## MSc Thesis

## Methods for mapping and linkage map integration in tetraploid potato.



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# "Let the sky rain potatoes" - Sir John Falstaff in Shakespeare - The Merry Wives of Windsor 

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Methods for mapping and linkage map integration in tetraploid potato


#### Abstract

Potato, Solanum tuberosum ssp. tuberosum, is an economically important crop. Cultivated potato is an autotetraploid with four homologs of every chromosome. Due to its polyploidy, genetic analysis of potato is more complicated than that of diploids. Linkage mapping is an important tool in genetic analysis, but due to the more complicated genetics, programmes or algorithms that can handle polyploid species are lacking or very basic. In this thesis, methods are presented to cover all the steps in linkage mapping process of autotetraploid crops. First, the recombination frequencies between simplex x nulliplex ( SxN ) markers are calculated and these markers are assigned to chromosomes on the basis of their pairwise LOD-scores. Thereafter, the markers are assigned to homologs based on a novel approach, namely a phase-tree, together with and duplex x nulliplex ( DxN ) linkages. The recombination frequencies and LOD-scores of these marker types, as well as those of others, were used in a linear regression approach for the ordering and position estimation of the markers on the homologs. As a final step, the homolog maps were integrated per chromosome using the graph theory approach of the R package LPmerge. This led to a high marker density integrated linkage map of potato which covered 1406.13 cM for 12 chromosomes with 5165 SNP markers. The integrated map has a high coverage and can be used for haplotyping, QTL analysis and as a reference linkage map.


Keywords: potato, autotetraploidy, linkage mapping, homologs, integration, LPmerge

## Samenvatting

Aardappel, Solanum tuberosum ssp. tuberosum, is een economisch belangrijk gewas. De gecultiveerde aardappel is een autotetraploide plant met vier homologen van elk chromosoom. Door de polyploïdie-graad is genetische analyse van aardappel gecompliceerder dan dat van diploïde planten. Het maken van een genetische kaart is een belangrijk gereedschap in de genetische analyse, maar door de complexe genetica zijn programmas of algoritmes die dit aankunnen afwezig of simpel. In deze thesis worden methodes gepresenteerd die alle stappen in het maken van een genetische kaart dekken van autotetraploïde gewassen. Allereerst werden de recombinatie frequenties tussen simplex x nulliplex ( SxN ) merkers berekend en werden deze merkers toegewezen aan chromosomen op de basis hun paarsgewijze LOD-scores. Daarna werden deze merkers toegewezen aan homologen op basis van een nieuwe techniek, namelijk een fase-boom, samen met DxN koppeling. De recombinatie frequenties en LOD-scores van deze merkertypes, alswel als de recombinatie frequencies en LODscores van andere merkertypes, werden gebruikt in een lineare regressie aanpak voor het ordenen van merkers en positie bepaling van de merkers op de homologen. Als laatste stap werden de homoloog kaarten geintegreerd per chromosoom door middel van de R-package LPmerge, die werkt met een grafentheorie. Dit leidde tot een genetische kaart van aardappel met een hoge merkerdichtheid die 1406.13 cM spant voor 12 chromosomen met5165 SNP merkers. De geintegreerde kaart heeft een hoge dekking en kan gebruikt worden voor haplotypering, QTL analyse, en als referentie kaart.

Trefwoorden: aardappel, autotetraploïdie, genetische kaart, homologen, integratie, LPmerge

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## Introduction

## Potato and polyploidy

Potato, Solanum tuberosum ssp. tuberosum, is the $5^{\text {th }}$ most produced crop globally, after sugar cane, maize, rice and wheat, with a production of 365 million mega tonnes in 2012 (FAOSTAT, 2012). The biggest producer of potato is China, but the origin of potato lies in the Andes of Chile (Hosaka \& Hanneman, 1988). From there on it was spread to other regions in Southern America and in the $16^{\text {th }}$ century was brought to Europe by the Spanish.

The origin and evolution of potato is intriguing, since the potato is an autotetraploid (Felcher et al., 2012), which means that is has four copies of every chromosomes (these copies are called homologues chromosomes or homologs) due to whole genome duplication arisen from unreduced gametes. Because potato is an autopolyploid ( $2 \mathrm{n}=4 \mathrm{x}=48$ ), and has polysomic inheritance ( Wu et al., 2002) , no preferential pairing of the chromosomes occurs in contrast with allopolyploids, like wheat, in which preferential pairing does happen (Jauhar et al., 1991). Autpolyploidy means that every homologous chromosome has an equal chance of pairing with any of the other homologs in meiosis. Potato has mainly bivalent pairing, although multivalent formation does occur sometimes (Gavrilenko et al., 2007), which in turn can lead to double reduction (Wu et al., 2002). Furthermore, potato is an outcrossing species suffering from inbreeding depression and has a high level of heterozygosity in its genome (The Potato Genome Sequencing Consortium, 2011).

## SNP markers

When molecular markers are considered for tetraploids, it is good to notice that nowadays SNPs are often used during genetic analysis. SNPs are markers that are polymorphic at a single nucleotide site and therefore four different alleles (GACT) can occur (Mammadov et al., 2012). SNPs are codominant and highly abundant in the genome, which makes them useful for all kinds of genome studies. Autopolyploidy means that during meiosis, the homologs form random pairs of bivalents or multivalents and for a highly heterozygous outbreeding species, like potato, this can result in a large number of allelic combinations. 36 genotypes could be found in the most extreme case if 8 different alleles segregate independently (Meyer et al., 1998). However, in this thesis the focus is on SNPs which are biallelic, which makes scoring more reliable. The markers can be assigned to five different dosage classes in tetraploids, namely nulliplex (aaaa), simplex (Aaaa), duplex (AAaa), triplex(AAAa) and quadruplex (AAAA) (Rifkin et al., 2012), while diploids have a maximum of three possible genotypes (aa, Aa and AA). It is good to keep in mind that every dosage can be converted by using symmetry argumentation, for example a triplex is a simplex for the other allele (Vukosavljev et al., 2014). Furthermore, the classification of these five classes takes only one parent into account, while during genetic studies usually two parents are crossed. Therefore the dosages of both parents are considered in combination with the symmetry argumentation (Table 1). By doing so, 6 marker segregation types (of which 4 are used in this thesis) of SNP markers can be recognized: simplex x nulliplex (SxN), duplex x nulliplex (DxN), simplex x simplex (SxS), simplex x triplex (SxT), duplex x simplex (DxS) and duplex x duplex (DxD). These SNP markers can thus be used in genetic studies, such a linkage mapping.

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The SNP markers are used in a pipeline for genetic analysis that spans from marker development to QTL (Quantative Trait Loci) analysis. A general pipeline that can be used for both diploid and polyploid species is briefly explained in Figure 1. An important step in this pipeline from marker development to QTL-analysis is the development of a linkage map, which is the focus of this thesis.

## Linkage mapping

Linkage mapping is an important tool in breeding for potato, since it can be used for the study of inheritance (Ripol et al., 1999), anchoring the genome (Sharma et al., 2013), as a requisite for QTL analysis (Wu et al., 2004a), which in itself is a step towards marker assisted breeding, or estimation of the physical chromosome size (Chakravarti et al., 1991). An approach to linkage mapping in tetraploids is to use a related diploid species (Rifkin et al., 2012) or to use a doubled monoploid developed from a tetraploid (The Potato Genome Sequencing Consortium, 2011). In both cases a diploid is mapped and this procedure is developed well over the past years. However a linkage map based on diploids, lacks important dosage information. The number of genotypes in a tetraploid is larger than in a diploid (Ripol et al., 1999) and this may lead to dosage effects and allele interactions not present in diploids. Thus, it may well be that not all characteristics of a tetraploid can be mapped in a diploid background (Yu \& Pauls, 1993). In addition to that, polyploidization during evolution is a dynamic process and therefore it may not be wise to use a diploid approximation for a tetraploid (Luo et al., 2004). Thus, making inferences from the diploid level to the tetraploid level has its difficulties and is undesired, since scientists and breeders want to carry out their experiments or breeding efforts on crosses of tetraploid potatoes rather than on diploid potato populations. These reasons are all about the inference of the diploid to the tetraploid level, but there is also a more practical reason, namely by mapping tetraploid potato directly, precious time and laboratory labour can be saved (Hackett et al., 1998) because doubled monoploids potatoes, created from tetraploids, are generally male-sterile (Mann et al., 2011). A reason why linkage mapping is done at all, on both diploid and tetraploid level, is that with comparing the physical map with the linkage map, genotyping, or sequence alignment errors can be found which would otherwise go unnoticed.

Considering these arguments, it is useful to focus on mapping tetraploid potatoes. The steps of linkage mapping in tetraploids are 1) creating a mapping population, 2) genotyping the parents and the offspring, 3) calculating the recombination frequencies 4), grouping of the markers into linkage groups and homologs, 5) determining the order within the homolog and 6) integrating the homologs (Figure 1). Mapping cross-pollinated diploids and tetraploids, including potato, is often done by creating linkage maps for the parents separately and integrating those maps thereafter (Mann et al., 2011). This strategy is called the pseudo-test cross strategy.

The most important step of the development of a linkage map is the ordering of the markers. For a linkage map with only a few markers, it will not be a problem to consider all the possible orders (n!/2 possible orders for every n markers to be ordered (Liu, 1997c), but for large datasets this is a huge computational problem, which bears similarity to the "travelling salesman problem" (Nelson, 2005). To cope with this problem, algorithms have been developed to find (near-)optimal orders while avoiding time consuming calculations, for example seriation (Nelson, 2005) which is a 'greedy' algorithm that grows outwards by adding one marker at a time to the order. Another algorithm, simulated annealing, uses 'temperature' to accept changes in the order that might be unfavourable and does this so avoid getting stuck in a local optimum (Nelson, 2005).

Other algorithms are stepwise search, branch and bound, genetic algorithms (Hackett et al., 2003) or evolutionary strategy algorithms (Mester et al., 2003a). In this thesis, a linear regression approach is used to order the markers, because it is theoretically easy to understand and implement practically (Chapter 5 and 6).

All algorithms use criteria to find the optimum order given all the estimated recombination frequencies or the counts of recombination events. Examples of optimization criteria are minimum the sum of adjacent recombination frequencies (SARF) (Van Os et al., 2005), the maximum likelihood, the maximum sum of adjacent LOD scores (SALOD), the minimum number of cross-overs, the minimum least square locus order, the minimization of the total number of expected recombinations (Hackett et al., 2003), sum of adjacent distances (SAD) or the weighted least squares(WLS) (Stam, n.d.), which is used in this thesis. The algorithms are used together with the criteria, for example RECORD minimises the number of cross-overs by a branch and bound algorithm, while JoinMap can use a stepwise search to minimise the sum of adjacent recombination (Isidore et al., 2003).

It is good to keep in mind that there are no 'good' or 'bad' algorithms and criteria, but the final ordering result is based on the genotype data, model and criteria used. Therefore there is a demand to simulate how the different algorithms handle data with, for example, missing data or genotype errors. Also, it should be noted that programmes or algorithms that can handle polyploid species are lacking, very basic (Dufresne et al., 2014) or cannot handle large number of markers (Hackett \& Luo, 2003), since polyploids have a more complex segregation pattern (Voorrips et al., 2011) when compared to diploids. Fortunately, some options for mapping exist. A map can be estimated based on SxN markers in coupling phase because the segregation ratio and recombination frequencies are the same as with a diploid cross between a homozygous and heterozygous parent (Voorrips et al., 2011). These maps based on SxN markers can serve as a backbone map for the other segregation type markers which can be added one by one. It is also possible to calculate the recombination frequencies beforehand and present them to programmes like JoinMap (Nelson, 2005).

Once the map order is there, the relative position between the markers is something that one would want to know. The distance between markers can be calculated by transforming the recombination frequencies into map distances. The two most widely used mapping functions are Haldane's and Kosambi's. Haldane's mapping function assumes that the crossovers follow a Poisson distribution and are independent regardless of their relative location, while Kosambi's mapping function takes positive interference into account (Vinod, 2011; Chapter 5). Kosambi's mapping function has been used to convert recombination frequencies into mapping distances of diploid potato (Sharma et al., 2013), while Haldane's mapping function was used to map tetraploid potato (Hackett et al., 2013). On the other hand, the differences between these mapping functions may be small when the marker density is high and adjacent distances are small (Van Eck, personal communication).

The ordering step in linkage mapping leads to 96 (2 parents x 4 homologs x 12 chromosome) homolog maps for tetraploid potato. Those individual maps still need to be integrated to be highly powerful for QTLanalysis. By combining the homolog information into one integrated map, the QTL analysis will be more powerful when compared to a QTL analysis on the homolog level. There are several strategies to integrate the homolog maps into a single consensus map, namely visual alignment, determination the consensus map directly from the recombination frequencies and LOD-scores, or a graph-theory approach (Yap et al., 2003). In this thesis a graph-theory approach is used (Chapter 6).

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## Goal and strategy

The goal of this thesis is the development of methods for linkage mapping autotetraploids. The strategy used in in this thesis to estimate a genetic linkage map, with a linear regression approach, was to start with calculating the map based on the highly informative SxN markers. Another reason, apart from the informativeness, is that SxN markers in coupling phase can be analysed in the same way as if the markers came from a diploid population instead of a tetraploid one. Thereafter, homolog maps with the other marker segregation types were estimated by calculating the linkage between SxN markers and those other markers.

During this thesis potato was used as a model crop since it is considered to be a true autotetraploid, the abundant SNP data available and access to the physical locations of most markers. Every step of linkage mapping tetraploid potato is elaborated in the subsequent chapters. Every chapter starts first with a theoretical introduction of the (statistical) method used and thereafter the results from the analysis of tetraploid potato are shown and briefly discussed. In Chapter 1, the mode of inheritance of potato is investigated by calculating the recombination frequencies of $\operatorname{SxN}$ markers. In Chapter 2, the $\operatorname{SxN}$ markers are assigned to linkage groups. In Chapter 3, the SxN markers are assigned to homologs based on a so-called phase-tree and DxN linkage Furthermore DxN and SxS markers are assigned to chromosomes and homologs. In Chapter 4, the recombination frequencies of the other marker types are calculated. In addition, the SxT markers are assigned to chromosomes and homologs. In Chapter 5, the theory of ordering markers of a homolog with the linear regression method is explained. The results of the mapping procedure are presented in Chapter 6. In Chapter 7, the homolog maps are integrated into a consensus map. In order to simplify explanation and limit the number of results to be presented, all these topics are explained on the basis of a single chromosome, chromosome 11, while information of the other chromosomes can be found in the Appendices.

