Bioinspired nanopatterned surfaces via colloidal templating; a pathway for tuning wetting and adhesion

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To all those ‘sacrificed’ for science
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1 Introduction
Nature shows extraordinary examples of surfaces deriving functions using surface structures. Designing surface structures is therefore an interesting pathway to tune functions. In this thesis, we focus on two functions, namely adhesion and wetting. Although we understand adhesion and wetting of ideal surfaces (perfectly flat and homogeneous), our insights are less strong when switching to more complex systems by also including surface patterns. A systematic study on the influence of structure on function is needed. Such study should include a systematic way to fabricate surface structures, and test properties derived from the structure. This thesis is a step in that direction.

1.1 Functional surfaces in nature

The surface of a bacterium, fungus, plant, or animal is often complex. Living creatures must feed, move, breath, excrete, grow, sense and reproduce. Their surface is therefore not just a boundary between the inside and the outside, but entails essential properties and functions to survive.

It was not until the 20th century that these surfaces could be studied on scales smaller than the wavelength of visible light by the invention of techniques like the scanning electron microscope\textsuperscript{1} and atomic force microscope.\textsuperscript{2} These techniques can magnify surfaces to length scales previously unimaginable. And it is on these tiny scales that nature reveals one of its secrets to surfaces with special functions: surface structures.

For example: a plant needs sunlight reaching its leaves unperturbed in order to use it for photosynthesis. This is tricky for plants living in ponds, where dirt is everywhere. The lotus plant has the remarkable property that the dirt on its leaves simply roll off from its surface along with rain droplets (Figure 1A). Its secret? Small surface structures (Figure 1B).\textsuperscript{3} Another water-based creature, a shark, uses surface structures to mute the effect of turbulence, thereby reducing the amount of energy needed to swim around (Figure 1D).\textsuperscript{4} For springtails their surface structure is more vital: this structure (Figure 1F) holds an air bubble when the creatures are immersed in a liquid, preventing them
Figure 1. Patterned surfaces in nature: A) photograph and B) scanning electron microscopy (SEM) image of lotus leaf. C) Cartoon and D) SEM image of the scale structure of shark skin. E) Photograph and F) SEM image of the surface of a spring tail. G) Photograph and H) SEM image of Gekko gecko adhesive structures. BR: branch. Adapted with permission from ref 4.
from suffocation. And without the surface structure on their feet (Figure 1H), geckos would not be able to climb and cling as well as they can.

1.2 Bioinspiration

It is therefore instructive to look at nature for inspiration when you want to design a surface with functions of your choice. Unfortunately, we do not have the machinery to directly mimic nature. And, since surfaces in nature have often multiple functions and limitations and only have to function under ambient conditions, a structure that resembles nature’s examples may not always be the most optimal surface structure for our purpose.

An example is the gecko toe pad as shown in Figure 1GH. This animal is the most prominent source of inspiration in the field of bioinspired, dry adhesion. The relatively large size of the animal and its ability to stick to almost any surface, has caught the attention of researchers since the 1900s. Scientific interest intensified from the start of this millennium, and the first bioinspired surfaces were developed mimicking the gecko’s toepad by making vertical pillars. This was not very successful: the adhesion of these mimics did not even come close to that of the gecko’s toepads. The gecko’s toepads namely consist of a hierarchical and highly branched structure, called setae, which are made of beta keratin. Beta keratin is a very stiff material, and this stiffness provides the strength, whereas the setae are compliant due to the structure. Therefore, the toe-pads can make contact with the surface, a property that is vital for good adhesion. The adhesive properties are lost when the structures of the toepads are simplified to pillars. However, fabricating a structure closer in design and material stiffness to that of a toepad, is difficult due to the scale of the structures (the smallest features at the end of the setae are on the nanometre scale) and the brittleness of small features made from stiff materials.

A more fruitful approach is trying to understand how the function is derived from the surface structure, and then design surface structures that achieve the same effect. To achieve this, the effect of surface structures on functions should be known. A first step in this approach is to focus on the properties of flat surfaces, and then study the effect of
surface structuring. We will limit ourselves to the two properties that are the topics in this thesis: adhesion and wetting of surfaces.

1.3 Adhesion and wetting of flat surfaces

Let us consider perfectly flat surfaces as a first step. Wetting and adhesion of flat solid surfaces can be discussed in terms of surface free energy $\gamma$. Creating surfaces costs energy (even when done so in a reversible way). Since the energy is not dissipated (because it has been done reversibly), this means that the extra energy ended up at the freshly made surface, and this is $\gamma$.

A molecular picture behind the concept of surface free energy, is that within the bulk, a molecule is surrounded by the same molecules, allowing it to have favourable interactions in all directions. A molecule at the surface, on the other hand, only has half of the favourable interactions of neighbouring molecules, since the other half is occupied by air. This is unfavourable. Another contribution, that cannot be neglected when a liquid is considered, is of entropic origin: the density gradients at an air/liquid interface allow for more translational freedom of the molecules, and thus an increase in entropy.

Strictly speaking, $\gamma$ is defined in vacuo, however, we will discuss it with vapour present. Both adhesion and wetting can be discussed in terms of the $\gamma$ of all materials present. We will consider adhesion first.

1.3.1 Adhesion

Adhesion is the energy cost of separating two materials (see Figure 2). This creates two new surfaces (dotted line), and one interface is lost. The work of adhesion $W_{\text{adh}}$, defined in terms of $\gamma$, reflects this:

$$W_{\text{adh}} = \gamma_1 + \gamma_2 - \gamma_{12}$$

(1)

An important and universal origin of adhesion is the Van der Waals interaction. This attractive interaction is found between practically all atoms and molecules in close proximity, and is caused by the fluctuating random dipole moments due to electron movement. Due to this close proximity, a dipole moment in one of the atoms or molecules...
Figure 2: two materials that were attached, are separated, thereby creating additional surface (dotted line).

will induce a corresponding dipole moment in a neighbouring atom or molecule. The result is attraction between the two atoms or molecules. Therefore, materials tend to adhere to each other.

When one material is separated into two pieces, the term ‘cohesion’ is used, and $W_{coh}$ can be defined as:

$$W_{coh} = 2\gamma_1$$

$W_{coh}$ is equal to Van der Waals interaction in the absence of other contributions (e.g. hydrogen bonding).

In practice, other phenomena, besides the $\gamma$ of both materials, contribute to the adhesion that is measured. Examples include chemical reactions, rearrangements of polymer chains, and surface structures.\textsuperscript{16}

The measured work, or interface toughness $G_c$, is given by

$$G_c = W_{adh} + \psi$$

with $\psi$ representing various energy dissipating mechanisms.\textsuperscript{17} The contribution of $\psi$ on $G_c$ is often much larger than that of $W_{adh}$.

### 1.3.2 Wetting

We shift from two materials on top of each other to a three-phase system, consisting of a solid (S), a liquid (L) and a vapour (V). We defined the surface free energy of the solid $\gamma_S$ and the liquid $\gamma_L$ with vapour present, so only one new term has to be introduced. This is the surface free energy between the solid and the liquid, $\gamma_{SL}$. The forces
derived from these surface free energies on the contact line of a liquid on a solid are shown in Figure 3.\textsuperscript{18} In equilibrium, by definition, the three contributions add up to $0$ (the vertical component is hereby not taken into account because we assume that the solid is stiff). As a consequence, the liquid droplet wets the solid with a fixed contact angle $\theta$, given by Young’s equation:\textsuperscript{17}

$$\gamma_S = \gamma_{SL} + \gamma_L \cos \theta$$

(4)

\textit{Figure 3: The contact angle $\theta$ of a droplet on a flat surface is determined by the surface free energies $\gamma$ of all three components.}

1.4 Adhesion and wetting of structured surfaces

1.4.1 Adhesion

No general equations exist to describe the effect of structuring on adhesion. There are, however, guiding principles, some of which are listed here.

For two (effectively) stiff materials, structuring often reduces the true contact area: only the peaks of the two surfaces come in close contact, and therefore the Van der Waals interaction is limited. This reduces the overall adhesion.\textsuperscript{19-20}

For a stiff and an soft material in contact, multiple effects play a role. Two adhesion enhancing effects are (i) increase in contact area because the soft material can conform to the surface of the stiff material, and (ii) energy dissipation due to unstable crack propagation during pull-off (see Chapter 3). Two adhesion decreasing effects are (i)
elastic penalty: the energy needed to deform an elastic surface during approach, facilitates detachment, and (ii) crack initiation at patches were the two surfaces are not in contact. Which of these effects dominates the others, depends on the exact surface topology, and whether the stiff or the elastic material is structured.

These effects are valid for all surface structures, whether it is random surface roughness or a carefully designed pattern. For some patterns, more specific effects come into play. A well-studied example is making long, fiber-like surface structures from stiff materials, mimicking the structures on the feet of the gecko. The geometry of this surface structure makes the stiff material compliant, allowing the structures to conform to the counter surface, thereby increasing contact area. The stiff material thus adopts some characteristics of a soft material due to the structure. We see here an example of a surface structure changing the properties in a dramatic way.

Also, detachment of one fiber-like pillar is in principle independent from the detachment of another pillar. Therefore, the energy required to remove one pillar, cannot be used to remove the next one. This results in more energy needed to pull the structured surface off, hence a higher adhesion. However, the overall contact area of an array of pillars is small, since the pillars should be spaced apart to prevent sticking to each other.

The detachment of one pillar depends on the geometry of the pillar. A simple pillar can more easily detach because the highest stress during pull-off is located at the edge of a pillar, which makes crack initiation and thus detachment, easy. If the pillar has a mushroom shape or a cap, the highest stress when the pillar is pulled, is not at the edge anymore, making detachment more difficult and therefore the adhesion better.

These examples show that the effect of structuring on adhesion can be understood for some specific cases of different geometries. Unfortunately, our understanding is still too limited to be able to predict the final adhesion once the geometry and material properties of a new design are known.
1.4.2 Wetting

The effect of surface structures on wetting is an classic field of research -Young worked on this problem at the start of the 19th century\textsuperscript{23} - and hence more established. Two well-known models describe the deviation of $\theta$ due to the surface not being perfectly flat. The first model, developed by Wenzel, introduces the parameter $r$, which is the ratio between the true and the projected area. The apparent contact angle $\theta_W$ is then given by:\textsuperscript{24}

$$\cos \theta_W = r \cos \theta$$  \hspace{1cm} (5)

For a flat surface, $r$ is equal to 1, and $\theta_W$ is therefore simply $\theta$. For rough or structured surfaces, $r > 1$, and this results in $\theta_W < \theta$ for $\theta < 90^\circ$ (hydrophilic surfaces) and $\theta_W > \theta$ for $\theta > 90^\circ$ (hydrophobic surfaces). According to this model, hydrophilic surfaces become more hydrophilic, and hydrophobic surfaces become more hydrophobic.\textsuperscript{25}

The second model, the Cassie-Baxter model, assumes that air is trapped between the (structured) surface and the droplet. This results in contact angles, $\theta_{CB}$, given by\textsuperscript{26}

$$\cos \theta_{CB} = \varphi_s \cos \theta - (1 - \varphi_s)$$  \hspace{1cm} (6)

where $\varphi_s$ is the area under the droplet in contact with the solid, and $(1-\varphi_s)$ the area under the droplet in contact with the entrapped air. The air effectively lowers the average surface energy, leading to high apparent contact angles.\textsuperscript{27,28} Since air entrapment is energetically unfavourable for hydrophilic surfaces, this model only explains an increase in $\theta_{CB}$ for hydrophobic materials. However, the lotus leaf of Figure 1 AB, is superhydrophobic ($\theta > 150^\circ$), while the material itself is hydrophilic.\textsuperscript{29} Neither the equation of Wenzel nor the Cassie-Baxter model can explain this. These models only describe equilibrium wetting states, whereas a meta-stable Cassie-Baxter wetting state is the dominant wetting state of the lotus leaf.
1.5 From nature to research

We have seen examples of nature assigning functions to surfaces by structuring them in Figure 1. The challenge is to close the gap between our theories and models describing the effect of structuring on function, and how surface structures influence a function in the real world. The most promising structures to start investigating, are those that resemble the structures found in nature in terms of dimensions and shape. The area over which these structures can be made, should be large enough for our measurements of adhesion and wetting. Two fabrication methods that are commonly used are soft lithography and wrinkling techniques, which will be presented next. We, however, use a different approach, which meets all the requirements regarding dimensions and shape of the surface structures, namely colloidal templating (Chapter 2 and 4).

1.6 Fabrication of patterned surfaces

Two methods commonly used to make patterned surfaces include soft lithography and wrinkling techniques.

1.6.1 Soft lithography

Soft lithography is a multistep process (see Scheme 1). First, a photoresist layer is spincoated on a surface. The thickness of this photoresist determines the amplitude of the final structure. Next, a mask with the negative of the desired pattern is placed above the photoresist, and the uncovered areas are exposed to UV to crosslink the resin. The unexposed resin is subsequently removed, and this patterned surface is used as mold. The final patterned surface is obtained after peeling off from the mold.

The smallest features that can be made using soft lithography are several microns, the area is limited to the size of the mask and the features most often have straight walls. Within these limitations, every
Scheme 1: Fabrication of surface structures using soft lithography. First, photoresist is spincoated onto a substrate. Surface structures are introduced by partially curing the photoresist through a mask and removing the non-crosslinked parts. The surface can be used as mold after removal of non-crosslinked photoresist.

design can be realized, but these designs are often too simple to create enhanced properties. Hierarchical structures, or structures with overhangs, can be made by additional steps, such as adding a thin film on top of the structures, inking or using two layers of photoresist that are patterned and cured sequentially.

1.6.2 Wrinkling techniques

Several methods developed to make wrinkled elastomer surfaces. Three of these methods are shown in Scheme 2.
Chapter 1

Scheme 2: Fabricating surface structures using wrinkling approaches: (i) Generating a stiff upper layer on a stretched piece of PDMS and use this as mold upon stress release; (ii) Scooping up a thin, stiff film from the air/water interface and use this as mold; (iii) Attaching elastomer to rigid substrate, swell and cure the elastomer, and use this as mold.

One way is to expose a stretched strip of completely cured PDMS to UVO or \( \text{O}_2 \) plasma (Scheme 2i). This oxidizes the surface, generating a thin, stiff layer, causing the PDMS to wrinkle upon stress release.\(^{42}\) Another way is to use a fully cured strip of elastomer to scoop up a thin stiff polymer film floating at the air/water interface (Scheme 2ii). The elastomer is stretched at the air/water contact line, the polymer layer is not. When the stress is released, the stiff polymer film buckles, generating a wrinkled surface.\(^{43}\) These two methods result in parallel wrinkle formation, yielding a surface with anisotropic properties. A method to fabricate an isotropic surface with short wrinkles, is by swelling a polymeric film attached to a solid support, and subsequently UV-cure the swollen films (Scheme 2iii).\(^{36}\) The solid support prevents the
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polymeric film from swelling in every direction, resulting in non-aligned wrinkles.

The wrinkled surfaces can be used as mold to obtain the final nanopatterned surfaces. The adhesion of these surfaces have been investigated in depth, and we will show in Chapter 3 that we can learn from these adhesion studies when discussing the adhesion of our surface structures.

1.6.3 Colloidal lithography

We use colloidal lithography to fabricate our surface structures. This technique uses colloids (spherical particles with diameters between a couple of nanometres to several hundreds of microns) as template.

Scheme 3: Fabricating surface structures using colloidal lithography in 2 different ways, by templating from the air (top of the scheme) or from the water (bottom of the scheme).

We use a monolayer as template (see Scheme 3). The particles of this monolayer can either be templated from the vapour phase (top part of Scheme 3), or via the water phase (bottom part of Scheme 3). One monolayer can thus be used to make two different nanopatterned surfaces.

Colloidal lithography is an promising method to make bio-inspired materials for several reasons. Surface structures in nature often
consist of simple, 3D structures on the nanometre to micrometre scale, that are repeated over macroscopic length scales. These characteristics are readily achieved using colloids, but especially the 3D aspect is not easily achieved with soft lithography or wrinkling techniques. Another advantage is that it does not require extensive procedures or expensive equipment: beautiful, complex structures can be made in a plastic Petri dish in a not-so-clean room (see Figure 4).

Figure 4: Making bio-inspired nanopatterned surfaces using colloidal lithography does not require expensive equipment. Some plain surface in the form of tables is, however, desirable.

1.7 Outline of this thesis

We have used colloidal lithography to study the effect of structuring on adhesion and wetting. The fabrication of the nanopatterned materials starts with the fabrication of and control over the colloidal monolayer. In Chapter 2 we present our method, in which colloids are dispersed in ethanol and applied to an air/water interface using a clean glass slide. We show that the crystallinity of the monolayers can be tuned by changing the pH of the water phase. A method to assess this crystallinity is presented. The monolayers are used as templates directly at the air/water interface, by carefully
applying the elastomer PDMS on top. After crosslinking, the particles are easily removed, resulting in a nanopatterned elastomer surface.

A function of this nanopatterned surface, namely adhesion, is investigated in Chapter 3. Three different nanopatterned surfaces with varying dimple depth and dimple density are selected. Two spherical probes are used as counter surface: a macroscopic probe (diameter = 4.76 mm) and a microscopic probe (diameter = 8 μm). In this way, adhesion is probed on two different length scales. The increase in adhesion is explained using an energy dissipating mechanism, and the influence of dimple depth and dimple density on adhesion, are discussed.

The same monolayer of Chapter 2 is used in a completely different templating method in Chapter 4. In this case, the material is not deposited on top, but polymerized at the colloid/water interface. This is achieved by first swelling the particles with monomers, and subsequently adding an oxidant to the water, thereby starting polymerization. After removal of the colloids, a nanopatterned surface consisting of the stiff, highly-crosslinked polypyrrole, is obtained. Different surface structures can be fabricated by choosing the amount of monomer, the polymerization time and the monomer : oxidant ratio. These surface structures are used for wetting experiments.

The wetting experiments show that droplets of water on those surface structures, have contact angles > 90°, whereas the contact angle is < 90° for water on non-structured polypyrrole surfaces. To understand this, we modelled the system in silico by extending the regular solution theory to three dimensions. This approach is presented in Chapter 5. Modelling allows us to systematically study the effect of particle diameter, immersion depth of the templated particles, and interparticle distance on the final droplet shape.

In the final chapter, number 6, we reflect on the previous chapters, and give suggestions for the next steps in research. We discuss the ideas we have of how the fabrication method can be improved and how other surface structures can be made using colloidal templating. The effect on adhesion of our structures are compared to other surface patterns and the influence of the important parameters on adhesion, is discussed. For our wetting experiments, we already performed modelling
studies. The validity of our modelling studies is tested by additional experiments and results from literature. For example, we indeed find the contact angle hysteresis as predicted by our modelling studies. Finally, an outlook for this field of research is presented.

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Introduction

2 Fabrication of nanopatterned elastomers using colloidal lithography directly at the air/water interface

This chapter is based on:
2.1 Abstract

We describe a fast and scalable method to fabricate nanopatterned polydimethylsiloxane (PDMS) using colloidal lithography directly at the air/water interface. Micron-sized polystyrene particles with parking areas of 0.11 nm$^2$ per –COOH group, are synthesized and applied to the air/water interface using ethanol as spreading agent. Close-packed monolayers are formed at the interface, on which PDMS is applied. PDMS completely wets the air/water interface at first contact with water, thereby compressing the monolayer, similarly as is usually achieved using a Langmuir trough. PDMS curing and particle extraction results in nanopatterned elastomers. Pattern disruption of the monolayer is minimized by omitting transfer and drying steps during the process. The order of the colloidal monolayer and the immersion depth of the particles are tuned by the pH of the subphase. This leads to direct control of the topography of PDMS surfaces. Crystallinity of the monolayer, which is quantified by counting the number of particles with six neighboring particles, shows a rapid increase when the pH of the subphase is higher than the first dissociation constant of the COOH-groups on the surface of the particles.

2.2 Introduction

Colloidal lithography is a technique that utilizes self-assembled colloidal monolayers for fabricating topologically-patterned surfaces with nanometer precision. This technique has proven to be a fast and cost-effective alternative to other nanofabrication processes such as electron beam lithography or focused ion beam lithography. Furthermore, nanopatterned surfaces are applied in a wide variety of technologically relevant areas including sensing, photonics, electronics, energy conversion and adhesion. Different methods have been developed to create colloidal monolayers directly on target solid substrates. A limitation to these methods is the low degree of lateral mobility of the particles upon contact with the substrate, which makes it difficult to prevent free void and multilayer formation. To overcome this limitation, gas/liquid interface deposition methods were developed, which provide enhanced particle mobility resulting in highly ordered monolayers.
Recently, several groups have reported on methods to produce large-area, highly ordered, colloidal crystals. For example, Pan et al. introduced a dynamic interface, by stirring the aqueous subphase, to facilitate colloidal crystal formation at the air/water interface. Retsch et al. reported a two-step procedure in which colloids are applied to a glass slide by spin-coating. Subsequently, a colloidal monolayer was formed upon immersion of the glass slide in an aqueous surfactant solution. Assembly at the air/water interface was also successfully achieved by using interfacial deposition via a glass slide and a needle tip. In these examples, the liquid interface acts as the assembly scaffold after which the monolayers are transferred to a solid substrate. Alternatively, material can be deposited via chemical reactions directly onto the colloidal monolayer at the air/liquid interface. This method was used to fabricate free-standing porous films and nanobowls by reacting monomers or inorganic precursors at the gas/liquid interface and at the liquid/solid interface, respectively. Ideally, however, deposition should not be limited to interfacial reactions and generalization towards other material systems would enable the fabrication of films with different property profiles. Yet, such approaches remain virtually unexplored.

In the study presented here, we describe a facile method to fabricate nanopatterned polydimethylsiloxane (PDMS) using colloidal lithography directly at the air/water interface. We show that close-packed monolayers at the air/water interface can be used as a template without the need to transfer the monolayer to a solid substrate. By omitting transfer and drying steps in the process, pattern disruption is minimized. Colloidal monolayers were obtained for a range of particle sizes. Moreover, the subphase is used to systematically tune the order of the colloidal monolayer and to control the immersion depth of the particles. This leads to direct control of the topography of PDMS surfaces.

2.3 Experimental

2.3.1 Materials

All materials were purchased from Sigma Aldrich and used as received. PDMS (Sylgard 184) was mixed in a ratio of 1:10 of crosslinker
prepolymer by weight and degassed by centrifugation. Deionized water, from an Easypure-UV-system (Barnstead), was used in all experiments.

### 2.3.2 Particle synthesis

Carboxylated polystyrene particles were synthesized in a one-step synthesis according to ref 10. Briefly, for the biggest particles, water (120 g), itaconic acid (0.5 g) and styrene (24.5 g) were heated to 80°C in a round bottom flask, and flushed with nitrogen for 45 minutes. Meanwhile, 4,4′-Azobis(4-cyanovaleric acid) (ACVA, 252.4 mg) was dissolved in water (6.3 g) and 1M NaOH (2 g). After adding this mixture to the round bottom flask, the solution reacted overnight under continuous stirring at 500 rpm.

The smaller particles were synthesized using 125 mL water, 5 or 10 g styrene, and 0.1 g (for 5 g styrene) or 0.2 g (for 10 g styrene) itaconic acid, and a temperature of 85°C. The reaction was initiated with 0.05 g ACVA (for 5 g styrene) or 0.1 g ACVA (for 10 g styrene).

The product was filtered over glass wool to discard some coagulum that was formed during the reaction. The filtered particles were treated using two different protocols. Colloidal dispersion CP (‘Carboxylated Particles’) was directly exchanged to ethanol by three cycles of centrifugation at 4500 RPM for one hour followed by resuspension in ethanol. Colloidal dispersion CP-W (‘Carboxylated Particles- Washed’) was washed in water by three cycles of centrifugation at 4500 RPM for one hour followed by resuspension in Milli-Q water. After this washing step, CP-W was exchanged to ethanol, using the same procedure. The smaller particles were treated similar to CP-W.

### 2.3.3 Particle characterization

**Static Light Scattering (SLS)**

Light-scattering measurements were performed on an ALV instrument equipped with an ALV7002 external correlator and a 300 mW Cobolt Samba-300 DPSS laser operating at a wavelength of 532 nm. The scattering intensity was recorded at $15° \leq \theta \leq 120°$ in intervals of $2°$, and
the curve was fitted to a form factor of a solid sphere. From this measurement an average radius of $574 \text{ nm}$ and a polydispersity index ($R_w/R_n$) of 1.01 (see Figure 1A) were obtained.

**Figure 1**: Characterization of the carboxylated particles, A) Size distribution as determined with SLS-measurements. B) Titration of ultrapure water, CP and CP-W with 0.1 M NaOH.

**Determination of surface charge density**

The surface charge of the particles was determined by titration of 50 mL colloidal dispersion in Milli-Q water (26 g/L for CP and 11 g/L for CP-W) with 0.1 M NaOH and using the titration of 50 mL Milli-Q water (brought to low pH with 2 mL 1M HCl) as reference (see Figure 1B). The difference in NaOH added to reach a pH of 9.4 (well above the pK$_{a1}$-values of itaconic acid, which are pK$_{a1} = 3.85$ and pK$_{a2} = 5.44^{11}$), but below the plateau in the pH-curve) between the dispersion and the reference sample is taken as the number of itaconic acid groups in the sample. The weight per particle is calculated using the density of polystyrene. Since the weight of all particles in during titration is known, the number of charges per particle can be calculated. The parking area is then (particle area)/(number of charges per particle), and is 0.11 nm$^2$ for both CP and CP-W.
2.3.4 Surface structure fabrication

Samples were prepared in polystyrene Petri dishes. This procedure is shown in Figure 2. The pH of the subphase was varied between 1 and 11, keeping the ionic strength constant at either $10^{-3}$ or 0.1 M. A piranha-cleaned coverslip was placed diagonally against the side, and a suspension of particles in ethanol (20 wt-%) was applied via this coverslip onto the water subphase using a pipette (Figure 2A (a)). The area covered by the particles at the air/water interface was well visible, and thus the amount of particles could be adjusted during preparation. The monolayer was left to equilibrate for at least one hour before further processing, to ensure evaporation of all ethanol from the air/water interface.

A syringe with a blunt tip needle was filled with PDMS and a small droplet was applied to the side of the Petri dish containing the monolayer of particles. Upon reaching the water surface, the droplet spread quickly (Figure 2A (b)). Next, PDMS was applied to the complete circumference of the Petri dish. This resulted in a ring of PDMS on water. By slowly adding more PDMS to this ring in a spiraling manner, PDMS eventually covered the whole interface. PDMS was allowed to crosslink at RT for 2 days, resulting in PDMS layers of 0.2–0.6 mm thickness (Figure 2A (c)).

To remove the template particles from the PDMS mold, we first applied Scotch Magic Tape, which removed the largest portion of templating particles. The remaining particles were removed by soaking the sample in N-methyl-2-pyrrolidone (NMP) for 1 hour, followed by dipping the samples 30 times in NMP in an ultrasonic bath (Figure 2A (d)). NMP was chosen as solvent because it dissolves polystyrene, yet does not swell PDMS. The samples were stored at RT.
Figure 2: Fabrication of nanopatterned polydimethylsiloxane (PDMS) using colloidal lithography directly at the air/water interface. A) Schematic outline of the experimental procedure: (a) Spreading of the particles using a glass slide; (b) Application of the PDMS against the side of the Petri dish; (c) Crosslinking of the PDMS; (d) Nanopatterned PDMS prepared by extraction of the particles. B) Sketch of the charge distribution on a particle when submerged in water at high enough pH. C) Photograph of PDMS-sample with a colloidal monolayer. Note the clear PDMS spot in the upper left corner, where the PDMS first touched the water, thereby pushing the particles away.

2.3.5 Crystallinity determination

Monolayers were scooped from the air/water interface with wet, piranha-cleaned coverslips. The area of the monolayers on these coverslips ranged between 0.5 – 2 cm². Twenty statistically-independent images were acquired with bright field microscopy at random locations across each sample. The centroid positions of all particles in the images were determined using standard particle tracking algorithms\textsuperscript{13} with a lateral resolution of approximately 20 nm. Approximately 10,000 particles
were found per image; per experiment we thus analyzed $20 \times 10,000 = 200,000$ particles to assess the crystallinity of the monolayers. We then computed the number of nearest neighbours, using a cut-off distance of $1.25 \times$ the particle diameter (for Matlab-code: see ref 14). We considered a particle crystalline only when it had exactly 6 nearest-neighbours in these hexagonal lattices. This method of assessing crystallinity is very strict: for example, all six particles surrounding vacancy are not regarded as crystalline, while in fact they are part of the crystal lattice. However, assessing the crystallinity by using the more elaborate Steinhardt orientational bond order parameter, $\psi_6$,$^{15}$ showed the same trends as simply counting the number of nearest neighbours.$^{16}$ Therefore, the nearest neighbour method was used here.

Figure 3: The apparent radius $R_h$ of the particles is related to the immersion depth as shown on the left. $R_h$ can thus be used to calculate the immersion depth using Pythagorean theorem (see right).

2.3.6 Immersion depth determination

We put Petri dishes with monolayers in a desiccator, added some droplets of ethyl cyanoacrylate in a separate dish, and let the system react under reduced pressure for 2 hours. Ethyl cyanoacrylate starts to polymerize when it comes in contact with water. The apparent radii of the particles embedded in poly(ethyl cyanoacrylate) was determined in SEM images (68 to 78 particles per image) in using the Analyze Particles function in ImageJ. See Figure 3 for a definition of apparent radius. Six two-tailed t-tests were performed to test whether the differences in apparent radii were significant (with $p<0.001$) and the Bonferroni method
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was used to correct for multiple testing. This apparent radius was used to calculate the immersion depth, which is the height percentage of the particle that is immersed in the subphase, via (immersed height)/(diameter particle) \( \times 100 \), using immersed height = \( R_p + l \) and

\[
l = \sqrt{R_p^2 - R_h^2}
\]

(see Figure 3).

2.3.7 Scanning Electron Microscopy (SEM)

Samples were sputtered with gold (30mA, 40s) using a JEOL JFC-1300 autofine coater, and imaged using a JEOL JAMP-9500F Field Emission Auger Microprobe. High magnification and tilt images were measured using a FEI Magellan FESEM.

2.3.8 Light Microscope

Images were made at a magnification of 100 using a Zeiss Axiovert 200 equipped with a Phantom V91 camera.

2.4 Results and discussion

2.4.1 Surface structure fabrication and characterization

Monolayers were prepared according to Figure 2A. Upon applying ethanol on water, a surface tension gradient is generated that causes the dispersion to rapidly spread outwards and cover the interface with particles. Regions with distinct Bragg reflections formed spontaneously, which indicated the formation of close-packed and organized domains. The self-assembly of charged micrometre sized colloidal particles at an air-water interface is governed by a competition between attractive capillary forces and repulsive electrostatic dipolar forces. We observed the spontaneous formation of islands of close-packed particles, which suggests that attractive forces dominate. The charges on the particles originate from copolymerization with itaconic acid (see Figure 2B). The charge density increased with increasing pH as more itaconic acid groups got deprotonated. The parking area at pH 9.4 was calculated to

27
be 0.11 nm² per COOH group. This value is relatively small compared to values in literature,¹⁸ but the substantial ionic strength of the subphase screened the electrostatic repulsion between the particles, and thus attractive forces dominated nonetheless.

