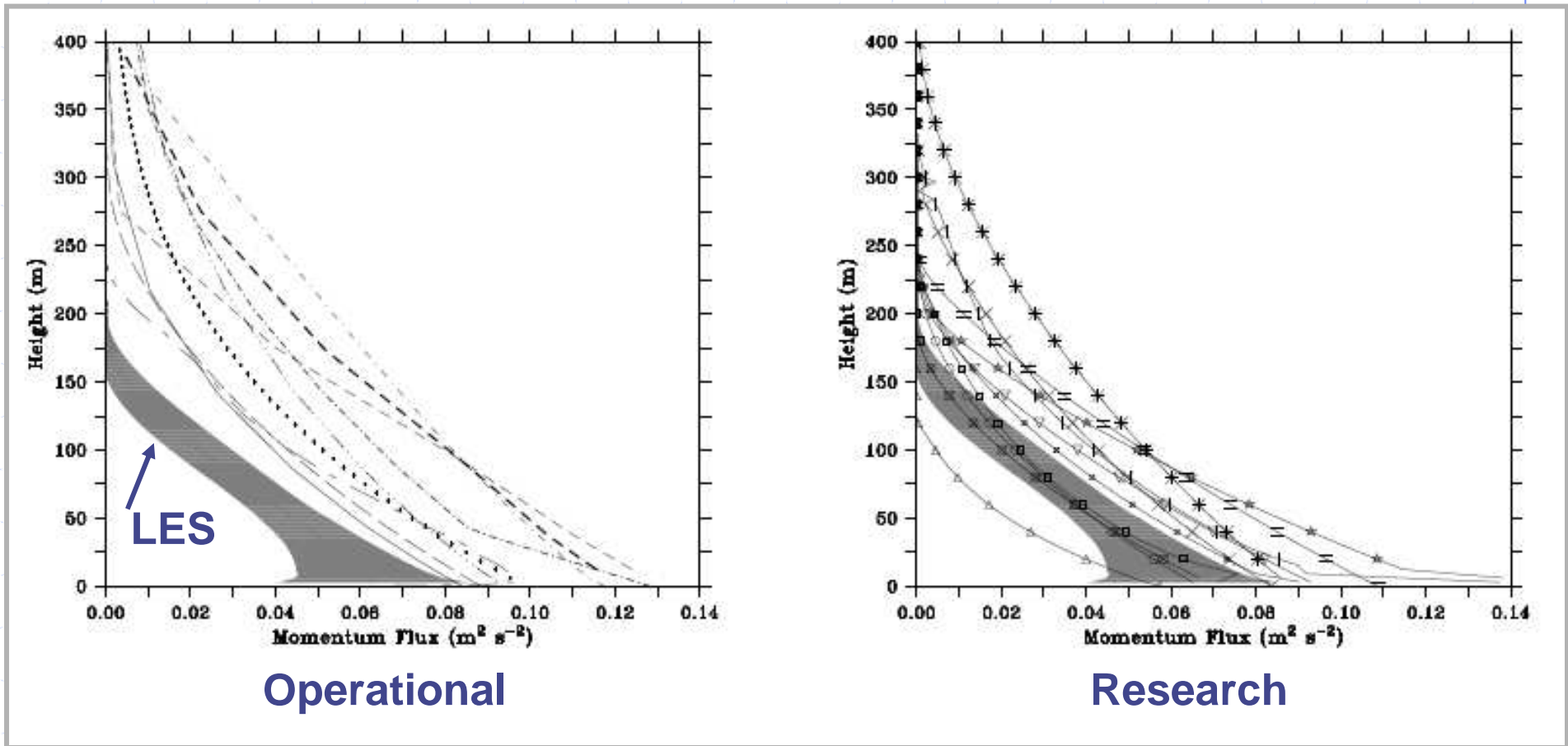


Resolution (most) operational models is set to 6.25 m!