Apart from the development of an integrated linkage map of potato, methods are developed for linkage mapping for other autotetraploids. This is in done in $R$, since it is scriptable ( $R$ Core Team, 2012), in contrast to JoinMap. Furthermore, the methods are developed in R as an alternative to JoinMap since JoinMap was designed for diploids and although the integration procedure of JoinMap could be used, it will take a long time to run when the marker number exceeds 150 (Wu et al., 2008). Time is a problem for many people, although others claim that a good solution is more important than a fast algorithm (Mester et al., 2004).

During this thesis the physical genome information is used to verify the results. However, one should be careful with the physical genome information as well, since it is in itself estimation and might require rearrangements in the initial years after sequencing (Cheema \& Dicks, 2009; Felcher et al., 2012). The use of genome information is limited, since for other species the genome sequence might not be available, and thus the sequence positions are primarily used as verification of the methodology in the case of potato. The steps carried out in this thesis are developed to be general so that they can be applied to marker data sets in mapping populations of other autotetraploid crops, even though their sequence is not available.

Table 1. Segregation ratios of an autotetraploid of different biallelic SNP marker types. Six marker types can be distinguished based on their segregation ratio. The segregation ratios are not considering double reduction and according to Mendelian laws.

|  | Type of parents |  |  | Dose of parents |  |  | Possible Gametes |  | Possible offspring | Segregation |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Parent 1 | x | Parent 2 | Parent 1 | x | Parent 2 | P1 | P2 |  | Codominant | Dominant (Presence: Absence) |
| Simplex x Nulliplex | Simplex |  | Nulliplex | Aaaa | X | aaaa | Aa, aa | aa | Aaaa, aaaa | 1:1 | 1:1 |
|  | Triplex | x | Nulliplex | AAAa | x | aaaa | AA, Aa | aa | AAaa, Aaaa | 1:1 | 1:0 |
|  | Triplex | x | Quadriplex | AAAa | x | AAAA | AA, Aa | AA | AAAA, AAAa | 1:1 | 1:0 |
|  | Simplex |  | Quadriplex | Aaaa | x | AAAA | Aa, aa | AA | AAAa, AAaa | 1:1 | 1:0 |
| Duplex x Nulliplex | Duplex |  | Nulliplex | AAaa |  | aaaa | AA, Aa, a |  | AAaa, Aaaa, aaaa | 1:4:1 | 5:1 |
|  | Duplex |  | Quadriplex | AAaa | x | AAAA | $\mathrm{AA}, \mathrm{Aa}, \mathrm{aa}$ | AA | AAAA, AAAa, AAaa | 1:4:1 | 1:0 |
| Simplex x Simplex | Simplex |  | Simplex | Aaaa | x | Aaaa | Aa, aa | Aa, aa | AAaa, Aaaa, aaaa | 1:2:1 | 3:1 |
|  | Triplex |  | Triplex | AAAa | x | AAAa | AA, Aa | AA, Aa | AAAA, AAAa, AAaa | 1:2:1 | 1:0 |
| Triplex x Simplex | Triplex | x | Simplex | AAAa | x | Aaaa | AA,Aa | Aa,aa | AAAa,AAaa, Aaaa | 1:2:1 | 1:0 |
| Duplex x Simplex | Duplex | X | Simplex | AAaa | x | Aaaa | AA, Aa, a | Aa, aa | AAAa, AAaa, Aaaa, aaaa | 1:5:5:1 | 11:1 |
|  | Duplex |  | Triplex | AAaa | x | AAAa | AA, Aa, a | AA, Aa | AAAA, AAAa, AAaa, Aaaa | 1:5:5:1 | 1:0 |
| Duplex x Duplex | Duplex | x | Duplex | AAaa | x | AAaa | AA, Aa, aa | AA, Aa, aa | AAAA, AAAa, AAaa, Aaaa, aaa | 1:8:18:8:1 | 35:1 |

## Marker development

When molecular markers are developed, the following criteria are considered: polymorphism, distribution throughout the genome, resolution of genetic differences, expenses, labour, time, amount of DNA-sample needed and linkage to phenotypes (Agarwal et al., 2008).


## Population

Whenever two plants are crossed, the offspring forms a population which the can be used during the genetic analysis. Backcrosses, doubled haploids, recombinant inbred lines and F2-populations are examples of such crossing strategies (Schneider, 2005). The few people that are working on tetraploid potato create F1 populations (Douches \& Coombs, 2012,
Hackett et al., 2013), since there is already segregation in the F1 because the parental lines are heterozygous. Another reason is that the possibility of using other population types, such as commonly used inbred lines, is limited by constrains like inbreeding depression.


## Genotyping and dosages

In the distant past, linkage maps were based on morphological characteristics, however nowadays mostly molecular markers are used. There are several marker types ranging from RFLPs to SNPs, which all can be used in linkage mapping for both diploid and tetraploid populations (Nguyen \& Wu, 2005), although currently mostly SNPs are used. Software such as fitTetra (Voorrips et al., 2011) can be used to translate the raw genotypes of tetraploids into useful dosages.


Linkage map
Linkage mapping is an important tool in breeding for potato, since it can be used for the study of inheritance (Ripol et al., 1999), anchoring the genome (Sharma et al., 2013) and QTL-analysis (Wu et al., 2004), which in itself is a step in marker assisted breeding.

## Haplotype propoabilites or phase reconstruction

The reconstruction of the linkage phase of the parents is the last step in linkage analysis (Luo et al., 2001). This means that the markers are mapped over the homologs within a parent and not across a parent. The markers are assigned to one of the parents in coupling or repulsion phase

This step is useful for further analysis such as QTL-analysis. Reconstructing a tetraploid is more difficult than constructing a diploid since a tetraploid has twice as many homologs.


## QTL-analysis

QTLs, or Quantitative trait loci, are common in plants and are of interest due to commercial important traits. QTL mapping is a combination of linkage mapping and traditional quantative genetics (Liu, 1997e). During QTL analysis, an significant association between traits and markers is searched for. Significant association between traits and markers may be evidance that a QTL is located nearby. By using the marker of an integrated linkage map, one makes sure to combine all the marker as efficient as possible. This leads to greater power to find QTLs.

## Calculation recombination frequencies and LOD-scores

The calculation of the recombination frequency between two markers is determined by the used model, which ,in turn, is determined by the population type and expected genotype frequencies. For some situation an analticaly estimator can be calculated, while for situatons the recombination frequency cannot be found analytically, but can still be found by an iterative maximum likelihood estimation (Luo et al., 2001)

## Marker assignment to linkage groups

The markers are grouped after the recombination frequencies and LOD scores are calculated. When markers in a tetraploid are grouped, the chromosomes are likely to be reconstructed by grouping the markers into linkage groups. Grouping, or clustering, can be done by making a dendogram with a nearest-neighbour analysis (Luo et al., 2001), k-means clustering (Hackett et al., 2013), or clustering based on the significance of the chi-square test for independent segregation (Hackett et al., 2013) together with corrections for multiple-testing (Luo et al., 2001)
$\qquad$


## Marker assignment to homologs

Apart from grouping the markers into 'chromosome'-groups, the markers are also clustered in homologous groups and this is unique to autopolyploids (Ripol et al., 1999) and this is not done for diploids Several cluster analyses may be run and combined manually as well (Hackett et al., 2013).


Ordering the markers within each linkage group is the most important step of linkage mapping. The possible orders of markers increases exponentially with every marker added to the analysis (Van Os et al., 2005). There are several algorithms which are used in ordering programmes. All algorithms use criteria to find the optimum order given all the estimated recombination frequencies or the counts of recombination events. Mapping functions are used that can convert recombination frequencies into genetic distances.


## Integration

Integration of the homolog map is desired for QTL-analysis. There are several strategies to integrate the homolog maps into a single consensu map, namely visual alignment, determine the consensus map directly from the recombination frequencies and LOD-scores, or a graph-theory approach (Yap et al., 2003).

Figure 1, previous page. Summary of the pipeline from genotype to QTL-analysis for diploid and tetraploids and a pipeline for linkage mapping in tetraploids. The pipeline covers all the essential steps from genotyping to QTL analysis with a focus on linkage mapping in tetraploids

## Programmes, Data and Assumptions

The programmes, data and assumptions are the starting point for linkage mapping in this thesis. Therefore the data, assumptions and programmes are explained here.

## Data

Linkage mapping is basically a data analysis and it is therefore wise to take a look at the data first. In the beginning two tetraploid potato accessions ( $\mathrm{A} \times \mathrm{C}$ ) were crossed. The population consists of 237 individuals, and such population size would be enough to identify the homologs (Hackett et al., 1998). Thereafter, the DNA was extracted of 237 F 1 offspring, the parents, 3 grandparents and 1 great-grandparent (Maliepaard et al., n.d.). The DNA was then applied to the recently developed 20K SolSTW array. This array contains 17987 useful SNPs (Vos et al., 2014). The SNPs on the array are biallelic, which makes scoring easier when compared to SNPs with four different alleles. When the extracted DNA was applied on the array, two fluorescent probes were added which bind to one of the two alleles. Thereafter, the fluorescence signal was measured.

The raw SNP data needed to be converted to useful dosages, the number of copies of a SNP allele. By using fitTetra software, markers were scored for dosages ranging from 0 to 4 copies (Voorrips et al., 2011). The markers were selected based on consistency of parental scores across the replicates and expected segregation ratios. Thereafter, the markers were divided according to the (Mendelian) segregation ratio (Table 1) in the progeny.

Diving the markers according to their segregation ratio resulted in four datasets: a $\operatorname{SxN}$ dataset for both P1 and P2 (with an expected segregation ratio of 1:1), a DxN dataset (1:4:1) and a SxS and SxT dataset (1:2:1; SxS and SxT are in one dataset). The SxN dataset contains 1547 SNPs for P1 and 1733 SNPs for P2, the DxN dataset contains 471 SNPs for P1 and 424 for P2 (Maliepaard et al., n.d.) and the SxS dataset contains 956 SxS SNPs and 445 SxT SNPs. To give a quick impression of what these datasets contain, an example of the SxN dataset of P1 is given in Figure 2 and the dataset is briefly explained below.


Figure 2. Part of the $\mathbf{S x N}$ dataset of P1. This dataset contains the marker names, the dosages and other information.

In Figure 2, the different symbols represent different types of information:
A) represents the names of the SNP markers (Vos et al., 2014).
B) stands for the parental dosages. This can be simplex $x$ nulliplex (10), triplex $x$ quadruplex (34), triplex $x$ nulliplex (30) or simplex x quadruplex (14), which all have the same segregation ratios. Obviously, the segregating allele is segregating in P1.
C) represents the physical chromosome on which the SNP markers are supposed to be located. The ST4 format is used for information about physical chromosomes based on the sequence, while to others format types come from different information sources.
D) gives information of the physical position of the marker based on the genome assembly in base pairs. When a 0 is given, it means that this marker has not been given a position on the physical sequence map yet.
E) stands for the chromosome to which the markers are assigned to by JoinMap. Although JoinMap is designed for linkage mapping in diploids, it can handle coupling SxN data. Although, the repulsion estimate for the recombination frequency of SxN marker is wrong, the assignment still works.
F) represents the homolog to which a certain marker belongs. This is based on several types on information, of which JoinMap is the main information source. As mentioned above, JoinMap can handle coupling SxN markers and will give chromosome assignment. JoinMap will map the markers along this chromosome. From the position of this linkage map, the homologs can be deduced (Hackett et al., 2013; Maliepaard, personal communication). However, in some cases JoinMap will not give four homologs, but more than that. In those cases other information, like the physical position and DxN data was used to assign the markers to the homologs. G) gives the assigned dosages for the two replicates of each of the parents by fitTetra.
H) gives the assigned dosages for the three grandparents and the single great-grandparent by fitTetra.
J) gives the assigned dosages of the 237 offspring plants by fitTetra.

The four datasets have a slightly different format, and the differences compared to the SxN dataset of P1 is briefly explained here:

The SxN dataset for P2 has does not contain information about the chromosomes and homologs assigned by JoinMap (E \& J). Also it does not contain the parental dosages (B) but this can be deduced from the dosages of the two replicates for each parent (G). Furthermore, the missing values in this dataset are split into two categories, namely the missing values caused by double reduction (see Assumptions) and the missing values caused by an incorrect dosage assignment or no dosage assignment by fitTetra. In addition to this, it has a summary about these missing values for each SNP marker. The DxN dataset for P1 and P2 look similar to the SxN dataset of P2.

The SxS dataset has information about the parental dosages (B) as well as the information of the assignment of each marker to a certain chromosome JoinMap (E), but not the assignment of the homologs (F). Furthermore, the missing values are categorized into two groups mentioned above, but are not summarized.

However, in the SxS dataset the SxT and TxS markers were transformed incorrectly. Therefore, another dataset, with the raw-dosages, was created. This dataset contains all the markers with their names (A), and the correctly transformed dosages (J). The raw dosages dataset is therefore mainly used for TxS markers.

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Halfway during the thesis, another dataset became available, namely a dataset which contains an updated version of the physical positions (Figure 3). From Chapter 6 onwards, this dataset is used. In Figure 3, the different symbols represent different types of information:
A) represents the names of the SNP markers (Vos et al., 2014).

B \& D) represent the physical chromosome on which the SNP markers are supposed to be located (sites about genome ref). ST4.01 is the chromosome assignment of version 1 of July 2012, ST4.03 is version 3 of September 2012.

C \& E) gives information of the physical position of the marker based on the genome assembly (July 2012 and September 2012) in base pairs. When a \#N/B is given, it means that this marker has not been given a position of the physical genome yet.

The 5 datasets were slightly edited before the usage in this thesis for practical reasons (Appendix 1).


Figure 3. Dataset containing the physical position. This dataset contains two versions of the physical positions of the markers.