To use the monolayer of particles at the air-water interface as a template, the deposition material should (i) be immiscible and nonreactive with water, (ii) be able to crosslink in the presence of water, (iii) be able to replicate micron to nanoscale features and (iv) have a lower density than water. PDMS was selected because it fulfills these criteria and is a well-characterized material. PDMS completely wet the air-water interface¹⁹, and thus formed a homogeneous film at the interface. During spreading of the initial PDMS droplet, the particles are pushed together, similar to compression in a Langmuir trough. This resulted in close-packed monolayers composed of the islands formed during deposition. A representative example of nanopatterned PDMS is shown in Figure 2C, in which the Bragg reflections can be clearly seen.

2.4.1 Determination of the monolayer crystallinity

The order of the monolayer was assessed by scooping monolayers, which were not cast in PDMS and imaging them with brightfield microscopy (Figure 4 A-C). We confirmed the presence of a monolayer, rather than multilayers, by changing the focus, and thus scanning through the sample. The positions of all particles in the images was found using a particle tracking algorithms and this spatial information was used to quantify the number of crystalline particles, i.e. particles with exactly 6 nearest-neighbours (see experimental section).

An exemplary result of this analysis is shown in Figure 4 D-F, where crystalline particles are shown in light grey, and non-crystalline particles are shown in dark grey. The normalized crystallinity per image was then calculated using:

The normalized crystallinity per image was calculated using:

\[
\text{normalized crystallinity} = \frac{\text{crystalline particles}}{\text{total number of particles}}
\]

(1)
This quantitative assessment of the crystallinity of the monolayer proved insightful to study effects of subphase characteristics on the order (see Figure 7, discussed below).

Common, more qualitative methods include visual inspection of micrographs or iridiscence of the monolayer, Moiré patterns observation upon thin film folding, diffraction pattern analysis, Fourier transformation and microscopy to see grain sizes. In these methods, subtle differences in order are not easily picked up, while our approach allows for straight-forward comparison of the crystallinity of different monolayers.

![Figure 4: Part of light microscopy images of CP-W colloidal monolayers self-assembled onto water at A) pH 3, B) pH 7 and C) pH 10. Crystallinity diagrams obtained from light microscopy images at D) pH 3, E) pH 7 and F) pH 10. SEM images of colloidal monolayers embedded in PDMS at G) pH 3, H) pH 7 and I) pH 10. SEM images of PDMS replicas at G) pH 3, H) pH 7 and I) pH 10.](image-url)
Figure 5. SEM images of PDMS replicas of colloidal monolayers self-assembled onto water at A) pH 3, B) pH 7 and C,D) pH 10.

Figure 4 G-F show scanning electron microscopy (SEM) images of the monolayer embedded in PDMS. We found that PDMS does not disrupt the monolayer, as similar order was obtained in light microscopy and SEM images. Figure 5 presents SEM images of the resulting nanopatterned PDMS surfaces after particle removal. Colloidal monolayers were obtained for a range of particle sizes, which resulted in nanostructured PDMS with different feature sizes (Figure 6). These results indicate that this method leads to direct control over the topography of PDMS by tuning the colloidal monolayer.
2.4.2 Influence of subphase

Figure 4 clearly shows that the degree of crystallinity of the colloidal monolayer was strongly dependent on the pH of the subphase. The sample at pH = 3 (Figure 4A) was largely disordered, while large domain sizes were obtained for samples prepared at pH = 10 (Figure 4C). Samples prepared at intermediate pH value (pH = 7) exhibited intermediate order (Figure 4B). We then systematically investigated the degree of order of the samples as function of the composition of the subphase for two types of particle dispersions, CP and CP-W (Figure 7). Particle dispersion CP contained residual styrene-itaconic acid oligomers,
whereas dispersion CP-W was thoroughly washed with ultrapure water to remove these oligomers to a great extent. To study the pH effect on monolayer formation, the pH was adjusted with HCl and NaOH, while keeping the ionic strength constant. The pH was calculated from the known composition of the subphase and not determined experimentally, but we expect no strong deviations between calculated and actual values due to the low particle concentration in the overall system. The crystallinity was again determined by scooping monolayers and subsequent light microscopy imaging.

Figure 7: Degree of order as a function of subphase composition. A) Normalized crystallinity as function of pH for CP (▲) and CP-W (●) at [salt]= 0.1 M. B) Normalized crystallinity as function of pH for CP at [salt] = 0.1M. Black symbols denote samples for which the pH of the subphase was constant during processing. Blue symbols denote samples for which the pH of the subphase was kept at pH 10 during self-assembly and adjusted afterwards. C) Normalized crystallinity as function of pH for CP-W at [salt] = 10^{-3} M. Black symbols denote samples for which the pH of the subphase was constant during processing. Blue symbols denote samples for which the pH of the subphase was kept at pH 10 during self-assembly and adjusted afterwards.

Figure 7A shows that the crystallinity increased with increasing pH for both CP and CP-W. At higher pH the charge density at the particle surface is increased. Itaconic acid groups contain two carboxyl groups, with pK_{a1}=3.85 and pK_{a2}=5.44.\textsuperscript{11} The onset of increasing crystallinity indeed coincides with dissociation of the first carboxyl group at pH higher than 4. The increased charge density resulted in larger electrostatic repulsion between the particles. The increased electrostatic repulsion counteracts the attractive van der Waals and capillary forces.
Consequently, the particles remained more mobile at the interface resulting in more ordered monolayers.\textsuperscript{2, 5-6} Thus, at pH 3, particles that approach each other closely (i.e., by capillary forces), immediately feel the attractive van der Waals forces that bring them in close contact. This process immobilizes the particles and results in monolayers with relatively low crystallinities. At pH 10, the electrostatic repulsion is greatly increased. This increases the energy barrier for a close contact between particles and the particles have sufficient time and mobility to crystallize in a low free energy position. Hence, monolayers with higher crystallinities are obtained.\textsuperscript{6}

It was observed that monolayers made from CP were less mobile and more robust as compared to CP-W monolayers. More specifically, when part of the CP-monolayer was scooped with a coverslip, the hole left in the monolayer remained square, whereas for CP-W, the particles within the monolayer rearranged after scooping, leaving an irregular shaped hole in the monolayer. We speculate that the surface active styrene-itaconic acid oligomers left in the CP dispersions ‘glue’ the particles together, in a similar fashion as was observed by Ho et al. for polyethylene oxide polymers.\textsuperscript{27} To study the difference in robustness, CP and CP-W samples were prepared at high pH that resulted in well-ordered monolayers. HCl was added to the subphase to lower the pH while keeping the salt concentration constant. For CP monolayers order was maintained, even when the pH was as low as 2 (Figure 7B). By contrast, lowering the pH of CP-W monolayers decreased the crystallinity significantly (Figure 7C). The cohesive layer between the CP particles thus plays an important role in preserving the order during further processing of the monolayer.

2.4.3 Immersion depth of the particles

We also altered the properties of the monolayer through changes in ionic strength of the subphase at constant pH. We determined the immersion depth of CP-W particles in subphases at different pH and ionic strength by fixing their position at the interface in a polymeric matrix (Figure 8). The matrix was formed by interfacial polymerization of ethyl cyanoacrylate, which was introduced via the gas phase and started
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to polymerize when it came in contact with water. After drying, immersion depths were determined by imaging the poly(ethyl cyanoacrylate) layer with SEM.

Figure 8A-D show top-view images of monolayers embedded in the cyanoacrylate matrix, where deeper immersion of the particle resulted in a smaller spherical cap and thus a smaller apparent radius. The boxplots of the immersion depth of the particles in Figure 8E show that both salt concentration and pH influenced the immersion depth. Statistical analysis showed that the differences between the apparent radius of all four samples were significant (with \( p < 0.001 \)). Figure 8B and C show that an increase in pH led to a deeper particle immersion. A and D also show that an increase in ionic strength (at pH = 7, thus above the pKₐ-values of itaconic acid) resulted in a deeper immersion which illustrates that the influence of ionic strength on immersion depth can be more pronounced than that of pH. As discussed earlier, at higher pH, the charge density increases, making the particle more hydrophilic thus leading to deeper immersion into the water phase. Similarly, increasing the ionic strength, leads to screening of the densely-packed charges at the particle surface, and thus enhances deprotonation. This in turn also increases the surface charge density and increases the immersion depth in the aqueous subphase.²⁸

CP-W monolayers using the same four subphases were prepared and used as templates for PDMS. Figure 8 F-I show SEM images of the resulting nanopatterned PDMS surfaces. Subtle differences in dimple depth are observed, yet not as pronounced as observed with ethyl cyanoacrylate. Upon application of PDMS, the immersion depth of the particles may change because of PDMS-PS interactions, thereby reducing the effect of pH and ionic strength. Nevertheless, the results showed that ionic strength and pH of the subphase, as well as particle size can be used to tune the final topography of the PDMS surface.

2.5 Conclusion

In summary, we developed a fast, scalable method to pattern PDMS. Particles formed close-packed islands at the air/water interface that transitioned to well-ordered monolayers upon compression by adding PDMS. Colloidal monolayers at the air/water interface were used
directly as template for PDMS. The composition of the subphase was altered to tune order and immersion depth of the monolayer, which was translated into the PDMS patterned surfaces. We anticipate this method to be advantageous in various fields including surface wetting, sensing and biomimetic fabrication.

References

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Chapter 2

3 Adhesion enhancement of nanopatterned surfaces on two different length scales

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3.1 Abstract

Adhesion and friction of nanopatterned surfaces with varying dimple depth and dimple density were studied. A macroscopic probe (diameter = 4.76 mm) and a colloidal probe (diameter = 8 µm) were used as counter surface. Compared to smooth surfaces, adhesion of nanopatterned surfaces was enhanced for both probe sizes. The relative increase in adhesion was similar for both probe sizes, and is attributed to an energy dissipating mechanism during pull-off. Every dimple acts hereby as a location for unstable crack propagation. The pull-off force is influenced by dimple depth and dimple density. For the macroscopic probe, deeper dimples result in more energy dissipation per dimple during pull-off. For the colloidal probe, the dimple density seems to dominate the effect on adhesion; a higher density resulted in a higher adhesion. All nanopatterned surfaces showed a significant decrease in friction compared to smooth surfaces for the macroscopic probe.

3.2 Introduction

Many animals have evolved adhesive organs on their feet enabling them to strongly attach to and quickly detach from nearly any kind of surface. These organs come in two basic designs: (i) pads densely covered with micro- or nanosized fibrils (“hairs”) with a wide variety of tip shapes observed in e.g. spiders, geckos, beetles, and flies, and (ii) pads with macroscopically smooth surface profiles, observed in e.g. tree frogs, ants and grasshoppers.\(^1\) Regardless of the design, both types use non-covalent surface forces to achieve adhesion, and research suggests that they rely primarily on van der Waals forces.\(^2\) The surface structure, not the chemistry, is therefore dominating the function of natural adhesive systems.

Over the last decade, synthetic patterned surfaces have been developed to mimic the geometry of natural attachment systems.\(^3\)-\(^4\) Initial research focused on the development of vertical pillars with diameters in the micron range.\(^5\)-\(^7\) To fabricate more complex structures, closer in design and performance to natural systems, relatively expensive semiconductor technologies and multi-step patterning techniques have been used.\(^8\)-\(^13\) Alternatively, wrinkling techniques have
been explored as a scalable, potentially cheaper production method. Wrinkled surfaces have been shown to increase or decrease adhesion depending on the testing geometry and wrinkle dimensions.\textsuperscript{14-18} Ideally, however, scalable methods should not be limited to two-dimensional patterns, as more complex, three-dimensional sub-micron structures would enable the fabrication of surfaces with different property profiles.\textsuperscript{19}

In Chapter 2 we presented a novel method to fabricate scalable nanopatterned surfaces. In this chapter, three structured surfaces are selected, and the adhesion of these surfaces, compared to a flat surface, is studied. The adhesion is determined on two different length scales, using counter surfaces of different size. For counter-surfaces of the same order of magnitude, the influence of a single or a few surface features on adhesion can be probed, whereas the average effect of structuring on adhesion is found for probe sizes which are orders of magnitude larger. Two different experimental set-ups are used to measure pull-off forces on both a macroscopic (mm) and a microscopic length scale (µm). The macroscopic probe (diameter = 4.76 mm) is used in a force-controlled homebuilt adhesion tester. The microscopic probe (diameter = 8 µm) is attached to an AFM cantilever and used in a (force-controlled) force robot.

3.3 Experimental

3.3.1 Samples

Nanopatterned PDMS surfaces were fabricated as described in Chapter 2. Three different nanopatterned PDMS surfaces and a flat control were selected for the adhesion measurements. The difference in fabrication between the structured samples is solely the pH of the subphase, which was 10 for Sample 1, 5 for Sample 2 and 3 for Sample 3.

AFM was used to visualize the surface structures. The PDMS samples were cut and glued with Norland Optical Adhesive on a silicon wafer. Samples were cleaned with Scotch Magic Tape and were imaged using a Nanoscope V in Scan Asyst imaging mode, using nonconductive silicon nitride probes (Veeco, NY, U.S.A.) with a spring constant of 0.32 N/m.
Images were recorded at 0.990 Hz with a resolution of 512 lines and further processed with NanoScope Analysis 1.40 software. The software calculates the area per projected area by creating a 3D tessellation of the surface. More specifically, the actual area is defined as the sum of the areas of every triangle formed by three adjacent data points using the (x,y,z) position of each data point. Three independent AFM images were used to determine the actual area per sample. After this, the height with highest frequency was subtracted, such that the peak was positioned at zero, and all values were multiplied with -1, so that negative values denote negative asperities and positive values denote positive asperities. The dimple depth was determined from the histogram at 0.1 A.U.

3.3.2 Macroscopic probe

Adhesion measurements Adhesion measurements were performed using the force-controlled set-up shown in Figure 1 as described in ref 20. Forces were measured using a bending beam with a spring constant in the normal direction of 27.3 N m⁻¹, and in the in-plane direction of 9.8 N m⁻¹.

Figure 1: Schematic representation of test-setup for adhesion and friction measurements.

A spherical Al₂O₃ probe with a diameter of 4.76 mm (Edmund Optics) was glued with Norland Optical Adhesive 61 to a glass coverslip and this coverslip was attached to the distal end of the bending beam. The probe was brought in contact with the PDMS 50 times before the
measurements started, and not cleaned in between measurements. This avoids variation in pull-off forces due to transfer of PDMS oligomers between the surfaces. For all measurements, the probe was moved against the sample until a predefined preload within 5 s, and the time lag thus varies between 0 and 5 s. Pull-off forces were measured at 9 different preloads, ranging between 0.2 and 5 mN, and using a motor velocity during pull-off of 1 µm s$^{-1}$, at the same spot.

**Friction** Friction was measured at least 10 times per sample by applying a normal force of 0.5, 1 and 2 mN for 5 s, followed by shearing the probe with a motor velocity of 100 µm s$^{-1}$ for 20 s, while keeping the normal force constant via a 20Hz force feedback mechanism. For the friction measurements of flat PDMS, a stiffer bending beam (spring constant in in-plane direction: 27.6 N/m) and a normal force of 0.5 mN were used. However, the friction force required to initiate sliding was not met, and thus we can only say that the static friction force of smooth PDMS is >70 mN. The available beams were not suitable to measure the static friction of Sample 2 at a preload of 2 mN.

### 3.3.3 Colloidal probe

**Cantilever preparation.** A SiO$_2$ particle of 8 µm (Fiber Optic Center) was glued to a triangular silicon nitride cantilever with a spring constant of 0.12 N/m (Veeco) using a micromanipulator. Norland Optical Adhesive was used as glue. The glue was cured under UV irradiation for 300s.

**Adhesion measurements.** The probe was first contaminated with PDMS by bringing it in contact with flat PDMS at least 100 times. To calibrate the cantilever, a silicon wafer was used as hard counter surface. The wafer was cleaned with water and ethanol, then contaminated by pressing a piece of PDMS ~10 times against it to reduce capillary condensation and hence adhesion between the probe and the wafer. The sensitivity was determined from the approach curve in the constant compliance regime and the spring constant was determined via the thermal tuning method.

Force curves (~500-600 per measurement) were recorded with the Force Robot 300 (JPK), at an approach and retract velocity of 2 µm/s unless stated otherwise. The preload was 0.5 nN.
All curves were checked by eye, and curves with abnormalities were discarded. The curves were analyzed using the JPK data processing software.

3.4 Results & Discussion

3.4.1 Models for adhesion

Surface structures can significantly alter the adhesive properties of surfaces. To understand the effect of surface structures on adhesion, it is instructive to discuss models for adhesion between two spheres first.

Model of Hertz

The simplest is a model by Hertz. He studied the deformation of two elastic spheres that are pushed together in frictionless contact.\(^{24}\)

![Diagram of Hertz model](image)

\( r^3 = \frac{3}{4} \frac{PR}{E^*} \)  

(1)

with \( P \) the force pushing the spheres together, \( R \) the relative radius of curvature and \( E^* \) the reduced Young’ modulus. The latter two are defined as follows:
Adhesion of nanopatterned surfaces

\[
\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2} 
\]

(2)

\[
\frac{1}{E^*} = \frac{1-v_1^2}{E_1} + \frac{1-v_2^2}{E_2} 
\]

(3)

with \( v \) the Poisson’s ratio and \( E \) the elastic modulus.

The model of Hertz is only valid for spheres without adhesion which behave in a linear elastic way, and for \( r<<R \).

The JKR model

Johnson, Kendall and Roberts extended the Hertz model to include adhesion. In this JKR-model, Van der Waals interactions inside the contact area are taken into account.\(^{25}\) The contact area in this model is

\[
r^3 = \frac{P R K}{K} \left[ 1 + \frac{3\pi W_{adh} R}{p} + \sqrt{2\frac{3\pi W_{adh} R}{p} + \left(\frac{3\pi W_{adh} R}{p}\right)^2} \right] 
\]

(4)

with \( W_{adh} \) the work of adhesion and \( K \) the reduced stiffness, which can be described by

\[
W_{adh} = \gamma_1 + \gamma_2 - \gamma_{12} 
\]

(5)

with \( \gamma_1 \) and \( \gamma_2 \) the surface energies and \( \gamma_{12} \) the interfacial energy for the two contacting materials (see also Chapter 1, Figure 2).

\[
\frac{1}{K} = \frac{3}{4} \left( \frac{1-v_1^2}{E_1} + \frac{1-v_2^2}{E_2} \right) 
\]

(6)

The contact area under the same compression is larger for the JKR-model than for the Hertz model.

\( W_{adh} \) has the same value for making contact (approach) as for breaking contact (retraction) when all interactions are derived solely from the contribution of surface energies. However, other contributions, such as chemical reactions, rearrangements of polymer chains, and surface structures often give rise to adhesion hysteresis. For clarity, the work done when breaking contact is often called \( G_c \), the interface toughness.\(^{26}\) This includes the thermodynamic \( W_{adh} \) and energy dissipation.

In the JKR model, two spheres in contact can withstand a certain tensile load due to the attractive Van der Waals interaction. If the tensile
load is bigger than a critical load, the two spheres separate. The force at which this occurs, is given by

\[ P_c = -\frac{3}{2} \pi W_{adh} R \]  

(7)

The DMT model

The JKR model is suitable for large soft spheres with high surface energies. For small, hard spheres with low surface energies, the DMT theory has been developed by Derjaguin, Muller and Toporov.\textsuperscript{27} In this model, only Van der Waals interactions outside the contact area are taken into account, and the interactions within the contact area are neglected. This results in the following expressions for the contact radius and critical tensile load:

\[ r^3 = \frac{R P}{K} + \frac{2 \pi W_{adh} R^2}{K} \]  

(8)

and

\[ P_c = -2 \pi W_{adh} R \]  

(9)

The Tabor parameter

A continuous transition between the JKR model and DMT theory exists,\textsuperscript{28} and the Tabor parameter can be used to determine which model should be used.\textsuperscript{29} The Tabor parameter is given by

\[ \mu = \left( \frac{R W_{adh}^2}{E^2 z_0^3} \right)^{1/3} \]  

(10)

with \( z_0 \) the equilibrium separation of the two surfaces (usually 0.3 - 0.5 nm). The JKR model is suitable for \( \mu > 5 \), and the DMT model for \( \mu < 0.1 \).

The JKR and DMT models both describe adhesion between a spherical probe and a flat surface, and do not take the effect of surface structuring into account.
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Effect of structures on adhesion

Previous studies have shown that wrinkles and surface roughness typically decrease adhesive properties \(^{17-18, 30-31}\), but in some studies adhesion enhancement was found. \(^{14, 32}\) Adhesion enhancement between compliant smooth surfaces and rigid rough surfaces is often attributed to an increase in true contact area. \(^{31}\) As long as the roughness of this rigid surface is small enough, the positive effect from the true contact area will outweigh the negative effect from the stored elastic energy, and adhesion will be enhanced. In this study, the maximum true contact area is defined by the smooth rigid probe, and hence does not change. Therefore, the increase in true contact area does not play a role in our system.

The Guduru model

An explanation for adhesion enhancement for surface structures without increase in true contact area, has been described theoretically \(^{33}\) and observed experimentally \(^{34}\) by Guduru et al. The surface structure in this study consisted of concentric wrinkles. The detachment of a spherical probe centred above the central wrinkle was studied.

For a smooth surface, the detachment of a spherical probe is given by the JKR model, and results in a smooth force-displacement curve with unique force values at any given displacement (see Figure 3, dotted line). When shallow concentric wrinkles are introduced, undulations show up at this force-displacement curve (Figure 3, black line). These undulations appear because the crack front has to climb up the crest of a wrinkle, which requires more force, and afterwards propagates towards the through of a wrinkle, which requires less force when compared to a smooth surface.

Even for this surface with shallow wrinkles, an increase in pull-off force compared to a smooth surface has been found (y-axis in Figure 3), though no energy dissipating mechanism is found in this case.
The undulations of the force-displacement curve increases with increasing wrinkle amplitude. Eventually, the undulations are large enough to allow for non-unique force values at a given displacement. This results in an energy dissipating mechanism which is not present in the JKR model, and is shown in Figure 4. When the crack would propagate reversibly, it would follow the dotted line in Figure 4. However, this equilibrium path is not followed, but the detachment occurs via unstable jumps (vertical arrows in Figure 4). The crack front remains stable as it climbs towards the top of a wrinkle. There, the crack is trapped and an increased force is needed to move it forward. Just after passing the top, the crack becomes unstable and quickly propagates past the trough. This is the vertical jump in the Figure. Energy is dissipated during detachment from the unstable regions, resulting in increased separation energy. This adhesion enhancing

Figure 3: Force–displacement curve for a flat surface (dotted line) and a surface with shallow concentric circles (black line). Printed with permission from 33.
mechanism is only applicable in regimes where the JKR-model is valid, thus for $\mu > 5.35$.

This mechanism to enhance adhesion via surface patterns, functions only when the probe is directly centred above the central wrinkle. Ideally, adhesion enhancement should not depend on the exact position of the probe with respect to the surface structures. Therefore, a design of surface dimples has been chosen.

![Graph](image)

**Figure 4:** Dissipated energy due to unstable crack propagation for detachment of a spherical probe from a surface with concentric wrinkles. The dashed line shows the equilibrium path during detachment, the solid line shows the actual path. The vertical arrows indicate the (unstable) jump from one stable region to the next. The energy that is dissipated during this jump, is indicated as the hatched area. Printed with permission from 33.

### 3.4.2 Sample characterization

Samples were prepared according to the fabrication process described in Chapter 2. Carboxylated polystyrene particles are hereby applied to the air/water interface to obtain a monolayer. The crystallinity
of this monolayer is controlled by the pH of the water phase. PDMS is
applied on top of the monolayer and allowed to crosslink, after which the
particles are removed.

Three samples (S₁, S₂ and S₃) were selected for adhesion
measurements. The difference between the samples was the pH of the
subphase during monolayer preparation, which was 10, 5 and 3 for S₁, S₂
and S₃, respectively. A smooth PDMS surface was used as control. AFM
images of the samples are shown in Figure 5.

![AFM images](image-url)

**Figure 5**: AFM height images (A-D) and peak force images (A’-D’) of samples
used in adhesion experiments. A, A’) Flat PDMS, B, B’) Sample 1 (S₁), C, C’) Sample 2 (S₂) and D, D’) Sample 3 (S₃). Color scale on the right ranges from -150 nm (bottom) to 150 nm (top) for the height images and from -850 (bottom) to 850 mV for the peak force error images. Scale bars are 1 µm.
As expected, the normalized crystallinity differed between the three samples and decreased with decreasing pH value of the subphase: 54% for S1, 35% for S2 and 14% for S3. Apart from the crystallinity, the dimple depth also differed between the three samples.

![Figure 6: Different (nanopatterned) surface structures. For A-B: ( ) Smooth PDMS; ( ) Sample 1; ( ) Sample 2; and ( ) Sample 3. A) Cross section from AFM image for smooth PDMS and S1-S3. B) Histogram of height differences from an AFM picture for smooth PDMS and S1-S3.](image)

First, a cross-section through the center of a dimple of each of these samples was drawn, as shown in Figure 6A. Profiles were created by selecting dimples with relatively large inter-dimple regions to obtain flat inter-dimple regions. As expected, upon decreasing the pH, the dimple depth increased from Sample 1 (S1, dark grey), to Sample 2 (S2, grey), and to Sample 3 (S3, light grey). Second, histograms of the height distributions of the three nanopatterned samples and smooth PDMS were determined by AFM (see Figure 6B) and show that the same trend in depth was also found over larger areas (5×5 µm). The histogram for smooth PDMS (black) peaks around the normalized zero and extends slightly to the right, indicating the presence of some small bumps or dirt particles. The histograms of the nanopatterned structures show a broad distribution and extend to the left, indicating dimples. These data were used to determine dimple depths.

The characteristics are summarized in Table 1. The cross-section through the samples was approximated by hemispherical dimples separated by flat inter-dimple regions, with \( a \) as the dimple depth and \( \lambda \) as...
as the dimple wavelength. The wavelength $\lambda$ is defined as the diameter of the particles for a cross-section through the center of the particles. Actual average wavelengths of the samples are a function of the degree of crystallinity and will deviate slightly from this value.

### Table 1: Sample characteristics of samples S1-S3.

<table>
<thead>
<tr>
<th>Sample</th>
<th>Subphase</th>
<th>Crystallinity</th>
<th>$a^*$ (nm)</th>
<th>$\lambda$ (nm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>S1</td>
<td>pH=10, [salt]=0.1 M</td>
<td>0.54 ± 0.04</td>
<td>86</td>
<td>1150</td>
</tr>
<tr>
<td>S2</td>
<td>pH=5, [salt]=0.1 M</td>
<td>0.35 ± 0.04</td>
<td>135</td>
<td>1150</td>
</tr>
<tr>
<td>S3</td>
<td>pH=3, [salt]=0.1 M</td>
<td>0.13 ±0.02</td>
<td>173</td>
<td>1150</td>
</tr>
</tbody>
</table>

* determined by AFM.

### 3.4.3 Measuring adhesion: interpretation of a force-distance curve

Adhesion can be studied by measuring force-distance curves. An example of such a curve is shown in Figure 7 for a colloidal probe on a nanopatterned surface. The interpretation of these curves is discussed first.

Upon approach, the force-distance curve shows a jump-to-contact, which is caused by attractive surface forces. In the JKR-model, the surface itself bends towards the probe to achieve this contact. Then, the approach curve goes through zero. The deflection of the cantilever hereby has the same value as found when it is not in contact with the surface, and this baseline value is set to zero when analyzing the curve.
This point on the curve is the point of initial contact when the model of Hertz applies, but when the JKR-theory applies, it is the point where adhesive forces at the edge of the area in contact, are balanced by the repulsive forces in the center of the area in contact. The point of zero indentation for the JKR model is found at an applied force of $-\left(\frac{8}{3}\right)P_c$.\textsuperscript{37}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure7.png}
\caption{Representative force-distance curve of nanopatterned PDMS. Preload is the maximum on the y-axis (0.5 nN), and pull-off force is the minimum on the y-axis (29 nN).}
\end{figure}

When the cantilever continues to approach the surface even further, the probe is pushed into the surface. The slope of this part of the force curve is determined by both the cantilever stiffness and the stiffness of the sample. Since the same cantilever is used for all measurements, the experimentally determined slope gives information about the effective stiffness of the (nanopatterned) surfaces.\textsuperscript{36}

The cantilever indents the sample until a predefined preload is achieved, after which the cantilever reverses. The retraction curve in Figure 7 does not overlap completely with the approach curve. This difference may indicate viscoelastic deformation of the sample and is also observed for smooth PDMS.\textsuperscript{36}
Eventually, the probe detaches from the surface when the cantilever force overcomes the probe-sample interaction, and the deflection goes back to its initial value (set to zero by the software). The maximum force before the probe detaches for the flat surface is the experimentally determined $P_c$ from the JKR-model. The area under the peak can be integrated, resulting in the experimental work of adhesion, $W_{\text{exp}}$. From $W_{\text{exp}}$ the interface toughness, $G_c$ can be derived, when the contact area is known. Cohesive failure is, due to the short contact time, not expected.26

3.4.4 Macroscopic probe

Force-displacement curves were obtained by moving a smooth spherical probe (of 4.76 mm diameter) against the sample to a defined preload. Subsequently, the probe was retracted with a constant velocity of 1 µm/s until the final detachment event occurred giving the pull-off force, which is a measure of the adhesion performance. This cycle repeated, with increasing preloads, nine times on the same location.

\[ 	ext{Figure 8: Time-force curve for a series of 9 measurements performed at 9 different preloads for Si.} \]

The example in Figure 8 shows that the pull-off force did not change within the series. This indicates that we did not damage our
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structures during attachment and detachment, and thus that our nanopatterned structures can be used repeatedly.

Pull-off forces

A representative force-displacement curve is given in Figure 9A. At least 5 series of 9 force-displacement curves with 9 different preloads were measured on at least 5 different areas per sample. All pull-off forces are presented in Figure 9B.

Figure 9: Adhesion of different (nanopatterned) surface structures. For B-D: ( ) Smooth PDMS; ( ) Sample 1; ( ) Sample 2; and ( ) Sample 3. A) Representative force-displacement curve of nanopatterned PDMS. Preload is the maximum on y-axis (5 mN), and pull-off force is the minimum on y-axis (0.92 mN). Note the loading curve consists of only 14 data points due to the quick approach. B) Pull-off forces of all measurements for smooth PDMS and S1-S3 as function of preload. C) Pull-off force of smooth PDMS and S1-S3 as function of preload with 95% confidence intervals. D) Normalized pull-off force against normalized actual area for smooth PDMS and S1-S3 with 95% confidence intervals.
Figure 9C shows the average pull-off forces plotted against the applied preload for smooth PDMS and for patterned surfaces. The pull-off force values for patterned surfaces were higher compared to the smooth surface at almost any preload. Only S2 showed a preload dependency and exhibited a lower pull-off force than the smooth surface at the highest preload. Due to the relatively low preload forces used in this study, and the small dimple size this decreased pull-off force is unlikely due to mechanical damage. For all other samples, the pull-off force did not vary significantly with the preload. Normalized pull-off forces in the preload independent regime (i.e. < 5 mN) are plotted in Figure 9D.