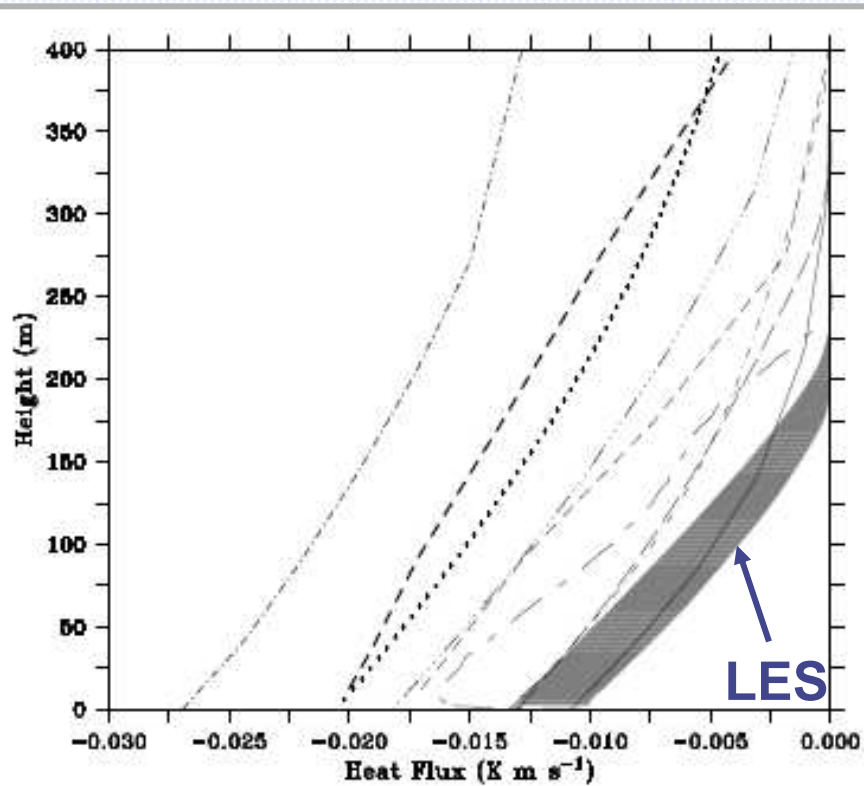
# Wind speed



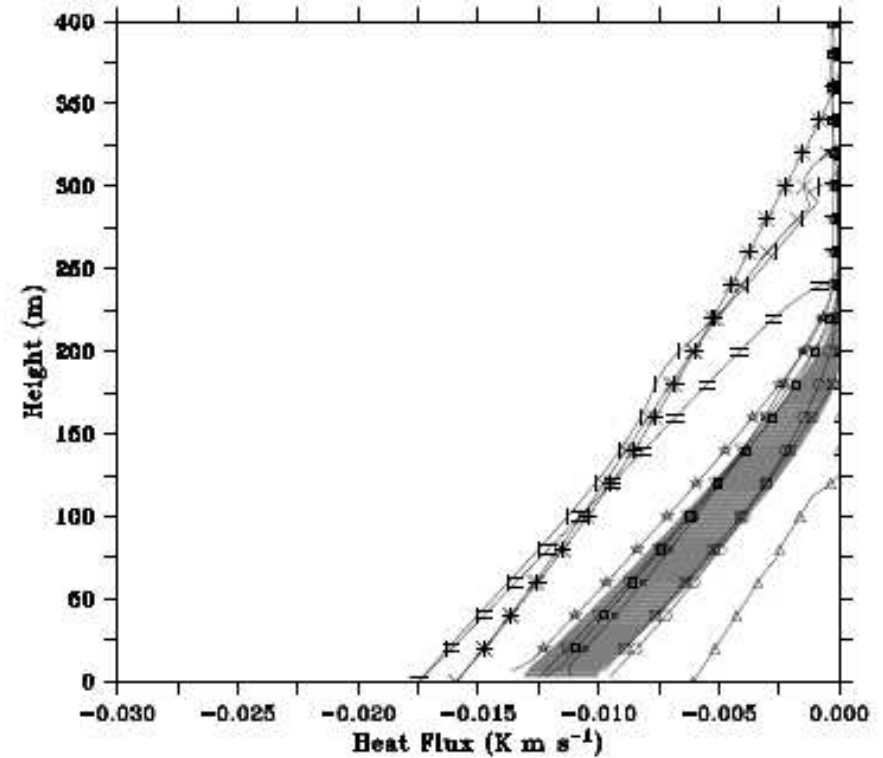