Now that origin of the data has been explained, it is time to take a look at it. The first thing to do is to look at how the different segregation type markers are distributed over the chromosomes (Figure 4). It should be taken into account that these markers need to cover 96 homologs ( 2 parents x 12 chromosomes x 4 homologs). On a first glance it seems that the marker density is good enough for mapping and integration but when a closer look is taken at the density of the markers, it can be noted that, for example, the coverage of duplex x nulliplex markers of P1 on chromosome 2 is not high. This can have implications for clustering and ordering the markers. Furthermore, it is good to point out that the resolution of the map does not depend on the amount of markers but it depends on the amount of recombination events, which in turn depends on the amount of offspring. In addition to population size, the spacing of the markers is also important.


Figure 4. Distribution of the marker types over the physical chromosomes. The different marker types are plotted against their physical position on the chromosomes. This gives some indication of coverage.

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## Assumptions

Linkage mapping is a form of genetic modelling. During a modelling procedure, assumptions are made and it is good to keep these assumptions in mind while doing the linkage mapping and test, whenever possible, if the assumptions are violated. Ripol et al. (1999) summarized the following assumptions for linkage mapping in tetraploids:

- Assumption 1: "homologous chromosomes segregate from each other at meiosis".
- Assumption 2: "non-homologous chromosomes segregate independently".
- Assumption 3: "no segregation distortion".
- Assumption 4: "no cross-over position interference".
- Assumption 5: "no chromatid interference".
- Assumption 6: "each locus can belong to only one homologous group".
- Assumption 7: "homologous chromosomes form random pairs at meiosis".
- Assumption 8: "no double reduction - each chromosome will segregate from its pair at meiosis into a different gamete".

As a consequence of assumption 1, all the gametes should have one of every kind of chromosome. Also aneuploidy should not be possible. Assumptions 2 and 3 lead to equal probability for every homolog to be transmitted to the gametes and absence of selection at gamete or zygote level. Assumption 4 means that recombination events are randomly distributed over the genome and Assumption 5 means that all sister chromatids are equally likely to be involved in a recombination event (Zhao et al., 1995). In reality, hot-spots and cold-spots are observed where recombination happens more often or more rarely (Petes, 2001). In turn, this can lead to non-linearity when the genetic maps are compared to the physical maps. Assumption 6 is related to the SNPs used. These SNPs should only be present on one location in the genome. This assumption can therefore be violated when a certain SNP is duplicated and can thus be found on multiple locations across the genome. Assumption 7 states that the potatoes act like an autopolyploid since all the homologs have an equal chance to pair with the other homologs (and thus no preferential pairing occurs). This also means that during meiosis mainly bivalents are formed in contrast to multivalents (Gavrilenko et al., 2007). According to literature potatoes are considered to be autopolyploid (Bradshaw, 1994) and therefore this is a safe assumption. As a consequence of Assumption 7, Assumption 8 states that no double reduction occurs throughout the genome. Bourke et al. (2015) and Haynes \& Douches (1993) observed that double reduction occurs in potato.

In the addition to the assumption Ripol et al. (1999) made, there are a few more assumptions in this thesis with regards to mapping and map integration of a tetraploid species:

- Assumption 9: the pairwise recombination estimates are accurate.
- Assumption 10: the residuals of the pairwise recombination estimates are independent of each other.
- Assumption 11: the recombination rate is equal in both parents.
- Assumption 12: mapping functions designed for diploids are applicable to tetraploids.
- Assumption 13: there is a single correct order of markers for the cross as a whole.

During this thesis, pairwise recombination frequencies were calculated, while some studies suggest that the multipoint recombination fractions could correspond more closely to the physical distance between markers (Liu, 1997a), although in general there is no fixed relationship between the physical distance and recombination frequency of markers, since the commonly used mapping function do not take the physical location or the genome region into account (Liu, 1997d). Furthermore, the residuals of the recombination frequencies are treated as independent of each other for the linear regression approach used in Chapter 5. For the calculation of recombination frequency of SxS and SxT markers (that are across both parents), it is assumed that the recombination frequencies in both parents are equal. This is also a common assumption in linkage mapping of diploids. It is known for other plant species that this might not always be true (Plomion \& O'Malley, 1996), however, if unequal recombination frequency in the parents is also a phenomenon in potato is currently not known, although very unlikely. In this thesis, the Haldane mapping function is used. This mapping function, like all other mapping functions, was designed for diploids and one could argue whether it can also be applied to tetraploids (Van Ooijen, personal communication). Furthermore, for integration, there is the assumption that there is an single correct order for the cross and that the homolog maps are all different samples of the single correct order (Yap et al., 2003).

## Programmes

## R

R is a language designed for statistical analysis and graphics ( R Core Team, 2012). R is based on the S language, but has since then become more dominant. R is an interactive language and allows the users to write their own scripts and functions for powerful analysis of the data. R and its source code are freely available and this is one of the key factors of its success. RStudio has a more user friendly interface when compared to R (Verzani, 2011). For this thesis both R version i386 3.1.2 and RStudio version 0.98.1102 are used.
$R$ has a highly active community. This community is not only active on help-forums, but also in the creation of packages for R. Packages include specialized functions and corresponding documentation. Currently there are over 6,000 packages on the Comprehensive R Archive Network (CRAN), on which R packages are stored (Wickham, 2015). The variety of R packages is tremendous and this is one of the reasons why R is popular. During this thesis several packages are used, namely abind (Plate \& Heiberger, 2011), MASS (Venables \& Ripley, 2002), R/qtl (Broman et al., 2003), Combinat (Chasalow, 2005), RVAideMemoire (Hervé, 2014), NMF (Gaujoux \& Seoighe, 2010), flexclust (Leisch, 2005). Furthermore the package fitTetra was used to acquire the dosages (Voorrips \& Gort, 2011), which are explained in the Data chapter. LPmerge (Endelman \& Plomion, 2014) is used for the integration of homologs and will be further explained in Chapter 7.

## JoinMap

The recombination frequencies between $S x N$ markers in coupling phase can be calculated as if the markers came from a diploid backcross instead of a tetraploid. JoinMap, one of the most popular linkage mapping programmes (Cheema \& Dicks, 2009), is designed for the calculation of diploid linkage maps, can thus be used for coupling phase SxN markers of tetraploids. In the past this has been done for several tetraploids crops like medicago (Julier et al., 2003), rose (Vukosavljev et al., 2014), and potato (Meyer et al., 1998). JoinMap is developed by Kyazma B.V. and Biometris of the Wageningen University (Van Ooijen, 2006).

The user-friendly interface of JoinMap allows users to inspect errors by colouring the marker genotypes. This allows users to quickly check for labelling errors. Furthermore, the genotype frequencies and segregation ratios (Table 1) of every SNP can be inspected.

The second thing the programme does is grouping the markers in linkage groups. There are four criteria JoinMap can use (Van Ooijen, 2006).The first criterion is the pairwise recombination frequency. The second criterion is the LOD-score of the estimated pairwise recombination frequency compared with a recombination frequency of 0.5 , corresponding to 'no linkage'. This is called the LOD for linkage. The third criterion is the $\mathrm{G}^{2}$ statistic. The last criterion JoinMap can use is the independence LOD-score, which is a LOD score based on the $\mathrm{G}^{2}$-test statistic and which is not affected by distorted marker segregation ratios as the LOD for linkage is. The users can choose which criterion JoinMap will use to group the markers into linkage groups. JoinMap allows different thresholds for grouping the SNP markers and in this way ideally the number of linkage groups should be equal to the number of chromosomes. In the case of potato, there are 12 linkage groups which represent the 12 chromosomes when the LOD-threshold for grouping between 4 and 6 is used (Maliepaard et al., n.d.). If the physical position of the markers is available, a careful user should check whether the assigned linkage group of an individual marker in genetic mapping corresponds to the same linkage group on the physical chromosome.

Previous analysis showed that occasional differences were observed between the assignment of SxN markers to linkage groups and physical chromosomes (Maliepaard et al., n.d.).

Once the linkage groups are determined, the linkage map can be calculated for each group. The user can choose between two algorithms by which the grouped markers are mapped, namely by linear regression or by maximum likelihood. Both methods should "lead to more-or-less the same map orders" (Van Ooijen, 2006). After mapping, the user can evaluate the mapping by several quality parameters.

As mentioned above, JoinMap is not designed for the analysis of tetraploids. However, when the recombination frequencies and LOD-scores of marker pairs are calculated beforehand and thereafter supplied to JoinMap, JoinMap is able to produce a map based on those recombination estimates. Furthermore, in the same fashion, JoinMap can integrate map of different population by the use of its linear regression algorithm, hence the name JoinMap (see Chapter 7).

JoinMap has no option to assign markers to homologs. Still JoinMap can be used for the assignment of markers to homologs. The approach is to assign markers to linkage groups, order the markers within this linkage group, then deduce the homologs and do the ordering again for a single homolog (Hackett et al., 2013; Maliepaard, personal communication).

One of the advantages of JoinMap is, is that it presents maps based on MapChart (Voorrips, 2002). The visualisation of JoinMap by MapChart allows easy comparison of maps by visualisation.

## MapChart

MapChart is a computer programme that displays linkage maps (Voorrips, 2002). The linkage maps are projected as vertical bars. Furthermore it allows for inclusion of QTL-projection. Mapchart is incorporated in JoinMap. In this thesis MapChart version 2.2 is used

## PedigreeSim

PedigreeSim is a computer package that allows the simulation of offspring of crosses of multiple polyploidy levels (Voorrips \& Maliepaard, 2012). These kinds of simulations prove to be very useful to check if genetic models and its assumptions are correct. PedigreeSim is used in this thesis to check the maximum likelihood estimators for the recombination frequencies and the corresponding likelihood functions as well.

## Chapter 1: Mode of inheritance

## Summary Chapter 1:

Potato is assumed to be an autotetraploid, which means that there is tetrasomic inheritance. The recombination frequencies between $S x N$ markers are calculated under disomic and tetrasomic inheritance. The recombination frequency between $S x N$ markers in coupling phase is the same under both models, but is different for SxN markers in repulsion. By performing a Binomial test, together with a Bonferroni correction to account for multiple testing, the mode of inheritance was investigated. Only a few repulsion marker pairs were found to be significant for disomic inheritance, meaning that the assumption of tetrasomic inheritance is not falsified. After this, the recombination frequencies allowing only for the tetrasomic inheritance were calculated.

## Counting the offspring

In the Programmes, Data and Assumptions, the assumptions of this research are mentioned. One of the assumptions is that potato is an autotetraploid, which means that there is tetrasomic inheritance. This assumption is tested in this chapter by calculating the recombination frequencies and LOD-scores between SxN markers. This follows one of the approaches to study inheritance as indicated in an inheritance investigation of garden rose (Vukosavljev et al., 2014).

The first obvious step in calculating the recombination frequencies between two markers is counting the number of offspring with a specific dosage. The number of offspring with a certain dosage combination of two markers are indicated as $\mathrm{n}_{\mathrm{xy}}$, with x being the dosage of marker A and y being the dosage of marker B . This notation deviates from previous literature, which mainly works with letters (a to d for example), however the notation here has the advantage that it can be applied to every pair of markers, regardless of its marker segregation type.

## Preferential pairing and multiple testing

Based on the number of offspring with a certain dosage, linkage between markers can be estimated. Mather (1951) found that systematic association between two markers, and thus linkage, can be estimated by using a $\chi^{2}$-test (Equation 1). Due to the large number of $\chi^{2}$-tests, a multiple-testing correction is necessary. A common way to account for multiple testing is to adjust the $\alpha$, commonly 0.05 or 0.01 , to a stricter threshold by using the Bonferroni correction, which needs an $\alpha$ and the number of independent tests. A Bonferroni correction is used in genetic studies to gain an experiment-wide threshold (Cheverud, 2001; Lander \& Botstein, 1989). In this thesis, the number of independent test is considered to be the number of chromosomes, and so the Bonferroni correction was calculated (Equation 2) to adjust $\alpha$, the threshold for significance. In this case, significance means that the two markers tested are significantly linked.

Equation $1 \chi^{2}=(n 00+n 11-n 01-n 10)^{2} / n t o t \sim \chi_{1}^{2}$
Equation $2 \alpha^{\prime}=\alpha / k=0.01 / 12=0.0083$

* $\chi^{2}$ is the Chi-square test statistic following, under the null hypothesis, a $\chi^{2}$-distribution with 1 degree of freedom, n01 is the number of markers that have genotype aaaa and Bbbb, n10 is the number of markers that have genotype Aaaa and bbbb, n00 is the number of markers that have genotype aaaa and bbbb, n11 is the number of markers that have genotype Aaaa and Bbbb, ntot is the sum of n10, n01, n00 and n 11 , the A's (for example Aaaa) and B's (for example Bbbb) are not position dependent, $\alpha$ is the a significance threshold of $0.01, \alpha$ ' is the adjusted $\alpha$ and k is the number of independent test, in this case 12 , since there are 12 chromosomes.


## Recombination frequency and LOD-score between SxN Markers

If two markers are found to be significant linked according to Mathers test, the procedure is continued by calculating the logarithm of odds (LOD-score). The remarkable thing about the LOD-score of a pair of SxN markers is that the equation is the same regardless of the phase or mode of inheritance (Equation 3; Box 1).

In cases of complete linkage either $n 00+n 11$ or $n 10+n 01$ is equal to 0 , since recombinants do not occur. A $\log$ of 0 is infinite and likewise calculations will return non-realistic values. Therefore Equation 3 (Box 1) is modified to cope with this situation. Although a $\log$ of 0 is infinite, this infinite value is multiplied by the amount of recombinants, which is 0 and thus the product of the two will also be 0 . Therefore the recombinants are neglected in the new formula. This leaves the parental types, which are then equal to the total number of offspring. By doing so, Equation 4 (Box 1) arises and this formula is used when the recombination frequency is zero.

After calculating the LOD-score of a marker pair, the recombination frequencies for repulsion and coupling phase under disomic and tetrasomic inheritance are calculated. The recombination frequency in repulsion phase is different for the repulsion phase for tetrasomic inheritance (equation 6 in Box 1) and disomic inheritance (Equation 7 in box 1), while the recombination frequency for coupling phase is the same under both models (Equation 5 in Box 1).