Contact between sample and probe

Full contact was likely always achieved for our structures. Although we did not observe the contact area directly due to the relatively small size of our surface structures, we conclude that full contact was achieved by comparing our surface feature dimensions and material properties to similar surface structures in previous reports.\textsuperscript{16, 38-39} For example, Jin et al. experimentally observed complete contact independent of preload for PDMS wrinkles with a wavelength of 27 µm and amplitudes (analogous to dimple depth) smaller than 0.6 µm, while wrinkles with amplitudes higher than 3.3 µm showed partial contact. The sample with an amplitude of 1.8 µm showed only complete contact upon applying preload.\textsuperscript{38} In addition, in a theoretical study by McMeeking et al. an approximate condition for complete contact of dimpled surfaces without the application of preload, i.e. spontaneous jump-to-contact, was derived. They showed that the depth of a dimple in a compliant material below which full contact occurs depended on dimple wavelength, \( \lambda \), work of adhesion, \( W_{ad} \), and effective modulus, \( E^* \), as\textsuperscript{40}:

\[
a < \sqrt{\frac{\pi \lambda W_{ad}}{E^*}}
\]

Substituting parameter values as obtained by Jin et al.\textsuperscript{38} for PDMS with similar material properties, i.e. \( E^*=1.5 \) MPa and \( W_{ad} = 0.163 \) J/m\(^2\), we obtain a maximum dimple depth of 0.6 µm, which is a larger value than the depths of our samples. Thus, the dimples in this study are most likely shallow enough to spontaneously jump-to-contact.
Although theoretical considerations suggest that complete contact formation may occur for our dimple dimensions, in practice air can be trapped in the dimples and prevent complete contact from being achieved. A difference between our dimpled structures and wrinkles or an array of pillars, is that dimples are isolated and air can get locked in. However, PDMS is known to have good air permeability, and air will be removed through the material.41

Our results thus support complete contact formation. As stated above, for complete contact the true contact area is defined by the probe and, therefore, our results cannot be explained by a difference in contact area. Instead, the increase in adhesion of our materials may be attributed to a mechanical instability resulting from crack trapping as proposed by Guduru.33 A prerequisite for this explanation is that the Tabor parameter \( \mu > 5 \). and filling in Equation 10, using \( W_{adh} = 0.068 \) J m\(^{-2}\) and \( E^* = 1.43 \) MPa 7, shows that for our system, \( \mu >> 5 \).

Energy dissipation

The origin of this dissipation, namely the specific surface structure, is also present in our materials, and for both concentric wrinkles and dimples the crack can be trapped. Each dimple provides the possibility for the crack trapping and energy-dissipating mechanism. When the dimples are closely packed, the effect of structuring on adhesion is present over the whole area of the sample, and this eliminates the need to position the probe on a unique spot above the sample.

In contrast, for 2D wrinkled surfaces, it has been observed that the crack first moves parallel to the wrinkles after which it jumps in the direction perpendicular to the wrinkles.17 Therefore, for 2D wrinkles this crack trapping mechanism only applies to the last part of the detachment and may explain why no adhesion enhancement was found for 2D wrinkled surfaces with similar wrinkle dimensions to our dimple dimensions.17

An alternative energy dissipating mechanism may be provided by discrete crack initiation, which has been found for small wrinkle amplitudes of 0.5 to 5 \( \mu \)m and an aspect ratio of 0.1, but not for slightly bigger wrinkles (amplitude of 3 \( \mu \)m with the same aspect ratio).17 For these small wrinkles, the individual wrinkles detach first, during pull-off.
This discrete crack initiation throughout the surface dissipates energy. Additional energy could thus be dissipated ahead of the crack front. It should be pointed out that this crack initiation mechanism was found for a planar wrinkled surface in contact with a flat probe whereas in our case the probe is spherical. Therefore, in our case, the middle region will stay under compressive stress much longer during detachment compared to measurements with a flat probe. This means that energy dissipation due to discrete crack initiation can only occur in the vicinity of the crack front.

Effect of dimple depth and dimple density

The difference in adhesion enhancement for the three structured samples can be explained considering two parameters: (i) dimple depth and (ii) dimple density. The dimple depth determines both the magnitude of the crack trapping effect and the elastic penalty upon compression. These two effects counteract each other. A deeper dimple results in more energy dissipation. However, the larger the dimple depth, the more elastic energy is stored due to surface deformation to achieve complete contact. This stored elastic energy is (partly) recovered and may help to break interfacial bonds. Since all three structured samples show enhancement of adhesion compared to the flat control, the energy dissipation through unstable detachment outweighs the elastic penalty, and the net effect of one dimple, is an increase in adhesion.

In addition to the dimple depth, the dimple density will also affect the adhesion. More specifically, a higher density may have a larger influence on adhesion. For our samples the dimple density can be assessed by the crystallinity. A higher (normalized) crystallinity stems from a more efficient packing and thus a higher dimple density. Indeed, if we count all particles within the same area for all three monolayers and compare S1 (pH 10, normalized crystallinity 0.54) and S2 (pH 5, normalized crystallinity 0.35) a decrease in number of particles of 6% is found. Comparing S2 and S3 (pH 3, normalized crystallinity 0.13) results in a decrease of 13%.

In our experiments, both the dimple depth and the dimple density are varied for each sample. We find that the largest increase in adhesion
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for the sample with intermediate dimple density and depth. The increase in adhesion per dimple should therefore be higher with increasing depth in this range of depths, but the decrease in number of dimples with increasing depth counters this effect.

Friction

The friction of the samples was measured by lowering the probe onto the sample, applying a defined constant normal load, and subsequently moving the probe in plane with $100 \mu m \ s^{-1}$ for 20 s. The static friction of flat PDMS was too high ($>70$ mN) to be measured with our set-up. For the nanopatterned samples the shear force first rose up to a peak (static friction), and subsequently dropped to a nearly constant value (dynamic friction), which indicates a sliding frictional mechanism (see Figure 10A).42

**Figure 10:** Effect of nanopatterns on frictional force at different normal loads. A) Three typical friction curves for S1 (red), S2 (blue), and S3 (green). Normal load of 0.5 mN (solid line), 1 mN (intermittent line) and 2 mN (dotted line). B) Average static friction with 95% confidence interval for ) Sample 1;  ) Sample 2; and  ) Sample 3.

Figure 10B shows that, compared to flat surfaces, friction was decreased by the patterns. This is in agreement with several previous publications on patterned elastomers: whereas friction measurements on flat PDMS resulted in pronounced stick-slip motion, patterned surfaces with vastly different patterns did not show stick-slip instabilities and showed decreased friction42-43 Lorenz and Persson explained the
disappearance of stick-slip motion for patterned surfaces by the occurrence of sequential interfacial slip. They showed that surface patterns with millimeter sized surface features will reduce the elastic coupling between the different surface features, which can cause these features to move more independently of each other than surface patches on the flat homogeneous surface.\textsuperscript{44} This reduces the tendency for macroscopic stick-slip motion. Whereas our dimples are relatively small and shallow they still result in a heterogeneous stress distribution and a decrease in lateral stiffness, as explained by Rand and Crosby.\textsuperscript{45} This decreases the friction.

### 3.4.5 Effect of relative size of probe to surface structure

The adhesion of the nanopatterned surfaces was increased compared to a smooth surface when using a macroscopic probe as counter surface. Interestingly, Guduru predicted an effect of probe size on adhesion of a structured surface compared to adhesion on a flat substrate.\textsuperscript{33}

*Figure 11: Dependence of maximum pull-off force as function of $a/\lambda$ for different values of $\lambda/R$. Printed with permission from ref 33.*
Figure 11 shows this effect for the surface with concentric circles with the probe centred above it. Since $a/\lambda \approx 0.10$ for our nanopatterned surfaces, the solid line is of interest. For both small and large values of $\lambda/R$, the maximal pull-off force as predicted by the JKR theory is found. For moderate values ($0.1 < \lambda/R < 0.8$), an increase in adhesion is predicted. This corresponds to probes with a diameter between 2 and 20 $\mu$m. To enter this regime, a colloid with $d = 8 \mu$m is chosen as probe to measure the adhesion of our nanopatterned surfaces.

![Figure 12: A) Schematic representation of a 4.76 mm probe on a nanopatterned surface with $a = 110$ nm. B) Schematic representation of a 8 $\mu$m colloidal probe on a nanopatterned surface with $a = 110$ nm.](image)

Figure 12 shows the size of both the macroscopic probe (A) and the microscopic probe (B) relative to the dimensions of the surface structures. The macroscopic probe appears to be flat compared to the surface structures, whereas the microscopic probe is of the same order of magnitude.

### 3.4.6 Colloidal probe

Force-displacement curves have been recorded with the colloidal probe for all three samples and the flat control. An example is shown in Figure 7. Since our cantilever is quite flexible, choosing a high preload introduces shear forces. Therefore, a low preload of 0.5 nN was chosen. The jump-to-contact position and jump-to-contact force, $P_c$, $W_{exp}$, and slope have been determined for at least 5 locations per sample, using at least 500 force-displacement curves per location.
Chapter 3

Work of adhesion and pull-off forces

Figure 13 shows the work of adhesion and pull-off forces for all samples. The nanopatterned surfaces showed an increase in both $W_{\text{exp}}$ and $P_c$. Both were highest for S1 (Figure 13BC), which is the sample with smallest dimple depth $a$ and highest dimple density. The increase in $W_{\text{exp}}$ for the patterned samples compared to the flat sample, shows that energy is indeed dissipated due to structuring during pull-off.

The relative increase in $P_c$ as compared to the flat surface, was similar for both probe sizes (Figures 9D and 13D). However, $P_c$ measured with the colloidal probe was two orders of magnitude smaller than the expected value of $\sim 3$ mN, as calculated using Equation 7, the probe radius of 4 µm and the literature value for $W_{\text{adh}}$ for PDMS from ref 38.
which is 0.163 J/m². There is no clear explanation for this deviation. We hypothesize that either the model is not applicable to our system, or the deviation is caused by a difference in $W_{adh}$ from literature and in our system (e.g. due to aging of the sample). We assume that the latter explanation is the most likely of the two. Since $W_{adh}$ and the contact area are related to each other (see Equation 4) we cannot use the JKR model to find an estimate for the contact area. However, the deviation in $W_{adh}$ from the literature value should be constant for all four samples. Therefore, our measurements can still be used to study the effect of structuring on adhesion by comparing the values for the nanopatterned samples to the values found for the flat control sample.

Also, the enhancement in $P_c$ of the nanopatterned surfaces as predicted by Guduru (Figure 11), was not found. This shows that the fine details of the theoretical framework on concentric wrinkles are not directly applicable to a surface with dimples. An important factor for the surface with concentric wrinkles is that, upon increase or decrease in probe size, the number of wrinkles in contact changes in discrete steps (recall that the probe for this system is centred in the middle of all concentric wrinkles). An increase in $P_c$ is found when, apart from the central crest, also wrinkles are in contact. Upon increasing the probe size, more wrinkles will be in contact, and for up to three wrinkles, this results in increasing values of $P_c$. For even more wrinkles, $P_c$ for the structured surface goes back to the value for $P_{c,JKR}$. The load during pull-off is spread over more crack trapping locations, resulting in a smaller $P_c$. For the nanopatterned surfaces, a lot of crack trapping locations exist during pull-off, namely every dimple in contact. The dimpled surface may therefore be more similar to a surface with a lot of concentric wrinkles in contact, even though the ratio $a/\lambda$ is similar for both surfaces.

Variations within one sample

For the sample with concentric wrinkles from literature, the precise positioning of the probe above the surface structure is of vital importance for the adhesion enhancement. Given the dimensions of our surface structures and the probe (see Figure 12), this may also be the case for our nanopatterned surfaces. The contact area with the small probe is small, thus only a few dimples are in contact and can contribute
to the energy dissipation. With decreasing dimple density for S1 > S2 > S3, the number of dimples in contact may differ significantly between the samples; if the probe approaches the surface on a non-crystalline area (mostly found on S3), less dimples are present in the contact area than when the probe is positioned above a crystalline area (mostly found on S1). This effect is averaged out for the large contact areas when using a large probe, but a small probe can be positioned such that almost no dimples are in contact. The local dimple density is therefore expected to have an effect on the pull-off force for the small probe. And even within one sample, \( P_c \) may be different. The centre of the probe may be positioned directly above a dimple, or directly above an interdimple region. The area in contact may have dimples in a hexagonal packing, or the dimples are on a grain boundary. This all may influence the adhesion within one sample.\(^{46}\)

To test this, \( P_c \) is measured 500 times at five different locations per sample (Figure 14).

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**Figure 14:** Peak force for series of 500 force-displacement curves at five different locations for A) smooth PDMS, B) Sample 1, C) Sample 2, D) Sample 3.
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$P_c$ was of the same order of magnitude for all samples as well as for all locations within one sample. It is unlikely that the probe was positioned on a similar location each time. Hence, the exact positioning of the probe on our nanopatterned surface only influences adhesion in a rather subtle way.

Influence of contact time

Another factor that is important for the value of $W_{adh}$ is the contact time. For a system consisting of a flat, solid surface (mica) and a colloidal probe made of PDMS a logarithmic increase of $W_{adh}$ with contact time was found. When the PDMS and the substrate are in contact the polymers at the interface can reorganize, and, if the contact is kept long enough, can even form covalent bonds if the counter surface is glass. It is therefore instructive to look at the approach curves of our samples to see if the contact time was constant for our different samples. The jump-to-contact position and force from the approach curves have therefore been plotted in Figure 15.

![Figure 15: Jump-to-contact of the colloidal probe during approach to the nanopatterned surfaces for five different locations per sample. For A-B: .](image)

Smooth PDMS; Sample 1; Sample 2; and Sample 3. A) Jump-to-contact force as a function of jump-in-contact position. B) Average jump-to-contact force.

The jump-to-contact position is the difference in position from the jump to the point of zero deflection. It consists of the initial jump due to attraction between the surfaces, indentation due to adhesion and the
Figure 16: Peak force at pull-off velocities $v$ of 0.2 $\mu$m s$^{-1}$ ( □ ), 2 $\mu$m s$^{-1}$ ( ● ) and 20 $\mu$m s$^{-1}$ ( △ ) for A) smooth PDMS, B) Sample 1, C) Sample 2, D) Sample 3.

deployment of both the sample surface and the probe. The jump-to-contact force was significantly larger than the preload of 0.5 nN.

In a previous study, the contact area for a colloidal PDMS probe and mica counter surface showed hardly any increase from the jump-to-contact (at 0 $\mu$N) to the preload (6.7 $\mu$N). Therefore, we expect a constant contact area during jump-to-contact to maximum preload for our system.

The jump-to-contact force and position were both higher for the nanopatterned surfaces compared to the flat surface. It was highest for the sample with the highest dimple density and lowest dimple depth, a. This can be partly attributed to bulk and interfacial viscoelasticity. The contribution of the interfacial viscoelastic component on energy dissipation depends on the contact time. The contact time is not constant in our case because the jump-to-contact varied per sample and spot on the sample. The larger the jump, the longer the contact time.
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However, given that the difference in jump-to-contact distance is 20 nm at most (Figure 15A), this contribution is close to negligible. Therefore, we cannot use contact time to determine whether viscoelasticity is important in our system. This, however, can be determined by varying the retraction velocity.

Influence of retraction velocity

If our material is indeed viscoelastic, then the $P_c$ is expected to depend on the retraction velocity. The velocity dependence on the pull-off force is shown in Figure 16. The curve for S3 with $v=0.2$ showed a drift that we cannot explain, and hence this curve will not be discussed. For all other curves, we see that a higher velocity results in a higher pull-off force for all samples.

![Graph](image)

*Figure 17: Average peak force as function of velocity for \( \bullet \) Smooth PDMS; \( \diamond \) Sample 1; \( \triangle \) Sample 2; and \( \square \) Sample 3.*

The velocity dependence is higher for the structured samples than for the flat sample: the difference between the average pull-off force at low speed (0.2 $\mu$m s$^{-1}$ or 2 $\mu$m s$^{-1}$) and high speed (20 $\mu$m s$^{-1}$) is smallest for the flat control sample (Figure 17).

Since we find a velocity dependence, we can conclude that PDMS is not a completely elastic material. The oligomers at the surface result in
some viscous behaviour. The oligomers stretch and can be detached when the probe retracts.\textsuperscript{22}

**Influence of apparent stiffness**

The bulk stiffness of the four samples is the same: samples were prepared with the same material. However, structuring materials can alter the apparent stiffness and this parameter is important for the pull-off. A measure of the stiffness of the sample is the slope of the constant compliance region in the force-displacement curve. This is shown in Figure 18.

![Figure 18: Slope of the force-distance curve during approach for five different locations per sample. For A-B: \(\bullet\) Smooth PDMS; \(\blacklozenge\) Sample 1; \(\blacktriangle\) Sample 2; and \(\blacksquare\) Sample 3. A) Slope of the force-distance curve during the approach as function of pull-off force. B) Average slope of the force-distance curve during approach.](image)

It is clear that structuring the surfaces decreases the apparent stiffness; the slope of the flat sample is higher than that of the nanopatterned samples. This can be understood: a probe has to deform more material when encountering a flat substrate compared to a structured sample upon approach.

The decisive parameter influencing surface stiffness does not seem to be the dimple depth \(a\), but the dimple density: the more dimples are present, the more the nanopatterned surface deviates from a flat surface, and the more compliant the surface appears to be.
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Influence of the elastic penalty

For the macroscopic probe, we observed that the higher the dimple depth $a$, the more energy is dissipated per dimple. The elastic penalty, which is higher for deeper dimples, does thus not overrule the increase in energy dissipation per dimple for deeper dimples. Since the sample with the deepest dimples (S3) is also the sample with the smallest density, a trade-off between dimple density and dimple depth was found, in which the sample with medium dimple depth and density (S2) showed the highest pull-off force.

For the small probe, this trade-off between dimple density and dimple depth is not found; not S2 but S1 shows the highest adhesion. The explanation may lie in the effect of probe size on the elastic penalty. The macroscopic probe is so large that it can be considered a flat surface on the scale of a dimple (see Figure 12). For the smaller probe, the curvature of the probe itself is present on the scale of a dimple. The surface has to deform more in order to make full contact with the surface of the colloidal probe compared to that of the macroscopic probe. This deformation is more easily achieved for samples with a lower apparent stiffness, and thus with the higher dimple densities.

Due to these larger deformations that are required for a dimple to make contact, it is expected that the elastic penalty has a stronger effect on the final pull-off force. The deeper the dimple, the more deformation is needed, thus the higher is the elastic penalty. Using this line of reasoning, S1 shows the highest pull-off force for the colloidal probe because it has more and shallow dimples.

3.4.7 Conclusion

Nanopatterned surfaces have been made according to the method presented in Chapter 2. Three samples with varying dimple depth and dimple density were selected. The effect of the surface structures were investigated using two spherical probes with different size as counter surface, and the resulting force-displacement curves were analysed. The pull-off force was increased for all nanopatterned surfaces and for both probe sizes. The increase is attributed to energy dissipation during pull-off; the detachment process shows stable and unstable regions due to
the surface structures. The two parameters controlling the final pull-off force are dimple density and dimple depth. Every dimple contributes to energy dissipation, thus the higher the dimple density, the more energy dissipation. The effect of dimple depth depends on the counter-surface used. For the large probe, the highest $a$ gives the highest energy dissipation per dimple, but this trend is not found for the smaller probe. The scaling of pull-off force with probe size as described for a surface consisting of concentric wrinkles, has not been found for our nanopatterned surfaces. It is therefore suggested that not the ratio $a/\lambda$, but the number of crack trapping locations is important for the increase in $P_c$.

These results show that interfacial templating of colloidal particles provides a promising route for creating functional surfaces of which the three-dimensional topology can be tuned without elaborate and energy-consuming lithographic methods. With the emergence of a wide variety of new methods to tailor the size and shape of colloids, and their organisation at liquid interfaces, this opens a wealth of opportunities for lithography-free design of new adhesive and low-frictional materials.

References


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4 Controlled fabrication of polypyrrole surfaces with overhang structures by colloidal templating

This chapter is based on:
4.1 Abstract

Here we present the fabrication of polypyrrole (PPy) surfaces with a controlled overhang structure using a crystalline colloidal monolayer at the air/water interface as a template. With a scalable fabrication process, consisting of interfacial polymerization around sacrificial polystyrene particles, regularly structured PPy films were produced. The morphology of the final inverse colloidal PPy film is controlled by the amount of monomer, the monomer : oxidant ratio and polymerization time. The PPy films exhibit an overhang structure due to depth of particle immersion in the water phase. As a result of the overhang structure, the PPy films are made hydrophobic, although the material itself is hydrophilic. The apparent contact angle of water on the structured surfaces is $109.5^\circ$, which is in agreement with the predicted contact angle using the Cassie-Baxter equation for air-filled cavities. This fabrication technique can be readily extended to other systems where controlled wettability is required.

4.2 Introduction

Conducting polymers are an interesting class of materials due to the combination of traditional polymer properties with novel optical and electronic behaviour. They can be used in electronic nanodevices, as chemical or optical sensors, in catalysis, and energy storage. A key parameter in many applications is the control of surface wetting. One common method to control wetting is to chemically change the surface energy. In the specific case of polypyrrole (PPy), chemical modification has been performed by copolymerizing pyrrole with a modified fluorinated pyrrole monomer, adding different hydrophobic codopants or by silanization of PPy.

Alternatively, wetting properties can be changed upon structuring the surface. In this way, the intrinsic electronic and optical properties of the PPy will be conserved. When pyrrole is polymerized, it usually grows in uncontrollable globules and becomes a highly crosslinked, insoluble powder. The crosslinked nature makes PPy difficult to process. One of the few reports on structuring PPy after synthesis
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uses laser patterning;\textsuperscript{30} however, complex 3D structures cannot be fabricated in this way. A bottom up approach with the desired surface structure fabricated in-situ during PPy synthesis is therefore highly desirable. This can be accomplished either by electrochemical or chemical synthesis. During electrochemical synthesis, pyrrole is polymerized to PPy at the anode. By changing the conditions, different structures can be fabricated\textsuperscript{9, 31}, including hollow microhorn arrays\textsuperscript{32}, butterfly scale-like ordered porous structures\textsuperscript{33}, 2D honeycomb structures\textsuperscript{34}, and nanopillars.\textsuperscript{35} Methods to chemically synthesize structured PPy films and coatings include interfacial synthesis at the water/organic solvent interface\textsuperscript{36-38}, oxidant assisted synthesis\textsuperscript{39}, and the use of templates. Both soft templates, consisting of surfactants\textsuperscript{40-42}, and hard templates, consisting of colloids, have been employed to synthesize coated microspheres\textsuperscript{43-47} and nanocups.\textsuperscript{48}

As PPy is a hydrophilic material, structuring the surface by simply increasing the roughness of the PPy surface is likely to result in complete contact between the water and the solid surface under the droplet, also called the Wenzel state. The apparent contact angle in the Wenzel state ($\theta_w$) is related to the roughness $r$ of the material as\textsuperscript{49}

$$\cos \theta_W = r \cos \theta$$

with $\theta$ the contact angle of the droplet on a perfectly flat substrate, and $r$ the roughness of the surface (true contact area/projected area). The Wenzel state always magnifies the underlying wetting properties: the apparent contact angle for hydrophilic materials decreases, and the apparent contact angle for hydrophobic materials increases.\textsuperscript{50} As the Wenzel equation therefore cannot be used to predict an increase in contact angle due to structuring of a hydrophilic material, the Cassie-Baxter state is defined to describe this regime. In the Cassie-Baxter state, air is trapped underneath a droplet. The presence of air (which has a contact angle of $180^\circ$ with water) effectively lowers the average surface energy,\textsuperscript{51,52} which can yield hydrophobic apparent contact angles on intrinsically hydrophilic materials ($\theta < 90^\circ$). The apparent contact angle for a Cassie-Baxter state, $\theta_{CB}$, is given by\textsuperscript{53}

$$\cos \theta_{CB} = \phi_s \cos \theta - (1 - \phi_s)$$

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with $\varphi_s$ the fraction of the droplet that is in contact with the solid and $(1-\varphi_s)$ the fraction of the droplet in contact with air.

However, for hydrophilic materials ($\theta < 90^\circ$) the Wenzel state is energetically more favourable. Therefore, to achieve hydrophobic behaviour on hydrophilic materials, an energy barrier is required to maintain the Cassie-Baxter state.\textsuperscript{25} For a surface containing cavities, this barrier can be provided by capillary forces that prevent water from entering these cavities.

This condition is met when the cavity has an overhang structure; in other words, the overhang angle, $\theta_{\text{overhang}}$, is smaller than the contact angle $\theta$ of water on a flat substrate.\textsuperscript{25} Figure 1 shows this behaviour for spherical cavities. If $\theta_{\text{overhang}} > \theta$, the inside of the cavity is readily wetted and the cavity fills with water (Figure 1B). When $\theta_{\text{overhang}} < \theta$, the air/water interface has to increase to reach the equilibrium contact angle $\theta$ (Figure 1C). The energy cost of creating this additional interfacial area is not compensated by the energy gain of the water wetting the hydrophilic walls and the droplet will thus not enter the cavity.\textsuperscript{54}

![Figure 1: A) Contact angle $\theta$ of water on a smooth substrate. This angle is denoted with a dashed line in A-C. B) $\theta_{\text{overhang}}$ (solid line) $> \theta$ (dashed line): the droplet will wet the cavity. C) $\theta_{\text{overhang}}$ (solid line) $< \theta$ (dashed line); the air/water interface needs to enlarge to wet the cavity which is energetically unfavourable.](image)

In this chapter, we use a colloidal template to create PPy surfaces with overhang structures. The colloidal template consists of a monolayer of polystyrene (PS) particles at the air/water interface with PPy grown at the particle/water interface. To obtain overhang structures, colloidal particles that are hydrophilic, and hence deeply immersed in the water phase, are used. We systematically study the different morphologies
that can be fabricated using this method, and show that the surface switches from hydrophilic to hydrophobic upon structuring.

4.3 Experimental

4.3.1 Materials

All materials were purchased from Sigma Aldrich and used as received.

4.3.2 Particle synthesis

Carboxylated PS particles were synthesized in a one-step synthesis according to ref 55. Briefly, Milli-Q water (120 g), itaconic acid (0.5 g) and styrene (24.5 g) were heated to 80 °C in a round bottom flask, and flushed with nitrogen for 45 minutes. Meanwhile, 4,4’-azobis(4-cyanovarlic acid) (252.4 mg) was dissolved in 1M NaOH (2 g) : water (6.3 g) solution. After adding this solution to the round bottom flask, the mixture was reacted overnight under continuous stirring at 500 rpm. The product was filtered over glass wool to discard waste coagulum that formed during the reaction, and was washed in water by three cycles of centrifugation at 4500 rpm for one hour followed by re-suspension in Milli-Q water. After this washing step, the colloids were exchanged to ethanol, and washed three times in ethanol following the same procedure. Using static light scattering, the radius of the particle, $R_p$ was found to be 574 nm, and the polydispersity index (PDI) ($R_w/R_n$) was 1.01. The parking area (particle surface area)/(number of charges per particle), was determined using titration and found to be 0.11 nm$^2$ per charge.$^{56}$

4.3.3 Surface structure preparation

Crystalline colloidal monolayers were prepared according to ref 56. The monolayers were prepared in PS Petri dishes (typical diameter 50 mm) filled with water at pH 8–10, and ionic strength of $10^{-1} – 10^{-3}$ M, unless stated otherwise. A dispersion of particles in ethanol was applied to the air/water interface via a piranha-cleaned coverslip using a pipette (see Scheme 1A). The samples were left to equilibrate for at least
Scheme 1: Schematic representation of the preparation of PPy inverse crystalline colloidal monolayers. A) Monodisperse carboxylated PS particles are applied to the air/water interface. B) Pyrrole is added to the subphase. C) Fe$^{3+}$ is added to the subphase and interfacial polymerization of pyrrole starts. D) The film is washed with water and PS particles are removed with THF.

30 minutes to ensure evaporation or dissolution of all ethanol. Pyrrole was added to the subphase (i.e. water underneath the particles) (Scheme 1B). Pyrrole either remained as a droplet on the bottom of the Petri dish, or formed a ring at the air/water/Petri dish contact line. Two hours after pyrrole addition, a 1M solution of ferric chloride was added to start the interfacial polymerization (Scheme 1C). The sample turned black upon polymerization of PPy, which was immediately after Fe$^{3+}$ addition for high amounts of pyrrole, while it could take hours for low amounts. The reaction was allowed to proceed for at least 24 h to ensure complete conversion.$^{57}$ This step is especially important for samples with low amounts of pyrrole or Fe$^{3+}$. The lid of the Petri dish was closed
during this time, to prevent pyrrole evaporation. PPy crystalline colloidal monolayers (PPy-ccm) were washed by removing the subphase using a syringe and replacing it with ultrapure water (Scheme 1D). This washing step was repeated three times. The monolayers were subsequently transferred by immersing the Petri dish in a large clean water bath, containing at least 250 mL water. As the monolayers float, they can be scooped up with another clean Petri dish. PS particles were removed by soaking cleaned PPy monolayers in THF for at least 2 hours, resulting in PPy inverse crystalline colloidal monolayers (PPy-iccm) (Scheme 1D).

4.3.4 Flat PPy surfaces

Flat PPy surfaces were prepared according to ref 59. Briefly, microscope slides were submerged in KOH (5 M) for 30 minutes and thoroughly rinsed with water. Water (10 mL), ethanol (90 mL) and (3-aminopropyl)triethoxysilane (APTES, 100 µL) were mixed and stirred for 2h to hydrolyze the APTES. The microscope slides were subsequently submerged in hydrolyzed APTES solution for 6 hours. After this, the microscope slides were rinsed with ultrapure water and put under vacuum at RT overnight. The contact angle changed from <5° (after KOH treatment) to 52.2° ± 0.6° after APTES treatment, which is consistent with the initial contact angle found for APTES monolayers. The dried microscope slides were placed diagonally in a 50 mL beaker, containing a 36 mM aqueous solution of FeCl₃ (40 mL). Pyrrole (100 µL) was added and the reaction was allowed to proceed for 8 hours under gentle stirring. PPy aggregates were removed from the surface with a tissue and by using excessive rinsing.

4.3.5 Characterization

Scanning Electron Microscopy (SEM)

Samples were prepared by scooping part of the floating monolayer from the air/water interface using cut silicon wafers as substrate. To prevent self-folding upon drying, Leitsilber 200 Silver Paint (Ted Pella) was used to glue the films to the substrate. Samples were sputtered...
with gold (30mA, 40s) using a JEOL JFC-1300 autofine coater, and imaged using a JEOL JAMP-9500F Field Emission Auger Microprobe at 10 kV.

X-ray photoelectron Spectroscopy (XPS)

XPS spectra were measured on a JPS–9200 X-ray photoelectron spectrometer (JEOL, Japan). High resolution spectra were obtained under UHV conditions using monochromatic Al Kα X-ray radiation at an angle of 80° at 12 kV and 20 mA, using an analyzer pass energy of 10 eV. Spectra were corrected with a standard background subtraction according to a linear procedure before fitting. The spectra were fitted using Casa XPS software (version 2.3.15) and to compensate for the surface charging effects, the N 1s peak was calibrated at a binding energy of 399.6 eV, in accordance with ref 61. Calculated atomic percentages were normalized by the corresponding atomic sensitivity factors.

Energy-dispersive spectroscopy (EDS)

Samples were first imaged at 2 kV, 6 pA, at room temperature, in a field emission scanning electron microscope (Magellan 400, FEI, Eindhoven, the Netherlands). EDS analyses were accomplished by an Oxford X-max detector and analysis software (Oxford Instruments Analytical, High Wycombe, England) at an acceleration voltage of 10 kV, 0.8 nA.