# Momentum flux



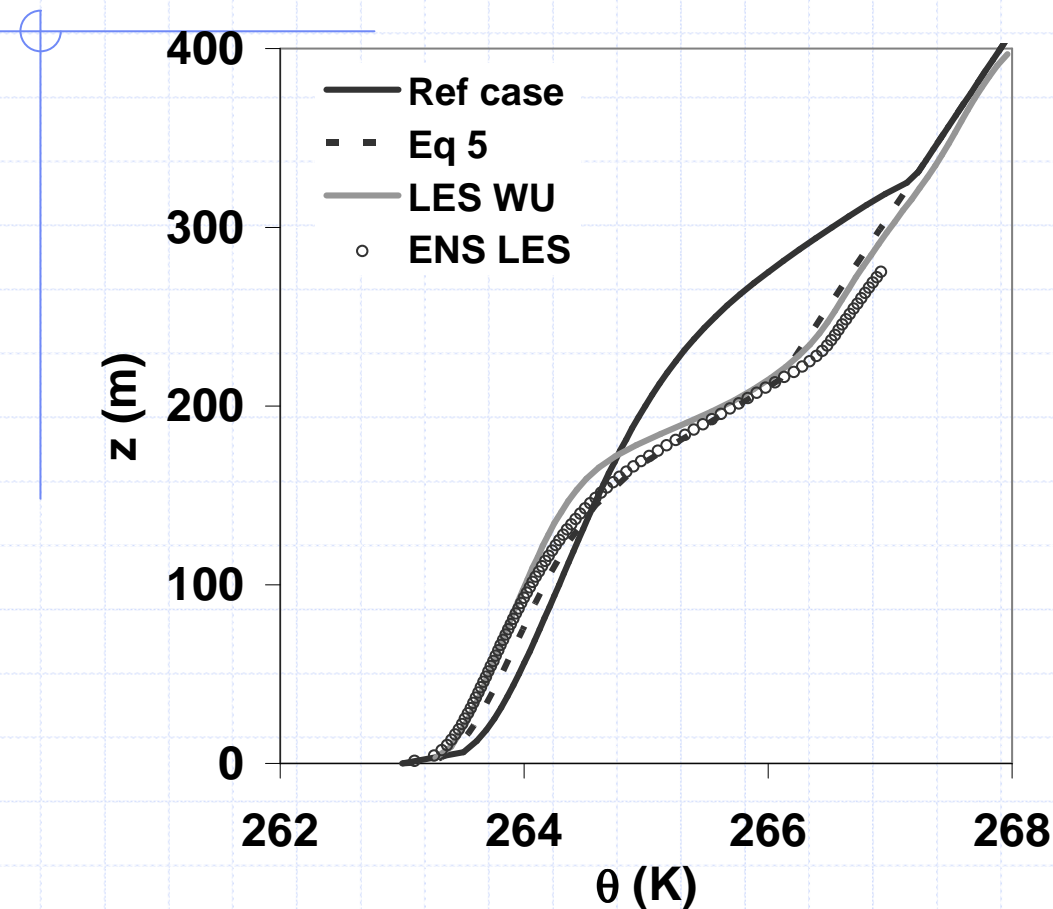
# Heat flux



Operational