All three estimates for the recombination frequency are calculated. If the estimate of r 1 is the minimum of the three estimates, the two markers are considered to be in coupling phase with each other. If $r 1$ is not the minimum of the three, then either r 2 or r 3 is chosen to be the correct estimate and the two markers are considered to be repulsion phase. Under the tetrasomic model, the expected proportion of recombinants ( $\mathrm{n} 00+\mathrm{n} 11$ ) is $1 / 3$ for completely linked markers (Qu \& Hancock, 2001), while under the disomic model with complete preferential pairing there are no recombinants expected ( $\mathrm{r} 3=0$ ). To determine whether r 2 or r 3 is the correct estimate, a Binomial test was carried out for the repulsion marker pair. In this test, the recombinants (n00+n11) are compared to $1 / 3$. Again due to the many marker pairs tested, a multiple testing correction is needed. Within one chromosome (one linkage group) there are 36 linkages $(8+7+6+5+4+3+2+1)$ possible between two markers, when a chromosome arm is taken as the entity of independent tests. Of all these linkages, 8 are in coupling within the same chromosome arm, 4 are in coupling linkages on different chromosome arms (but still on the same homolog), while the majority of the linkages (24) is across the different homologs (Figure 5). Only the repulsion linkages are of interest to test for preferential pairing with a Binomial test. The amount of possible repulsion linkages is used in the Bonferroni correction (Equation 8).

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Equation $3 \alpha^{\prime}=\alpha / k=0.01 / 24=0.00417$
${ }^{*} \alpha$ is the significance threshold of $0.01, \alpha^{\prime}$ is the adjusted $\alpha$ and $k$ is the number of independent test, in this case 24 , since there are 24 repulsion linkages within one chromosome (Figure 5).

If the observed frequency of recombinants is significantly lower than $1 / 3$, the two markers are evidence for preferential pairing, while on the other hand, when the test is not significant, the two markers are in repulsion under the tetrasomic model or in repulsion in disomic inheritance at a large distance.

If the null-hypothesis is accepted (tetrasomic inheritance), r 2 is estimated to be the correct recombination frequency. When r 2 is below zero, r 2 is set to 0 , following the approach by Hackett et al. (1998), to get an allowed estimate between 0 and 0.5 . This is done since an under estimation of the recombination frequency is better than an over estimation (Hackett et al., 1998). Negative estimates for $r 2$ can happen and when this happens often, this could indicate a violation of the assumptions (Wu et al., 1992). Hackett et al. (1998) suggest that setting the recombination frequency at 0 when there is a negative estimate of the recombination frequency might shorten the integrated linkage map when integration is done with a regression method, or sometimes otherwise called, a statistical pooled approach (Jackson et al., 2005; Chapter 7). However, it was mentioned that "smaller true recombination fractions may give smaller negative estimates, and therefore that using zero as an estimate, regardless of the size of the negative estimator, is losing some information."

The procedure, as described above, was carried out for all SxN marker pairs for both parental types.

— Repulsion linkage

- Coupling linkage, different chromosome arm
- Coupling linkage, same chromosome arm

Figure 5. Possible linkages within one chromosome (or linkage group) of one parent. Considering, two chromosome arms per homolog, there are 36 linkages possible, of which 8 are in coupling phase on the same chromosome arm, 4 in coupling phase on different chromosome arms of the same chromosomes and 24 repulsion linkages

Box 1. Recombination frequency and LOD calculations between two SxN markers. In this box the calculations for the LOD-score between two SxN markers are shown for the different-phase situations are shown.

## Simplex x nulliplex Simplex x nulliplex

Equation $4 L O D=\operatorname{ntot} * \log 10(2 / n t o t)+(n 00+n 11) * \log 10(n 00+n 11)+(n 10+n 01) *$ $\log 10(\mathrm{n} 10+\mathrm{n} 01)$

Equation $5 L O D_{r=0}=n t o t * \log 10\left({ }^{2} / n t o t\right)+n t o t * \log 10(n t o t)=n t o t * \log 10(2 / n t o t * n t o t)=$ ntot $* \log 10(2)$

Coupling
Aaaa x aaaa
Bbbb x bbbb

Equation $6 r 1=\frac{\mathrm{n} 01+\mathrm{n} 10}{\text { ntot }}$
Repulsion
Aaaa x aaaa
bBbb x bbbb
Equation $7 r 2=\frac{2 *(\mathrm{n} 00+\mathrm{n} 11)-(\mathrm{n} 10+\mathrm{n} 01)}{\text { ntot }}$

$$
\text { Equation } 8 r 3=\frac{\mathrm{n} 11+\mathrm{n} 00}{\mathrm{ntot}}
$$

* LOD is the logarithm of odds ratio, rl is the estimate of the recombination frequency of two SxN markers in coupling phase, r 2 is the estimate of the recombination frequency of two SxN markers in repulsion phase under tetrasomic inheritance, r3 is the estimate of the recombination frequency of two $S x N$ markers in repulsion phase under disomic inheritance (or preferential pairing), $n 01$ is the number of markers that have genotype aaaa and Bbbb, n 10 is the number of markers that have genotype Aaaa and bbbb, n00 is the number of markers that have genotype aaaa and bbbb, n11 is the number of markers that have genotype Aaaa and Bbbb, ntot is the sum of n10, n01, n00 and n 11 , the A's (for example Aaaa) and B's (for example Bbbb) are not position dependent.


## Results

The majority of the repulsion pairs are in repulsion under tetrasomic inheritance while only a few marker pairs show signs of preferential pairing under disomic inheritance (Appendix 2). From this, it can be concluded that there is indeed no preferential pairing as was assumed and the tetrasomic model is the best model, which corresponds to literature (Bradshaw, 1994). Thus, the recombination frequencies and LOD-scores were calculated again by only considering the tetrasomic estimators (r1 and r2).

## Conclusion Chapter 1:

In this chapter, the mode of inheritance was investigated by calculating the recombination frequencies of SxN markers under the tetrasomic and disomic model. Only a few repulsion marker pairs were found to be significant for disomic inheritance, meaning that the assumption of tetrasomic inheritance is good. After this, the recombination frequencies under the tetrasomic model only were calculated.

## Chapter 2: Clustering of SxN markers along chromosomes

## Summary Chapter 2:

The SxN markers are assigned to linkage groups based on the LOD-scores, the measurement of linkage. The approach used here follows the approach of JoinMap. The SxN markers of P1 were clustered at a LOD-threshold of 5, while the SxN markers of P2 were clustered at a LOD-threshold of 5.15. In both cases this resulted in 12 linkage groups, corresponding to the number of chromosomes. The results of the clustering method were compared with JoinMap and the physical positions. The clustering and the clustering of JoinMap gave identical results, while there were some deviations between the clustering and the physical chromosomes. In total 1545 SxN markers for P1 and 1727 SxN markers for P2 were clustered into linkage groups.

## Algorithm for clustering SxN markers into linkage groups

In the previous chapter, the recombination frequencies of $S x N$ markers were calculated. The next step in the mapping process is assigning each $S x N$ marker to a linkage group. This is necessary since markers that are not from the same linkage map inherit independently and therefore a linear map between those markers is not possible or meaningful (Van Ooijen \& Jansen, 2013a). Ideally, the clusters (or linkage groups) are the same number as the number of chromosomes.

One of the cluster criteria to group markers is based on the LOD-score of linkage, the measurement for the likelihood of linkage. JoinMap presents a foldable tree by which the user can check the robustness of the clustering. Van Ooijen \& Jansen (2013a) describe the easy procedure how this is done by the software:

- Step la: start with the first pair of markers.
- Step $1 b$ : assess the next pair of markers.
- Step 2: if the marker pair is unlinked, continue with step $1 b$.
- Step 3: if the marker pair is linked, there are four situations possible:
- Step 3a: if one of the markers has already been assigned to a linkage group. $\rightarrow$ assign the other marker to this linkage group as well.
- Step $3 b$ : if both markers have been assigned to different linkage group. $\rightarrow$ combine the linkage groups as one linkage group.
- Step 3c: if both markers have been assigned to the same linkage group. $\rightarrow$ do nothing
- Step $3 d$ : if both markers have not been assigned to a linkage group yet. $\rightarrow$ create a new linkage group and assign both markers to it.
- Step 4: Continue with step $1 b$ until all marker pairs are accounted for.


## Clustering thresholds

By following this procedure every marker pair is only considered once for each given linkage-threshold which increases the computational efficiency of the procedure. Different kinds of linkage measurements, like the test-statistic of Mather used in Chapter 1, are possible depending on the preference of the user. Here the LODscore of linkage, as was calculated in Chapter 1, is used as a linkage-threshold to determine the amount of linkage groups as this is also one of the clustering criteria of JoinMap. Therefore, this will make comparison between the clustering method of JoinMap and the clustering method described above meaningful. The LODthresholds considered here are $3,4,5,6,7,8$ for P 1 and $3,4,5,5.1,5.15,5.2,5.3,5.4,5.5,6,7,8$ for P 2 . The reason why these LOD-thresholds were chosen is described below. The result of each clustering threshold was compared to the physical positions and, for P1, also with the clustering of JoinMap (since the clustering by JoinMap was only available for P1 at the time (see Data)).

To quantify the comparison between the clusters, the Rand Index is used. The Rand Index is a measurement for the similarity between two clustering methods, which, in this case, relates to the accuracy (Rand, 1971). The value for the Rand Index ranges between 0 and 1 with 1 indicating that the two clustering methods are identical while a 0 indicates that there is no agreement between the two clustering methods (Equation 9).

Equation 9

$$
R=\frac{a+b}{a+b+c+d}
$$

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## Clustering results

The Rand Index of the comparison between the clustering method used here and the physical chromosomes was 0.978 for P 1 at a LOD-score of 5 and 0.982 for P 2 at a LOD-score of 5.15 (Figure 6), meaning that the clustering method is very similar to the grouping according to the physical chromosomes. In both cases, the Rand Index was the maximum of all LOD-thresholds considered. The Rand Index of the clustering at a LOD of 5 was not optimal for P2 and did not contain 12 linkage groups, therefore, a LODthreshold slightly higher than a LOD of 5.15 was chosen (Figure 6). With the optimal LOD-thresholds chosen, the number of clusters (or linkage groups) is equal to the number of chromosomes and this fact is of great importance (which could otherwise be used as criterion for the selection of the LOD-threshold). An explanation for the fact that the Rand Index was not 1 could be that the marker assignment to physical chromosomes was not correct for some markers (Appendix 3).

Furthermore, the clustering method of JoinMap for P1 was compared with the clustering method used here. The Rand Index was 1 at a LOD-threshold of 5. This means that the clustering method used by JoinMap and the method used here gave identical clusters.

In total 1545 SxN markers of P 1 and 1727 SxN markers of P 2 were assigned to the respective linkage groups (Table 2). Two SxN markers, PotVar0055484 and PotVar0077706, were not assigned to linkage groups in P2 and two SxN markers, PotVar0079248 and PotVar0059901 were not assigned to linkage groups n P1. This means that those four markers were not significantly linked with any other marker.

Table 2. Total number of $S x N$ markers assigned to a certain linkage group or chromosome. The SxN markers are assigned on the basis of a LOD-threshold of 5 for P 1 and 5.15 for P 2 .

|  | P1 |  | P2 |  |
| :---: | :---: | :---: | :---: | :---: |
| Chromosome | Cluster | Markers | Cluster | Markers |
| 1 | 2 | 159 | 5 | 183 |
| 2 | 3 | 155 | 1 | 235 |
| 3 | 4 | 109 | 2 | 225 |
| 4 | 5 | 144 | 8 | 134 |
| 5 | 6 | 192 | 10 | 195 |
| 6 | 7 | 76 | 7 | 152 |
| 7 | 8 | 105 | 3 | 134 |
| 8 | 1 | 186 | 4 | 104 |
| 9 | 9 | 117 | 11 | 107 |
| 10 | 10 | 83 | 12 | 43 |
| 11 | 11 | 137 | 9 | 129 |
| 12 | 12 | 82 | 6 | 86 |
| Total |  | 1545 |  | 1727 |



Figure 6. Rand Index of the clustering method used in this thesis compared with the physical positions and JoinMap. P1 is compared with both the physical chromosomes and JoinMap, while P2 is only compared with the physical chromosomes. The maximum of the Rand Index was at LOD 5 for P1 for both comparisons, while the maximum Rand Index for P2 was at 5.15 for the comparison with the physical chromosomes.

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## Conclusion Chapter 2:

The SxN markers were clustered in 12 linkage groups, corresponding to the number of chromosomes. The clustering method used in this thesis and the clustering method of JoinMap gave identical results, while there were some deviations between the clustering method and the physical chromosomes. This means that the clustering method is a good method of clustering SxN markers along linkage groups. In total 1545 SxN markers for P1 and 1727 SxN markers for P2 were clustered into linkage groups.

## Chapter 3: Clustering of SxN markers along homologs

## Summary Chapter 3:

In this chapter, the SxN markers are assigned to homologs. This is done by constructing a so-called phase-tree, which is based on the phase information of a SxN marker pair (coupling or repulsion). For most chromosomes, the phase-tree method led to four distinctive homologs to which the SxN markers were assigned. However, in some cases five or six sub clusters (or artificial homologs) were found. In those situations, the sub clusters were put together into homologs based on linkages between DxN and SxN markers that closed the gap between the artificial homologs. In two occasions other information sources had to be used to end up with four distinctive homologs. In addition, by using this methodology the DxN and SxS markers were assigned to chromosomes and homologs.

## Clustering of SxN markers into homologs with a phase-tree

In the previous chapter the SxN markers were clustered into the linkage groups (corresponding to chromosomes). The next step is to assign the markers to homologs and this step is unique for polyploids.

A previous approach to assign SxN markers to homologs was to use JoinMap to estimate the homologs. When JoinMap assigned the SxN markers to linkage groups and the SxN markers within this linkage group were ordered, the homologs can be deduced from the map positions (Hackett et al., 2013; Maliepaard, personal communication). However, this approach was laborious. Therefore, there is a desire to have software that can assign markers to homologs within the R pipeline. A new approach to estimate the homologs is given in this chapter.

In Chapter 1 information about the phase of marker pairs (coupling or repulsion) has been gathered. The phase information provides much information about the homologs, since markers on the same homolog should ideally be in coupling phase with each other while being in repulsion with markers on other homologs. Markers close together on the same homolog have a similar phase-pattern, meaning that linked markers are in coupling or repulsion with regards to other markers. To make use of this pattern, a phase matrix was constructed based on the phase-information. The marker pairs in coupling phase were given the value of 1 while the marker pairs in repulsion phase were given the value of 0.1 . Although the actual values given are not of great importance, the fact that those values are dissimilar is important.