Contact angle measurements

Contact angles were determined using the Kruss Contact Angle measuring System G10 and using the “Drop Shape Analysis” software. Samples consisted of PPy films mounted on a cover slip using double sided tape and left to dry for at least a week at RT. Contact angles were measured on at least 5 locations using droplets of 5 µL.
4.4 Results and discussion

4.4.1 Fabrication and characterization of PPy-inverse crystalline colloidal monolayers

Fabrication outline

The fabrication process of PPy inverse colloidal monolayers (PPy-iccm) is shown in Scheme 1. First, a crystalline colloidal monolayer is prepared using carboxylated PS particles as described in ref 56 (Scheme 1A). These carboxylated PS particles \(d = 1.15 \mu m\) are selected because the carboxylic acid surface groups (i) allow control over the PS particle ordering by pH, and (ii) make the particles hydrophilic, ensuring high immersion depths in the subphase.

Second, pyrrole is added to the subphase (Scheme 1B). Since pyrrole is more soluble in PS than in water, these monomers diffuse into the PS particles. Each particle thus acts as a reservoir for monomers, as has also been observed for aniline.\(^\text{62-63}\) Third, pyrrole is polymerized (Scheme 1C). This oxidation polymerization of pyrrole starts by \(\text{Fe}^{3+}\) adding as oxidant. As polymerization occurs only where \(\text{Fe}^{3+}\) and pyrrole are present, the reaction is limited to the PPy/water interface.\(^\text{64}\) The ferric chloride in the water can either oxidize a pyrrole monomer directly\(^\text{65}\), or first act as a Lewis acid, after which an electron from the aromatic ring can more easily be taken, resulting in an oxidized pyrrole monomer.\(^\text{58}\) Next, the radical cation reacts either with another monomer, after which oxidation and deprotonation results in a dimer or it reacts with another oxidized monomer.\(^\text{65}\) This dimer can be oxidized again, and hereafter attack another monomer, thus driving the polymerization. Pyrrole monomers are supplied by diffusion of the monomers through the PS and PPy matrix to the polymer/water interface.

During pyrrole polymerization, the colour of the samples changes from yellow/orange (from \(\text{Fe}^{3+}\)) to black. This colour change happens within a minute when a high amount of pyrrole and a high \(\text{Fe}^{3+}\): Py ratio are used, but can take hours for lower amounts of pyrrole and low \(\text{Fe}^{3+}\):
Py ratio. No colour change is observed within 24h when no ferric chloride is added.

![SEM micrographs](image)

**Figure 2**: SEM micrographs of washed PPy surface structure (PPy-iccm) made with 2.1 μL Py cm$^{-2}$ and a Fe$^{3+}$: Py ratio of 2.3 (mol/mol). A) Top-surface (facing air during polymerization); B) Side view; C) Bottom-surface (facing water during polymerization). All scale bars represent 1 μm.

Fourth, after polymerization, the PPy film is transferred to a clean water bath and removed from the bath using a glass Petri dish. The particles are extracted from their PPy matrix by dissolving the film in THF (Scheme 1D), resulting in a PPy inverse crystalline colloidal monolayer (PPy-iccm). The PPy matrix is thick and stiff enough (Young’s modulus of around 1 GPa$^{66}$) to prevent collapse of the inverse colloidal structure. An example of a PPy-iccm is shown in Figure 2, and more examples can be found in Figure 3.

**Chemical characterization of PPy-iccm**

The wetting behaviour is heavily influenced by the chemical composition of the system. To confirm that PPy was fully formed during iccm preparation, the elemental composition of the films was determined by XPS measurements and EDS measurements were performed to check for compositional variations within the film.
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Figure 3: SEM micrographs of washed polypyrrole surface structures (PPy-iccm) 
A) 2.9 \mu L Py cm^{-2} and Fe^{3+}: Py ratio of 2.3 (left), 2.1 \mu L Py cm^{-2} and Fe^{3+}: Py ratio of 2.3 (right); B) 1.3 \mu L Py cm^{-2} and Fe^{3+}: Py ratio of 2.3; C) 0.42 \mu L Py cm^{-2} and Fe^{3+}: Py ratio of 0.85; D) 0.42 \mu L Py cm^{-2} and Fe^{3+}: Py ratio of 0.33.

XPS measurements

Elemental composition was determined with XPS measurements on a PPy-iccm sample synthesized with 2.1 \mu L Py cm^{-2} and Fe^{3+}: Py = 2.3, both at the top-surface of the sample (facing air during polymerization) and bottom-surface (facing water during polymerization). The XPS survey scan (Figure 4A-B) shows C and N as expected for pure PPy, as well as contaminants Cl, O and, at the bottom-surface, Fe. Core level peaks for C and N (see SI 1) are fitted and assigned as described in ref 61. The assigned peaks are listed in Figure 4C. The fitting procedure for N 1s and C 1s indicated that our iccm indeed consists of PPy (see SI 1).
Based on the reaction as presented in Scheme 1, only signals from N 1s and C 1s are expected. Assuming that all N originates from pyrrole (and thus neglecting any N from the initiator during particle synthesis) and that no N is cleaved off during side reactions, the percentage of C 1s
alpha and beta signal that can be attributed to polypyrrole (one N is attached to 4 C, thus pure pyrrole is $5 \times$ N 1s) can be determined. These calculations indicate a lower amount of pyrrole at the bottom surface (38% vs 64% for the top-surface). The rest of the C1s signal may be attributed to two additional processes: residue PS adsorption after particle dissolution and side reactions during pyrrole polymerization.

A common side reaction is overoxidation, which is the gradual oxidation of PPy by water in the presence of FeCl$_3$ and results in O incorporation in the polymer matrix.$^{44-45, 61, 67-68}$ Another common side reaction is the incorporation of dopants, such as chloride, that results in the Cl 2p signal from charge transfer interactions with the polymer backbone.$^{45}$ Other dopant species, i.e. iron(III) chlorides (FeCl$_3^-$, FeCl$_2$) $^{57}$, can only be found at the bottom-surface, since the Fe 2p signal is absent at the top-surface. Part of this Fe is coordinated to N, as evidenced by the N 1s core level spectrum for the bottom-surface (see SI 2). The pyrrole rings at the bottom-surface thus underwent further reactions while in contact with the FeCl$_3$ solution. Additional evidence for further reactions at the bottom-surface can be determined from the (NH, N-pyrrole): N=C ratio. For the bottom-surface we find a high ratio of 6.7, while this ratio is only 4.8 for the top-surface.

In addition to the presence of oxygen from overoxidation, O may stem from incomplete removal of the PS particles. The particles consist of copolymerized styrene (C$_8$H$_8$) and itaconic acid (C$_5$H$_6$O$_4$). The presence of polystyrene-co-poly(itaconic acid) residues is also indicated by the enrichment of the signal in C compared to N (N : C of 1 : 5.2 for the top-surface, and N : C of 1 : 7.8 for the bottom-surface).

**EDS measurements**

In SEM micrographs of PPy-iccm (2.1 µL Py cm$^{-2}$, Fe$^{3+}$: Py = 2.3), triangular protrusions were observed at the top-surface that appear white in SEM (see Figure 2A and B). This contrast is either due to the surface topology or due to differences in chemical composition. EDS was performed to study compositional variations, and the maps can be found in Figure 5 and the EDS spectra in Figure 6. C and O are evenly distributed over the sample (Figure 5A and 5C), and no differences are found between the protrusions and the rest of the sample. There is
Figure 5: EDS maps of PPy-iccm (2.1 µL Py cm⁻², Fe²⁺: Py = 2.3) for A) C Kα, B) Fe Kα, and C) O Kα. D) overlay map with C Kα (turquoise), Fe Kα (green) and Si Kα (red, from support material).

almost no Fe found on the top-surface (Figure 5B), in agreement with the XPS data. In the overlay map Si is observed (indicated in red), which stems from the support material. The visible features in the SEM micrographs can thus be attributed solely to surface topology.

4.4.2 Control over surface morphology

Control over monolayer crystallinity

PPy-ccms were fabricated using colloidal monolayers prepared at the air/water interface using water at different pH values, namely pH 3, pH 5, and pH 10. The ionic strength was kept constant at 1 mM. The
ordering of the particles during monolayer formation is governed by the competition between capillary attraction and electrostatic dipolar repulsion between the particles. This balance between attraction and repulsion can be controlled by the pH and ionic strength of the
Figure 7: Scanning electron micrographs showing the effect of subphase composition on PPy surface structure at fixed [Py] of 2.9 µL cm$^{-2}$ and Fe$^{3+}$ : Py ratio of 2.3 mol/mol. Subphases: A) pH = 3, [salt] = 1 mM; B) ultrapure water; C) pH = 10, [salt] = 1 mM; All scale bars represent 1 µm.
At high pH, the carboxylic acid groups of the itaconic acid (with $pK_{a1} = 3.85$ and $pK_{a2} = 5.44$) are deprotonated, giving rise to an asymmetric counter-ion distribution, resulting in a dipole moment. The dipole-dipole repulsion between the different particles counteracts the attractive van der Waals interactions. Consequently, the particles remain more mobile at the interface resulting in more ordered monolayers. This allows the particles to assemble in a hexagonal packing, thus resulting in crystalline monolayers. At low pH, the carboxylic acid groups on the surface of the monomers are protonated, and hence no electrostatic repulsion between the particles exists. Particles that approach each other closely thus immediately feel the attractive van der Waals forces that bring them in close contact. This process immobilizes the particles and results in close-packed monolayers with relatively low crystallinities.

The final PPy-ccm structure prepared at pH = 3, though close-packed, shows low crystallinity (Figure 7A), which is consistent with the poor order in the monolayer. The crystallinity of the monolayers prepared at neutral and high pH increases with increasing pH and is preserved in the PPy-ccm (Figure 7B and 7C), although both the pH and the ionic strength of the subphase change during polymerization. The ionic strength increases dramatically upon addition of the Fe$^{3+}$, and the pH drops during polymerization due to proton release (see Scheme 1B). Assuming complete conversion of pyrrole monomers, the theoretical pH value for this sample decreased to 1 during polymerization. Conserving the crystallinity is therefore surprising, as it has previously been observed that changing the pH after the preparation of the monolayer decreases the particle order. The pyrrole here appears to act as a glue between the particles early in the polymerization process, preserving the crystallinity in the PPy-ccm layer.

**Amount of pyrrole**

The samples in Figure 7 are made using 2.9 $\mu$L pyrrole per cm$^2$ of monolayer. The molar ratio Fe$^{3+}$ to pyrrole is chosen to be 2.3, which is the same value as used in ref 72. Keeping this ratio and the crystallinity of the monolayer fixed, samples were prepared using different amounts...
Figure 8: SEM micrographs showing the effect of amount of PPy on PPy surface structure at fixed Fe³⁺: Py ratio of 2.3. Pyrrole (µL cm⁻²) added: A) 0.042 B) 0.084 C) 0.21 D) 0.42 E) 0.84 and F) 2.1. All scale bars represent 1 µm.

of pyrrole ranging from 0.042 to 8.4 µL cm⁻². At the lowest amount of pyrrole, PPy-fibrils appear to be adsorbed on the PS particles (Figure 8A). Increasing the amount of pyrrole to 0.084 µL cm⁻², results in particles coated with a PPy layer (Figure 8B). This PPy layer thickens upon increasing the amount of pyrrole (Figure 8C), and at 0.42 µL pyrrole cm⁻² the PPy forms a continuous layer with triangular dimples (Figure
At even higher PPy concentrations, the edges of these triangular dimples protrude from the PPy surface (0.84 μL pyrrole cm$^{-2}$) (Figure 8E) and at 2.1 μL pyrrole cm$^{-2}$ triangular protrusions are formed (Figure 8F). The final structure of the PPy-iccm can thus be varied by choosing the amount of pyrrole at fixed Fe$^{3+}$: Py molar ratio.

**Molar ratio Py : Fe**

A similar effect can be obtained by varying the Fe$^{3+}$: Py molar ratio. Figure 7 shows the results of varying this ratio from 0.07 to 1.5 at a fixed amount of 0.42 μL pyrrole cm$^{-2}$. At the highest ratio, the final structure is a continuous PPy surface with triangular dimples (Figure 9D). However, at the lowest ratio, no traces of PPy are visible (Figure 9A). In between these extremes, PPy coatings on the PS particles were obtained that increased in thickness with increasing molar ratio (Figure 9B and 9C).

*Figure 9: SEM micrographs showing the effect of Fe$^{3+}$: Py ratio on PPy surface structure at fixed [Py] of 0.42 of μL cm$^{-2}$. Fe$^{3+}$ : Py ratio. A) 0.07 B) 0.33 C) 0.72 and D) 1.5. All scale bars represent 1 μm.*
Morphology diagram

The different PPy surface structures obtained for different amounts of pyrrole and Py: Fe ratios as determined from SEM micrographs can be divided in four classes: 1) PPy fibrils; 2) thin coating on the PS particles; 3) interconnecting PPy matrix with triangular dimples at the interstitial spaces; 4) interconnecting PPy matrix with triangular protrusions. These four classes are shown in a two-dimensional morphology diagram in Figure 10.

**Figure 10:** PPy surface morphology diagram. 0) –, no PPy visible; 1) ◇, PPy fibrils; 2) □, PS particles coated with a PPy layer; 3) O, interconnecting PPy matrix with triangular dimples; 4) Δ, interconnecting PPy matrix with triangular protrusions. Lines are added as guide to the eye.

PPy matrix growth

Close inspection of the SEM micrographs of morphology class 4 (see for example Figure 2A and 2B) shows that the PPy top-surface (facing air during polymerization), is smooth. In most reports in the literature, PPy layers show a granular morphology. In addition we note that the PPy surface is not flat in between the particles, but rather,
follows a positive slope radiating from the particle (see for example Figure 9C). The SEM image in Figure 2C shows the bottom-surface of the PPy-iccm. The PPy coating around the particles follows the outline of the particles, and the surface is rough.

To study how these features arise during interfacial polymerization, colloidal monolayers were swollen with 2.9 µL pyrrole cm⁻² and investigated at different incubation times after adding the ferric chloride. The molar ratio of Fe³⁺: Py was kept constant at 2.3. The first sample was taken immediately after ferric chloride addition (Scheme 2A)

\[ \text{Scheme 2: Growth of PPy in time (not to scale) and SEM micrographs. SEM micrographs taken at A) 1 minute; B) 7 minutes; C) 44 minutes; and D) 4h 19 minutes after Fe³⁺ addition. The [Py] is 2.9µL cm⁻² and Fe³⁺: Py ratio is 2.3 mol/mol. All scale bars represent 1 µm.} \]

and shows that a thin, rough PPy layer on the outside of the immersed parts of the particles is directly synthesized. The layer around the particle thickens after longer incubation times (Scheme 2B), resulting in an interconnecting PPy matrix. The water present in the interstitial space of the particles at the top-surface, may thereby be cut off from the bulk water below. The PPy keeps growing at the rough water/PPy interface
and while doing so, it is pushed upwards, enabling the PPy to grow higher than the original water level (Scheme 2C). The smooth layer radiating from the particle is believed to originate from the air/water/PPy contact line, which slowly moves upward. Protrusions may arise due to polymer formation in the small remaining water droplet sitting at the interstitial sites (Scheme 2D).

Figure 11: Gradient of PPy surface structures within one sample with 0.98 µL Py cm\(^{-2}\) and a Fe\(^{3+}\): Py ratio of 2.6. A) Sample shortly after Fe\(^{3+}\) addition. Pyrrole and Fe\(^{3+}\) were added on the left hand side. B) Sample after 24h. C, D) Surface structures at different locations, as indicated in A) and B). All scale bars represent 1 µm.

The variation in surface structure with time is used to produce a PPy-ccm with a surface structure gradient. To this end, a colloidal crystal monolayer was prepared in a Petri dish with a diameter of 13.6 cm and 0.98 µL pyrrole cm\(^{-2}\) was added to the left side. Fe\(^{3+}\) in a molar ratio Fe\(^{3+}\): Py of 2.6, was added after 15 minutes at the same location as where the pyrrole was added. Figure 11A shows a picture taken almost immediately after Fe\(^{3+}\) addition. The Fe\(^{3+}\) solution spread quickly: the subphase was completely yellow. However, only on the left side rapid polymerization of
the pyrrole was observed, as evidenced by the black colour. The picture in Figure 11B shows the sample after 24 hours, and it can be seen that the complete Petri dish is covered with a PPy-ccm.

Four samples were scooped from left to right using silicon wafers of around 1 cm². These PPy surface structures are shown in Figure 11C-F. The surface structure of the sample taken nearest to the location where pyrrole was added, location C, shows triangular protrusions (morphology class 4), while triangular dimples (morphology class 3) are found that grow in size as the sample is taken farther to the right.

4.4.3 Wetting of PPy

Wetting of flat and structured PPy

The contact angles, \( \theta \), of water on PPy-iccms with different morphologies (Class 2–4 from morphology diagram) were measured and were all found to be very similar: \( 109.5 \pm 0.7^\circ \) for PPy-iccm with triangular protrusions (Class 4), \( 109.2 \pm 1.0^\circ \) for PPy-iccm with triangular dimples (Class 3) and \( 111.0 \pm 0.5^\circ \) for PPy-iccm with coated particles (Class 2) (see Figure 12). This similarity can be attributed to the similar overhang structure, as described in the next section, for the various morphologies. The \( \theta \) of the bottom-surface of the sample was \( 62.9 \pm 1.6^\circ \). This shows that the film is hydrophobic on the top-surface and hydrophilic on the bottom-surface.

As a reference, \( \theta \) of water on PPy grafted on a silicon wafer was measured. The average \( \theta \) for this reference PPy is \( 21.1 \pm 1.9^\circ \) (Figure 12A). Unstructured PPy has been previously found to have \( \theta \) between \( 20^\circ \) and \( 55^\circ \). As our surface has micrometre-sized roughness, as is shown in the SEM image in Figure 10, the droplet is probably in a Wenzel state, and \( \theta \) is therefore lower than \( \theta \) of water on a perfectly flat PPy substrate.

Additionally, the excess C observed in the XPS measurements suggest that residual PS is left after etch removal of the template particles. As polymers tend to coat surfaces with a thin layer even at very low concentrations, and because PS has a higher \( \theta \) with water of \( 91^\circ \), the effect of this residue layer on the \( \theta \) of unstructured PPy was
measured. PS particles were brought into contact with unstructured PPy layer, then removed by etching in a manner similar to that used to prepare the PPy-iccms. The residue changed $\theta$ of the soaked PPy surface to $82.7 \pm 0.7^\circ$. We attribute this change in $\theta$ mainly to a change in interfacial tension of the solid-air interface, although polymer adsorption also subtly changes the roughness of the surface.

![Contact angles $\theta$ of a droplet of water on PPy. A) reference sample (PPy grafted on a silicon wafer), B) reference sample contaminated with PS, C) bottom of PPy-iccm, D-F) PPy-iccms. Error bars are smaller than the symbols. Scale bars represent 10$\mu$m for A-B and 1 $\mu$m for C-F.](image)

**Figure 12:** Contact angles $\theta$ of a droplet of water on PPy. A) reference sample (PPy grafted on a silicon wafer), B) reference sample contaminated with PS, C) bottom of PPy-iccm, D-F) PPy-iccms. Error bars are smaller than the symbols. Scale bars represent 10$\mu$m for A-B and 1 $\mu$m for C-F.

**From hydrophilic to hydrophobic**

The hydrophobic behaviour of the PPy-iccms could be linked to the presence of the overhang structure.$^{34, 73}$ The angle of overhang was determined by analysing SEM micrographs of the different morphologies and was calculated to be $37^\circ$ for all morphologies (see SI 2 for calculation details). All morphologies have the same angle of overhang, because the particles were immersed in the water to the same extent
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during polymerization. The immersion depth is mainly determined by the subphase, as the dissociation of –COOH groups on the surface of the particles and hence its hydrophilicity depends on the pH and ionic strength of the subphase. This also explains the fact that the contact angles for the three different morphologies of PPy-iccm are very similar.

The angle of overhang is well below $\theta$ of water on the PS-contaminated reference of $82.7 \pm 0.7^\circ$, and hence it is possible that capillary forces act as barrier preventing water to enter the cavity (see Figure 1).

To compare the obtained results with theory, we use the Cassie-Baxter equation, where the water cannot enter the cavities (Equation 2), to calculate $\theta$ of water on our structures. The fraction of solid, $\varphi_s$, can be calculated in two ways: either by adding the area of all holes in the SEM image, and dividing this by the total area of the SEM image, or by assuming hexagonal packing of the particles and using the radius of the particle, $R_p$ and the radius of the opening of the cavities, $R_h$ (see SI 2 for further details). The first method underestimates $\varphi_s$ due to the neglect of holes at the edge of the image and non-spherical holes, while the second method overestimates $\varphi_s$ due to the assumption that the surface is covered with one perfect crystal lattice without defects or grain boundaries. The effective $\varphi_s$ is therefore taken as the average of these two measurements. For our samples, the first method yields a $\varphi_s$ of 0.67, and the second method yields a $\varphi_s$ of 0.65. Therefore, an effective $\varphi_s$ of 0.66 is used for further calculations.

Using $\varphi_s = 0.66$ and $\theta_{reference} = 82.7$, we find a $\theta$ of $105^\circ$. As the $\theta$ is in good agreement with the observed contact angles on the different morphologies, which are all similar, the increase in $\theta$ to hydrophobic behaviour may be attributed to air entrapment in the cavities.

4.5 Conclusion

In summary, we introduced a scalable fabrication method to create PPy films with overhang structures yielding hydrophobic wetting behaviour on a hydrophilic material. Using carboxylated PS particles at the air/water interface as template enables control over the crystallinity by choosing the pH of the subphase. By varying the monomer and
oxidant concentrations, different nanopatterned surface structures can be fabricated under mild conditions. Using this approach, synthesis of surface gradients is achieved by controlling the time between adding the monomer and the oxidant. The final inverse crystalline colloidal monolayer is obtained by soaking the PPy film in THF. The $\theta$ of water on top of the PPy-iccm is 109.5° which indicates a switch from hydrophilic behaviour for the unstructured material to hydrophobic behaviour upon structuring. Comparing our experimentally determined $\theta$ with the prediction of the Cassie-Baxter model, we found that the increase in $\theta$ may be explained by air entrapment in the cavities. The presence of an overhang may prevent water from entering the cavities.

We have demonstrated that colloidal templating in combination with interfacial polymerization provides a promising approach to design surfaces with overhang structures. This approach is quite general and may be applied to manufacture different materials where controlled wetting behaviour is required.

References


Supporting information

SI 1: XPS core level high resolution scans of PPy-iccm

The C 1s core level can be fit with four C 1s peaks for both the top-surface (facing air during polymerization) and the bottom-surface (facing water during polymerization): (1) C$_{\text{beta}}$ (~283.6 eV), (2) C$_{\text{alpha}}$ (~284.4 eV), (3) C-OH, C=N and C-N$^-$ (~285.4 eV), and (4) C=O (~287.1 eV for top-side and ~287.6 eV for bottom-side). The C=O peak of the bottom-side was shifted +0.5 eV compared to the top-side, which suggests the presence of an additional chemical charged species on the bottom-side (e.g. C-N$^-$).

Figure S1: XPS core level spectra for C 1s on the top and bottom surface of the PPy-iccm films, with peak deconvolution

Figure S2: XPS core level spectra for N 1s on the top and bottom surface of the PPy-iccm films, with peak deconvolution
The N 1s signal of both top- and bottom-surfaces can be fit with three peaks that can be assigned to pyrrole: (1) N=C (~398.2 eV), (2) N-H in pyrrole (~399.6 eV), and (3) polaron charge carrier species -N\textsuperscript{+} (~400.5 eV).\textsuperscript{74} In the N 1s scan of the bottom-surface, an extra peak is observed at ~ 401.4 eV compared to the narrow scan of N 1s at the top-surface. This peak is assigned to nitrogen in a bipolaron charged carrier species \textsuperscript{=}N\textsuperscript{+} group. The N=C group arises from deprotonation of the nitrogen in the PPy ring. The N\textsuperscript{+} peak is from oxidized nitrogen in doped pyrrole. The contribution of oxidized/charged N (-N\textsuperscript{+} and/or \textsuperscript{=}N\textsuperscript{+}) to the N 1s peak is comparable to the overall PPy doping level. This suggests that the doping level of the bottom-surface is higher than the top-surface (1.1 : 8.9 vs 0.8 : 9.2 respectively).\textsuperscript{45} The bottom-surface has, in addition to these three peaks, a broad peak at lower binding energy ~396.5 eV which is assigned to a strong Fe-N bond.\textsuperscript{75-77}

![Figure S3: XPS core level spectra for O 1s on the top and bottom surface of the PPy-iccm films, with peak deconvolution](image.png)

Two O 1s peaks are found both at the top- and bottom-surface at ~531.3 eV and ~532.8 eV. These peaks can be assigned to oxygen from C=O and C-OH, respectively.\textsuperscript{61} On the bottom surface, an extra peak is observed on the low binding energy side. This extra peak is assigned to Fe-O at ~529.8 eV\textsuperscript{78} and makes up 21% of the oxygen signal for the bottom-surface.
Figure S4: XPS core level spectra for Fe 2p on the top and bottom surface of the PPY-iccm films.

On the top-surface, no traces of Fe 2p are found. On the bottom-surface, a cluster of Fe 2p peaks can be found, indicating the presence of Fe. Part of the Fe 2p signal can be explained by iron chloride dopant species (FeCl$_4^-$, FeCl$_3$)$_{57}$ and a part can be explained by the presence of strong Fe-N or Fe-O bonds.
SI 2: Immersion depth and $\theta_{\text{overhang}}$ determination

To obtain the immersion depth and thereby $\theta_{\text{overhang}}$ of our structures, five SEM micrographs of different PPy-iccms with a magnification of 5000× were analyzed. The subphase was the same for all these samples. The radius of the opening of the cavities, $R_h$ (for definition: see Scheme S1) is obtained using the Analyze Particle function of ImageJ.

To exclude defects at grain boundaries of the crystal lattice, only openings with a circularity > 0.7 were selected. $R_h$ was calculated using the areas of each opening (which is the output of the program), and are listed in Table S1.
Table S1: Image analysis of SEM micrographs

<table>
<thead>
<tr>
<th>Py (µL cm⁻²)</th>
<th>Fe²⁺/Py (mol/mol)</th>
<th># holes</th>
<th>Radius opening, (R_h) ± standard deviation (nm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>5.05</td>
<td>2.33</td>
<td>432</td>
<td>366 ± 44</td>
</tr>
<tr>
<td>1.26</td>
<td>2.33</td>
<td>445</td>
<td>336 ± 26</td>
</tr>
<tr>
<td>1.26</td>
<td>0.33</td>
<td>422</td>
<td>322 ± 29</td>
</tr>
<tr>
<td>0.42</td>
<td>2.33</td>
<td>436</td>
<td>353 ± 27</td>
</tr>
<tr>
<td>0.42</td>
<td>0.65</td>
<td>438</td>
<td>352 ± 21</td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td></td>
<td><strong>2173</strong></td>
<td><strong>346 ± 42</strong></td>
</tr>
</tbody>
</table>

Since the spread of radii of openings within one image is larger than the spread between the five samples, the average radius over all openings is used for further calculations. This radius, \(R_h\), is 346 ± 42 nm.

The immersion depth \((\frac{R_p + R_i}{2R_p} \times 100)\) can be calculated using \(R_h\), \(R_p\) and Pythagoras’s theorem (see Scheme S1). The immersion depth dictates both the overhang angle, \(\theta_{\text{overhang}}\), and the fraction solid-liquid interface per particle under the droplet \(\varphi_s\) (see Equation 2). \(R_p\) is determined for a diluted sol of the particles in water using dynamic light scattering and is 575 nm. The immersion depth in our case is 90%. The angle of overhang can be calculated using \(\theta_{\text{overhang}} = \beta' = \beta\) (see Scheme S1), thus \(\sin(\theta_{\text{overhang}}) = \frac{R_h}{R_p}\). Using the average hole radius, \(R_h\), of 346 nm, \(\theta_{\text{overhang}}\) is calculated to be 37°. In this calculation, the increase in particle size due to swelling with the pyrrole monomers, is neglected. If swelling of the particle is taken into account, a higher value for \(R_p\) should be used, resulting in even lower values of \(\theta_{\text{overhang}}\).
5 Three-gradient regular solution model for simple liquids, wetting complex surface topologies

This chapter is based on:
S. Akerboom, M. Kamperman, F.A.M. Leermakers, Three-gradient regular solution model for simple liquids, wetting complex surface topologies (submitted)
5.1 Abstract

We use regular solution theory and implement a three-gradient model for a liquid-vapour system in contact with a complex surface topology to study the shape of a liquid drop in advancing and receding wetting scenarios. More specifically, we study droplets on an inverse opal: spherical cavities in a hexagonal pattern. In line with experimental data, we find that the surface may switch from hydrophilic (contact angle on a smooth surface \( \theta_r < 90^\circ \)) to hydrophobic (effective advancing contact angle \( \theta > 90^\circ \)). Both the Wenzel wetting state, that is cavities under the liquid are filled, as well as the Cassie-Baxter wetting state, that is air entrapment in the cavities under the liquid, were observed using our approach, without a discontinuity in the water front shape or in the water advancing contact angle \( \theta \). Therefore, air entrapment cannot be the main reason why the contact angle \( \theta \) for an advancing water front varies. Rather, the contact line is pinned and curved due to the surface structures, inducing curvature perpendicular to the plane in which the contact angle \( \theta \) is observed, and the contact line does not move in a continuous way, but via depinning transitions. The pinning is not limited to kinks in the surface with angles \( \theta_{\text{kink}} \) smaller than the angle \( \theta_r \). Even for \( \theta_{\text{kink}} > \theta_r \), contact line pinning is found. Therefore, the full 3D-structure of the inverse opal, rather than a simple parameter such as the wetting state or the \( \theta_{\text{kink}} \), determines the final observed contact angle. Our approach can easily be extended to include more molecular details.

5.2 Introduction

Wetting of surfaces is a key feature for many applications. The wetting properties of a surface, e.g. by water, depend on both the material and the surface topography. A famous example is the surface of a lotus leaf: although the material of the leaf is hydrophilic (contact angle on a smooth substrate \( \theta_r < 90^\circ \)), the structured surface is hydrophobic (apparent contact angle \( \theta > 90^\circ \)).\(^1\) Recently, different surface structures have been designed and fabricated from hydrophilic materials that show hydrophobic contact angles.\(^2-10\) An example is an inverse opal as schematically shown in Figure 1. Our group recently
reported an increase of $\theta$ from $\sim 80^\circ$ to $\sim 110^\circ$ for an inverse opal of polypyrrole.$^{10}$

Our study is targeted to obtain (close to) molecular level insight in the wetting features of such surfaces using a simplistic modelling toolbox based on regular solution theory. To understand the increase in $\theta$, which is observed at macroscopic length scales, details about the microscopic scale should be considered. For the simplest case in which a water droplet wets the structured surface on a microscopic level with its preferred angle $\theta_Y$ (see Figure 1B), the apparent contact angle, $\theta_W$ is given by$^{11}$

$$\cos \theta_W = r \cos \theta_Y$$

with $r$ the roughness of the surface (true contact area/projected area). This is called the Wenzel state, and it always magnifies the underlying wetting properties: $\theta$ decreases for hydrophilic materials and increases for hydrophobic materials. As the structured surfaces of interest, which are composed of a hydrophilic material, show an increase in $\theta$, this implies that the droplet in these systems cannot be in the Wenzel state, or that the assumption of this model that the parameter $r$ captures all features of a surface topography relevant for the final droplet shape, is too simplistic.