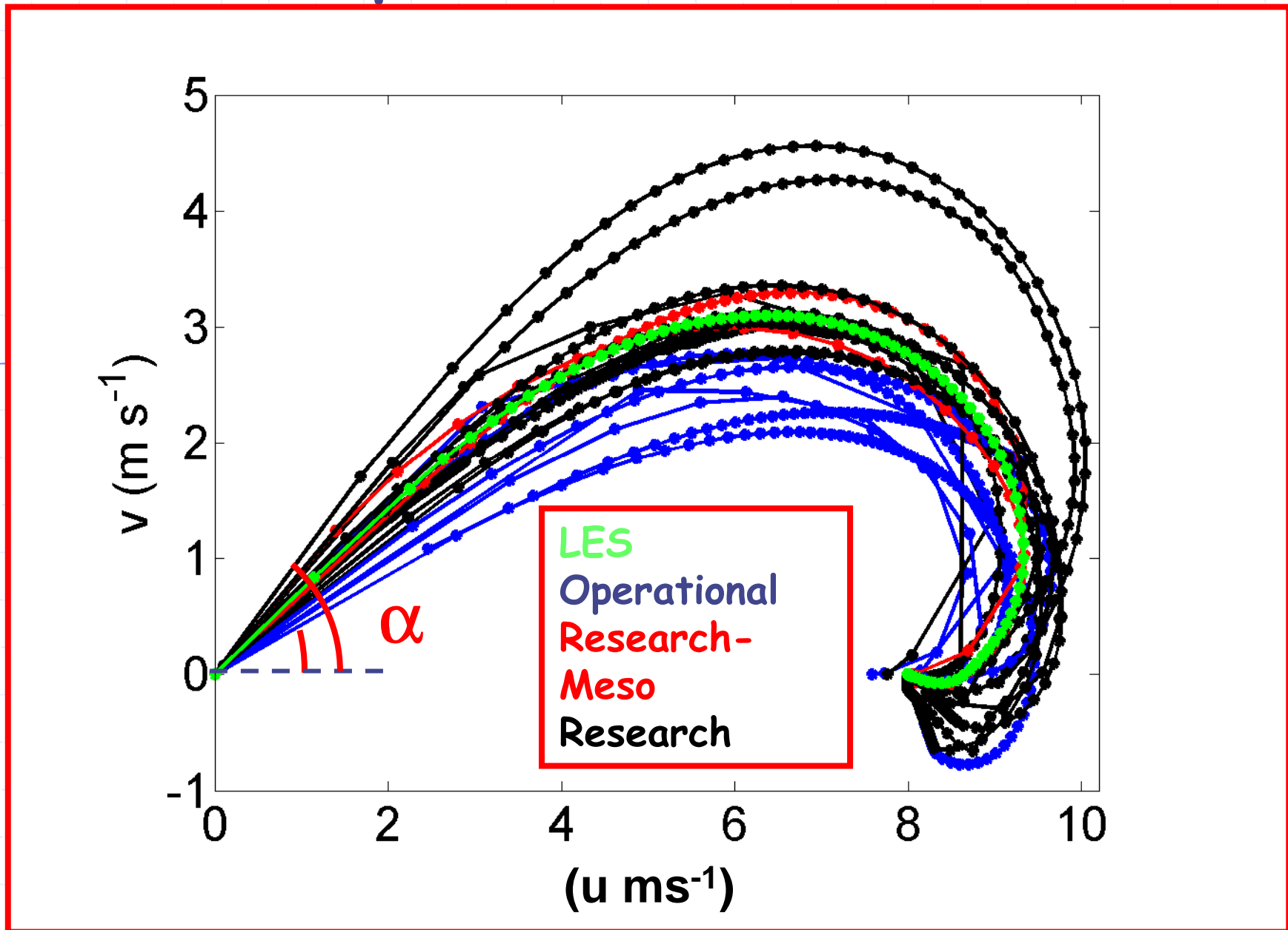


Research

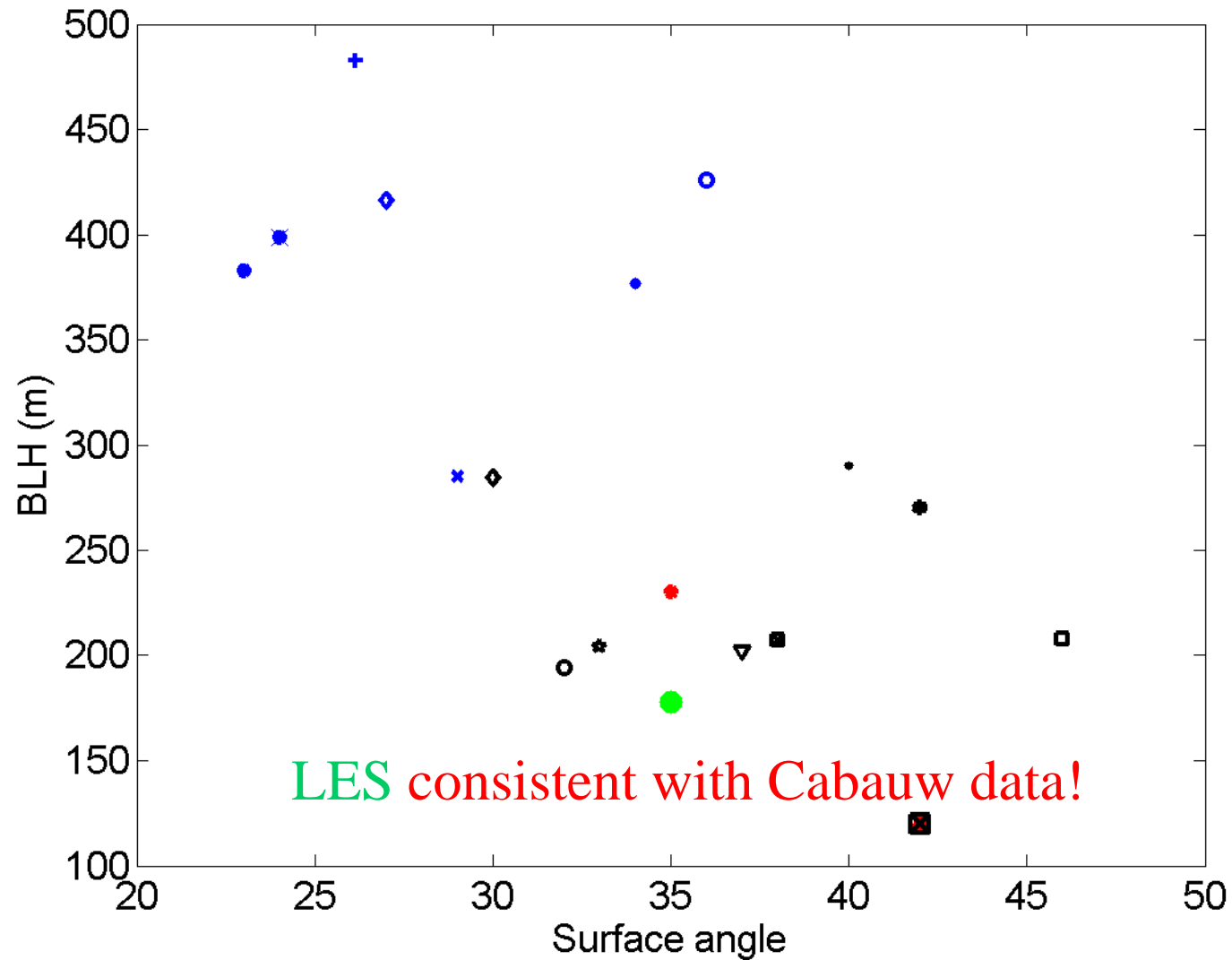


Note:  
Models can represent  
main LES results  
after adjusting  
parameters in  
turbulence scheme