After this phase matrix was constructed, the Euclidean distances were calculated between the markers in the matrix. This resulted in a distance matrix, which was used to construct a hierarchical tree, or a phase-tree. The hierarchical tree produced from SxN markers within one linkage group gave usually four distinct subclusters (or homologs; Table 3), as can be seen, for example, in the hierarchical clustering of chromosome 11 of P2 (Figure 7). By careful visual inspection of the trees of every chromosome, the trees were cut into four, five or six sub clusters (or homologs) (Appendix 4).

For some chromosomes the numbers of SxN markers are more or less distributed over the homologs while on other chromosomes some homologs are over- or underrepresented (Table 3).


Figure 7. The phase-tree of chromosome $\mathbf{1 1}$ of $\mathbf{P 2}$. The phase-tree of chromosome 11 of P 2 clearly splits into 4 distinctive homologs (or sub clusters). The phase-trees of the other chromosomes can be found in Appendix 4.

Table 3. Number of SxN markers divided over chromosomes and homologs based of the clustering method based on the LOD-threshold and based on the phase-tree. Some chromosomes have more than 4 homologs, which are therefore called sub clusters and are in those situations not biologically meaningful.

|  | P1 |  |  |  |  |  |  | P2 |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Chromosome | Cluster | Sub cluster |  |  |  |  |  | Cluster | Sub cluster |  |  |  |  |
|  |  | 1 | 2 | 3 | 4 | 5 | 6 |  | 1 | 2 | 3 | 4 | 5 |
| 1 | 2 | 44 | 55 | 34 | 26 |  |  | 5 | 61 | 60 | 25 | 24 | 13 |
| 2 | 3 | 46 | 44 | 34 | 31 |  |  | 1 | 55 | 75 | 89 | 8 | 8 |
| 3 | 4 | 6 | 11 | 23 | 12 | 57 |  | 2 | 42 | 110 | 47 | 26 |  |
| 4 | 5 | 21 | 98 | 5 | 20 |  |  | 8 | 46 | 38 | 32 | 18 |  |
| 5 | 6 | 50 | 101 | 32 | 9 |  |  | 10 | 76 | 69 | 34 | 10 | 6 |
| 6 | 7 | 12 | 35 | 15 | 14 |  |  | 7 | 50 | 28 | 51 | 23 |  |
| 7 | 8 | 21 | 36 | 13 | 35 |  |  | 3 | 46 | 48 | 28 | 12 |  |
| 8 | 1 | 99 | 24 | 40 | 20 | 3 |  | 4 | 24 | 37 | 31 | 12 |  |
| 9 | 9 | 61 | 8 | 24 | 8 | 15 | 1 | 11 | 15 | 41 | 39 | 12 |  |
| 10 | 10 | 22 | 14 | 13 | 30 | 4 |  | 12 | 23 | 11 | 5 | 4 |  |
| 11 | 11 | 37 | 34 | 22 | 44 |  |  | 9 | 34 | 51 | 23 | 21 |  |
| 12 | 12 | 20 | 27 | 15 | 20 |  |  | 6 | 14 | 20 | 19 | 25 | 8 |

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## Clustering of SxN markers into homologs by means of DxN linkage

Four chromosomes for each parent have more than four homologs (8 chromosomes in total). This is of course not desired and artificial. These artificial homologs have to be merged together into biologically meaningful homologs. One method of doing this is by looking at DxN markers that could bridge the gaps within a homolog (Figure 8). When a DxN marker shows significant linkage to three sub clusters instead of two, then this is an indication that two of the three sub clusters are actually the same homolog. Concluding that two sub clusters are actually the same homolog based on just a single DxN marker alone is not considered to be reliable (but could theoretically be enough in some situations). Therefore, recombination frequencies are calculated between all pairs of DxN and SxN markers and are considered for a chromosome in cases where there were 5 or more homologs.

The number of individuals in each of the dosage classes of DxN markers and SxN markers are counted and the recombination frequencies for coupling and repulsion phase are estimated from these (Equation 12 and 14 in Box 2). The minimum recombination frequency (of the repulsion and coupling estimate) is estimated to be the most likely estimate. Thereafter, the LOD-score corresponding to the minimum recombination frequency is calculated (Equation 13 and 15 in Box 2). The DxN markers are assigned to homologs based on the majority of linkages with a SxN marker with a LOD-score equal or higher than 3 . The DxN markers are assigned to the two homologs based on the majority of coupling-linkages within the same chromosome if the total number of coupling linkages were more than 1 . Whenever a chromosome had more than 4 homologs, the DxN marker was assigned 3 sub clusters (in case of 5 sub clusters within the chromosome, when there were coupling linkages with 3 sub clusters) or 4 (in case of 6 sub clusters, when there were coupling linkages with 4 sub clusters).


Figure 8 DxN and SxN linkage that can bridge the gaps between sub clusters of the same homolog. The
DxN marker that has yet to be assigned to a homolog has coupling linkages with 3 (out of the 5) homologs. This indicates that 2 of the 3 homologs should be merged into a single biologically meaningful homolog.

Box 2. Recombination frequency and LOD calculations between a SxN marker and a DxN marker. In this box the calculations for the LOD-score between a SxN marker and a DxN marker are shown. Furthermore, the different recombination frequency estimates for the different-phase situations are shown.

## Duplex x nulliplex <br> Simplex x nulliplex

Coupling rl
AAaa x aaaa
Bbbb x bbbb

$$
\text { Equation } 12 \quad r 1=\frac{\mathrm{n} 20+\mathrm{n} 01}{\mathrm{n} 00+\mathrm{n} 21+\mathrm{n} 20+\mathrm{n} 01}
$$

Equation $13 L O D=(n 00+n 21+n 20+n 01) * \log 10(2)+(n 00+n 21) * \log 10(1-r)+$

$$
(n 20+n 01) * \log 10(r)
$$

## Repulsion $r 2$ <br> AAaa x aaaa

bbBb x bbbb

$$
\text { Equation } 14 r 2=\frac{\mathrm{n} 00+\mathrm{n} 21}{\mathrm{n} 00+\mathrm{n} 21+\mathrm{n} 20+\mathrm{n} 01}
$$

Equation $15 L O D=(n 00+n 21+n 20+n 01) * \log 10(2)+(n 00+n 21) * \log 10(r)+(n 20+$

$$
n 01) * \log 10(1-r)
$$

* LOD is the logarithm of odds ratio, r1 is the estimate of the recombination frequency of a DxN marker and a SxN marker in coupling phase, r 2 is the estimate of the recombination frequency of DxN marker and a SxN marker in repulsion phase, n 01 is the number of markers that have genotype aaaa and Bbbb, $n 20$ is the number of markers that have genotype AAaa and bbbb, n 00 is the number of markers that have genotype aaaa and bbbb, n 21 is the number of markers that have genotype AAaa and Bbbb, the A's (for example Aaaa) and B's (for example Bbbb) are not position dependent.

After the DxN markers have been assigned to sub clusters (or homologs), the number of DxN markers are counted for each sub cluster, in cases when a chromosome had more than 4 sub clusters or artificial homologs. For example, chromosome 8 of P1 has 5 sub clusters. 19 DxN markers have been assigned to sub cluster 1 , of which 4 are also assigned to sub cluster 2, 9 also assigned to sub cluster 3,6 also assigned to sub cluster 4 and 4 also assigned to sub cluster 5 (Table 4). As was mentioned above, when DxN markers on two sub clusters inherited together, this is an indication that the two sub clusters are part of the same homolog. In other words, the DxN markers close the gap between the distantly linked SxN markers on the same homolog.

The counted number of DxN markers can also be presented as a percentage to make inspection, visualisation, and judgement more easy. The number of DxN markers assigned to a certain sub cluster as well as to another are divided by the total number of DxN markers assigned to this sub cluster (the diagonal). For example, the 4 DxN markers that were assigned to sub cluster 1 and sub cluster 2 make up $21 \%$ of the total DxN markers on sub cluster 1 and $19 \%$ on sub cluster 2 (Table 5). This can be done for every combination of sub clusters. For this chromosome, sub cluster 5 always (100\%) inherits together with sub cluster 2, meaning that these are part of the same biological homolog. This was done similarly for all chromosomes with more than 4 sub clusters.

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Table 4. The number of DxN markers assigned to sub clusters for chromosome $\mathbf{8}$ of P1. Every DxN marker has been assigned to three sub clusters.

|  | Sub cluster 1 | Sub cluster 2 | Sub cluster 3 | Sub cluster 4 | Sub cluster 5 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Sub cluster 1 | 19 | 4 | 9 | 6 | 4 |
| Sub cluster 2 | 4 | 21 | 9 | 8 | 6 |
| Sub cluster 3 | 9 | 9 | 23 | 5 | 2 |
| Sub cluster 4 | 6 | 8 | 5 | 19 | 0 |
| Sub cluster 5 | 4 | 6 | 2 | 0 | 6 |

Table 5. The percentage of $D x N$ markers assigned to a certain sub cluster over the total number of $D x N$ markers assigned to that sub cluster for chromosome 8 of P1. The percentage of DxN markers is based on the number of DxN markers presented in Table 5. Due to rounding the percentages of the sub clusters might not add up to $100 \%$.

|  | Sub cluster 1 | Sub cluster 2 | Sub cluster 3 | Sub cluster 4 | Sub cluster 5 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Sub cluster 1 | $100 \%$ | $19 \%$ | $39 \%$ | $31 \%$ | $67 \%$ |
| Sub cluster 2 | $21 \%$ | $100 \%$ | $39 \%$ | $42 \%$ | $100 \%$ |
| Sub cluster 3 | $47 \%$ | $43 \%$ | $100 \%$ | $26 \%$ | $33 \%$ |
| Sub cluster 4 | $31 \%$ | $39 \%$ | $22 \%$ | $100 \%$ | $0 \%$ |
| Sub cluster 5 | $21 \%$ | $29 \%$ | $9 \%$ | $0 \%$ | $100 \%$ |

For chromosome 3, sub cluster 1 inherits together with sub cluster 2 ( $100 \%$ ). For chromosome 9 sub cluster 6 inherits always together with sub cluster $1(100 \%)$ but in this case there is still one sub cluster too many. For chromosome 10, sub cluster 5 inherits together with sub cluster 2 and with sub cluster 4 (both $100 \%$ ). The DxN markers of P2 that are assigned to the different sub clusters of chromosome 2 of show no clear inheritance of two homologs (with a maximum of $64 \%$ ). For chromosome 1, sub cluster 5 always inherits together with sub cluster $4(100 \%)$. For chromosome 5 the assigned DxN markers show no clear inheritance of two homologs (with a maximum of $57 \%$ ). For chromosome 12, sub cluster 5 inherits always together with sub cluster 1 (100\%).

As described above, the coupling information of the DxN markers with SxN information provided some information to combine sub clusters in cases where there are more than 4 sub clusters. However, the information is not conclusive in some other cases (meaning that sub clusters could not be merged based on coupling DxN information only). Therefore, also information about the repulsion phase of DxN with SxN is taken into account since the repulsion phase has the same information content.

However, the repulsion estimates did not provide a clear homolog inheritance either, and therefore this repulsion information was combined with the coupling information by adding the two percentages up (in this way a total of $200 \%$ can be reached).

For chromosome 1 of P2, the highest cumulative percentage was that of sub cluster 5 with sub cluster 4 with $152 \%$ while the second most likely candidate (sub cluster 5 with sub cluster 2) had only $132 \%$, it can therefore be concluded that the most likely situation is that sub cluster 4 and 5 are part of the same homolog. For chromosome 5 of P2, the highest cumulative percentage was that of sub cluster 5 with sub cluster 4 with $132 \%$ while the second most likely candidate (sub cluster 2 with sub cluster 1) had only $115.8 \%$, it can therefore be concluded that the most likely situation is that sub cluster 4 and 5 are part of the same homolog. For chromosome 9 of P1, the three pairs of sub clusters had a high cumulative percentage (sub cluster 6 with sub cluster $2173 \%$, sub cluster 4 with sub cluster $3173 \%$ and sub cluster 2 with sub cluster $1175 \%$ ) and thus it cannot be concluded which sub clusters are actually one homolog. For chromosome 10 of P1, both sub cluster 5 with sub cluster 2 and sub cluster 5 with sub cluster 4 inherited together $200 \%$ of the time, and therefore it can also not be concluded if either sub cluster 4 or sub cluster 2 is a real homolog together with sub cluster 5 .

## Clustering of SxN markers into homologs by means of other types of information

To get four homologs in the last two cases, chromosome 10 and chromosome 9 of P1, the physical positions are considered. By plotting the physical positions of the SxN markers against the sub clusters, sub clusters could potentially be inferred (Figure 9). For chromosome 9 of P1, the physical positions of the SxN markers indicate that sub cluster 5 and sub cluster 4 could be part of the same real homolog. For chromosome 10 of P1, such a thing could not be said, since sub cluster 5 could be linked to sub cluster 4 and sub cluster 2 as also the DxN information indicated. Therefore, the sub clusters are linked together based on the work of Bourke et al. (2015), which means that sub clusters 5 and 2 are joined together as one real homolog.

The assignment of SxN markers by the two methods, by hierarchical clustering and DxN information, leads to the same homolog clustering as with JoinMap. As can be seen from Table 6 and 7, the SxN markers are not equally distributed over the chromosomes and the homologs, for example 110 SxN markers were assigned to homolog 2 of chromosome of P2, while only 4 markers were assigned to homolog 4 of chromosome 10 of P2.

The correct homolog assignment can be checked with other marker types. Therefore, the recombination frequencies and LOD-scores between SxS markers and SxN markers are calculated, since this is also an informative marker type. First, the usual counting of the dosages happens. Secondly the different estimates for the recombination frequency are calculated (Equations 16 and 18 in Box 3 ). When r 1 is the smallest, the markers are estimated to be in coupling of each other. When r 2 is smaller than r 1 and is positive, the phase is estimate to be repulsion. When r 2 is negative, but r 1 is below 0.5 , the phase is also coupling. When r 2 is negative but r 1 is above 0.5 , then r 2 is set at 0 (as was previously done with negative recombination frequencies between two SxN markers). After the estimation of the recombination frequency, the corresponding LOD-score is calculated (Equations 17 and 19 in Box 3).