A possible explanation of the increase in $\theta$ on structured surfaces, is air entrapment$^{12-13}$; air acts as hydrophobic patch ($\theta_{\alpha}$ for the water/air interface is $180^\circ$), and these patches lower the average surface energy of the surface (see Figure 1C).$^{14-15}$ The resulting apparent contact angle for this so-called Cassie-Baxter state is then given by$^{16}$

$$\cos \theta_{CB} = \Phi_s \cos \theta_Y - (1 - \Phi_s)$$
with $\Phi_s$ the fraction under the droplet that is in contact with the solid and $(1 - \Phi_s)$ the fraction under the droplet in contact with air. This approach thus defines the solid as a new material with a different effective surface energy on a macroscopic scale, and does not entail details about the droplet shape close to the surface structures on a microscopic level.

Another explanation of the difference in $\theta$ for a structured and unstructured surface of the same material is contact line pinning.\textsuperscript{17-19} The three-phase contact line is hereby immobilized. Apart from chemical heterogeneities (which will not be discussed here), pinning occurs for a simple 1D system when the contact line encounters a kink in the surface, indicated with angle $\theta_{\text{kink}}$ in Figure 2. If $\theta_Y < \theta_{\text{kink}}$, the angle of the droplet with respect to the surface should exceed $\theta_Y$ in order to wet the surface after the kink (dotted area in Figure 2), and the droplet is thus pinned.

However, pinning cannot result in any arbitrary shape. The mean curvature $J$ of the liquid-vapour (L/V) interface of a droplet, is related to the pressure difference across the L/V interface, $\Delta P$, and the interfacial tension $\gamma$ according to the Young-Laplace equation:\textsuperscript{17}

$$\Delta P = 2J\gamma$$

(3)
\( \Delta P \) and \( \gamma \) can be considered constant for a droplet (neglecting small curvature corrections, the deformation due to gravity and the near surface contributions expressed in the disjoining pressure), thus \( J \) should also be constant.\(^{13}\) This implies that if the surface structure induces a curvature in one direction due to pinning, this should be compensated by the opposite curvature in the perpendicular direction. Hence, if structuring of a surface induces a noticeable curvature of the droplet parallel to the surface, this should lead to deformations of the droplet perpendicular to the surface. As the latter curvature is coupled to the apparent contact angle, which is commonly measured perpendicular to the surface, we notice contact angle variations.

The feature of hydrophilic surfaces showing hydrophobic contact angles is, for reasons mentioned above, often linked to re-entrant angles of the surface structures.\(^{20-21}\) An additional argument besides pinning, is that the liquid/air interfacial area should increase upon penetration of the liquid, creating more liquid/vapour interface.\(^{13}\) This may imply that air entrapment occurs, even for hydrophilic materials.\(^ {12, 22}\)

Common contact angle measurements typically do not have the correct resolution to see the local curvatures in both directions close to the surface. A better resolution can be achieved using AFM for non-volatile liquids,\(^ {23}\) but this method is not suitable for droplets with \( \theta > 90^\circ \). Recently droplet shapes have been studied using confocal microscopy with a resolution of hundreds of nanometres.\(^ {18, 24}\) Although this is an improvement, the length scale may still be too high to observe curvature in the three phase contact line. Since it is difficult to reach these small length scales experimentally in the lab, we may find inspirations from the computational arena and therefore we turn to ‘experiments in silico’. The present study is targeted to obtain insight in the wetting features of surfaces of hydrophilic materials that show hydrophobic contact angles and to differentiate between air entrapment and contact line pinning using a modelling approach.

Using macroscopic approaches such as solving the Young-Laplace equation,\(^ {25-26}\) minimizing the availability,\(^ {27}\) or using geometry and energy\(^ {12}\) to find the droplet shape do not take molecular details into account, and often require the contact angle as input parameter.
Furthermore, air entrapment and coalescence cannot be obtained by solving the Young-Laplace equation, and surfaces with re-entrant curvatures give impossible solutions. Phase field methods, molecular dynamics (MD), and mesoscopic lattice-Boltzmann (LB) models are a viable option for this problem, but are challenging because wetting on complex structures involves multiple length scales and the time needed to converge to a solution can be long.

In this paper we focus on the very well-known regular solution theory, which is frequently used throughout the field of physical chemistry, but not so often applied for studying wetting on complex surface topologies in 3 dimensions. Our models can be solved using a surprisingly simple algorithm (see Appendix) on a desktop PC in a few minutes CPU time. However, similarly to some of the theoretical approaches mentioned above, there are limitations with respect to the size of the systems that realistically can be considered, albeit that these limitations can easily be lifted with a factor of 10 when the equations are solved using modern supercomputer facilities (which we here did not do). Here we focus on equilibrium and metastable states, which allows us to consider both advancing as well as receding contact angles. Even though the regular solution model is very well known, we will start by giving some backgrounds and highlights of the regular solution model. This gives us an opportunity to fix some of our parameters in the system. We then present the model and study the wetting of inverse opal structures.

5.3 Experimental

5.3.1 Regular solution theory

The start is a lattice model wherein the sites with linear length \( b \) are arranged in a cubic lattice geometry, that is, each cell has \( Z = 6 \) neighbours. Let there be \( M \) sites in the system and thus the volume is given by \( V = Mb^3 \). Sites are either filled by a solvent molecule, or the site is empty. The latter sites are said to be vacant and the number of vacant sites is \( N_V \). The remaining sites are filled by solvent and hence there are \( N = M - N_V \) sites filled. It is assumed that the solvent molecules only interact with each other when they occupy neighbouring
sites and in this setting it is common to introduce the dimensionless Flory-Huggins interaction parameter, which is an Archimedes-like parameter needed for unlike-contacts:

\[
\chi = \frac{Z}{2k_B T} (2U_{LV} - U_{LL} - U_{VV})
\]

A positive value means that LL contacts and VV ‘contacts’ are favoured over LV ones and this implies a tendency towards demixing. When we assume random mixing (mean-field approximation) we can evaluate the mixing interaction energy in the system by

\[
U_{\text{mix}} = N \chi \varphi_v
\]

where we ignored boundary effects and \( \varphi_v = N_v / M \) is the volume fraction of vacancies. The entropy of mixing can be evaluated when we assume once more that the sites are randomly filled by solvent. The total number of ways to arrange the fluid and the vacancies is given by \( \Omega = \frac{M!}{N!} \) and the mixing entropy is found by

\[
S_{\text{mix}} = -k_B \ln \Omega = -k_B (N \ln \varphi + N_v \ln \varphi_v)
\]

with \( \varphi = N/M \) and \( k_B \) the Boltzmann constant. The free energy of mixing is given by

\[
F_{\text{mix}} = U_{\text{mix}} - TS_{\text{mix}}
\]

Introducing the dimensionless free energy density

\[
f = F_{\text{mix}}/(M b^3 k_B T)
\]

wherein the thermal energy \( k_B T \) and the volume \( V \) are used to reduce the free energy, we obtain the well-known regular solution free energy density:

\[
f = \varphi \ln \varphi + \varphi_V \ln \varphi_V + \chi \varphi \varphi_V
\]

with \( \varphi + \varphi_V = 1 \). The first two terms are negative and promote the mixing of the solvent and vapour. The last term drives the demixing. The critical conditions are found by setting the second and third derivatives of the free energy density Equation 5 with respect to the volume fraction of liquid to zero. From such analysis it is found that there is a solubility gap as soon as \( \chi > \chi^{cr} = 2 \). By symmetry the critical density \( \varphi^{cr} = 1/2 \).

### 5.3.2 Liquid/vapour interface

Very famous is the extension of the regular solution theory to the description of the L/V interface. In the footsteps of Van der Waals\(^{38}\) we like to find the density profile across a L/V interface \( \varphi(z) \). Here \( z \) is a (lattice) coordinate running perpendicular to the interface. We set \( z = 0 \) at the interface and consider a lattice model with layer numbers \( z = -M, -(M-1), \ldots, -1, 0, 1, \ldots, M-1, M \). The boundary layers \( -M \) and \( M \) are taken
large enough so that the interface is not perturbed. We generalise Equation 5 and define a dimensionless free energy $F$ as follows

$$F = \sum_{M}^{M} \varphi(z) \ln \varphi(z) + \varphi_V(z) \ln \varphi_V(z) + \chi \varphi(z) \langle \varphi_V(z) \rangle$$  \hspace{1cm} (6)

where it is understood that the mean-field approximation is now applied along lattice layers. The angular brackets in the last term indicate that in the interaction term ‘curvature’ information is included - needed to evaluate the number of liquid-vacancy contacts in the presence of density gradients. In continuous language, we need to introduce

$$\langle \varphi \rangle = \varphi + \frac{1}{6} \Delta \varphi$$  \hspace{1cm} (7)

in the interaction term, which on a lattice and in a one-gradient functional of Equation 6, translates to a local averaging operation:

$$\langle \varphi(z) \rangle = \frac{1}{6} (\varphi(z - 1) + 4\varphi(z) + \varphi(z + 1))$$  \hspace{1cm} (8)

The target is to find the best volume fraction profiles which optimise the free energy $F$. In the Appendix we detail how such a solution can routinely be found numerically using the self-consistent field protocol. Results are summarised in Figure 3.

Figure 3: A) Examples of volume fraction profiles across a liquid/vapour interface found numerically by exact minimisation of Equation 6, with the interaction parameter $\chi = 2.05$, 2.2 as indicated. B) Width of the interface ($W$), density difference between the two phases ($\Delta \varphi$) and dimensionless surface tension ($\gamma$) as function of $\Delta \chi = \chi - 2$ in double logarithmic coordinates.

Two volume fraction profiles are presented in Figure 3A, which were found numerically by minimizing Equation 6, for two values of $\chi$, $\chi$
not far but above $\chi^{ct} = 2$. We have set the liquid phase at negative values of $z$, whereas the vapour is at positive $z$. The position of the interface is set at $z = 0$ found by searching for $\phi = 0.5$ (in three-gradient results we will find the interface by the same criterion). The profiles follow very accurately the tanh dependence (see Figure 3A for numerical results). We note that for $\chi = 2.2$ used below, this results deviate from the analytical predictions. Far from the interface the volume fraction profile levels off to the binodal values. The difference in volume fractions between the binodal values, here defined by $\Delta \phi = \phi(-M) - \phi(M)$, is indicated in Figure 3A. The width $W$ of the interface is numerically found by intersection of the tangent line at $z = 0$ with the binodal value. We can evaluate the surface tension $\gamma$, which is given in units $k_B T/b^2$, numerically as discussed in the Appendix.

In Figure 3B we prove that near the critical point (i) the surface tension, (ii) the width of the interface and (iii) $\Delta \phi$ as found by our numerical solution accurately obey scaling relations with respect to the difference to the critical point $\Delta \chi = \chi - 2$.

Interestingly, near the critical point there is an analytical route to optimise the free energy $F$. In short, near the critical point the density of the liquid (and thus also for the vacancies) is never far from the critical value. Introducing an order parameter $\phi = \phi - 0.5$, we can write $F$ as a function of the order parameter and then Taylor series expand the logarithms up to fourth order in the order parameter. As a result we obtain a Landau free energy in terms of the order parameter. An Euler Lagrange optimisation then leads to the famous tanh profile already known by Van der Waals. We do not go into these details and mention that fully in line with the numerical results presented in Figure 3B the scaling exponents as found by this analytical route are in line with the numerical results: for the surface tension the value is $-3/2$, it is $1/2$ for the width of the interface, while the difference in densities of the two phases vanishes with an exponent $-1/2$.

Our aim is to present results which are relevant for the water/vapour system. Of course a symmetric lattice model falls short in this respect, because it assumes that as much water will be in the vapour phase as free volume will be in the water phase. The symmetry can only be broken in a more elaborate model wherein water is more
realistically represented. We mention that such an approach is (at least in principle) possible, but here we choose not to go into such complications. We know that at ambient temperatures the water/vapour system is not near critical. Indeed it is very far from critical. Hence it is necessary to choose a sufficiently high \( \chi \) value. In a lattice model it is advised to keep the width of the interface larger than the size of a lattice site (i.e. \( W > b \)). In the other limit one experiences many so-called lattice artefacts, which may frustrate the analysis of the shape of a droplet on top of a structurally complex surface. For this reason we choose here \( \chi = 2.2 \) for the liquid/vapour interactions, unless stated otherwise. For this value the width of the interface \( W \) is approximately 8 in units \( b \). As the width of an air with water interface is just a few \( \text{Å} \) we may infer that when the water/vapour system is the target of our calculations, the corresponding value of \( b \) is a value less than an \( \text{Å} \). Again we accept deviations from the air/water system and advice to consider the value of \( b \) to be in the order of a few \( \text{Å} \) (say 0.2 nm). The fraction of liquid in the liquid-rich phase for \( \chi = 2.2 \) is \( \sim 0.7515 \), and the fraction liquid in the vapour-rich bulk phase has the binodal value \( \phi^* = 0.2485 \). Again these values differ dramatically from our experimental system of water in air at 100% relative humidity. Finally, the interfacial tension in this system is given by \( \gamma = 0.03326 \) in units \( k_B T / b^2 \), which translates with \( b = 0.2 \) nm to 3.422 mN/m. This value is less than the known value for water. All these differences with respect to our experimental system are accepted as we search only for scenarios. For ease of reference we may call the liquid-rich phase ‘water’ and the vacancy-rich phase ‘vapour’.

We stress that even though our regular solution model is far from the experimental water/vapour system, the trends can still be qualitatively compared to the experimental case. A quantitative comparison to our experiments is beyond the scope of this paper.

5.3.3 Droplet on an unstructured solid

Still using the one-gradient approach, it is possible to study wetting phenomena using the regular solution model. We need remarkably few modifications in the system. The only issue is that we need to introduce a substrate. To do so, we first specify the lattice
Model of simple liquid on complex geometry

coordinates $z = 0, 1, 2, \ldots, M$, and introduce a surface component $S$ as a boundary condition, that is, we choose $\phi_S(0) = 1$ and $\phi_S(z) = 0$ for all $z > 0$. The liquid and the vapour are allowed to be in the half-space $z > 0$. We have in principle two new interaction parameters $\chi_{LS}$ and $\chi_{VS}$ by introducing a ‘third’ component.

Without losing generality we can set $\chi_{VS} = 0$, and keep $\chi_S = \chi_{LS}$ to specify the preferential adsorption of the liquid component on the surface. A negative value means that the solvent has a preference to sit next to the surface over the vapour. At $\chi_S = 0$ we expect a contact angle of $90^\circ$. Hydrophobic surfaces are modelled when $\chi_S > 0$. We will mostly restrict ourselves to hydrophilic surfaces, thus to $\chi_S < 0$.

In the case of a L/V system next to a surface the regular solution free energy assumes the form

$$ F = \sum_{z=1}^{M} \phi(z) \ln \phi(z) + \phi_V(z) \ln \phi_V(z) + \chi \phi(z) \langle \phi_V(z) \rangle + \chi_S \phi(z) \langle \phi_S(z) \rangle $$

(9)

where it is understood that the last term is only non-zero when $z = 1$, where it assumes the value $\chi_S \phi(1) \langle \phi_S(1) \rangle = \chi_S \phi(1)/6$. Again Equation 9 is easily optimised using a numerical SCF scheme (see Appendix).

There are several routes to study wetting. Our preference goes to study so-called adsorption isotherms. Of course we need a solubility gap and thus $\chi > 2$ (we use a value 2.2 throughout). Next, we consider a specific value of $\chi_S < 0$ and specify a given amount of solvent $\Gamma = N = \sum_{z=1}^{M} \phi(z)$ in the system. Again, we numerically optimise the free energy, which is equivalent in solving the self-consistent field equations (see Appendix) and obtain the optimised density profile $\phi(z)$. Far from the surface the density profile converges to the bulk value $\phi^b$. The adsorbed amount (surface excess) of liquid is found by:

$$ \Gamma^\sigma = \sum_{z=1}^{M} (\phi(z) - \phi^b) $$

(10)

We focus on how the adsorption isotherms, $\Gamma^\sigma(\phi^b)$ behave near the bulk binodal $\phi^\#$. When upon the approach of the bulk binodal the adsorbed amount simply increases and diverges at the binodal value, we have a complete wetting situation and the contact angle is zero. Alternatively, the isotherm crosses the binodal at a finite value of the adsorbed amount, that is, for an amount $\Gamma^\# = \Gamma^\sigma(\phi^\#) < \infty$. We refer to this first
crossing as the ‘microscopically thin film’ adsorbed at the surface $S$. By means of a Van der Waals loop the isotherm then returns to the binodal and approaches the infinite adsorbed amount upon the final approach towards the bulk binodal. We refer to this adsorbed amount as the ‘macroscopically thick film’ on the surface. Such situation is typical for partial wetting states, where the macroscopically thick film represents the situation under a drop, and the thin film is found far away from the drop where a gas-like film resides on the substrate. As for each solution along the isotherm we have the surface tension accurately available from the SCF solution, we can find the contact angle from Young’s law:

$$\cos \theta_Y - 1 = \frac{\gamma_{SV} - (\gamma_{SL} + \gamma_{LV})}{\gamma_{LV}} = \frac{\gamma_{\text{thin}} - \gamma_{\text{thick}}}{\gamma_{LV}}$$

(11)

where all interfacial tensions are computed for systems in which the chemical potential is that corresponding to the bulk binodal. The $\gamma_{\text{thin}}$ is found from the first crossing of the binodal, and $\gamma_{\text{thick}}$ is the surface free energy in the system when there is a very thick adsorbed layer at the surface. Hence, we can obtain contact angle information without explicitly generating droplets. In passing we mention that for not too small droplets the contact angle as obtained by a three-gradient analysis (as used below) gives identical contact angles as the ones that follow from Equation 11, which used information from one-gradient regular solution models.

![Figure 4: Contact angle of liquid on flat solid, $\theta_Y$ as function of the interaction parameter of the liquid with the solid, $\chi_S$, for three different values of the interaction parameter of the liquid with the vapour, $\chi$.](image)

122
The contact angle of a liquid droplet $\theta_i$ is calculated for various adsorption strengths $\chi_S$ and for different strengths of interaction between liquid and vapour $\chi$ (see Figure 4). The more negative $\chi_S$, the more favourable the interaction between S and L, and the more the droplet spreads, resulting in smaller $\theta_i$. Eventually, the liquid prefers to wet the solid completely, i.e. $\theta_i = 0^\circ$. At $\chi$ near the critical value of 2, the droplet enters the complete wetting regime ($\theta_i = 0^\circ$) already for very low values of the surface affinity $\chi_S$. For strong segregations the interfacial energies increase and we need larger adsorption energies to enforce wetting.

In this paper we aim to mimic a polypyrrole surface for which the water contact angle of a smooth surface is about $\theta_i = 80^\circ$. As we already selected $\chi = 2.2$, we will be in the correct contact angle regime when we set the adsorption energies around $\chi_S = -0.2$. Below we will always mention the strength of adsorption.

### 5.3.4 Liquid condensation in parallel slit

The inverse opal surface structure consists of close to spherical cavities. In such structures we should anticipate the occurrence of capillary condensation or alternatively, capillary drying. For this reason we use the regular solution model to study classical capillary condensation. To this end we consider a system that contains two surfaces. One at $z = 0$ and another one at $z = D + 1$. Hence $\varphi_S(z) = 0$ for $z = 1, 2, \ldots, D$ and unity elsewhere. Now our regular solution free energy is given by

$$ F = \sum_{z=1}^{D} \varphi(z) \ln \varphi(z) + \varphi_V(z) \ln \varphi_V(z) + \chi \varphi(z)\langle \varphi_V(z) \rangle + \chi_S \varphi(z)\langle \varphi_S(z) \rangle $$

In this case the last term automatically accounts for the interactions with the surfaces, as it is nonzero for $z = 1$ and $z = D$. More specifically, $F$ has two surface contributions $\chi_S \varphi(1)/6 + \chi_S \varphi(D)/6$.

As there are two interfaces, we anticipate the adsorption of the liquid onto both surfaces simultaneously. We want to record the adsorbed amount in the slit as a function of the (dimensionless)
chemical potential ($\mu = \ln \phi^b$) of the liquid component. One complication arises because in layers $z = 1, \cdots, D$, the bulk volume fraction may not be reached and we cannot simply 'pick up' this value from the profiles. As explained in the Appendix, the SCF protocol gives (as an output) the volume fraction of a reference system which is in equilibrium with the molecules in the slit. This reference value is used to compute the isotherms.

![Figure 5: A) Adsorption amount $\Gamma^a$ of the liquid component as a function of the volume fraction of liquid in the vapour $\phi^v$ in lin-ln coordinates (x-axis is chemical potential), in a slit with surfaces that are a distance $D = 10$ apart and have an adsorption energy $\chi_S = -0.2$. The metastable branches are dashed. The unstable part is dotted. The chemical potential $\mu^b$ is indicated as the grey vertical line. The solid vertical line is placed at the chemical potential where a step in the isotherm takes place (local binodal). This step is found by the Maxwell construction, that is by the equal area argument (the two shaded regions have the same area). The difference in chemical potential $\Delta \mu$ between the place of the step and the binodal, is indicated. The vertical dotted lines are placed at chemical potentials corresponding to the spinodal points. B) The chemical potential where the step in the isotherm (compared to value of the bulk binodal) $\Delta \mu$ takes place (at equilibrium) as function of $\chi_S$ for slit distances $D = 10, 20,$ and $40$ as indicated. The solvent-vacancy interaction is set to $\chi = 2.2$. The label A on the curve for $D = 10$ corresponds to the condition used in panel A.]

In Figure 5A we present an example for a slit distance $D = 10$ (in lattice units) and our default interaction parameters $\chi = 2.2$ and $\chi_S = -0.3$. Recall that in these conditions the surfaces are preferentially solvated by the liquid, and $\theta$ is $68^\circ$. In such situations there is a large Van der Waals loop in the adsorption isotherm (cf. Figure 5A). The Maxwell construction can be used to find where, in equilibrium, the step in the isotherm should take place. In line with the hydrophilic character of the surfaces we find the step in the sub-saturated region. In Figure 5A
the grey vertical line represents the bulk binodal value. The step takes place at a lower chemical potential (local binodal) than that corresponding to the bulk binodal. We define $\Delta \mu$ as the difference in $\ln \phi^b$ between the local and bulk binodals as indicated in Figure 5A.

It is important to consider the isotherm in slightly more detail. After the jump in the isotherm the adsorbed amount only marginally increases further: the isotherm continues into the supersaturated region and as the system increases the bulk volume fraction, in the limit of very high concentrations the excess should go down again to become zero in the limit of $\phi^b$ to 1.

The most interesting feature of the isotherm the presence of a loop. Associated to the loop there are two spinodal points. These spinodal points are located at the turning points of the isotherm. There are two regions of metastability, namely between the local binodal and the first turning point. This spinodal point is found in supersaturated conditions. The other metastable region is found between the turning point in the sub-saturated region and the local binodal in the top region of the isotherm. In the isotherm the metastable branches are indicated by dashed line parts. When in the absence of strong fluctuations the bulk volume fraction is increased, the slit may not necessarily change its contents at the local binodal, but instead remains dry up to -in the extreme case- the spinodal point is reached, and the slit is filled with liquid following the dashed line. Inversely, when the slit is wet, and the bulk concentration is reduced, the drying does not necessarily take place at the local binodal, but enter the other metastable branch. Again the drying must take place before or at the lower spinodal point (following the other dashed line). Hence in dynamical situations a hysteresis loop may be followed where the steps at the spinodal are indicated by the vertical dotted lines. The spinodal points have important roles in the advancing or receding contact line calculations (see below). Even though the Van der Waals loop in the isotherm is due to the mean-field approximation, it is found that in real life experiments the system also may be trapped in metastable states very much alike those found in the mean-field model.

In Figure 5B we report that the difference between the local and the bulk binodal in confined spaces is a function of the affinity of the
solvent for the substrate. When $\chi_s$ is more negative the $\Delta \mu$ increases to more negative values. Indeed when $\chi_s > 0$, that is for hydrophobic surfaces, the local binodal occurs at supersaturated solutions. With increasing $D$ the local binodal shifts towards the bulk binodal.

**5.3.5 Curved L/V interfaces; Kelvin & Laplace**

Macroscopic droplets (with negligible curvature) cannot be generated using our method. As the system size is limited, our drops have L/V interfaces which are typically strongly curved. The thermodynamics of curved interfaces is well understood, but there are several complications. One of the issues is that the location of the interface is somewhat arbitrary. On top of this the interfacial tension in curved interfaces cannot uniquely be computed. It depends on the notion of the position of the interface. There exists a choice of the position of the interface, the so-called surface of tension, for which a small notional change of the radius does not influence the value of the surface tension. For this special case the Laplace equation simplifies to Equation 3, and the value of the interfacial tension does not deviate much from the planar value.

From the Laplace equation we know that in droplets with curved L/V interfaces there is a Laplace pressure. As a consequence the chemical potential of the liquid in a drop is at a higher chemical potential compared to systems with planar interfaces. The increased chemical potential is reflected in the oversaturation of water in the vapour phase; a phenomenon named after Kelvin. With oversaturation of the system, which necessarily occurs in our calculations due to the finite size of our droplets, one will invariably get closer to the spinodal point of the capillary condensation process. Hence, oversaturation may trigger the filling of confined regions by the liquid. Small droplets cause a stronger oversaturation than larger droplets and the presence of small droplets may result in a spontaneous filling of the voids by capillary condensation when this may not yet occur for larger drops.

The radius specified by the surface of tension $R_{SOT}$ coincides with the visual inspection of where the interface is for many systems. Below we therefore do not exactly determine the exact $R_{SOT}$ and use the Ansatz
that the interface position is where the solvent volume fraction hits the value $\varphi = 0.5$.

### 5.3.6 Three-gradient regular solution model

Let us next extend the regular solution theory to model liquid drops at a complex surface topology. We consider a three-gradient coordinate system $\mathbf{r} = (x, y, z)$ with $x = 1, 2, \ldots, M_x$, $y = 1, 2, \ldots, M_y$ and $z = 1, 2, \ldots, M_z$. In contrast to the one-gradient systems where the surfaces were treated through the boundary conditions, in three gradient models it is more natural that the surface component $S$ will occupy lattice sites within the specified volume. Hence, we will specify all the lattice sites within the system: the volume fraction of $S$ is unity and the remainder of the lattice sites are filled by the liquid and vapour components in the usual way. The regular solution free energy is straightforwardly generalised and both interactions between $L$ and $V$ as well as with the surface component $S$ are accounted for:

$$F = \sum_{x=1}^{M_x} \sum_{y=1}^{M_y} \sum_{z=1}^{M_z} \varphi(\mathbf{r}) \ln \varphi(\mathbf{r}) + \varphi_V(\mathbf{r}) \ln \varphi_V(\mathbf{r}) + \chi \varphi(\mathbf{r}) \langle \varphi_S(\mathbf{r}) \rangle$$

wherein the angular brackets indicate that the free energy accounts for the ‘curvature’ information in three directions. The lattice implementation is simply:

$$\langle \varphi(\mathbf{r}) \rangle = \langle \varphi(x, y, z) \rangle = \frac{1}{6} (\varphi(x-1, y, z) + \varphi(x+1, y, z) + \varphi(x, y-1, z) + \varphi(x, y+1, z) + \varphi(x, y, z-1) + \varphi(x, y, z+1))$$

Mirror-like, no-gradient boundary conditions are implemented in boundary layers in the system. This is implemented by setting $\varphi(0, y, z) = \varphi(1, y, z)$, $\varphi(M_x + 1, y, z) = \varphi(M_x, y, z)$, and similarly for the other boundaries in $y$- and $z$-directions. Using these boundary conditions it is possible to consider a representative part of the surface, while keeping the computation times and system volumes to a minimum.
Table 1: Parameters that determine the structure of the inverse opal. Even and odd rows of cavities are displaced by half the distance between the cavities in a row, that is, by $s/2$. All quantities are given in lattice units, that is in values of $b$. Below also the cut-off ratio $c = h/d$ (to specify which part of the cavity is cut-off) and $\phi_S$ (the fraction of the top of the surface that is solid) is used.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$D$</td>
<td>diameter of a cavity (integer $&gt; 0$)</td>
</tr>
<tr>
<td>$S$</td>
<td>spacing between two cavities in a row (integer of order $d$)</td>
</tr>
<tr>
<td>$T$</td>
<td>distance between the two rows (integer of order $d$)</td>
</tr>
<tr>
<td>$N$</td>
<td>‘number’ of cavities in a row ($&gt; 0$) may also be non-integer</td>
</tr>
<tr>
<td>$m$</td>
<td>number of rows (integer $&gt; 1$)</td>
</tr>
<tr>
<td>$H$</td>
<td>cut-off height of the solid phase (integer $&gt; 0$)</td>
</tr>
</tbody>
</table>

5.3.7 Specifying the inverse opal

The regular solution free energy of Equation 13 still requires detailed information on the distribution of the solid material $S$ in the inverse opal. The idea is to consider a representative piece of a substrate that contains spherical cavities in a specified arrangement (i.e. crystalline ordering with close to hexagonal or square packing symmetries). The cut-off height controls the opening of the cavities as shown in the example of Figure 6. The parameters that control the surface topology are listed in Table 1. Below we will use the parameter $c = h/d$, which is a fraction at which the cavities was cut and $\phi_S$ is the fraction of the ‘top’ of the surface which is solid.

The parameters of Table 1 completely specify how many cavities are present in the computation volume. Let the cavities be numbered by $i = 1, 2, 3, \ldots, N_c$. In the example of Figure 6 there are 2 rows of 3.5 cavities and thus we need $i = 1, \ldots, 8$ cavity positions. The input parameters thus specify the coordinates of the cavities $\{\mathbf{r}_1, \mathbf{r}_2, \ldots, \mathbf{r}_i, \ldots, \mathbf{r}_N\}$. The cavities in the inverse opal are placed in rows along the $y$-direction, the direction perpendicular to the rows is the $x$-direction and the cavities
are positioned at the lowest z-values possible, that is for all cavities \( i \), \( r_{iz} = d/2 \) (cavity radius). The solid phase extends up to a height \( z = h \) where \( h \) is the cut-off height. The solution above the inverse opal starts at a height \( z > h \). The first and last row in the \( y \)-direction have their centres on the boundary that is at \( y = 1/2 \) and \( y = M_y+1/2 \), respectively. This implies that the system size in the \( y \)-direction is \( M_y = (m−1)t \), where \( t \) is the distance between two rows and \( m \) is the number of rows. The system size in the \( x \)-direction is given by \( M_x = ns \), with \( n \) the number of cavities in a row (when half the cavity is in the system the cavity counts by 0.5), and \( s \) the distance between cavities in a row. In the example of Figure 6, \( M_x = 3.5s \). The system size in the \( z \)-direction should exceed \( h \) sufficiently so that a sessile drop can be on the substrate. In the first row the first cavity is by default with its centre on \( x = 1/2 \), that
is, on the lower boundary. The first cavity in the second row is positioned at \( x = (s + 1)/2 \), etcetera.