# 'Ekman spirals' (Svensson+Holtslag, 2008)

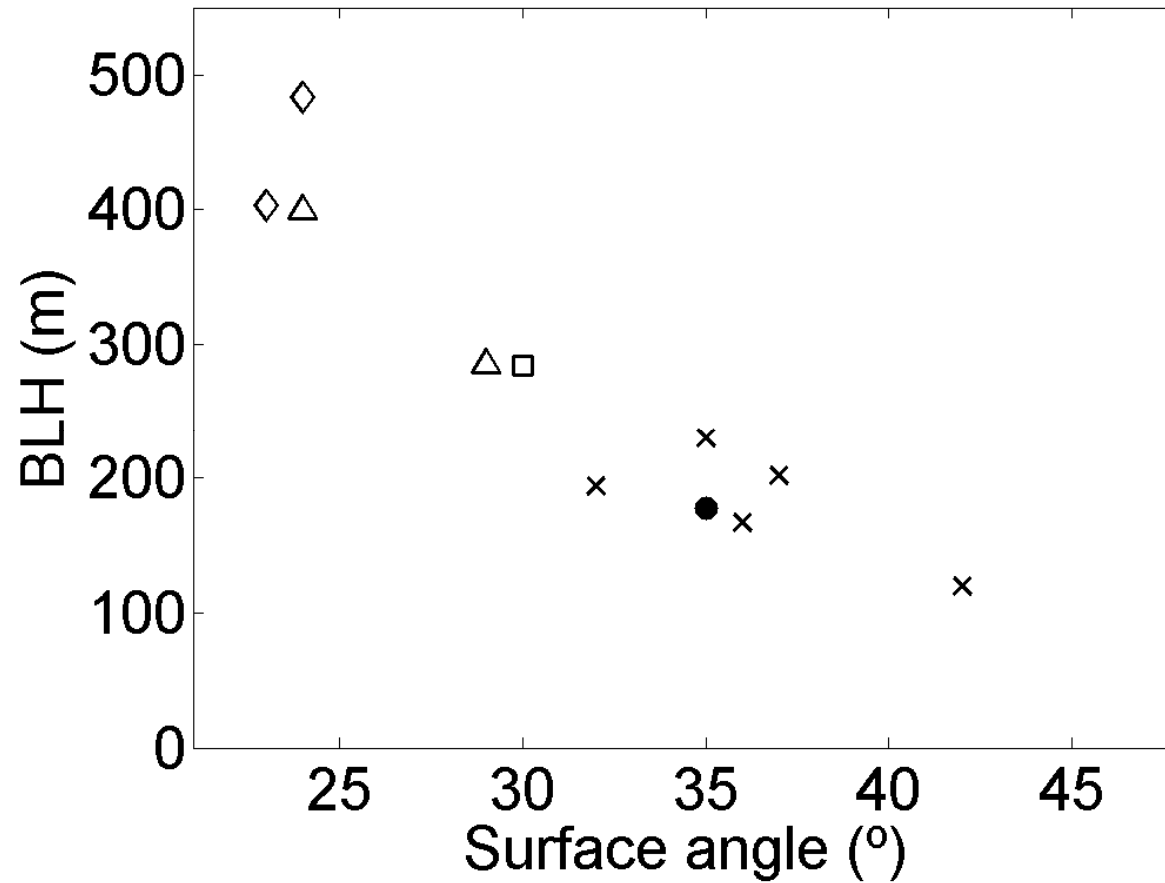


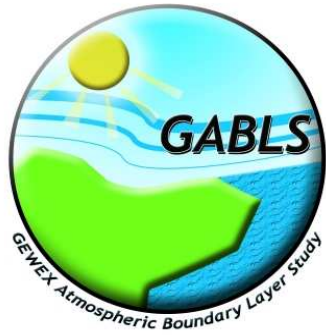
# Boundary-layer height and surface angle





# Models with surface problems removed





## *Summary*

### *First GABLS model intercomparison on stable boundary layers*

Large variation among 1D models, but all operational models show too strong mixing!

Results of LES models in good agreement with observations in relatively homogeneous cases (e.g. Nieuwstadt, 1984)

*Eight papers in special GABLS issue of Boundary Layer Meteorology, Feb. 2006*

## Why do Operational Models need Enhanced Mixing in Stable Cases?

To prevent unrealistic 'runaway' surface cooling

To have sufficient 'Ekman pumping'

To compensate for model errors?