The SxS markers are assigned to homologs based on the majority of linkages with a SxN marker with a LOD-score equal or higher than 3 . The SxS markers are assigned to a homolog based on the majority of coupling-linkages within the same chromosome if there was more than one coupling linkage.

Visual inspection of the assignment of SxS markers to homologs confirmed the homolog estimation and sub cluster merging based on the SxN phase tree, DxN markers, physical positions and prior information of Bourke et al. (2015). The advantage of checking the homologs with other marker types is that those other marker types are now already assigned to the chromosomes and homologs (Table 6 and 7).

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Figure 9. SxN markers on chromosome 9 and chromosome 10 of P1. The SxN markers are divided over the sub clusters. The sub clusters of chromosome 9 can be merged together based on DxN information and physical information. The sub clusters of chromosome 10 cannot be joined together in such a way and therefore prior knowledge (Bourke et al., 2015) is used to merge those sub clusters together.

Box 3. Recombination frequency and LOD calculations between a SxN marker and a SxS marker. In this box the calculations for the LOD-score between a SxN marker and a SxS marker are shown. Furthermore, the different recombination frequency estimates for the different-phase situations are shown.


Table 6. Number of markers per chromosome and homolog of P1. The number of markers of three marker types, $\mathrm{SxN}, \mathrm{DxN}$ and the total number of markers on each chromosome and homolog is shown.

| Chromosome | Cluster | SxN |  |  |  | DxN |  |  |  | SxS |  |  |  | Total |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1 | 2 | 3 | 4 | 1 | 2 | 3 | 4 | 1 | 2 | 3 | 4 | 1 | 2 | 3 | 4 |
| 1 | 2 | 44 | 55 | 34 | 26 | 30 | 37 | 24 | 39 | 20 | 24 | 61 | 29 | 94 | 116 | 119 | 94 |
| 2 | 3 | 46 | 44 | 34 | 31 | 8 | 8 | 9 | 7 | 20 | 52 | 31 | 17 | 74 | 104 | 74 | 55 |
| 3 | 4 | 17 | 23 | 12 | 57 | 24 | 20 | 18 | 19 | 9 | 10 | 31 | 17 | 50 | 53 | 61 | 93 |
| 4 | 5 | 21 | 98 | 5 | 20 | 15 | 17 | 7 | 21 | 25 | 41 | 26 | 11 | 61 | 156 | 38 | 52 |
| 5 | 6 | 50 | 101 | 32 | 9 | 34 | 25 | 19 | 20 | 13 | 18 | 7 | 17 | 97 | 144 | 58 | 46 |
| 6 | 7 | 12 | 35 | 15 | 14 | 11 | 15 | 12 | 18 | 38 | 21 | 15 | 4 | 61 | 71 | 42 | 36 |
| 7 | 8 | 21 | 36 | 13 | 35 | 20 | 30 | 16 | 36 | 16 | 13 | 28 | 46 | 57 | 79 | 57 | 117 |
| 8 | 1 | 99 | 27 | 40 | 20 | 19 | 27 | 23 | 19 | 24 | 14 | 10 | 20 | 142 | 68 | 73 | 59 |
| 9 | 9 | 62 | 8 | 24 | 23 | 32 | 18 | 22 | 24 | 12 | 12 | 29 | 19 | 106 | 38 | 75 | 66 |
| 10 | 10 | 22 | 18 | 13 | 30 | 17 | 28 | 17 | 16 | 9 | 9 | 13 | 7 | 48 | 55 | 43 | 53 |
| 11 | 11 | 37 | 34 | 22 | 44 | 15 | 13 | 10 | 16 | 11 | 8 | 28 | 19 | 63 | 55 | 60 | 79 |
| 12 | 12 | 20 | 27 | 15 | 20 | 21 | 24 | 24 | 21 | 8 | 6 | 2 | 23 | 49 | 57 | 41 | 64 |

Table 7. Number of markers per chromosome and homolog of P2. The number of markers of three marker types, $\mathrm{SxN}, \mathrm{DxN}$ and the total number of markers on each chromosome and homolog is shown.

| Chromosome | Cluster | SxN |  |  |  | DxN |  |  |  | SxS |  |  |  | Total |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1 | 2 | 3 | 4 | 1 | 2 | 3 | 4 | 1 | 2 | 3 | 4 | 1 | 2 | 3 | 4 |
| 1 | 5 | 61 | 60 | 25 | 37 | 17 | 16 | 17 | 35 | 33 | 19 | 27 | 52 | 111 | 95 | 69 | 124 |
| 2 | 1 | 55 | 75 | 89 | 16 | 22 | 13 | 20 | 14 | 24 | 22 | 45 | 29 | 101 | 110 | 154 | 59 |
| 3 | 2 | 42 | 110 | 47 | 26 | 42 | 45 | 29 | 27 | 19 | 29 | 6 | 13 | 103 | 184 | 82 | 66 |
| 4 | 8 | 46 | 38 | 32 | 18 | 26 | 26 | 27 | 25 | 32 | 22 | 8 | 37 | 104 | 86 | 67 | 80 |
| 5 | 10 | 76 | 69 | 34 | 16 | 23 | 20 | 25 | 31 | 25 | 9 | 9 | 12 | 124 | 98 | 68 | 59 |
| 6 | 7 | 50 | 28 | 51 | 23 | 3 | 12 | 15 | 6 | 12 | 33 | 26 | 7 | 65 | 73 | 92 | 36 |
| 7 | 3 | 46 | 48 | 28 | 12 | 26 | 27 | 34 | 27 | 46 | 16 | 30 | 11 | 118 | 91 | 92 | 50 |
| 8 | 4 | 24 | 37 | 31 | 12 | 8 | 4 | 2 | 4 | 19 | 10 | 20 | 29 | 51 | 51 | 53 | 45 |
| 9 | 11 | 15 | 41 | 39 | 12 | 12 | 22 | 19 | 17 | 16 | 23 | 26 | 7 | 43 | 86 | 84 | 36 |
| 10 | 12 | 23 | 11 | 5 | 4 | 7 | 10 | 4 | 7 | 6 | 7 | 15 | 12 | 36 | 28 | 24 | 23 |
| 11 | 9 | 34 | 51 | 23 | 21 | 17 | 19 | 15 | 15 | 10 | 32 | 16 | 8 | 61 | 102 | 54 | 44 |
| 12 | 6 | 39 | 20 | 19 | 8 | 12 | 9 | 8 | 9 | 7 | 9 | 13 | 10 | 58 | 38 | 40 | 27 |

## Conclusion Chapter 3:

The new methodology to assign the SxN markers to homologs is based on a so-called phase-tree and significant DxN linkages. The cutting of the phase-tree into homologs worked for most chromosomes. However, for some chromosomes SxN with DxN linkage was necessary to end up with four homologs instead of five or six sub clusters. For two chromosomes, other types of information were necessary to end up with four homologs. It can therefore be concluded that the methodology used here works decently, but is not perfect yet.

## Chapter 4: Other segregation type markers

## Summary Chapter 4:

The recombination frequencies that have not been calculated in the previous chapters are calculated between the different marker types. When an analytical estimator is available, this is used. However, in some cases the analytical estimator for the recombination frequency is not possible or complicated. In those situations Brent's algorithm is used to optimize the likelihood function and in this way the recombination frequency for the different phases is estimated. With the analytical estimator or optimization with Brent's algorithm, the recombination frequency, LOD-score and phase for every marker pair is estimated. Furthermore, the SxT markers are assigned to chromosomes and homologs.

## Estimation of the recombination frequency without analytical estimator

In the previous chapters, the recombination frequencies between $\operatorname{SxN}$ markers (Chapter 1), SxN with DxN markers and SxS with SxN markers (Chapter 3) have been calculated. In this chapter, the recombination frequencies between the other marker types and the corresponding LOD-scores are calculated.

There are many possibilities when pairs of markers of different types and in different phases are considered (Hackett et al., 2013). For every marker type and configuration the expected genotype frequencies in terms of dosages can be calculated. A maximum likelihood equation can be derived from the genotype frequencies. Bourke (personal communication) developed an algorithm to automatically derive the maximum likelihood equation from the genotype frequencies. Whenever an analytical estimator for the recombination frequency can be found, this estimator is given as well. However, in many situations there is no analytical estimator or the expression is rather complicated. In those cases the likelihood function is maximised numerically with Brent's algorithm (Brent, 1973). Brent's algorithm finds the optimum of a function without the use of derivatives within specified bounds ( 0 and 0.5 for recombination frequencies). The best estimate for the recombination frequency is the recombination frequency with the maximum likelihood.

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## Recombination frequencies between DxN markers

In Chapter 3, the recombination frequencies between $\operatorname{DxN}$ and SxN markers are calculated. The recombination frequency of DxN markers among themselves are calculated in this chapter. Two DxN markers can be either in coupling, repulsion or a mixed phase (coupling for one pair of alleles and repulsion for the other pair). Each phase-situation has its own likelihood function (Equations 20, 21 and 22 in Box 4). The three likelihood functions are optimized with Brent's algorithm to find the maximum likelihood estimator of the recombination frequency. The maximum corresponds to the recombination frequency for the three situations. The minimum of the three recombination frequency estimates of the different phase-situations is estimated to be the most likely estimate and the corresponding phase is estimated as the most likely phase. The mixed situation is not very informative and has a high standard error (Meyer et al., 1998) and has a smaller LOD-score. The coupling and repulsion situations are equally informative and these are more informative than to the mixed phase situation.

Box 4. Recombination frequency calculations between two DxN markers. In this box the calculations for the likelihood between two DxN markers are shown. This likelihood equation can be solved with an iterative approach

## Duplex x nulliplex Duplex x nulliplex

Coupling rl
AAaa x aaaa
BBbb x bbbb
Equation $20 L(r)_{\text {coupling }}=\left(1 / 3+1 / 3 *(1-r)^{2} * 1 / 3 r^{2}\right)^{\mathrm{n} 11} *\left(1 / 6 *(1-r)^{2}\right)^{n 22+\mathrm{n} 00} *(1 / 6 *$ $\left.\mathrm{r}^{2}\right)^{\mathrm{n} 20+\mathrm{n} 02} *(1 / 3 * r *(1-\mathrm{r}))^{\mathrm{n} 01+\mathrm{n} 10+\mathrm{n} 21+\mathrm{n} 12}$

Repulsion $r 2$
AAaa x Aaaa
bbBB x bbbb
Equation $21 L(r)_{\text {repulsion }}=\left(1 / 3+1 / 3 *(1-r)^{2} * 1 / 3 * r^{2}\right)^{\mathrm{n} 11} *\left(1 / 6 *(1-r)^{2}\right)^{\mathrm{n} 20+\mathrm{n} 02} *$ $\left(1 / 6 * r^{2}\right)^{n 22+\mathrm{n} 00} *(1 / 3 * r *(1-r))^{\mathrm{n} 01+\mathrm{n} 10+\mathrm{n} 21+\mathrm{n} 12}$

> Mixed (coupling-repulsion) r3
> AAaa x aaaa
> BbBb x bbbb

Equation $22 L(r)_{\text {mixed }}=(1 / 3+1 / 3 *(1-r) * r)^{\mathrm{n} 11} *(1 / 12 * \mathrm{r} *(1-\mathrm{r}))^{\mathrm{n} 20+\mathrm{n} 20+\mathrm{n} 00+\mathrm{n} 22} *$

$$
\left(1 / 12+1 / 12 *(1-r)^{2}+1 / 12 * r^{2}\right)_{\mathrm{n} 01+\mathrm{n} 10+\mathrm{n} 21+\mathrm{n} 12}
$$

[^1]
## Recombination frequencies between SxS markers and other marker types

Another marker type that was also introduced in Chapter 3 is the SxS marker. The recombination frequency between $\operatorname{SxS}$ and SxN markers were already calculated in Chapter 3, but the recombination frequencies between SxS and DxN markers are calculated here. The likelihood function between DxN and SxS markers can be calculated (Equations 23 and 24 in Box 5). The minimum of the two recombination frequency estimates (coupling or repulsion) of the marker pair is estimated to be the most likely estimate and the corresponding phase is estimated as the most likely phase

Furthermore, the recombination frequencies among SxS markers themselves can be estimated by optimization of the likelihood function (Equations 25, 26 and 27 in Box 6). The minimum of the three recombination frequency estimates of the different phase-situations is estimated to be the most likely estimate and the corresponding phase is estimated as the most likely phase. SxS markers in coupling phase both parents are highly informative and have the highest LOD-scores of all possible marker type and phase combinations (Hackett et al., 2013). The mixed and repulsion phase are likewise less informative and have a lower LOD-score.

Box 5. Recombination frequency calculations between a DxN marker and a SxS marker. In this box the calculations for the likelihood between a DxN and SxS marker are shown. This likelihood equation can be solved with an iterative and an analytical approach.

| Duplex x nulliplex <br> Simplex x simplex |
| :---: |
| Coupling rl |
| AAaa x aaaa |
| Bbbb x Bbbb |

Equation $23 L(r)_{\text {coupling }}=1 / 12^{n 00+n 01+n 10+n 21+n 20+n 12+n 02+n 22} * 2^{n 10+n 12} *(1-r)^{n 00+n 22} *$

$$
r^{n 20+n 02} * 1 / 3^{n 11}
$$

Repulsion $r 2$
AAaa x Aaaa
bbBb x bbbb
Equation $24 L(r)_{\text {repulsion }}=1 / 12^{n 00+n 01+n 10+n 21+n 20+n 12+n 02+n 22} * 2^{n 10+n 12} *(1-r)^{n 20+n 02} *$
$r^{n 00+n 22} * 1 / 3^{n 11}$

* $\mathrm{L}(\mathrm{r})$ is the likelihood of $\mathrm{r}, \mathrm{r} 1$ is the estimate of the recombination frequency of a SxS marker and a DxN marker in coupling phase, r 2 is the estimate of the recombination frequency of SxS marker and a DxN marker in repulsion phase, n 01 is the number of markers that have genotype aaaa and Bbbb, $n 20$ is the number of markers that have genotype AAaa and bbbb, n 00 is the number of markers that have genotype aaaa and bbbb, 221 is the number of markers that have genotype AAaa and Bbbb, n10 is the number of markers that have genotype Aaaa and bbbb, n02 is the number of markers that have genotype aaaa and $B B b b, n 22$ is the number of markers that have genotype AAaa and BBbb, n12 is the number of markers that have genotype Aaaa and BBbb, the A's (for example Aaaa) and B's (for example Bbbb) are not position dependent.