All nonzero surface densities can now be computed. When for a coordinate \( \mathbf{r}' \) the distance to all of the coordinates \( \{\mathbf{r}_1, \mathbf{r}_2, \cdots, \mathbf{r}_i, \cdots, \mathbf{r}_N\} \) is larger than the radius of a cavity, i.e., \( d/2 \) and when the \( z \)-value is less or equal to \( h \), we set the \( \varphi_S(\mathbf{r}') = 1 \) and \( \varphi_S(\mathbf{r}') = 0 \) otherwise:

\[
\varphi_S(\mathbf{r}') = \begin{cases} 
1 & r_z \leq h \quad \text{&} \quad |\mathbf{r}_i - \mathbf{r}'| > \frac{d}{2} \quad \forall i \\
0 & \text{otherwise}
\end{cases}
\] (15)

This solid distribution is fixed during the free energy optimisation. Of course only the coordinates that are not taken up by the S can be filled with L or V. On the ‘top’ of the solid phase it is of interest to know the fraction of sites occupied by S. These are easily evaluated by

\[
\Phi_S = \frac{1}{M_x M_y} \sum_{x=1}^{M_x} \sum_{y=1}^{M_y} \varphi_S(x, y, h)
\] (16)

Analytical estimates of Equation 16 are given in SI 2. The cut-off height \( h \) normalised by the particle diameter \( d \) will be referred to by \( c \):

\[
c = \frac{h}{d}
\] (17)

Below we will be interested in hexagonal ordered cavities. For an optimal hexagonal packing, the distance \( s \) between the particles along a row and the distance \( t \) between the rows, should obey \( t = \frac{s}{2} \sqrt{3} \). However, on the lattice only integer values are allowed. Rounding to closest integer values must be implemented. For some values of the particle distances \( s \) there is a reasonable value of \( t \), for other distances the error is relatively large. Only values of \( s \) which required < 0.15 rounding errors for the corresponding \( t \) value are used.

Parameters of Table 1 can be used to generate a large variety of inverse opal structures. As long as \( s > d \), we have the situation that the cavities are isolated. However, the cavities may become interconnected when \( s < d \). In experimental situations such overlap of cavities may occur, and then there are usually small openings connecting the cavities. This is why this particular parameter setting is allowed.
5.4 Results and discussion

5.4.1 Example 1. Liquid condensation in a weakly hydrophilic face centred square inverse opal

We first consider a simple inverse opal structure which has cavities with a diameter $d = 31$. The distance $s$ between the cavities is set to 88, and the distance between the rows $t = 44$. This implies a face centred square arrangement of the cavities. The number of cavities in a row is unity $n = 1$, whereas the number of rows is set to 3. As can be seen from Figure 7, this setting generates an equal box size in $x$ and $y$ directions. As the distance between the cavities exceeds the cavity diameter, we have isolated pockets. The surface interaction is set to a slightly hydrophilic value $\chi_S = -0.3$.

To compute the adsorption isotherm, we start with a low amount of liquid in the system and then increase this amount step by step. In the calculations the outcome of a given calculation serves as an initial guess for the subsequent calculation. This is why a system can be trapped in metastable states, similarly as in experimental counterparts.

In Figure 7A we present the adsorbed amount of the liquid component $\Gamma^\sigma = \Gamma - V'\varphi^b$, where $V'$ is the volume available for the L and V components, that is $V' = M_x M_y M_z - \Sigma \varphi_S(r)$, as a function of the volume fraction of the liquid component in the bulk. Here we did not normalise with respect to the available surface area and thus this amount is proportional to the surface area. The bulk volume fraction is normalised by the bulk binodal value. The curve is plotted in linear-ln coordinates. Upon an increase in the amount of liquid component in the system $\Gamma$, first the vapour phase is gradually saturated with liquid and the adsorbed excess remains modest: at the surface a gaseous adsorption layer develops. Then, upon further increase of the amount, the binodal value is crossed and the system enters the super-saturation regime. The liquid film remains homogeneous along the surface, until $\Gamma^\sigma \sim 4000$, then a first-order jump in the isotherm takes place (cf Figure 7A dotted line). As can be seen in Figure 7B, at this stage a droplet formed in the confined space of the cavity and the curvature on the L/V interface in
Figure 7: Liquid condensation in hydrophilic inverse opal \((d = 31, s = 88, t = 44, m = 3, n = 1, h = 25 (c = 0.8))\). A) Excess adsorbed amount of the liquid component in the system as a function of the volume fraction of the liquid normalised by the binodal value in lin-ln coordinates. The dashed part represents not the true part of the isotherm but rather connects two states, before the condensation of a pocket and after the condensation. The dotted, vertical line is at the bulk binodal \(\phi^\#\). The labels along the isotherm refer to the snapshot colour coded density distributions given in panels B,C,D. Red is high density liquid, white is low density (gas) phase.

the opening is concave, resulting in a negative Laplace pressure inside the droplet. Since the chemical potential of the liquid molecules should be the same everywhere, this means that the vapour phase is undersaturated (see Figure 7A).

The volume fraction of liquid in the bulk \(\phi^b\) increases as more liquid is added and passes the binodal value \(\phi^\#\) again. At this binodal point there is no under- or oversaturation, hence no curvature of the L/V interface at the opening (not shown). Additional liquid that is added to
the droplet induces a convex curvature on top of the droplet, and the bulk oversaturates up to C in Figure 7A. The $\Gamma^\sigma$ at this point is approximately 10 000, and consists of a thin film ($\Gamma^\sigma \sim 4000$) and the macroscopic droplet ($\Gamma^\sigma \sim 6000$). The volume of a sphere with $d = 31$ is about 15 600. Given that the density difference between the liquid-rich and vapour-rich phase is $\sim 0.5$, and that part of the thin liquid film becomes part of the macroscopic droplet, the $\Gamma^\sigma$ found at point C is in agreement with what is expected for a cavity with diameter $d = 31$.

Additional liquid is subsequently not used to fill the other cavities, but to increase the volume of the existing droplet (Figure 7D) and the droplet starts to spread on the substrate. Below we will follow this process in a slightly different geometry. The oversaturation needed for capillary condensation to occur for the other cavities is in this case not reached. This means that for this inverse opal, with $d = 31$, once condensation has taken place, a droplet grows on top of the filled cavity and the remaining cavities are not filled via capillary condensation, but typically rather fill once the central droplet spreads over and on top of the other cavities (not shown).

Most inverse opals in experiments, which are fabricated using sacrificial particles, have cavities of hundreds of nanometres or more (e.g. refs. 3, 10, 41–43) These sizes are much larger than the cavities considered in the current calculations. Smaller cavities can fill more easily via capillary condensation (cf. Figure 5B). Since the impregnating wetting state is not observed even for such small cavity sizes as used in Figure 7, we conclude that the impregnating wetting state due to capillary condensation is not likely to develop for practical inverse opals which are marginally hydrophilic.

In this surface structure, the cavities are not connected, whereas for some experimentally fabricated inverse opals all cavities may be interconnected via a small opening. Since the curvature of the droplet should be constant, the curvature of the liquid-vapour interface at the small opening is the same as for the rest of the macroscopic droplet, and hence the high curvature needed for the next cavity to be wetted via this opening, is not reached. Therefore, a cavity that is filled with liquid will wet the next cavity via the larger opening at the top, rather than through this small hole (not shown).
5.4.2 Droplets on top of the hexagonally ordered inverse opal

In the remainder of this paper we will focus on close-to-hexagonally packed cavities. In principle one can force a water-front to move along such a surface in an arbitrary direction. Here we focus on just one of the possible directions.

We consider solvent fronts along the $x$-direction, which spreads by increasing the volume of the droplet, in the $y$-direction. Recalling that mirror-like boundary conditions are implemented in $x$, $y$ and $z$-directions, in this scenario it suffices to have just two rows of cavities, that is $m = 2$. The system is much larger in the $y$-direction and we consider $n$ cavities with a spacing $s$. For a hexagonal packing of cavities the distance $s$ and the spacing $t$ between rows are interconnected and we will mention just one of these parameters. The number of cavities that are considered in the $y$-direction is taken sufficiently large so that there are no boundary effects. That is why below we will not systematically mention the value of this parameter. The surface is thus sufficiently specified by mentioning the cavity diameter $d$, the distance between the cavities $s$ and the cut-off height $h$, or equivalently $c = h/d$.

Typically, we will initiate the calculation by means of some initial guess of the SCF protocol such that a droplet develops with its symmetry plane along the $y = 1/2$ boundary.

5.4.3 Example 2: Advancing and receding drop fronts on a slightly hydrophilic hexagonally packed inverse opal

In Figure 8 we give representative examples of planar solvent droplets with its solvent front (on average) along the $x$-direction. The drops sit with their symmetry plane at $y = 1/2$. The inverse opal is
Figure 8: A-D: Four examples of droplets on an inverse opal with $d = 31$, $s = 30$, $c = 0.80$, $n = 3.5$, and $\chi_S = -0.3$. A and B) two advancing water fronts with relatively high contact angles; C and D) two receding water fronts with low contact angles. For each panel the left ($z, +y$), right ($z, -y$) and bottom images ($x, y$) are for different view-points, that is, the left image is taken from the front, the right image is taken from the back, the bottom image is the top-view. Colour coding: Red is high density liquid. Blue is low density gas. White is intermediate density. The snapshots are taken from the calculations of Figure 9.

characterised by the cavity diameter $d = 31$, the spacing between the cavities in the $y$-direction $s = 30$, the cut-off fraction $c = 0.80$, and the number of cavities in the $y$-direction, $n = 3.5$. The surface is slightly hydrophilic; $\chi_S = -0.3$. The cavities directly under the macroscopic water front are filled with liquid, while the other cavities remain empty. The water front is thus in the Wenzel wetting state (Figure 1). Notice that an additional cavity is filled going from A to B. Such an event gives discontinuities as discussed below: in B there is slightly more liquid in the system than in A, but the height of the drop in A is more than that
The panels A and B are taken as examples of the droplet shape in a series of calculations for which the droplet volume was increased (see also Figure 9). We refer to these as advancing front lines. The other two panels (C and D) are taken for the situation that the drop volume was decreased and we refer to this situation as receding front lines. Three different view positions of the same drop are given in this Figure to illustrate the features that present themselves in advancing and receding cases. From the top-view perspective, we see that the solvent front is not straight. It curves along the cavity openings and the exact shape of the front strongly ‘fluctuates’ depending on the exact value of the droplet volume. In one of the cases the front is at lower \( y \)-values at the low \( x \)-values and in the other case it is inversed, the lowest \( y \)-value is at a high \( x \)-value. In the four cases shown in Figure 8 we see that the absolute value of differences in the \( y \)-position does not depend much on the advancing or receding modes.

As the three-phase contact line is curved, necessarily the contact angle must vary as well. The contact angles are best viewed from the side. The top graphs in Figure 8 are images taken with a ‘front’ or ‘back’ view point. We present both of these to illustrate that the shape in the \( z\-y \) plane depends slightly on the \( x \)-coordinate. Clearly there is a huge difference in the contact angle between the advancing fronts (very high angles) and the receding fronts (very low angles). Furthermore, as can be seen in panel D, the receding droplet remains pinned on top of the liquid-filled cavity, resulting in a longer contact line as compared to advancing droplets.

For a given snapshot we can evaluate the contact angle \( \theta(x,z) \) in the \( z\-y \) plane by estimating by interpolation the position \( y' \) of the interface, where the \( \phi(x,y',z) = 0.5 \). In other words, the \( y' \)-position of the liquid-vapour interface depends both on \( x \) and \( z \): \( y' = y'(x,z) \). Then the local contact angle of the solvent front is a function of both \( x \) and \( z \):

\[
\theta(x,z) = \arctan(y'(x,z) - y'(x,z-1))
\]  

which implies that the contact angle can only be computed for \( z > 2 \). The average angle at a height \( z \) is found by averaging along the \( x \)-direction:

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Chapter 5

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in B; the liquid in the cavity is noticed as a volume reduction in the drop.
Model of simple liquid on complex geometry

\[ \theta(z) = \frac{1}{M_x} \sum_{x=1}^{M_x} \theta(x, z) \]  

(19)

while the standard deviation \( \Delta \theta(z) \) measured in the x-direction is given by

\[ \Delta \theta(z) = \frac{1}{\sqrt{\sum_{x=1}^{M_x} (\theta(x, z) - \theta(z))^2}} \]  

(20)

Similarly, the position of the interface \( y'(x,z) \), the average position of the interface \( y'(z) \) and the standard deviation \( \Delta y'(z) \) are straightforwardly recorded.

In Figure 9A we plot the standard deviations \( \Delta y'(z) \) as a function of \( z - h \) (height above the substrate), and in Figure 9B the \( \theta(z) \) together with the fluctuation in the angle \( \Delta \theta(z) \) as ‘error’-bars as a function of \( z - h \) for the four droplets already shown in Figure 8.

![Figure 9: Examples of drop characteristics. A) The standard deviation (measured in x-direction) of the position of the interface \( \Delta y' \) as a function of the height above the substrate \( z - h \). The horizontal grey line represents the result on a smooth surface. B) The angle of the liquid-vapour front in the z-y plane, \( \theta(z) \) together with the standard deviation of the angle measured in the x-direction plotted as ‘error’-bars. The grey curve is the contact angle of a similarly sized droplet on a smooth surface. The labels A-D correspond to the snapshots A-D in Figure 8: A,B advancing contact liquid front; C,D are receding liquid fronts.](image)

It is natural to expect that when the drop characteristics are considered further away from the surface that the influence of the surface is gradually lost. This is why the \( \Delta y'(z) \) is a decreasing function of \( z \). Again, as noticed already from the snapshots, the value of \( \Delta y'(z) \) does not depend much on the advancing or receding modes of wetting. That is why the four curves in Figure 9A are nearly the same. We refrain
from trying to provide further comments about the differences. Similarly, far from the surface the angles become independent on $x$. That is why in Figure 9B the ‘error’ bars diminish in size when $z - h$ is increased. Indeed very close to the substrate $z - h < 4$ the fluctuations are very large, that is about 50% of its value.

We already noticed that the advancing contact angles are much larger than the receding ones. Figure 9B gives the numerics more accurately: the advancing angles are on average larger than 90°, whereas the receding angles are about 45°, very close to the angles found for the unstructured surface (grey line). Interestingly, the average contact angle in the advancing mode can go through a small local maximum at a height $z - h = 3$. Such an effect hints to the presence of a foot on the droplets. However, at this height the fluctuations are large and we are hesitant not to over-interpret the results.

It is clear that, if we want to compare droplets and see trends, we need to reduce the outcome of the computations. That is why from hereon we will focus on the properties of the droplets on a height of $z - h = 3$ (as indicated by the arrow in Figure 9). At this height above the substrate the ‘foot’ is not disturbing too much, while the structure of the surface is still well noticeable. We thus define (if not mentioned otherwise) the fluctuations of the liquid front measured as the standard deviation along the $x$-direction as $\Delta y = \Delta y'(h + 3)$, and the average contact angle of the drop $\theta = \theta(h + 3)$, as well as the fluctuations $\Delta \theta = \Delta \theta(h + 3)$.

Calculations wherefrom the results of Figures 8 and 9 were taken were started with an initial amount of liquid $\Gamma = 3 \cdot 10^5$. The more liquid is added to the system and these molecules are consumed by the drop. Hence the drop volume was increased. Typically we performed ten liquid addition steps and for each of these new profiles are calculated to obtain an advancing angle. The amount of the liquid is subsequently stepwise decreased to check for hysteresis and to obtain a receding angle. The structural properties of the drops are recorded during this cycle and the results were collected in Figure 10.
Figure 10: Examples of structural features of advancing and receding drop fronts. A) The fluctuations of the position of the liquid front along the x-direction at a height \( z = h + 3 \) as a function of the \( \Delta \Gamma \) of the droplet component with an initial amount \( \Gamma = 3 \times 10^6 \). B) The corresponding average contact angle \( \theta \) (measured at a height \( z = h + 3 \)) and the standard deviation (plotted as error-bars). The advancing liquid front is given by the solid sphere data points, the receding ones in solid square data points. The lines are to guide the eye. A discontinuity in the line represents a jump-wise change of the drops on the substrate. The labels A-D correspond to the snapshots of Figure 8 and the structural data of Figure 9. A and B are along the advancing branch, whereas C and D are taken from the receding drop fronts. Parameters are similar as in Figures 8 and 9.

The starting point of the calculations is not extremely well defined in terms of advancing or receding states. The initial guess takes the system in this case close to an advancing situation: the contact angle \( \theta \) is rather high. Typically this initial drop is disregarded from our averaging (see below). Upon stepwise increase of the drop volume (closed spheres) the \( \Delta y \) decreases from 5.5 to 4, while the contact angle \( \theta \) increases gradually until point A is reached. The contact line did not move upon adding the liquid: the contact line is arrested as the contact line cannot be placed on top of a (water filled) cavity. Then with a small increase the system jumps from A to B. Above we saw that in this event one extra cavity is filled with liquid. At this event the contact line de-pins jump-like in an event that may be referred to as a de-pinning transition. In Figure 8AB we see that the three-phase contact line has the opposite curvature in the x-direction. At this de-pinning event the average contact angle jumps downward to \( \theta \approx 90^\circ \) (cf Figure 10B) and the \( \Delta y \) jump-like increases from 4 to 5.5 (cf Figure 10A). The contact angle close to the surface and directly in front of the cavity that fills up, switches thereby from \( \theta > 90^\circ \) to \( \theta \approx 90^\circ \) (cf. Figure 8A,B). This
increased contact angles with respect to $\theta_r$ ($68^\circ$ for $\chi_s = -0.3$) are hereby found for a hydrophilic surface without air entrapment. The system may suffer more of such events when more and more liquid is added. After another four additions of volume we were close to the initial condition and the advancing contact line calculations were stopped.

For receding water fronts (Figures 8CD), computed by taking liquid out of the system, the squares in Figure 10, we first retrace a part of the advancing curve, that is, the four latest volume additions were undone and the same results were recovered. However, as soon as the volume of the drop is decreased compared to point B we follow a different route. We do not jump to point A, but rather follow the trend downward for the average contact angle $\theta$ (cf Figure 10B) while also the fluctuations $\Delta y$ decreases. Close to the initial volume the contact angle is found to be close to the value on the smooth surface $\theta = \theta_r$. At this point the curvature of dependence $\Delta y(\Delta \Gamma)$ changes. Further reduction of the volume of the drop leads to a local minimum of $\Delta y$, while the contact angle drops significantly below the value of $\theta_r$. Then point C is reached (cf. Figure 8C). Now the receding front is pinned on top of a liquid filled cavity. The low contact angle on top of the cavity, clearly visible for the right-hand site of droplet Figure 8C, is explained by the fact that the liquid wets a surface of the same material (namely the liquid in the cavity). During receding, the water front is thus pinned at the liquid/liquid surface with a local $\theta$ of $0^\circ$. The cavity remains filled after the droplet has retracted from the cavity (see cavity on the right-hand site of droplet D) which occurs once again step-wise. During this de-pinning step the three-phase contact line rearranges its curvature again (cf Figures 8C,D). At this de-pinning transition the value of $\Delta y$ increases jump-like, while the average contact angle decreases somewhat. Upon further reduction of the drop volume the $\Delta y$ increases further while the contact angles remain low.

The traces of Figure 10AB imply a hysteresis: the curves for adding and reducing volume only overlap when no de-pinning transition has occurred in between the addition or removal steps. The contact line of the advancing droplet experiences a surface consisting of solid and vapour, whereas the contact line of the receding angle experiences a surface consisting of solid and liquid. The true receding angle is only visible at $\Delta \Gamma = -5 \cdot 10^4$ - $-7 \cdot 10^4$ (last 3 data points) and is $\sim 35^\circ$. If the
surface can be regarded as consisting of solid with a liquid, then the contact angle can be calculated using

\[
\cos \theta_{\text{water in cavity}} = 1 - \Phi_S + \Phi_S \cos \theta_Y
\]

(21)

with the fraction of solid on the top of the substrate \( \Phi_S = 0.43 \) (for \( c = 0.8 \)). The contact angle according to this calculation (40°) is in agreement with the contact angle we find here.

For these last droplets, high values of \( \Delta y \) are found. The contact line is in these cases pinned on the farther edge of a water-filled cavity (see Figure 8D).

5.4.4 Trends in the shape of advancing water fronts

In the remainder of this paper we will focus on advancing contact angles. Referring once again to the results of Figure 10B, we typically initiated calculations with the drop near the lower boundary on the y-axis in such a way that the resulting drop shape assumes properties of an advancing one. Then, as in Figure 10B ten subsequent increases of the amount of the liquid component were implemented. The average contact angle \( \theta \) (along the x-direction and at \( z = h + 3 \)) were again averaged over these ten droplets to obtain \( \langle \theta \rangle \). Typically one or more de-pinning events were accepted in this averaging. Recall, that in the advancing branch the contact angle in a de-pinning event changes only slightly. The standard deviations were averaged similarly.

5.4.5 Effect of cavity size \( d \)

The size of the inverse opals in the calculations, which is linked to experimental sizes by the width of the interface, invariably is much smaller than the size of inverse opals used in experiments. To study the effect of size of the structures on the (double) averaged advancing contact angle \( \langle \theta \rangle \), droplets on inverse opals with cavity diameter ranging from 9 to 52 have been recorded. The trend observed for this series of sizes, can be extrapolated to even bigger sizes without the need to calculate those. In these calculations the spacing between the cavities was set to \( d - 1 \), that is, the cavities were slightly overlapping so that a small hole connects the cavities. The cut-off fraction is kept at \( c = 0.8 \).
As shown in Figure 11, the average advancing $\langle \theta \rangle$ is an increasing function of the cavity diameter $d$. For $d > 40$ the advancing contact angle $\langle \theta \rangle$ reaches a plateau. The levelling off hence implies that it is not necessary to increase the cavity sizes even more to reach the experimental limits. Again, the fact that $\langle \theta \rangle$ can increase above $\theta_Y$ is attributed to the pinning of the contact line around the cavities. For very small cavities we observed that the average angle can be smaller than $\theta_Y$ (grey horizontal line in Figure 11). Small cavity sizes are similar to the small confinements $D$ used in the one-gradient slits of Figure 5. From these slit calculations we know that small values of $D$ need only a small oversaturation to fill the slit with the liquid. Similarly, very small cavities can easily be filled with the liquid. We refer to this situation as the impregnated wetting state (Figure 1). Indeed the inverse opal with $d < 10$ are in the impregnated state and it is natural to expect that for this case $\langle \theta \rangle < \theta_Y$: the effective top surface in front of the water front consists of the solid with patches of liquid, just as is the case for a receding droplet. The advancing $\langle \theta \rangle$ found for these structures (see Figure 11) corresponds to the receding contact angles presented in Figure 10B.

For the structure with $d = 15$ the situation is rather complex. It appears that some, but not all, cavities in front of the droplet are filled...
with liquid. In the process of advancing the liquid front, we add more and more of the liquid. As soon as an additional cavity is filled, the volume for the droplet decreases and this reduces the curvature and the corresponding oversaturation in the vapour phase. This decrease in oversaturation after filling subsequent cavities prevents other cavities to fill up. The number of cavities filled in front of the water front, depends on the size of the droplets on top of the inverse opal: the smaller the droplet, the higher the curvature, thus the more oversaturation. The more cavities are filled, the lower is the advancing contact angle \( \langle \theta \rangle \) as the surface becomes effectively hydrophilic. The droplet size dependence will imply small changes in the dependence of \( \langle \theta \rangle \) as a function of \( d \) in Figure 11. For the drop sizes used to compute Figure 11 the \( \langle \theta \rangle = \theta_Y \) occurs approximately at \( d = 20 \).

For the inverse opals with \( d \geq 20 \) only cavities directly under the droplet are filled (Wenzel wetting state). The water front encounters the same fraction of flat solid top surface, \( \Phi_S \) for all cavity sizes, but the increase in \( \langle \theta \rangle \) with \( d \) depends on the strength of the pinning effects and this allows \( \langle \theta \rangle \) to increase with \( d \) sufficiently above \( \theta_Y \).

![Graph](image)

**Figure 12:** Advancing contact angle \( \langle \theta \rangle \) and the corresponding fluctuations (measured along the x-direction) indicated as error-bars, as a function of the affinity of the solvent for the substrate phase \( \chi_S \) for a hexagonal inverse opal with cavity sizes \( d = 39 \), cut-off fraction \( c = 0.9 \) and spacing between the cavities \( s = d - l = 38 \). The contact angle on a smooth surface is shown with a grey line (copied from Figure 4). Stars indicate that the cavities under the water front remain empty (Cassie-Baxter wetting state).
5.4.6 Effect of the S/L interaction parameter $\chi_S$

Let us next focus on the interaction of the liquid with the substrate via the S/L interaction parameter $\chi_S$. The more negative this parameter the more hydrophilic (solvophilic) the surface is. When the $\chi_S$ is positive we may refer to the surface as hydrophobic (solvophobic). We select for this study hexagonal ordered inverse opals with a cavity size $d = 39$. As shown in Figure 11 such cavity sizes give wetting features in the plateau region where the size dependence was essentially lost. We consider here the case that the cut-off fraction $c = 0.9$. This $c$-value is chosen to mimic the inverse opal in ref 10. The distance between the cavities was set to $s = d - 1$ as before: the cavities are connected to each other by small openings.

In Figure 12 the grey curve represents the contact angle $\theta_r$ on the smooth surface as a function of $\chi_S$ and this result is reproduced from Figure 5 for ease of comparison. The average advancing contact angle $\langle \theta \rangle$ follows the dependence $\theta_r$: the advancing contact angle increases with decreasing hydrophilicity (solvophilicity) of the substrate. However, for $\chi_S > -0.6$ the advancing contact angle is systematically above $\theta_r$, whereas it is systematically below $\theta_r$ when $\chi_S < -0.6$.

The wetting transition, that is the point for which $\theta$ becomes 0, occurs at a $\chi_S$ which is slightly less hydrophilic for the inverse opal as for the smooth surface. In the low contact angle cases all cavities under the droplets are filled (impregnating wetting state). The filled cavities render the surface slightly more hydrophilic than the smooth surface (see Equation 1) and this caused the early wetting transition for the inverse opal as compared to the smooth surface.

The inverse opal remains in the impregnating wetting state for small but finite contact angles $\chi_S = -0.7$. In these cases the advancing contact angle is lower than the corresponding $\theta_r$. The wetting switches to the Wenzel state by increasing the hydrophilicity further to $\chi_S = -0.5$. Now the advancing contact angle is larger than the $\theta_r$. Eventually the wetting switches to a Cassie-Baxter wetting state for higher values of $\chi_S$. These cases are labelled by the asterisk in Figure 12. Again the
advancing contact angle is larger than $\theta_Y$, and the difference $\langle \theta \rangle - \theta_Y$ is roughly constant, that is, it does not depend whether there is the Wenzel or the Cassie-Baxter state. This result suggests that for the advancing angle, it does not matter whether air is entrapped underneath (observed for $\chi_S \geq -0.3$) the droplet or not (observed for $\chi_S \leq -0.5$). This implies that the increase in observed $\langle \theta \rangle$ compared to $\theta_Y$ cannot be explained in terms of wetting state. Rather, pinning of the contact line and the de-pinning transition should be considered. The immobilization of the contact line on the kinks in the surface (as explained in Figure 2) on this hexagonally packed inverse opal induces the contact line to curve and extend ($\Delta y > 0$), which is energetically unfavourable. The contact line is even further extended after a de-pinning transition (increase in $\Delta y$), indicating that in the stress perpendicular to the surface has increased. However, $\langle \theta \rangle$ decreased locally to values close to $\theta$ on a smooth surface, showing that stress in the vertical direction is released after the transition. The average $\langle \theta \rangle$ is still higher than $\theta_Y$ surface directly after the de-pinning transition. This is caused by the build-up of stress at the other cavity (we consider two rows of cavities).

The interplay between curvature perpendicular to the surface (here discussed in terms of $\langle \theta \rangle$) and parallel to the surface (here discussed in terms of $\Delta y$ of the contact line) results in an overall high $\langle \theta \rangle$. Whether the cavity under the moving water front fills with liquid or remains filled with air, depends on the $\chi_S$: air is entrapped for more hydrophobic materials, but the cavities fill for a more hydrophilic material.

The pinned water front on a surface with higher $\chi_S$ can withstand higher $\langle \theta \rangle$ before stress starts to build up and the de-pinning transition occurs.

5.4.7 Effect of cut-off height $c$ at constant spacing $s$

Experimentally one can control the inverse opal structure by the cut-off height $h$, or equivalently to the cut-off fraction $c$. It is of interest to consider the effect of the cut-off height from a computation point of view. We can study this for a fixed spacing $s$ between the cavities (in this paragraph) or with a fixed fraction of solid in the top of the substrate $\Phi_S$ (next paragraph). In both cases we choose slightly
Figure 13: A) Advancing contact angle $\langle \theta \rangle$ and the corresponding standard deviation as measure of variation in the $x$-direction as function of cut-off height. The horizontal grey line is the contact angle on the $\theta_Y$ on a smooth surface, the grey dashed line is the angle of the kink $\theta_{\text{kink}}$ at different values of $c$ and the grey dotted line is the $\Phi_S \cdot 100$. Stars indicate that the cavity under the water front are vapour-filled (Cassie-Baxter wetting state). B) Corresponding average variation in $y$-position $\langle \Delta y \rangle$ at $z = h + 3$ as function of cut-off height $c$. The hexagonally ordered inverse opal has cavity diameter $d = 39$, spacing between the cavities $s = d - 1 = 38$, and $\chi_S = -0.3$. C) The distribution of solid $S$ at the top layer of the substrate, that is $\Phi_S(x,y,h)$: the dark blue colour implies density of the solid is unity. The red colour indicates that the opening of the cavity is filled by the solvent. The white blue colour means that the cavity opening is filled with vapour. Orange colour implies that the solvent density is in between the liquid and the vapour. The value of $c$ is indicated.

hydrophilic substrates with $\chi_S = -0.3$. This value of $\chi_S$ gives a $\theta_Y = 68^\circ$. Similarly as in the previous paragraph we fix $d = 39$ and $s = d - 1$. Obviously the limits $c = 0$ and $c = 1$ are the same as the smooth surface. In between these two limits the surface structure is characterised by a top surface layer with a fraction of $\Phi_S$ of the sites being the solid. The top layers are given in two-gradient contour plots in Figure 13C. When $c = 0.5$ the amount of $S$ (dark blue colour) is minimal: both in the limits $c = 0$ and $c = 1$ the cross-section are completely blue (not shown).
Correspondingly, the contact line fluctuations, as monitored by $\Delta y$, are averaged over ten ‘snapshots’ while increasing the drop volume. The result is given by $\langle \Delta y \rangle$. In both limits $c = 0$ and $c = 1$ the surface is ideally smooth and the three-phase contact line will not fluctuate in the $x$-direction. In between these limits $\langle \Delta y \rangle > 0$ because the contact line becomes pinned.

The advancing contact angle $\langle \theta \rangle$ together with the standard deviation of this angle (measured in the $x$-direction) is presented in Figure 13A as a function of the parameter $c = h/d$. The corresponding fluctuations of the three-phase contact line $\langle \Delta y \rangle$ (measured in the $x$-direction at a height $z = h + 3$) are given in Figure 13B.