Do we overlook an atmospheric process  
e.g., gravity waves?

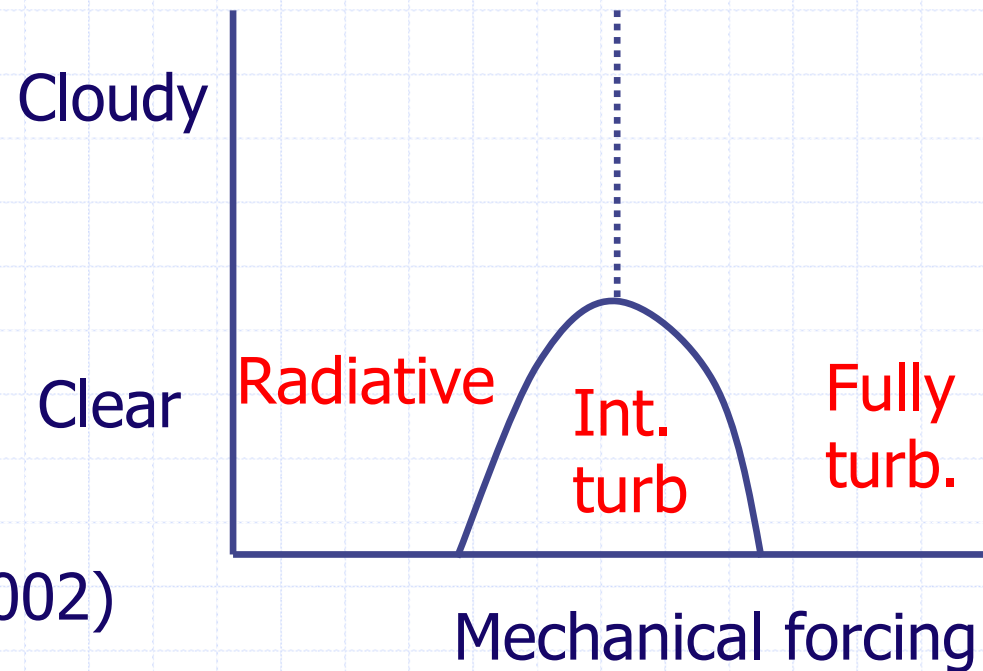
What is impact of surface heterogeneity?

What about more stable cases?

## Three different regimes in stable boundary layers over land:

- Fully turbulent (such as in GABLS1)
- Intermittent turbulent
- Radiation dominated

(see Van de Wiel et al, 2002)



Can we model these different regimes with a state of the art single column model?

## Some recent achievements

SBL modeling benefits from a detailed interaction with vegetation and radiation processes, in particular when local information is used for soil and vegetation parameters and with high resolution in atmosphere and soil near the surface (Steeneveld et al, 2006; 2008).

This also improves the mesoscale model (WRF/MM5)

Surface temperature feedback can compensate for some of the variety introduced by changing model parameters (Holtslag et al, BLM, 2007)



# Overview GABLS Studies

- GABLS1
  - Academic set-up
  - LES as reference
  - Special GABLS issue in *Boundary Layer Meteorology*, Feb. 2006
- GABLS2
  - Based on a dry case (CASES99)
  - Diurnal cycle
  - Notice Prescribed  $T_s$ !
  - Manuscripts in preparation!

GABLS3 using a more humid site (Cabauw)

Intercomparison of LES, 1D and possibly regional models with observations

Focus

- SBL, Morning and evening transition
- Land-atmosphere coupling
- Low-level jet

SCM case released, but participation still possible! (contact Fred Bosveld)

LES case released by July 2008 (contact Sukanta Basu)

# Take home messages



Many proposals in literature for turbulent mixing regarding diffusivities and length scales

Flux-gradient approach is doing well in stable conditions, with diffusivities on basis of local gradients. However, larger scale models seem to need more drag...

For convective cases, non-local corrections are needed and entrainment needs special attention

**Evaluation of approaches is a never ending job (GABLS)!**