Please note that an analytical estimator is possible as well.

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Box 6. Recombination frequency calculations between two SxS marker. In this box the calculations for the likelihood between two SxS markers are shown. This likelihood equation can be solved with an iterative approach.

## Simplex x simplex <br> Simplex x simplex

Coupling rl
Aaaa x Aaaa
Bbbb x Bbbb

Equation $25 L(r)_{\text {coupling }}=1 / 2^{\mathrm{n} 11+\mathrm{n} 01+\mathrm{n} 10+\mathrm{n} 21+\mathrm{n} 12} * 1 / 4^{\mathrm{n} 00+\mathrm{n} 20+\mathrm{n} 22+\mathrm{n} 02} *\left(\mathrm{r}^{2}\right)^{\mathrm{n} 02+\mathrm{n} 20} *((1-$ $\left.r)^{2}\right)^{\mathrm{n} 00+\mathrm{n} 22} *(\mathrm{r} *(1-\mathrm{r}))^{\mathrm{n} 01+\mathrm{n} 10+\mathrm{n} 21+\mathrm{n} 12} *\left(\mathrm{r}^{2}+(1-\mathrm{r})^{2}\right)^{\mathrm{n} 11}$

Repulsion $r 2$
Aaaa x Aaaa
bBbb x bBbb

Equation $26 L(r)_{\text {mixed }}=1 / 12^{\mathrm{n} 00+\mathrm{n} 01+\mathrm{n} 02+\mathrm{n} 10+\mathrm{n} 12+\mathrm{n} 10+\mathrm{n} 22} *\left(1-\mathrm{r}^{2}\right)^{\mathrm{n} 00+\mathrm{n} 22} *\left(2 * \mathrm{r}^{2}-2 \mathrm{r}+\right.$ $2)^{\mathrm{n} 01+\mathrm{n} 10+\mathrm{n} 21+\mathrm{n} 12} *(\mathrm{r} *(2-\mathrm{r}))^{\mathrm{n} 01+\mathrm{n} 20} *\left(4 * \mathrm{r}-4 * \mathrm{r}^{2}+2\right)^{\mathrm{n} 11}$ Mixed (coupling-repulsion) r3

Aaaa x Aaaa
Bbbb x bBbb
Equation $27 L(r)_{\text {repulsion }}=\left(5 / 18-1 / 6 * r+1 / 9 * r^{2}\right)^{n 11} *\left(1 / 36+1 / 18 * r+1 / 36 * r^{2}\right)^{n 00+n 22} *$

$$
\left(1 / 9+1 / 18 * r-1 / 18 * r^{2}\right)^{n 01+n 10+n 21+n 12} *\left(1 / 9-1 / 9 * r+1 / 36 * r^{2}\right)^{n 20+n 02}
$$

* $\mathrm{L}(\mathrm{r})$ is the likelihood of $\mathrm{r}, \mathrm{r} 1$ is the estimate of the recombination frequency between two $S x S$ markers in coupling phase, r 2 is the estimate of the recombination frequency between two $S x S$ markers in coupling phase, $r 3$ is the estimate of the recombination frequency between two $S x S$ markers in mixed phase, $n 01$ is the number of markers that have genotype aaaa and Bbbb, n 20 is the number of markers that have genotype AAaa and bbbb, n00 is the number of markers that have genotype aaaa and bbbb, n21 is the number of markers that have genotype AAaa and Bbbb, n10 is the number of markers that have genotype Aaaaa and bbbb, n02 is the number of markers that have genotype aaaa and BBbb, $n 22$ is the number of markers that have genotype AAaa and BBbb,, n12 is the number of markers that have genotype Aaaa and BBbb, $n 11$ is the number of markers that have genotype Aaaa and Bbbb, the A's (for example Aaaa) and B's (for example Bbbb) are not position dependent.


## Assignment of SxT markers to chromosomes and homologs

The last marker type that has not been considered so far is SxT. Hackett et al. (2013) call this marker type XSS, probably because the segregation ratio of a SxS marker and SxT marker is the same. However in this thesis this marker type is called SxT, since in one parent the marker has a simplex allele and in the other parent a triplex allele. In a normal SxS marker, both the segregating simplex alleles are informative, but in a SxT marker, the one simplex allele is informative in one parent whereas the segregating non-triplex allele is informative in the other. When one tries to transform SxT markers (to SxS), he or she will notice that this is not possible without wrongfully transforming one parent. The recombination frequencies and LOD-scores between a SxT marker and a $S x N$ can be estimated analytically (Equations 28 until 34 in Box 7).

The SxT markers are assigned to chromosomes based on the majority of linkages with a LOD-score equal or higher than 3. For P1 the SxT markers are assigned to homologs based on the majority of coupling linkage (meaning that the simplex alleles of both markers are in coupling; Box 7). For P2 the SxT markers are assigned to homologs based on repulsion linkage, since the segregating allele of the P 2 is the non-triplex allele (Box 7). The SxT markers are not equally distributed over the chromosomes and homologs (Table 8). Some chromosomes contain a fair amount of SxT markers while other chromosomes contain very few or none.

Table 8. Number of SxT markers divided over chromosomes and homologs. The SxT markers of P1 are assigned to chromosomes and homologs based on coupling linkage with SxN markers while the SxT marker of P2 are assigned to chromosomes and homologs based on repulsion linkage with SxN markers.

| Chromosome | $\mathbf{P 1}$ |  |  |  |  | $\mathbf{P 2}$ |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | $\mathbf{1}$ | 2 | 3 | 4 | 1 | 2 | 3 | 4 |
|  | 4 | 17 | 12 | 31 | 32 | 2 | 23 | 7 |
| 3 | 3 | 9 | 5 | 6 | 7 | 4 | 11 | 4 |
| 4 | 9 | 4 | 1 | 26 | 7 | 1 | 27 | 5 |
| 5 | 13 | 4 | 2 | 20 | 17 | 10 | 5 | 8 |
| 6 | 5 | 27 | 5 | 7 | 10 | 27 | 0 | 7 |
| 7 | 6 | 2 | 4 | 0 | 3 | 3 | 6 | 0 |
| 9 | 7 | 20 | 5 | 6 | 12 | 9 | 14 | 3 |
| 10 | 10 | 4 | 22 | 2 | 2 | 7 | 23 | 6 |
| 11 | 6 | 10 | 4 | 9 | 4 | 3 | 12 | 10 |
| 12 | 5 | 1 | 11 | 0 | 5 | 1 | 1 | 3 |
|  | 4 | 35 | 2 | 4 | 3 | 1 | 4 | 37 |

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Box 7. Recombination frequency and LOD calculations between a SxN marker and a SxT marker. In this box the calculations for the LOD-score and recombination frequencies between a SxN marker and a SxT marker are shown for the different-phase situations are shown. For P1 the calculations of SxT with SxN are used and for P2 the calculations of TxS with SxN are used.

## Simplex x triplex Simplex x nulliplex

Coupling r1
Aaaa x AAAa
Bbbb x bbbb

$$
\text { Equation } 28 r=\frac{\mathrm{n} 30+\mathrm{n} 11}{\mathrm{n} 30+\mathrm{n} 11+\mathrm{n} 31+\mathrm{n} 10}
$$

Equation $29 L O D=\log 10\left(\frac{1 / 4 *(\mathrm{n} 20+\mathrm{n} 11+\mathrm{n} 21+\mathrm{n} 10+\mathrm{n} 31+\mathrm{n} 30) *(1-\mathrm{r}) *(\mathrm{n} 11+\mathrm{n} 30) * \mathrm{r} *(\mathrm{n} 10+\mathrm{n} 31)}{1 / 4 *(\mathrm{n} 20+\mathrm{n} 11+\mathrm{n} 21+\mathrm{n} 10+\mathrm{n} 31+\mathrm{n} 30) *(1-1 / 2) *(\mathrm{n} 11+\mathrm{n} 30) * 1 / 2 *(\mathrm{n} 10+\mathrm{n} 31)}\right)$

> Repulsion $r 2$
> Aaaa x AAAa
> bBbb x bbbb

$$
\text { Equation } 30 \mathrm{r}=\frac{2 *(\mathrm{n} 10+\mathrm{n} 31)-(\mathrm{n} 11+\mathrm{n} 30)}{(\mathrm{n} 11+\mathrm{n} 30+\mathrm{n} 10+\mathrm{n} 31)}
$$

Equation $31 \mathrm{~L} O D=\log 10\left(\frac{1 / 4 *(\mathrm{n} 21+\mathrm{n} 20) *(1 / 12+1 / 12 * \mathrm{r}) *(\mathrm{n} 10+\mathrm{n} 31) *(1 / 6-1 / 12 * \mathrm{r}) *(\mathrm{n} 11+\mathrm{n} 30)}{1 / 4 *(\mathrm{n} 21+\mathrm{n} 20) *(1 / 12+1 / 12 * 1 / 2) *(\mathrm{n} 10+\mathrm{n} 31) *(1 / 6-1 / 12 * 1 / 2) *(\mathrm{n} 11+\mathrm{n} 30}\right)$

## Triplex x simplex <br> Simplex x nulliplex

Coupling r1
AAAa x Aaaa
Bbbb x bbbb
Equation $32 r=\frac{2 *(\mathrm{n} 11+\mathrm{n} 30)-(\mathrm{n} 10+\mathrm{n} 31)}{(\mathrm{n} 11+\mathrm{n} 30+\mathrm{n} 10+\mathrm{n} 31)}$
Equation 32 LOD $=\log 10\left(\frac{1 / 12 *(\mathrm{n} 21+\mathrm{n} 10+\mathrm{n} 20+\mathrm{n} 11+\mathrm{n} 31+\mathrm{n} 30) *(2-\mathrm{r}) *(\mathrm{n} 31+\mathrm{n} 10) *(1+\mathrm{r}) *(\mathrm{n} 11+\mathrm{n} 30)}{1 / 12 *(\mathrm{n} 21+\mathrm{n} 10+\mathrm{n} 20+\mathrm{n} 11+\mathrm{n} 31+\mathrm{n} 30) *(2-1 / 2) *(\mathrm{n} 31+\mathrm{n} 10) *(1+1 / 2) *(\mathrm{n} 11+\mathrm{n} 30)}\right)$

## Repulsion $r 2$ <br> AAAa x Aaaa <br> bbbB x bbbb

Equation $33 r=\frac{\mathrm{n} 31+\mathrm{n} 10}{\mathrm{n} 30+\mathrm{n} 11+\mathrm{n} 31+\mathrm{n} 10}$
Equation $34 L O D=\log 10\left(\frac{1 / 4 *(\mathrm{n} 20+\mathrm{n} 11+\mathrm{n} 21+\mathrm{n} 10+\mathrm{n} 31+\mathrm{n} 30) *(1-\mathrm{r}) *(\mathrm{n} 11+\mathrm{n} 30) * \mathrm{r} *(\mathrm{n} 10+\mathrm{n} 31)}{1 / 4 *(\mathrm{n} 20+\mathrm{n} 11+\mathrm{n} 21+\mathrm{n} 10+\mathrm{n} 31+\mathrm{n} 30) *(1-1 / 2) *(\mathrm{n} 11+\mathrm{n} 30) * 1 / 2 *(\mathrm{n} 10+\mathrm{n} 31)}\right)$

[^2]
## Recombination frequencies between SxT markers and other marker types

Furthermore, the linkages between the SxT markers and the other marker types can be calculated as well (Box 8, 9 and 10). Since an SxS and a SxT marker have the same segregation ratio, the informativeness and standard errors of SxT markers are similar to those of SxS markers. In addition, it should be noted that mixed and repulsion phases between SxS and SxT markers are very uninformative (Appendix 7). This can lead to a relative flat likelihood function and hence the optimization of the likelihood function may give wrong estimates for the recombination frequency. Experience showed that sometimes the estimated recombination frequency can be 0 for very distantly linked markers in the highly uninformative phases. Therefore extra care should be taken when considering estimated recombination frequencies of SxT with SxS markers in mixed and repulsion phase.

Box 8. Recombination frequency calculations between a SxT marker and a DxN marker. In this box the calculations for the likelihood between a SxT and DxN marker are shown. This likelihood equation can be solved with an iterative and an analytical approach.

## Simplex x triplex <br> Duplex x nulliplex <br> Coupling rl <br> Aaaa x AAAa <br> BBbb x bbbb

Equation $35 L(r)=(1 / 12 * \mathrm{r})^{\mathrm{n} 30+\mathrm{n} 12} * 1 / 6^{\mathrm{n} 31+\mathrm{n} 22+\mathrm{n} 20+\mathrm{n} 11} *(1 / 12-1 / 12 * \mathrm{r})^{\mathrm{n} 32+\mathrm{n} 10} * 1 / 3^{\mathrm{n} 21}$
Repulsion $r 2$
Aaaa x AAAa
bBBb x bbbb
Equation $36 L(r)=(1 / 12-1 / 12 * r)^{\mathrm{n} 30+\mathrm{n} 12} * 1 / 6^{\mathrm{n} 31+\mathrm{n} 22+\mathrm{n} 20+\mathrm{n} 11} *(1 / 12 * \mathrm{r})^{\mathrm{n} 32+\mathrm{n} 10} * 1 / 3^{\mathrm{n} 21}$

* $L(r)$ is the likelihood of $r$, $r 1$ is the estimate of the recombination frequency of a SxT marker and a DxN marker in coupling phase, r 2 is the estimate of the recombination frequency of SxT marker and a DxN marker in repulsion phase, n 32 is the number of markers that have genotype AAAa and BBbb, n20 is the number of markers that have genotype AAaa and bbbb, n30 is the number of markers that have genotype AAAa and bbbb, n21 is the number of markers that have genotype AAaa and Bbbb, n10 is the number of markers that have genotype Aaaa and bbbb, n22 is the number of markers that have genotype AAaa and BBbb, n01 is the number of markers that have genotype aaaa and $\mathrm{Bbbb}, \mathrm{n} 12$ is the number of markers that have genotype Aaaa and $\mathrm{BBbb}, \mathrm{n} 31$ is the number of markers that have genotype AAAa and Bbbb, n11 is the number of markers that have genotype Aaaa and Bbbb, the A's (for example Aaaa) and B's (for example Bbbb) are not position dependent.