Inspection of Figure 13A shows that by far the most interesting region is for $0.5 < c < 1$. For $c < 0.5$ the average advancing contact $\langle \theta \rangle$ hardly differs from $\theta_Y$. However, in small values of the cut-off fraction the contact line is already significantly curved (Figure 11B) and the surface structure alters the $\theta(x)$ locally to hydrophobic values $\theta > 90^\circ$. The average $\langle \theta \rangle$ for $0.51 < c < 0.95$ is higher than $\theta_Y$ on a smooth surface, though locally, the $\theta(x)$ may be smaller; the variation in $\theta$ along the $x$-direction (depicted as vertical line) extends to values $\theta < 68^\circ$ for most values of $c$. A maximum in $\langle \theta \rangle$ is found at $c \sim 0.80$, with $\langle \theta \rangle = 110 \pm 30^\circ$. A local minimum in $\Delta y$ at this $c$ is found, which likely is coupled to the need to keep the overall curvature in the drop constant.

Two parameters of the surface structure that are important for contact line pinning are changed when $c$ is varied: the fraction flat solid top surface $\Phi_S$, which is the fraction of flat solid at the top of the surface (dark blue in Figure 13C) and the angle of the kink, $\theta_{\text{kink}}$ (see SI 1 for calculation of $\theta_{\text{kink}}$ and SI 2 and Equation 16 for calculation of $\Phi_S$). Both $\Phi_S \cdot 100$ and $\theta_{\text{kink}}$ are plotted in Figure 11A. The $\Phi_S \cdot 100$ equals 100 in both limits of $c$ and has a minimum at $c = 0.5$. $\theta_{\text{kink}}$ is $180^\circ$ at $c = 0$, and decreases to 0 at $c = 1$. The latter parameter is considered important for hydrophilic materials to obtain hydrophobic contact angles: it has been suggested that only for $\theta_Y < \theta_{\text{kink}}$ pinning can occur, and a barrier for the water front to enter the cavities is obtained, resulting in air entrapment and hence the possibility of obtaining higher contact angles $\theta$. However, in our case, $\theta_{\text{kink}}$ is smaller than $\theta_Y$ for most values of $c$, and no jump in
\( \langle \theta \rangle \) is observed between \( c = 0.51 (\theta_{\text{kink}} > \theta_{t}) \) and \( c = 0.59 (\theta_{\text{kink}} < \theta_{t}) \), and no air entrapment is found for \( 0.59 < c < 0.85 \).

For \( c = 0.26 \), the \( \theta_{\text{kink}} \) is too large for pinning to occur according to the argument presented Figure 1. However, an advancing water front is immobilized at the front of a cavity, and moves in one step to a position in front of the next cavity. Hence, despite of the small \( \theta_{\text{kink}} \) in our calculations a true de-pinning transition is found.

In our case the pinning of the contact line is due to the complex 3D-structure of the surface: the cavities are placed close to each other, and the contact line thus encounters multiple cavities on a short distance. If the water front would not have been pinned at the front of a cavity, but rather partly fill the cavity, this result in more L-S interface and a longer contact line. This is apparently energetically more unfavourable than pinning the contact line in front of a cavity. Hence, the contact line pinning is governed by the 3D- structure, and not by the simple 1D-argument presented in Figure 2.

When looking at the top surface (Figure 13C) for \( c = 0.26 \), we see that some cavities on the left are filled (red), while the last 1.5 cavities are not filled (light blue). The last upper cavity is just in front of the contact line. Some liquid (red colour) is present at this value of \( z \). Moreover, the situation for \( c = 0.74 \), which has a similar top surface but a different \( \theta_{\text{kink}} \), is comparable.

For \( c \) close to 0.5, the substrate is not a continuous structure, but consists of discrete triangular ‘pillars’ (see Figure 13C). Contact line pinning also occurs for discrete shapes.\(^{19, 45}\) Assuming that pinning is mainly found on the top surface in line with observations for \( c = 0.26 \), the length over which pinning can take place is limited. However, also in this case a de-pinning transition is observed for an advancing water front. Hence the pinning is not limited to the flat part of the top surface (the dark blue surfaces in Figure 13C) for all values of \( c \), but pinning occurs over the 3D structure.

Decreasing or increasing \( c \) from \( c = 0.5 \) results in a continuous top layer. The contact line can hereby be pinned on the front of every cavity. For higher values of \( \Phi_{S} \), the contact line is expected to be exclusively located on the top surface (and thus at constant \( z \)). Higher
values of $\Phi_S$ (thus smaller cavities) also result in a surface that is more similar to a smooth surface.

In Figure 13C, the liquid-filled cavities are shown in red, whereas vapour-filled cavities are light blue. This is observed for all $c$ up to $c = 0.85$. However, for $c = 0.90$ and $c = 0.95$, we observe a colour in between red and white blue for cavities under the droplet (left hand side). This suggests that at that height, neither a liquid, nor a vapour phase is present, and thus that the interface is located at that value of $z$.

5.4.8 Effect of cut-off height $c$ at constant $\Phi_S$

One may argue that the true effect of the cut-off height is seen for cases where $h$ (or equivalently $c$) is varied at a fixed amount of $S$ in the top layer of the substrate, that is for fixed value of $\Phi_S$. To do so, one has to vary the inter-cavity spacing $s$ simultaneously when the cut-off height is changed. Note that the true limits $c = 0$ and $c = 1$ are hard to reach with fixed $\Phi_S$ as it requires odd distances between the cavities.

The dependence of the advancing contact angle as well as the contact line fluctuations are recorded for this scenario in Figure 14. Here we have chosen for a $\Phi_S = 0.43$ which is the value of $\Phi_S$ which corresponds to $c = 0.79$ (near the maximum) of Figure 13. Note that all the top surfaces used in Figure 14 are similar to the result shown in Figure 13C for $c = 0.79$.

It is natural to compare results between Figures 13 and 14. For values of $c < 0.79$, the average contact angles differ very little. In Figure 14 the average angle appears slightly larger. There is a dramatic difference between the cases of Figure 13 and 14. Compare, for example, the top surface for $c = 0.51$. While in the case of fixed distance between the cavities $s$ there are individual posts with $\Phi_S \sim 0.1$ (Figure 13C), there is a continuous solid phase in Figure 14 as $\Phi_S = 0.43$. Nevertheless, the average contact angles were hardly affected.

At $c > 0.79$, $\langle \theta \rangle$ at constant $\Phi_S$ (Figure 14) keeps growing with increase in $c$, while with fixed $s$ the contact angles decreased again. The decrease in $\langle \theta \rangle$ for $c > 0.79$ in the constant $s$ case (Figure 13) can thus be attributed to the top surface: higher $c$ results in smaller cavities and thus in a surface that is more similar to a smooth surface. The increase
in $\langle \theta \rangle$ found for increasing $c$ at constant $\Phi_S$ implies that, assuming a constant line tension, a higher $\theta_{kink}$ for a hexagonally packed surface structure gives rise to a higher barrier for a de-pinning transition to occur and thus higher average contact angles can be maintained. The higher average contact angles are produced with lower and lower fluctuations of the shape of the contact line. Eventually, in the limit of $c = 1$ the fluctuations must vanish by definition.

![Figure 14: A) The advancing contact angle $\langle \theta \rangle$ and standard deviation as function of cut-off height $c$ for fixed value of the solid fraction in the top-layer of the substrate $\Phi_S = 0.43$. The grey line is $\theta_Y$ on a smooth surface and the grey dashed line is the angle of the kink at different $c$. Stars indicate that the cavity under the liquid front are vapour-filled (Cassie-Baxter wetting state). B) Variation in y-position $\langle \Delta y \rangle$ as function of cut-off height $c$ for $d = 39$ and $\chi_S = -0.3$.](image)

Interestingly, it is found that the cavities under the water front remain empty for $c = 0.85$ (and up) at $\Phi_S = 0.43$, whereas the cavities were filled for $c = 0.85$ at $s = 38$ ($\Phi_S = 0.55$). Bringing the openings of the cavities closer to each other thus prevents water from entering the cavity.

### 5.5 Summary and Outlook

We have implemented a regular solution lattice model to study the wetting on a structurally complex surface. The interaction between vacancies and liquid is parameterised in a regular solution model by the Flory Huggins parameter $\chi$. This parameter controls the width of the interface between liquid and vapour. The model allows for a detailed description of the solid phase and the liquid-solid interaction parameter.
$\chi_s$ is the only parameter to control the hydrophilic/hydrophobic (solphophilic/solvophobic) character of the substrate. We find very complex and interesting wetting states when this model is applied to hexagonally ordered cavities in an inverse opal. It is found that the three-phase contact line is curved and becomes pinned at the cavity openings. Under the droplet the cavities can either be filled with water (impregnated; Wenzel) or filled with the vapour (Cassie-Baxter). No discontinuity in the contact angle $\theta$ is observed for water fronts that are either in the Wenzel state or Cassie-Baxter state, implying that the water front shape is not influenced by air entrapment under the water front, but is rather determined by the surface encountered by the contact line. The pinning of the contact line cannot solely be discussed in terms of the kink that a surface structure makes with respect to the top surface, $\theta_{\text{kink}}$: also for $\theta_{\text{kink}} > \theta_t$, de-pinning transitions are found, and the spacing between the cavities influence whether a cavity under a water front is solvent-filled or vapour-filled. Hence, the full 3D-structure, rather than one parameter ($\theta_{\text{kink}}$) should be taken into account. We found a large difference between advancing and receding contact angles, which are also attributed to pinning of the three-phase contact line. More specifically, it was found that while the smooth surface has a contact angle much lower than $90^\circ$ the advancing contact angles in the inverse opal can be much larger than $90^\circ$. That is, slightly hydrophilic substrates can give hydrophobic contact angles.

Our method can readily be extended to mimic more closely experimental conditions. An interesting case is the wetting of an inverse opal of polypyrrole.\textsuperscript{10} The inverse opal of polypyrrole did not have a smooth top surface. Rather, the top surface showed a positive slope radiating from the position of the sacrificial particle. This more complex surface structure can be implemented easily by a more elaborated way to represent the substrate. Furthermore, polypyrrole is a hydrophilic material. The $\theta_t$ on a polypyrrole surface was measured to be $\sim 20^\circ$. However, the inverse opal was made using sacrificial polystyrene particles. The particles were removed by dissolving them. This removal was expected to be incomplete, and the contact angle $\theta$ changed to $\sim 80^\circ$ for the polypyrrole surface. Polystyrene chains thus must have remained, e.g. in an adsorbed state onto the polypyrrole surface. These adsorbed polymers have a different hydrophilicity, but also changes the
local roughness of the surface structures, resulting in both chemical and structural heterogeneities. These heterogeneities on molecular scale can be studied using the approach presented in this paper when the Scheutjens-Fleer machinery is more fully implemented. For example, we can easily consider polymer chains pinned at random locations along the surface of the inverse opal. It is even possible to consider polymer brushes on such substrates which may e.g. preferentially change wetting characteristics of the top surface or the insides of the cavities.\footnote{Such decorated substrates may feature dramatic hysteresis effects in the contact angle, because the polymers can stabilize the three-phase contact line while the shape of the cavities induces pinning of the contact line. Hence polymers may introduce a second length scale in inverse opal surface structures.}

In the current work we have solved the regular solution model using the self-consistent field machinery. There are low memory routes to find the SCF solution (see Appendix). This implies that the memory needed to find an SCF solution is linearly proportional to the volume, that is, the number of lattice sites in the system \((M_x, M_y, M_z)\). Also the CPU time scales only linearly with the volume. Here we focused on very small systems and used a desktop PC and found accurate results in a few minutes CPU time. Alternatively, the complete set of equations can be solved on a GPU and using CUDA technology the results may be generated 10 to 100 times faster.\footnote{As a result systems which are 10 times larger in each direction should still be feasible, while keeping the wall-time for the computations less than an hour. In this case the regular solution model captures the macroscopically relevant sizes and we do not need to rely on extrapolations.}

\subsection*{5.6 Conclusions}

Regular solution theory is used to study the wetting behaviour of a simplistic molecular model on a complex inverse opal surface topology. The model features molecular input parameters and gives interfacial energies, contact angles and three-phase contact line shapes. As a result, advancing as well as receding wetting front scenarios were considered. It was found that there is a large contact angle hysteresis in these systems, which was attributed to contact line pinning. We have seen that the cavities can be filled by the liquid or remain dry, that is
filled by vapour. Cavities in front of the droplet may be filled by a capillary condensation effect, while receding contact angles typically do not empty the liquid filled cavities. Interestingly, when the substrate is slightly hydrophilic it is possible that advancing contact angles have contact angles larger than 90°. As calculation times are modest, it is possible, when detailed experimental evidence become available, to account for more complex molecular features on the inverse opal structures. For example we can envision a polymer brush as a means to modify either the top surface or the inside of the cavities to control the wetting characteristics to make truly responsive surfaces.

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Chapter 5

Appendix. Simple method to solve the regular solution equations efficiently.

Here we consider the SCF route to optimise the regular solution free energy. We take the simplest one-gradient case without surfaces as an example and trust that the reader can generalise the protocol to include surfaces and to account for more than one dimension. The starting point is Eqn 6:

\[
F = \sum_{z=1}^{M} \varphi(z) \ln \varphi(z) + \varphi_V(z) \ln \varphi_V(z) + \chi \varphi(z) \langle \varphi_V(z) \rangle
\]

(A1)

where we notice that the free energy is a functional of the volume fraction distribution of the liquid and the vapour. We also recall that for each coordinate \( z \) we have a compressibility relation

\[
\varphi(z) + \varphi_V(z) = 1
\]

(A2)

In the self-consistent field SCF theory the same free energy is expressed in terms of segment densities as well as segment potentials \( u(z) \) and \( u_v(z) \). We take it that these potentials are dimensionless, that is they are already normalised by the thermal energy \( k_B T \). The potentials are going to be used in Boltzmann equations:

\[
G(z) = \exp(-u(z))
\]

\[
G_V(z) = \exp(-u_V(z))
\]

(A3)

In the self-consistent field theory the starting point of the approach is the mean-field free energy:

\[
F = - \ln \frac{q^N}{N!} \frac{q_V^N}{N!} - \sum_{z=1}^{M} (u(z)\varphi(z) + u_V(z)\varphi_V(z)) + \sum_{z=1}^{M} \varphi(z)\chi(\varphi_V(z)) + \sum_{z=1}^{M} \alpha(z)[\varphi(z) + \varphi_V(z) - 1]
\]

(A4)

It is relatively easy to show that Eqns A4 and A1 are the same (we will not prove this here). For this we need to know that the single molecule partition functions \( q \) are found by the summation over corresponding Boltzmann weights:

\[
q = \sum_{z=1}^{M} G(z)
\]

\[
q_V = \sum_{z=1}^{M} G_V(z)
\]

(A5)
and the number of liquid and vapour sites is given by

\[ N = \sum_{z=1}^{M} \phi(z) \]
\[ N_V = \sum_{z=1}^{M} \phi_V(z) \]  

(A6)

The optimisation of the Free energy A4 with respect to the segment potentials lead the rule how to compute the volume fractions:

\[ \phi(z) = \frac{N}{q} G(z) \]
\[ \phi_V(z) = \frac{N_V}{q_V} G_V(z) \]  

(A7)

Optimisation of the free energy A4 with respect to the segment density leads to the rule to compute the segment potential:

\[ u(z) = \alpha(z) + E(z) \]
\[ u_V(z) = \alpha(z) + E_V(z) \]  

(A8)

where the interaction contribution to the segment potentials are given by

\[ E(z) = \chi(\phi_V(z)) \]
\[ E_V(z) = \chi(\phi(z)) \]  

(A9)

In summary we thus have the situation that

\[ u[\phi] \leftrightarrow_{\phi+\phi_V=1} \phi[u] \]  

(A10)

In words the left hand side says that the segment potentials depend on the volume fractions (that is \( u \) given by Eqn A8 depends on \( E \) which is given in A9 to be a function of the \( \phi \)). The right hand side of Eqn A10 says that the volume fractions A7 can be computed from the segment potentials, by two routes, namely via the Boltzmann weights Eqn A3 and the partition functions A5 which are also traced to A3. We need a numerical scheme to find the so-called SCF solution. We need a fixed point for which the segment potentials both follow from the volume fractions from which they are computed. Or inversely, we need the segment densities which determine the potentials on which they depend. Such a fixed point should obey to the compressibility relation of Eqn A2.

Self-consistent field solutions must be generated numerically. Once such a solution is found we can compute the thermodynamic quantities. Of more than average interest there is the grand potential
Model of simple liquid on complex geometry

(sum of the surface tensions) $\Omega_S$ of the system. It can be shown that $\Omega_S = \sum_{z=1}^{M} \omega(z)$, where the grand potential density is given by

$$\omega(z) = -\alpha(z) - \frac{\chi(\varphi(z)(\varphi_{vV}(z)) + \varphi_{vV}(z)(\varphi(z)))}{2} + \chi \varphi^b \varphi_{vV}^b$$

where the bulk volume fractions are found at large values of $z$ or equivalently follow from

$$\varphi^b = \frac{N}{q}$$
$$\varphi_{vV}^b = \frac{N_{vV}}{qV}$$

Consider the following pseudo code which makes use of a regularisation parameter $\beta$ (Pikar method). The code is safe but slow when this value is very small. When it is large (close to unity), the code is fast but the iterations may diverge. The suggested value will result in a solution in about 100 iterations and then there will be seven significant digits.

Specify the lattice coordinates, e.g. $z = 1, 2, \cdots, M$ e.g. take $M = 100$.

Specify $N = N_{vV} = 50$ (half system filled by liquid other half by vapour; interface halfway system)

Specify the $\chi$ parameter, e.g. $\chi = 2.2$

Set initial guesses:

$\varphi(z) = 1$ for $z = 1, \cdots, 50$ and zero otherwise.

$\varphi_{vV}(z) = 1 - \varphi(z)$

$\alpha(z) = 0$

- Compute interactions using Eqn A9

$it = 0$

$error = 1$

$\beta = 0.2$ (regularisation parameter)

$tolerance = 10^{-7}$

Loop while error > tolerance, it < 1000

Update it := it + 1

Store ‘old’ values of interactions: $E^o(z) = E(z)$; $E_{vV}^o(z) = E_{vV}(z)$
Chapter 5

Compute potentials Eqn A8
Compute Boltzmann weights Eqn A3
Compute partition functions Eqn A5
Compute volume fractions Eqn A7
Compute interactions Eqn A9

Update Lagrange field: $\alpha(z) := \alpha(z) + \beta(\varphi(z) + \varphi_v(z) - 1)$

Update 'interactions':
\[
E(z) := \beta(E(z)) + (1 - \beta)E^0(z) \\
E_V(z) := \beta(E_V(z)) + (1 - \beta)E_V^0(z)
\]

Compute error: $\text{error} = |E(z) - E^0(z)| + |E_V(z) - E_V^0(z)| + |\varphi(z) + \varphi_v(z) - 1|$

Compute grand potential Eqn A11 and write results.
SI 1: Calculation of $\theta_{\text{kink}}$

$\theta_{\text{kink}}$ can be calculated using $\cos \theta_{\text{kink}} = \frac{R_i}{R_p}$ and $R_p$ can be calculated from the input variables for the surface structure (see Table 1): $R_i$ is $(h - R_p)$ and $R_p$ is $\frac{1}{2}d$. 

*Figure SI 1: calculation of $\theta_{\text{kink}}$ (indicated in the picture as $\beta'$)*
SI 2: calculation of $\Phi_S$ and $s$ at constant $\Phi_S$

To calculate $\Phi_S$, first the area per cavity is calculated for a hexagonal packing.

![Diagram of hexagonal packing](image)

Figure SI 2: calculation of area per cavity.

$R_p$, which is in this case equal to $\frac{1}{2} s$ (Table 1), is related to $L$ via:

$$R_p = \frac{1/2 \cdot L}{\tan(30)} = \frac{\sqrt{3}}{2} L$$

The area per cavity $A_{\text{hexagon}}$ is then given by adding the areas of 12 triangles, i.e., 12 times $(1/2 \cdot R_p \cdot 1/2 \cdot L)$.

The area of a cavity $A_{\text{cavity}}$ is the area of a circle with radius $R_h$ (see SI 1). Since $d$ and $R_i$ are input parameters, $R_h$ is obtained via Pythagorean theorem, and $A_{\text{cavity}} = \pi (R_h)^2$

The fraction of solid on the top surface $\Phi_S$ is then given by

$$\Phi_S = 1 - \frac{A_{\text{cavity}}}{A_{\text{hexagon}}}$$

To calculate $s$ for different $c$ at constant $\Phi_S$, first, a constant $\Phi_S$ has to be defined. This sets the ratio $A_{\text{cavity}}:A_{\text{hexagon}}$. The cavity size depends on the value of $c$, and since the ratio is fixed, $A_{\text{hexagon}}$ is obtained per $c$. This area is used to calculated to an effective $R_{p,\text{effective}}$, and next a surface can be created with $s = 2 \cdot R_{p,\text{effective}}$. 
6 General discussion
We can learn from nature that, next to chemistry, surface structures can be used for tuning different functions of surfaces. In this thesis we presented new approaches that we developed to make bioinspired nanopatterned surfaces. We use these surfaces to study the effect of structuring on two functions namely adhesion and wetting.

In Chapters 2 and 4, we presented a novel fabrication method using colloidal templating. We described two distinct ways to obtain nanopatterned surfaces, namely (i) addition of PDMS on top of the colloidal monolayer and (ii) synthesis of polypyrrole around the particles of the monolayer, and we have shown the influence of these patterns on adhesion and wetting, respectively. In this chapter, we look back on what we have achieved and we put this in the broader context of research in the same area. We thus discuss some aspects of the fabrication of the nanopatterned surfaces, and the adhesion and wetting thereof.

### 6.1 Fabrication of nanopatterned surfaces

In this thesis, we chose colloidal templating to make nanopatterned surfaces. The use of colloidal assemblies to create surface patterns is an emerging research area and highly relevant. This is, for example, evidenced by a Feature Article entitled “Colloidal Surface Assemblies: Nanotechnology Meets Bioinspiration”.¹ The authors state that:

“Colloidal lithography holds great promise for realization of powerful hierarchical templates in silicon for molding polymers (e.g., PDMS) that is expected to mimic the nanostructure found on Gecko toes.”

and

“Colloidal particles form an interesting basis for bioinspired processes and structures. Artificial particles are sufficiently well understood and robust to employ them in material synthesis. They are easier to observe and analyze than softer objects such as proteins. They are also more familiar to industry. Processes that employ particles are therefore realistic candidates for actual production processes.”

Colloidal templating allows us to fabricate complex, 3D structures. Our structures have the same dimensions as found in nature, and are
repeated over macroscopic length scales.\textsuperscript{1-2} Furthermore, this method is fast and cost-effective compared to other nanopatterning techniques.

\section*{6.1.1 Colloidal monolayer}

\subsection*{Obtaining the colloidal monolayer}

Highly charged, monodispersed particles are required for colloidal templating, and these were not commercially available. A robust synthesis method has been developed, and monolayers suitable for templating consisting of these particles, with sizes in the range $500 \text{ nm} < d < 1.2 \text{ \mu m}$, were readily obtained in a one-step synthesis.\textsuperscript{3}

The fabrication of our nanopatterned materials started with a monolayer of colloids. Colloids are readily trapped at the air/water interface, but care must be taken to spread the particles homogeneously into a monolayer at the interface.\textsuperscript{4} To ensure monolayer formation, two methods are described in the literature: (i) application of particles at the air/water interface using a glass slide and using an alcohol as spreading agent\textsuperscript{5-6} and (ii) coating a surface with a sparse layer of (individual) particles, and dip this surface slowly in the water phase under an angle, so that the particles self-assemble at the air/water interface.\textsuperscript{7} The first method only requires transferring the particles to another solvent, whereas the second method contains multiple steps and is more time consuming. Therefore, the first method has been chosen.

\subsection*{Crystallinity of the monolayer}

A high crystallinity is desirable because a crystalline, hexagonal packing is the packing with highest particle density, resulting in regular structures and the possibility to model the surface structures. We investigated two parameters to control crystallinity, namely pH and ionic strength, $c_s$.

A high crystallinity is obtained when repulsion between the particles is combined with an external pressure pushing the particles together. This situation is difficult to achieve experimentally, since certain interactions are intrinsic to (charged) particles at interfaces. DLVO interactions, which include Born repulsion preventing two particles...
from overlapping, attractive Van der Waals interaction and electrostatic repulsion, are always found between two closely-spaced surfaces. Two additional forces that are found for particles at the interface are (i) attractive capillary interaction due to interface deformation, and (ii) repulsive dipole-dipole interactions. The first contribution is small in our case, since our particles are also small. The second contribution, however, is important. An asymmetric charge distribution arises due to dissociation of the $-\text{COOH}$-groups in water phase, but not in the air. Therefore, the counter-ion distribution is also asymmetrical. This causes a dipole moment perpendicular to the air/water interface for each particle, and because the particles are pinned at the interface, the dipoles cannot align, resulting in repulsion.

To obtain closely packed crystalline monolayers at the air/water interface, a high charge density on the particle surface is needed. A higher charge density results in more repulsion and therefore a higher mobility of the particles. For our particles, which contain $-\text{COOH}$ groups on their surface, the number of charges increases with pH. We indeed found an increase in crystallinity with increasing pH. The effect of $c_s$ on crystallinity however, has not yet been discussed.

$c_s$ is commonly used to control the interaction between charged objects in water. It sets the screening length between two charges: the higher the salt concentration, the shorter the Debye screening length $\kappa^{-1}$. On the other hand, a higher $c_s$ enables dissociation of $-\text{COOH}$ groups. The increase in charges with increasing ionic strength also results in more hydrophilic particles. The overall effect of changing the $c_s$ is hence not straightforward. Therefore, the effect of $c_s$ on crystallinity has been investigated for both CP and CP-W (Figure 1). CP are particles that are transferred to ethanol directly after synthesis, whereas CP-W are washed three times in water before transfer to ethanol. CP-W thus contains less oligomers than CP. The normalized crystallinity is defined as the ratio between particles with six neighbouring particles over the total number of particles. This was determined by scooping the monolayers from the air/water interface using a coverslip and imaging them using a brightfield microscope.

Figure 1 shows no effect of $c_s$ on crystallinity for both CP and CP-W. The trend that seems to be present for CP is mainly caused by the low crystallinity at an $c_s$ of $10^{-5}$ M, but this is not conclusive, given the spread.
in crystallinity for CP-W at $c_s$ of 0.001 M and 0.1 M. $c_s$ can thus not be used to tune the crystallinity, and careful control over $c_s$ is not required when making the monolayers.

Figure 1: Normalized crystallinity as function of ionic strength, $c_s$, for ▲) particles, CP, and ◆) washed particles, CP-W. The error bars show the standard deviation.

Packing density of the particles

Using our carboxylated polystyrene particles only results in close-packed monolayers at the air/water surface. This limits the possibilities for making different surface structures, because the centres of the features are always spaced one particle diameter apart.

The feature density can be increased by using binary crystals.\textsuperscript{11-12} These crystals exist of particles with two different diameters. The smaller particles can fill the interstitial sites of the larger particles. Different structures can be made using different combinations of sizes and different stoichiometry of the particles.\textsuperscript{2}

To decrease the particle density at an interface, long range repulsion is needed. Some particles exhibit this long-range repulsion at the air/water interface.\textsuperscript{13-15} A water/oil interface may also be suitable.\textsuperscript{16-18} The increase in repulsion for this interface compared to an air/water interface can be ascribed to a stronger dipole-dipole repulsion, and possibly unscreened charges at the part of the particle’s surface that sticks in the oil phase.\textsuperscript{2}
Influence of oligomers

Another parameter influencing the properties of the monolayer, is the presence of oligomers, originating from the particles, between the particles in the monolayer. These short itaconic acid-styrene polymer chains acted as a “glue” between the particles for CP, preserving high crystallinity even when the pH of the subphase was changed to a value below the $pK_{a1}$ of itaconic acid after monolayer formation. Removing oligomers by washing the particles (CP-W), resulted in higher mobility compared to the particles that were not washed (CP); crystallinity was decreased when the pH was brought to a low value.

The washing procedure was not completely reproducible, since a new CP-W stock from the same CP stock, did not result in the same monolayer characteristics; the mobility of the particles in this second CP-W stock was even larger and the yield at the air/water interface was smaller. Furthermore, SEM images indicated that an oligomer cohesive layer was still formed using the CP-W stock (see Figure 2), indicating that a substantial amount of oligomers were still present.

![SEM image of CP-W particles](image)

*Figure 2: SEM image of CP-W particles, scooped up from the air/water interface and dried in a vacuum oven. Scale bar is 1 μm.*

To remove these oligomers, the particles were cleaned even more thoroughly by steam distillation: the suspension of particles in water was heated to 80°C and flushed with nitrogen for ~30 min before
exchange to ethanol. This resulted in particles (CP-SD) with high mobility in the monolayer and very small yields at high pH. Monolayers with very mobile particles are unsuitable for further processing: both PDMS templating and PPy interfacial polymerization entail perturbations of the monolayer. These very clean particles could thus not be used as template for nanopatterned surfaces.

6.1.2 Templating the colloidal monolayer

Cohesion of particles within the monolayer

The presence of the oligomers proved to be vital for using the colloidal monolayer as template, yet this parameter was not well-controlled. Nanopatterned surfaces could only be fabricated reproducibly when using the particles of the same batch. To make the overall fabrication process reproducible, oligomer-free particles should be the starting point, and another method of reducing the mobility of the particles within a monolayer should be used. Ideally, to preserve the crystallinity, a cohesive layer should be formed after the particles self-assembled in a monolayer. One method is to add long polyethylene oxide polymers to the water phase after monolayer formation. The long polymers bridge between the particles, enhancing close packing, and preventing particles from rearranging during further processing of the monolayer. This method is only suitable if particles are templated via the gas phase. Templating via the water phase would result in incorporation of the polyethylene oxide polymers in the material of choice.

It has also been found that adding a surfactant increases the mechanical stability of a monolayer at the air/water interface. The surfactant molecules assemble at the air/water interface due to their amphiphilic nature and this creates forces at the interface, pushing the particles together.

Another approach would be using cyanoacrylate layers. Cyanoacrylate monomers can be introduced via the gas phase. The thickness of the polymer matrix can be varied, from a layer thicker than the particle diameter using butyl cyanoacrylate to a thin layer only at the air/water interface using ethyl cyanoacrylate. A SEM image of the
thin ethyl cyanoacrylate layer, made as described in Chapter 2, is shown in Figure 3.

![SEM image of a colloidal monolayer embedded in ethyl cyanoacrylate](image)

*Figure 3: SEM image of a colloidal monolayer embedded in ethyl cyanoacrylate. The contrast of this image is adjusted. Scale bar is 1 µm.*

The cyanoacrylate layer can provide enough strength during further processing of the monolayer, and is readily removed by an organic solvent when dissolving the particles.

Gel trapping techniques, in which the liquid phase is turned into a hydrogel after monolayer formation, may also be a promising method to immobilize the particles at the air/water interface. This method has indeed been used to trap particles and replicate them with PDMS. However, most of these gelling agents are dissolved at elevated temperatures, and set at room temperature. The particles should therefore be applied at elevated temperatures ( > 50 °C ), which we found to be disruptive for the formation of a close-packed crystalline monolayer.

**Double molding**

With one monolayer, two different surface structures can be fabricated, by either templating the air phase, or the water phase. However, the material of choice depends on the method of application: for example, PDMS cannot be applied via the water phase, and polypyrrole not via air. This limits the possible structures to be templated by PDMS to dimples and that of polypyrrole to a surface
structures with overhangs, if only direct templating is used. The properties of the two materials are very different: PDMS is an elastomer, whereas polypyrrole is a rigid material. A surface with the same structure, but consisting of a different material, may have different properties. It is therefore interesting to make the two different structures with the same material. A method to obtain PDMS surface structures as if it is templated via the liquid phase, is presented in Figure 4.

![Figure 4: Templating a colloidal monolayer with PDMS from the gas and liquid phase. A) PDMS is applied on top of a crystalline colloidal monolayer and cured. B) After removal from the water phase, the PDMS is silanized via vapour deposition. C) A second layer (PDMS 2) is applied on top of the first PDMS layer (PDMS 1). D) The two PDMS layers are peeled off and the particles are dissolved, resulting in dimples (PDMS 1) and an overhang structure (PDMS 2).]

The method follows the outline to obtain dimpled surface structures as presented in Chapter 2, but instead of removing the particles, the PDMS and particles are silanized. This makes the surface suitable for adding a second PDMS layer, because the silane layer prevents the new PDMS from sticking to the first PDMS layer. The two layers can therefore be easily peeled off from each other, resulting, after dissolving the particles, in a dimpled surface structure and a surface with overhang structures.
Attempts to make the PDMS 2 surface structure (see Figure 4) were unsuccessful due to the presence of the oligomers. These formed, also for CP-W, a layer between the particles (see Figure 3). The PDMS 2 surface structure consisted also of dimples, and was thus not of interest.

However, if we succeed in making this method work, the subtle differences in immersion depth due to ionic strength can be employed. Another method that may change the immersion depth of the particles, is the adsorption of surfactants\(^7\) or other small molecules. Ideally, these molecules should increase the hydrophobicity of the particles, thereby decreasing immersion depth. However, they should be introduced via the water phase, preferentially after monolayer formation, and should therefore be soluble in water. This limits the hydrophobicity that can be introduced via these surfactant.

Molding after transfer to solid substrate

Another method to obtain surface structures with overhangs is to scoop the particles from the air/water interface using a surface with a spincoated polystyrene layer.\(^{22}\) PDMS can be poured on top of the monolayer and cured, and the nanopatterned surface is released when the spincoated layer and the particles are dissolved. Again, this only works with particles without oligomer residues, and the surface structure cannot be adjusted by changing the immersion depth of the particles. This method is therefore a complement to the method outlined in Figure 4.

Transferring the particles to a solid substrate before templating can also be used as first step to decrease the particle density. To do so, reactive ion etching can be employed to reduce the particle size.\(^{20, 23-24}\) If the substrate is PDMS or another elastomer, the interparticle distance can be increased by solvent swelling or stretching the substrate.\(^{25-26}\) This is a promising method once the fabrication method outlined in Figure 4 is functioning. PDMS 1 should be stretched to different extents before silanization and application of PDMS 2. After crosslinking PDMS 2, PDMS 1 can be removed. PDMS 2 can be silanized after which yet another layer of PDMS can be applied, resulting in a surface with dimples that are spaced further apart than in the original PDMS 1.
6.2 Adhesion

We have fabricated nanopatterned elastomer surfaces, and we have shown that the adhesion of these surfaces was increased up to 22% compared to a flat surface. The adhesion was tested against a macroscopic spherical probe, which is so large that it is virtually flat at the length scale of a dimple, and a microscopic spherical probe, which is within the same order of magnitude as the surface structures. First, we compare these values to adhesion found for other patterned surfaces after which we discuss our results.

6.2.1 Pull-off forces of patterned surfaces

To compare the effect of structuring on adhesion, we use the parameter \( \bar{F} \). This is the ratio between the pull-off force on structured surfaces to the pull-off force on a flat surface.

For our nanopatterned surfaces, we found \( 1.08 < \bar{F} < 1.22 \) for the macroscopic probe and \( 1.02 < \bar{F} < 1.16 \) for the microscopic probe. These values are similar to values found by others for larger dimples: the adhesion for surfaces with holes of \( 50 \mu m < d < 500 \mu m \), with varying depth, was found to be \( 0.9 < \bar{F} < 1.2 \) and pull-off forces of \( 0.840 < \bar{F} < 1.024 \) were found for surfaces with dimples with \( d = 24 \mu m \).

Figure 5: Schematic representation of different shapes of bio-inspired, dry adhesives. A) different pillar tops with i) normal pillar, ii) rounded tip, iii) spherical tip, iv) concave tip, v) one-sided overhang, vi) two-sided overhang (mushroom). B) Hierarchical structure, consisting of mushroom-shaped micropillars on top of mushroom-shaped macropillars.

In the field of dry adhesives, a lot of designs are inspired by the gecko’s feet, and consist of simpler versions of their surface structure.
An array of simple pillars resulted in $0.200 < \bar{F} < 1.50$. Modification of the tip of the pillar changed adhesion tremendously: whereas rounding the edges, a spherical tip, and a concave tip where found to decrease the adhesion, pillars with overhang structures, either one-sided or two-sided (mushroom) structure, increased adhesion, at high preloads even up to $\bar{F} \approx 30$. The shapes of the different tips are shown in Figure 5A.

Since the gecko’s toepads have an hierarchical structure, much effort in the search for high $\bar{F}$ has been dedicated to make hierarchical structures. For example, one structure consisted of mushroom shaped micropillars on top of mushroom shaped macropillars (see Figure 5B). The resulting adhesion is $\bar{F} \approx 4.5$. Given the complexity of surface structure fabrication and our limited knowledge on the effect of simple surface structures on adhesion, one can wonder whether this is a promising route.

Another, more robust method to make patterned surfaces to tune the adhesion is via wrinkling. The effect of wrinkling on pull-off force resulted in $0.05 < \bar{F} < 1.9$. The decrease in adhesion, also compared to our dimpled surfaces, can be attributed to the reduced contact area due to high amplitudes, and the increase in number of crack initiation sites for the wrinkled surfaces.

$\bar{F}$ of our surfaces is for the (limited number of) surface structures presented here, of the same order of magnitude. The exception is the adhesion of mushroom pillars. The shape of the tip is thus important for the final adhesion. Different tips of the structures can be obtained using colloidal lithography if the immersion depth of the particles can be controlled. Therefore, we expect interesting adhesive behaviour for the different structures that are possible to fabricate using colloidal templating.

### 6.2.2 Effect of dimple density and dimple depth

In Chapter 3, the adhesion was tested using three nanopatterned surfaces. The surfaces differed both in dimple depth and dimple density. Therefore, it was not possible to differentiate between the effect of a single parameter on adhesion. For the tests with the macroscopic probe, we found that an increase in dimple density and an increase in dimple
depth result in higher adhesion, whereas for the colloidal probe, the
dimple density seemed to be the dominating effect.

To study the effect of dimple density on adhesion separate from
the dimple depth, binary crystals can be used or the interparticle
distance can be modified, as discussed above. It is expected that a
decreasing dimple density leads to decreasing adhesion, at least for the
structures consisting of shallow dimples. Ideally, a clear correlation
between dimple density and adhesion is found. With this relation, a high
crystallinity (and thus high dimple density) is not always needed, as
long as the particles are homogeneously distributed.

The effect of dimple depth on adhesion is less straightforward, and
therefore more interesting. Three different surface structures that can
be created with a crystalline colloidal monolayer are shown in Figure
6CD, and a schematic outline of a possible route of fabrication to show
the effect of immersion depth on final surface structure, is shown in
Figure 6AB.

![Figure 6: Effect of immersion depth of the particles on final surface
structure. A) Superposition of three immersion depths of the particles in
the water phase, as indicated with the three (dashed) lines; B) PDMS
1–3 is applied at the former air/water interface, as indicated with the
three (dashed) lines; C,D) the particles are removed, resulting in three
different PDMS surface structures, which are shown C) superimposed,
and D) separately. Image by A.W. Jongerius.](image)
In this thesis, the adhesion of D1 in Figure 6 has been discussed, and it has been found that a higher dimple depth, thus lower immersion depth, resulted in an increase in adhesion for the macroscopic sphere as counter surface. This may be the case for dimple depths up to that of Figure 6 D2. A prerequisite for adhesion enhancement is that the surface is in full contact with the counter surface. In Chapter 3, equation 11 we have seen that a spontaneous jump-to-contact is expected for dimples up to 0.6 μm. Since our particles have a radius < 0.6 μm, full contact is expected, and hence adhesion enhancement for macroscopic counter surfaces.

The effect on adhesion of structure D3 is less easy to predict.

These structures have an overhang structure, similar to a mushroom shape. The stress distribution on these shapes are such that the highest stress is not located at the edge of a post. Therefore, crack initiation must start in the middle of the post which requires much more energy, and thus a higher pull-off force is expected.

A third important factor, is that these surface structures are quite fragile: the PDMS structures with overhang can be regarded as consisting of triangular pillars with touching overhang structures. These pillars are very narrow at the thinnest point. Adhesion could be so strong that detachment results in structure destruction due to cohesive failure. It could therefore become necessary to strengthen the structure. A method to accomplish this, is to fill the dimples with a viscous material. This may not interfere with the advantage of dry adhesives, namely its reusability; it has been found that a viscoelastic PDMS film shows interfacial failure, rather than cohesive failure, for small feature sizes.

So far, we have seen that the shallow dimples that we have fabricated, showed a pronounced effect on adhesion. Other studies show that the shape of the tip influences the final adhesion significantly, and that mushroom shapes can increase adhesion tremendously. Fabricating this structure and measuring its adhesion is therefore the most interesting next step in this line of research.
6.3 Wetting

6.3.1 Wetting of PPY-iccms

We investigated the wetting of polypyrrole inverse crystalline colloidal monolayers (PPy-iccms). The hexagonal packing, the overhang structure and the length scale of these PPy-iccms reminded us of the surface structures of springtails. Springtails are able to entrap air in their (hierarchical) surface structure when immersed in liquids, allowing them to avoid suffocation.37-38 Air entrapment in any surface structure can lead to an increase in the contact angle $\theta$. For hydrophilic surfaces, air entrapment is only possible if an energy barrier prevents the air bubble from escaping.39 A hypothesis is that the presence of re-entrant angles in the surface structure provides this barrier.39-48 Reason enough to expect interesting phenomena to arise when wetting of PPy-iccms is studied.

We have seen that $\theta$ of water droplets on our hydrophilic material was indeed $> 90^\circ$. It was not possible to conclude from our experiments directly whether air was entrapped in the PPy-iccms or not. To obtain more insight in the wetting at small length scales, modelling studies were carried out (Chapter 5). In our models, depinning transitions were found, and these pinning effects are important for the final droplet shape, which is discussed in terms of $\theta$. Whether cavities under the droplet were filled with liquid (Wenzel wetting state) or vapour (Cassie-Baxter wetting state) did not matter for $\theta$. Furthermore, in the models we found that the complete 3D structure of a surface determines the $\theta$, and this cannot be reduced to one parameter, such as the angle of a kink in the surface.

We thus showed that we could model droplets of liquid on structured surfaces, and that in this way we could indeed find $\theta > 90^\circ$ on hydrophilic materials. However, our model is a simple one, and does not capture every detail of the experimental system. We know, for example, that our model does not represent water molecules realistically. It is therefore the question how to interpret the outcomes. It would be an indication that our model captured all relevant parameters if we experimentally can find trends that were predicted using our model.
Chapter 6

Trends in contact angle have been predicted as function of (i) cavity diameter (ii) surface wettability, (iii) cavity cut-off height, (iv) spacing between the cavities, and high contact angle hysteresis was also found. This part of the General Discussion will be mainly dedicated to validate our modelling via (new) experimental results.

6.3.2 Effect of cavity diameter on wetting

The cavity diameter only influences the droplet shape if water condenses in the cavities, resulting in an impregnated wetting state. This only happens for very small cavities according to our models. To test this trend, very small particles (<10 nm) should be used for templating, which is with our fabrication method not possible.

6.3.3 Effect of surface wettability on wetting

The influence of the surface wettability on the final droplet shape was found to be twofold: the surface structures decreased $\theta$ for materials with $\theta_Y < 60^\circ$, and increased $\theta$ for $\theta_Y > 60^\circ$. To test whether this could also be observed experimentally, PPy-iccms were modified in two ways: PPy-iccms were sputtered with gold to decrease $\theta_Y$, and silanized with trichloro (1H, 1H, 2H, 2H-perfluorooctyl)silane to increase the $\theta_Y$. Water wets a clean gold surface completely ($\theta_Y = 0^\circ$), although in practice organic contaminations increase $\theta_Y$. The $\theta_Y$ of the silane is $98^\circ$. The apparent contact angles of water on the (treated) PPy-iccms are shown in Figure 7.

The $\theta$ of the silanized PPy-iccm is indeed higher ($\sim 10^\circ$) than $\theta$ of the non-treated surface. However, coating the surface with gold does not result in a lower $\theta$ for the structured surface compared to a flat surface, although a decrease was predicted. The deviation can be explained in three ways: (i) our model is not valid; (ii) the gold layer was already contaminated and $\theta_Y$ for this contaminated layer is larger than the $\theta$ we measured on the PPy-iccms; or (iii) the inhomogeneous distribution of gold on the PPy-iccms caused an increase in $\theta$. Gold was deposited vertically on the surfaces. Only the top surface was thereby coated in a thin gold layer, leaving the cavities unaffected. This variation in surface chemistry may lead to air entrapment, rather than filling the
General Discussion

Figure 7: Contact angle of water on different polypyrrole inverse crystalline colloidal monolayers (PPy-iccms), with  PPy-iccm,  silanized PPy-iccm and  PPy-iccm coated in gold. Scale bars are 1 μm.

cavities with water. Since there are multiple explanations for the deviation from the predicted trend, we cannot use these experiments to test our model.

6.3.4 Effect of cavity cut-off height on wetting

The \( \theta \) of a liquid on the PPy-iccms was found to depend on the cut-off height \( c \), which is defined as the ratio between the cavity depth and the diameter of templated particles. The \( \theta \) showed a maximum around \( c = 0.8 \). It is difficult to systematically change the cut-off height with our system. Luckily, the influence of \( c \) on \( \theta \) was studied for a gold iccm surface.\(^4\) Smaller particles were used (diameter = 500 nm), and gold was grown to various thicknesses using electrodeposition.

The \( \theta \) is higher than \( \theta_Y \) of water on gold for all surface structures, and a maximum is present (see Figure 8). However, unlike our model, the highest \( \theta \) is found for \( c \approx 0.4 \). Also, the increase in \( \theta \) due to surface structuring, is found to be higher for the experiment than in our modelling work. Unfortunately, \( \theta \) on a flat substrate has not be determined in the article, making it even more difficult to compare.

It is interesting to see that \( \theta \) also increased with increasing \( c \) for dimpled surfaces ( \( < 0.5 \)). Air entrapment is, due to the absence of re-entrant angles, not expected. The most likely hypothesis for the variation in \( \theta \) due to structuring, is therefore pinning effects, which is in line with the conclusions of our modelling work.
6.3.5 Effect of cavity spacing on wetting

In our models, we could change the spacing between particles without any trouble and it was predicted that air entrapment occurs for lower values of $c$ when the cavities are closer together. It is more challenging to do so experimentally, and this has therefore not yet been done.

By choosing PPy, only fabrication methods with the particles directly at the water interface, can be used. To obtain a non-close packed monolayer, the air/water interface can be replaced by an oil/water interface. The pyrrole monomers may dissolve to a certain extent in this new phase, but since the polymerization only occurs at the oil/water or particle/water interface (because the oxidant is dissolved in water), PPy will only be synthetized at oil/water interface or particle/water, which is exactly where it is needed.

Particles cannot be packed closer than their diameter apart. A surface structure with smaller distances between the cavities can therefore not be fabricated with a simple monolayer consisting of monodisperse particles. Rather, one has to switch to binary crystal
colloidal monolayers. The angle of overhang may not be the same for the larger and the smaller colloids.

**6.3.6 Contact angle hysteresis**

Another phenomenon found in our models, is a large contact angle hysteresis: θ of an advancing water droplet is almost 80° higher than that of a receding water droplet. The low θ_{receding} in our models is caused by (i) pinning effects, and, in most cases, (ii) the presence of water instead of air in the cavities directly in front of the receding contact line. The contact angle hysteresis has also been found experimentally: θ on a PPy-iccm for an advancing droplet is indeed > 80° compared to that of a receding droplet (Figure 9).

![Figure 9: Picture of a water droplet on an inverse crystalline colloidal monolayer made from polypyrrole, for A) an advancing droplet; and B) a receding droplet.](image)

The experimental data on the influence of c on θ also seem to indicate that pinning effects may be responsible for the high θ on inverse opals, and the high contact angle hysteresis has also been found experimentally. This suggests that our simple model captures rich (wetting) behaviour, and that this method can be used to screen for interesting effects of surface structures on wetting.

However, the advantage of our model is also its disadvantage: our model is indeed a very simple one. The liquid phase, as said, does not capture all characteristics of a real solvent, and the surfaces in our model are completely smooth and clean, without any chemical inhomogeneity. Our PPy-iccms show a more complex geometry, and the
particle residues, probably present as adsorbed polymers, are not taken into account. After these improvements are included in the model, even more interesting phenomena and insights are expected to be observed.

6.4 Outlook

Suggestions for research directions that directly follow from this thesis, have been presented in the previous paragraphs. As a closing remark, we would like to present the ultimate goal: the development of a comprehensive model that can predict the surface functions once the surface structure is given as input, and, conversely, can suggest a surface structure design based on the input of desired functions.

To do so, the effect of surface structuring should be understood for all functions. In this thesis, only two functions are discussed, and not even to their full extent. For example, for wetting one can also think of superhydrophobicity or non-wetting to prevent ice formation, selective wetting for water/oil separation, or directional wetting.

Eventually, if our understanding of surface structuring on functions is sufficient, one can dream of one surface with different functions, just as is found in nature, and use the model to present the surface structure that should provide all desired characteristics. Hopefully the outcome is a design of a structure that can be fabricated experimentally, for example using a pipette, plastic Petri dish, some particles dispersed in ethanol and a not-so-clean room.

References


7 Summary
Nature shows remarkable examples of functions derived from surface structures. In this thesis, called “Bioinspired nanopatterned surfaces via colloidal templating; a pathway for tuning wetting and adhesion” we studied the effect of surface structuring on adhesion and wetting. Wetting and adhesion is largely understood for perfectly flat and clean surfaces, but switching to the real (and contaminated) world proves to be hard. Predicting the relationship between surface patterns and functions is therefore not yet possible for every surface structure design, but would be desirable. Making nanopatterned surfaces in a controlled way is the first step towards systematically studying the effect of structuring on different functions.

In Chapter 2, we present our fabrication method, namely colloidal templating. We synthesized anionic colloidal particles (450 < diameter (nm) < 1150), consisting of copolymers of styrene with itaconic acid, with parking areas of 0.11 nm$^2$ per –COOH group. These particles form a monolayer at the air/water interface. The crystallinity of these monolayers and the immersion depth of the particles can be controlled by the pH and ionic strength of the water phase. It is shown that the crystallinity increases with increasing dissociation of the –COOH groups on the particles, at pH > pK$_{a1}$ of itaconic acid: the increased electrostatic repulsion overcomes the attractive Van der Waals interactions, resulting in higher particle mobility. It was found that a higher ionic strength leads to a higher particle immersion depth. The monolayer can be used without pattern disruption of the template by careful application of PDMS, showing that control over the monolayer leads to control over the final surface pattern. After crosslinking, the particles are easily removed, resulting in elastomeric surfaces with dimples.

The nanopatterned PDMS described in Chapter 2 are used for adhesion experiments in Chapter 3. Three patterned surfaces, with varying dimple depth and dimple density, were selected. A macroscopic probe (diameter = 4.76 mm) and a colloidal probe (diameter = 8 µm) were used as counter surface to probe different length scales. Adhesion enhancement compared to a flat control was found for all three surfaces and both probe sizes. The origin of this increase in adhesion is attributed to energy dissipation whereby each dimple acts as an unstable crack propagation site.
Summary

In Chapter 4, another method to make nanopatterned surfaces using the same colloidal monolayer, is presented. Pyrrole is added to the water phase, and allowed to swell the particles in the monolayer. Subsequently, ferric chloride is added, and the presence of this oxidant starts the polymerization of pyrrole at the particle/water interface. The particles are dissolved afterwards, yielding a polypyrrole inverse crystalline colloidal monolayer (PPy-iccm). Different surface structures can be obtained by choosing the amount of pyrrole, the pyrrole: oxidant ratio and the polymerization time. The final PPy-iccms have cavities and a small angle of overhang because the particles were for ~90% immersed in the water phase. The contact angle $\theta$ of water on three different PPy-iccms is found to be similar with a value of ~110°, whereas the $\theta$ on the control surface consisting of flat PPy with particle residues is found to be 83°. Due to the pattern, the surface thus appears to be hydrophobic, although the material is hydrophilic. This may indicate that air is entrapped in the cavities of the surface structures.

To understand this increase in $\theta$ and thereby the origin of observing a hydrophobic contact angle on a hydrophilic surface, we employed modelling. In Chapter 5, we present this work. The regular solutions theory is extended to 3 dimensions, and this allows for finding droplet shapes on inverse opals in short computation time (~10 minutes). The effect of particle size $d$, surface wettability $\chi_{SL}$, immersion depth (using the cut-off height $c$), and particle spacing $s$ was studied. Both scenarios with water-filled cavities and air-filled cavities have been found, but the trend in $\theta$ did not show a discontinuity upon switching from water-filled to air-filled. This suggests that air entrapment is not responsible for the increase in $\theta$. Rather, the increase in $\theta$ is attributed to pinning effects, whereby the air/water/surface contact line is fixed at one position. Our model suggests that these pinning effects are not limited to small surface structure angles, since pinning was also found for obtuse angles. Pinning is furthermore influenced by the full 3D structure of a surface, not just to kinks in the surface.

The last chapter, Chapter 6, places our research in a broader context. Suggestions to improve control over the monolayer and to fabricate different nanopatterned elastomers are presented. Adhesion of our nanopatterned surfaces is compared to that of surfaces from literature, and we speculate on the effect of different surface structures
on adhesion. Furthermore, extra experimental data is provided to test predictions concerning wetting from our modelling work. As final paragraph, our ultimate goal is revealed: improve our understanding of the effect of structuring on functions to such an extent, that a comprehensive model can be made, which can predict the functions based on the surface structure, and vice versa.
8 Samenvatting
In de natuur zijn er opmerkelijke voorbeelden te vinden van functie door structuur. In dit proefschrift, genaamd “Bioinspired nanopatterned surfaces via colloidal templating; a pathway for tuning wetting and adhesion”, hebben we het effect van oppervlakstructuren op adhesie en bevochtiging bestudeerd. Adhesie en bevochtiging van perfect gladde en schone oppervlakken is grotendeels bekend, maar als we de overstap naar de echte wereld maken, wordt het lastiger. Het is daarom nog niet mogelijk om het verband tussen de oppervlaktestructuur en de functionaliteit te voorspellen voor elke oppervlaktestructuur, maar dit is wel wenselijk. Een systematische studie van het effect van oppervlaktestructuur op de functionaliteiten is daarom wenselijk. De eerste stap in deze studie is het maken van gestructureerde oppervlakten op de nanometer schaal op een gecontroleerde wijze.

In Hoofdstuk 2 laten we onze aanpak zien, namelijk het gebruiken van kolloïiden als mal. We hebben kolloïdale deeltjes (450 < diameter (nm) < 1150) met negatieve lading gemaakt, die bestaan uit copolymeren van styreen met itaconzuur, met op gemiddeld elke 0.11 nm^2 een –COOH-groep. Deze deeltjes vormen een monolaag op het luch/water grensvlak. De kristalliniteit van deze monolagen en de inzinkdiepte van de deeltjes kunnen worden ingesteld met behulp van de pH en de zoutsterkte van de waterfase. We laten zien dat de kristalliniteit toeneemt met toegenomen dissociatie van de –COOH-groepen op het oppervlak van de deeltjes als de pH hoger ligt dan de pK\textsubscript{a1} van itaconzuur: de toegenomen elektrostatische afstoting domineert de aantrekkingskracht van de Van der Waals-interactie, wat resulteert in een hogere mobiliteit van de deeltjes. Ook vonden we dat een hogere zoutsterkte resulteerde in een grotere inzinkdiepte van de deeltjes. De monolaag kan, zonder dat de ordening wordt verstoord, worden gebruikt als mal, door er voorzichtig PDMS op te gieten. Hierdoor leidt controle over de monolaag direct tot controle over de uiteindelijke structuur. Nadat het PDMS is gecrosslinked, kunnen de deeltjes makkelijk worden opgelost, wat resulteert in een rubberen oppervlak met kuiltjes.

De oppervlakten van PDMS met nanostructuren die zijn beschreven in Hoofdstuk 2, zijn gebruikt voor adhesiemetingen in Hoofdstuk 3. We hebben drie gepatroneerde oppervlakten, met variërende kuildiepten en kuildichtheden, geselecteerd. Een
macroscopische bol (diameter = 4.76 mm) en een microscopische bol (diameter = 8 µm) zijn gebruikt om de adhesie op verschillende lengteschalen te meten. Een toename in adhesie in vergelijking met de adhesie op een glad oppervlak, is gevonden voor alle gepatroneerde monsters en beide bolgroottes. De verklaring voor deze toename is toegeschreven aan dissipatie van energie, waarbij elk kuiltje dient als locatie voor het instabiel loslaten van het rubberen oppervlak. In Hoofdstuk 4 wordt een andere manier om nanogepatroneerde oppervlakten met dezelfde kolloïdale monolaag te maken. Pyrrool wordt aan de waterfase toegevoegd, en verzamelt zich in de deeltjes van de monolaag. Vervolgens wordt ijzerchloride toegevoegd, en de aanwezigheid van deze oxidant start de polymerisatie van pyrrool op het deeltje/water grensvlak. De deeltjes worden naderhand opgelost, wat resulteert in een geïnverteerd kristallijne kolloïdale monolaag van polypyrrool (polypyrroole inverse crystalline colloidal monolayer, PPy-iccm). Verschillende oppervlaktenstructuren kunnen worden verkregen door de hoeveelheden pyrrool, de verhouding pyrrool : oxidant of de polymerisatietijd te variëren. De uiteindelijke PPy-iccms hebben holtes en een scherpe hoek aan de bovenkant, omdat de deeltjes voor ongeveer 90% in het water staken. De randhoek $\theta$ van water op drie verschillende PPy-iccms bleek in alle drie de gevallen ongeveer $\sim 110^\circ$ te zijn, terwijl $\theta$ op het controleoppervlak, bestaande uit glad PPy met resten van de deeltjes, $83^\circ$ bleek te zijn. De oppervlaktestruktuur zorgt er dus voor dat het oppervlakte hydrofoob lijkt, terwijl het gemaakt is van een hydrofiel materiaal. Dit zou erop kunnen wijzen dat er lucht in de holtes achterblijft.

Om deze toename in randhoek te begrijpen, en daarmee een verklaring voor het vinden van een hydrofobe randhoek op een hydrofiel materiaal, hebben we gemodelleerd. We presenteren dit werk in Hoofdstuk 5. De regular solution theorie is uitgebreid naar drie dimensies, waardoor we de vorm van druppels op iccm’s kunnen vinden in korte rekentijd ($\sim 10$ minuten). De invloed van deeltjesgrootte $d$, bevochtigingseigenschappen van het oppervlak $\chi_{SL}$, inzinkdiepte van de deeltjes $c$ en afstand tussen de deeltjes $s$, is onderzocht. We hebben zowel scenario’s met lucht als met water in de holtes gevonden, maar we zagen geen discontinuïteit in het verband tussen de randhoek als de holtes van gevuld met water naar gevuld met lucht gingen. Dit suggereert dat het invangen van lucht niet de verklaring voor de
toename van $\theta$ kan zijn. Een verklaring die we met modelleren gevonden hebben, is dat de toename van verklaart $\theta$ kan worden doordat de druppel pint op een oppervlaktestructuur. Hierbij verplaatst de lucht/water/oppervlakte-contactlijn niet. Ons model suggereert dat deze pinningseffecten zich niet beperken tot structuren met kleine hoeken, want we hebben het ook gevonden voor stompe hoeken. Ook bleek de gehele 3D-structuur van een oppervlak belangrijk te zijn voor het pinnen van een druppel, en niet alleen een hoek in het oppervlak.

Het laatste hoofdstuk, nummer 6, plaatst ons onderzoek in een bredere context. We presenteren mogelijkheden om de monolaag beter te controleren en om verschillende structuren van rubber te maken. De adhesie van onze oppervlaktestructuren wordt vergeleken met literatuurwaarden, en we denken na over het effect van andere oppervlaktestructuren op adhesie. Ook wordt nieuw experimenteel werk gepresenteerd waarin de voorspellingen van ons modelleerwerk over bevochtiging, wordt bekeken. De allerlaatste paragraaf bespreekt ons uiteindelijke doel: het dusdanig vergroten van ons begrip over het verband tussen oppervlaktestructuren en functionaliteiten, dat we een alomvattend model kunnen maken dat functionaliteiten kan voorspellen op basis van oppervlaktestructuur, en omgekeerd.
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About the author

Sabine Akerboom was born on 14 January 1987 in The Hague, the Netherlands. She obtained her vwo diploma (secondary education) from the Fioretti College in 2005 and then moved to Wageningen to start her studies of Molecular Sciences. She obtained her Bsc in Molecular Science with a minor in Environmental chemistry and philosophy in September 2009. As part of her Msc, she carried out two research projects; At the Laboratory of Physical Chemistry and Colloid Science (later: Physical Chemistry and Soft Matter) of the Wageningen University, she worked on composite materials of silica particles with ABA-triblock copolymers. She worked on the adsorption of core/shell thermoresponsive microgels at the Applied Physical Chemistry group of TU Berlin. In October 2010 she graduated with an Msc in Molecular Life Sciences, and started her PhD research soon after at Physical Chemistry and Soft Matter in Wageningen. This thesis is the result.
List of publications

1. Akerboom, S; Kamperman, M; Leermakers F.A.M., Three-gradient regular solution model for simple liquids, wetting complex surface topologies (submitted)


Overview of completed training activities

**Discipline-specific activities**

Han-sur-Lesse winterschool  Han-sur-Lesse, Belgium,  2011&2012
Scattering summer school  Leuven , Belgium  2011
Conference on Adhesion  Lisbon, Portugal  2012
European Student Colloid Conference  Potsdam, Germany  2013
GRC Science of Adhesion  South Hadley, USA  2013
Dutch Polymer Days  Lunteren, The Netherlands  2014
GRC Biointerface Science  Barga, Italy  2014
Soft Matter Days  The Netherlands,  2011-2013

**General courses**

PhD Assessment  Wageningen  2011
Physics with Industry  Leiden  2011
Scientific Publishing  Wageningen  2012
Writing and presenting scientific research  Wageningen  2012
Pump your career  Amsterdam  2012
Share your results  Wageningen  2013
Career Orientation  Wageningen  2013
Career Assessment  Wageningen  2015

**Optionals**

PCC Meetings  Wageningen  2011-2015
Colloquia PCC  Wageningen  2011-2015
Organization PhD trip  Wageningen  2012-2013
PhD trip  California, USA  2013