Please note that an analytical estimator is possible as well.

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Box 9. Recombination frequency calculations between a SxT marker and a SxS marker. In this box the calculations for the likelihood between a SxT and SxS marker are shown. This likelihood equation can be solved with an iterative approach.

## Simplex $x$ triplex <br> Simplex x simplex

Coupling rl
Aaaa x AAAa
Bbbb x Bbbb

Equation $37 L(r)=\left(1 / 12 * r+1 / 12 * r^{2}\right)^{\mathrm{n} 30+\mathrm{n} 12} *\left(1 / 12+1 / 6 * \mathrm{r}-1 / 6 * \mathrm{r}^{2}\right)^{\mathrm{n} 31+\mathrm{n} 22+\mathrm{n} 20+\mathrm{n} 11} *$ $\left(1 / 6-1 / 4 * r+1 / 12 * r^{2}\right)^{n 32+n 10} *\left(1 / 3-1 / 3 * r+1 / 3 * r^{2}\right)^{n 21}$

Repulsion $r 2$
Aaaa x AAAa
bBbb x bbbB
Equation $38 L(r)=\left(1 / 6-1 / 4 * r+1 / 12 * r^{2}\right)^{n 30+n 12} *\left(1 / 12+1 / 6 * r-1 / 6 * r^{2}\right)^{n 31+n 22+n 20+n 11} *$ $\left(1 / 12 * r+1 / 12 * r^{2}\right)^{n 32+n 10} *\left(1 / 3-1 / 3 * r+1 / 3 * r^{2}\right)^{n 21}$

Mixed 1 (repulsion-coupling) r3
Aaaa x AAAa
bBbb x Bbbb

Equation 39

$$
\begin{gathered}
L(r)=\left(1 / 18+1 / 36 * r-1 / 36 * r^{2}\right)^{\mathrm{n} 30+\mathrm{n} 12} *\left(5 / 36-1 / 18 * r+1 / 18 * r^{2}\right)^{\mathrm{n} 31+\mathrm{n} 22+\mathrm{n} 20+\mathrm{n} 11} * \\
\left(1 / 18+1 / 36 * \mathrm{r}-1 / 36 * \mathrm{r}^{2}\right)^{\mathrm{n} 32+\mathrm{n} 10} *\left(2 / 9+1 / 9 * \mathrm{r}-1 / 9 * \mathrm{r}^{2}\right)^{\mathrm{n} 21}
\end{gathered}
$$

Mixed2 (coupling- repulsion) r4
Aaaa x AAAa
Bbbb x bbbB

$$
\text { Equation } 40 L(r)=\left(1 / 4 * \mathrm{r}-1 / 4 * \mathrm{r}^{2}\right)^{\mathrm{n} 30+\mathrm{n} 12} *\left(1 / 4-1 / 2 * \mathrm{r}+1 / 2 * \mathrm{r}^{2}\right)^{\mathrm{n} 31+\mathrm{n} 22+\mathrm{n} 20+\mathrm{n} 11} *
$$

$$
\left(1 / 4 * r-1 / 4 * r^{2}\right)^{n 32+n 10} *\left(r-r^{2}\right)^{n 21}
$$

* $\mathrm{L}(\mathrm{r})$ is the likelihood of $\mathrm{r}, \mathrm{r} 1$ is the estimate of the recombination frequency of a SxS marker and a SxT marker in coupling phase, r 2 is the estimate of the recombination frequency of SxS marker and a SxT marker in repulsion phase, r3 is the estimate of the recombination frequency of SxS marker and a SxT marker in mixed-1 phase, r4 is the estimate of the recombination frequency of SxS marker and a SxT marker in mixed-2 phase, n32 is the number of markers that have genotype AAAa and BBbb, n20 is the number of markers that have genotype AAaa and bbbb, n30 is the number of markers that have genotype AAAa and bbbb, n21 is the number of markers that have genotype AAaa and Bbbb, n10 is the number of markers that have genotype Aaaa and bbbb, n22 is the number of markers that have genotype AAaa and $\mathrm{BBbb}, \mathrm{n} 01$ is the number of markers that have genotype aaaa and $\mathrm{Bbbb}, \mathrm{n} 12$ is the number of markers that have genotype Aaaa and $B B b b, n 31$ is the number of markers that have genotype AAAa and Bbbb, n11 is the number of markers that have genotype Aaaa and Bbbb, the A's (for example Aaaa) and B's (for example Bbbb) are not position dependent.

Box 10. Recombination frequency calculations between two SxT markers. In this box the calculations for the likelihood between two SxT markers are shown. This likelihood equation can be solved with an iterative approach.

## Simplex x triplex Simplex $x$ triplex

Coupling rl
Aaaa x AAAa
Bbbb x BBBb
Equation $41 L(r)=\left(1 / 4 * r^{2}\right)^{\mathrm{n} 13+\mathrm{n} 31} *\left(1 / 2 * \mathrm{r}-1 / 2 * \mathrm{r}^{2}\right)^{\mathrm{n} 23+\mathrm{n} 32+\mathrm{n} 12+\mathrm{n} 21} *(1 / 4-1 / 2 * \mathrm{r}+1 / 4 *$ $\left.r^{2}\right)^{\mathrm{n} 33+\mathrm{n} 11} *\left(1 / 2-r+\mathrm{r}^{2}\right)^{\mathrm{n} 22}$

Repulsion $r 2$
Aaaa x AAAa
bBbb x BBbB
Equation $42 L(r)=\left(1 / 9-1 / 9 * r+1 / 36 * r^{2}\right)^{\mathrm{n} 13+\mathrm{n} 31} *\left(1 / 9+1 / 18 * \mathrm{r}-1 / 18 * \mathrm{r}^{2}\right)^{\mathrm{n} 23+\mathrm{n} 32+\mathrm{n} 12+\mathrm{n} 21} *$

$$
\left(1 / 36+1 / 18 * r+1 / 36 * r^{2}\right)^{n 33+n 11} *\left(5 / 18-1 / 9 * r+1 / 9 * r^{2}\right)^{n 22}
$$

Mixedl (repulsion-coupling) r3
Aaaa x AAAa
bBbb x BBBb

$$
\begin{aligned}
& \text { Equation } 43 L(r)=\left(1 / 6 * \mathrm{r}-1 / 12 * \mathrm{r}^{2}\right)^{\mathrm{n} 13+\mathrm{n} 31} *\left(1 / 6-1 / 6 * \mathrm{r}+1 / 6 * \mathrm{r}^{2}\right)^{\mathrm{n} 23+\mathrm{n} 32+\mathrm{n} 12+\mathrm{n} 21} * \\
& \begin{array}{c}
\left(1 / 12-1 / 12 * \mathrm{r}^{2}\right)^{\mathrm{n} 33+\mathrm{n} 11} *\left(1 / 6+1 / 3 * \mathrm{r}-1 / 3 * \mathrm{r}^{2}\right)^{\mathrm{n} 22} \\
\text { Mixed } 2(\text { coupling- repulsion }) r 4 \\
\text { Aaaa x AAAa } \\
\text { Bbbb x BBbB }
\end{array}
\end{aligned}
$$

$$
\text { Equation } 44 L(r)=\left(1 / 6 * \mathrm{r}-1 / 12 * \mathrm{r}^{2}\right)^{\mathrm{n} 13+\mathrm{n} 31} *\left(1 / 6-1 / 6 * \mathrm{r}+1 / 6 * \mathrm{r}^{2}\right)^{\mathrm{n} 23+\mathrm{n} 32+\mathrm{n} 12+\mathrm{n} 21} *
$$

$$
\left(1 / 12-1 / 12 * r^{2}\right)^{\mathrm{n} 33+\mathrm{n} 11} *\left(1 / 6+1 / 3 * r-1 / 3 * r^{2}\right)^{\mathrm{n} 22}
$$

* $\mathrm{L}(\mathrm{r})$ is the likelihood of $\mathrm{r}, \mathrm{r} 1$ is the estimate of the recombination frequency of between two SxT markers in coupling phase, r 2 is the estimate of the recombination frequency between two SxT markers in repulsion phase, r3 is the estimate of the recombination frequency between two SxT markers in mixed-1 phase, r 4 is the estimate of the recombination frequency between two SxT markers in mixed- 2 phase, $n 32$ is the number of markers that have genotype AAAa and $B B b b, n 23$ is the number of markers that have genotype AAaa and $\mathrm{BBBb}, \mathrm{n} 33$ is the number of markers that have genotype AAAa and $\mathrm{BBBb}, \mathrm{n} 21$ is the number of markers that have genotype AAaa and Bbbb, $n 10$ is the number of markers that have genotype Aaaaa and bbbb, $n 22$ is the number of markers that have genotype AAaa and BBbb, n01 is the number of markers that have genotype aaaa and Bbbb, n13 is the number of markers that have genotype Aaaa and BBBb, n12 is the number of markers that have genotype Aaaa and BBbb, n31 is the number of markers that have genotype AAAa and Bbbb, $n 11$ is the number of markers that have genotype Aaaa and Bbbb, the A's (for example Aaaa) and B's (for example Bbbb) are not position dependent.

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## Validation of the likelihood equation by means of simulation

Simulations with PedigreeSim showed that Brent's algorithm was able to give correct estimates of the simulated recombination frequencies by optimizing the likelihood function for the population size as used in this thesis (results not shown). However, for future estimations of the recombination frequency in this and other populations, the log-likelihood function would be recommended (Van Ooijen \& Jansen, 2013).

## Conclusion Chapter 4:

In this chapter the recombination frequencies, LOD-score and phase is estimated between all the marker pairs that were not considered in the previous chapters. This was done by using the analytical estimator or optimizing the likelihood function with Brent's algorithm, which worked well for the informative phases. Furthermore, the SxT markers were assigned to chromosomes and homologs in a similar matter as the other marker segregation types.

## Chapter 5: Ordering with linear regression - Theory

## Summary Chapter 5:

The recombination frequencies, calculated in the previous chapters, are transformed to distances with the Haldane's mapping function. The distances were used in a linear regression approach to estimate a linkage map. The linear regression approach is straightforward and deterministic. It uses the observed distances, the transformed recombination frequencies, to estimate the expected distances, the map distances, by minimising the sum of squares in a linear model. By doing so, the optimal map is found. Markers are added one by one based on the LOD-score. Markers can be rejected based on the Chi-square test-statistic, negative distances and a jumptest. The time to map markers with the linear regression approach is exponential with the number of markers.

## Converting the recombination frequencies into distances.

Numerous methods to estimate linkage maps have been developed by scientist over the past century. One of the methods to estimate a linkage map is a linear regression approach and this method was used in this thesis to estimate the linkage maps of the homologs. Linear regression is a so-called greedy or nearest-neighbour algorithm (Van Ooijen \& Jansen, 2013d). It is relatively straightforward and deterministic. The algorithm adds the closest marker to the marker order and builds the order step-by-step. How the linear regression works in practice is explained below.

Jensen and Jorgenson (1975) used the linear regression method for the first time to estimate a map of barley. They first converted the calculated recombination frequencies into map distances by a mapping function. The reason why recombination frequencies are converted to map distances first is that recombination frequencies are not additive (since they do not count even numbers of recombination events as recombinants). Therefore, mapping functions are used that can convert recombination frequencies into genetic distances that are additive. The two most widely used mapping functions are Haldane's and Kosambi's (Equation 46 and 47). Haldane's mapping function assumes that the crossovers follow a Poisson distribution and are independent of one another regardless of their relative location, while Kosambi's mapping function takes positive interference into account (Vinod, 2011). Before transforming the recombination frequencies into distances, the recombination frequencies of 0.5 are set at 0.499 (Hackett \& Broadfoot, 2003). The difference between Haldane's and Kosambi's mapping functions is very small for small recombination frequencies (Figure 10).

Equation $45 d_{\text {Morgan }}=r * 100$
Equation $46 d_{\text {Haldane }}=-\frac{1}{2} * \ln (1-2 * r) * 100$
Equation $47 d_{\text {Kosambi }}=\frac{1}{4} * \ln \left(\frac{1+2 * r}{1-2 * r}\right) * 100$
*d is the distance, r is the recombination frequency


Figure 10. Distances by mapping functions plotted against the recombination frequencies. The recombination frequencies between SxN markers of P 1 are used to create this plot. This plot corresponds to the plot described by Liu (1997d).

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For the study of local map regions the used mapping function is not of high relevance, but for studying the total map length the choice of the mapping function is of importance. Both mapping functions are used so far for linkage mapping of potato. Kosambi’s mapping function has been used to convert recombination frequencies into mapping distances of diploid potato (Sharma et al., 2013), while Haldane's mapping function was used to map tetraploid potato (Hackett et al., 2013; Hackett et al., 1998). Haldane's mapping function was used in this thesis to be in correspondence with Hackett et al. (2013) and Hackett et al. (1998) and the assumption of no interference (Assumption 4 and 5). Furthermore, in this thesis it is assumed that Haldane's mapping function is applicable to tetraploids although it was developed for diploids (Assumption 12).

## The linear model

Now that the recombination frequencies are translated into additive distances, they can be used in a linear model. The parameters in the linear model (the linkage map) are the adjacent distances between markers, while all the pairwise distances are considered when estimating the model (Van Ooijen \& Jansen., 2013b; Liu, 1997d). If a map with four markers in the order A-B-C-D, then the model can be defined as Set of equations 48.

Set of equations 48

$$
\begin{aligned}
d A B & =\delta A B+e A B \\
d B C & =\delta B C+e B C \\
d C D & =\delta C D+e C D \\
d A C & =\delta A B+\delta B C+e A C \\
d B D & =\delta B C+\delta C D+e B D \\
d A D & =\delta A B+\delta B C+\delta C D+e A D
\end{aligned}
$$

*With $\mathrm{d}_{\mathrm{xy}}$ being the observed distance (based on recombination frequency) between marker x and marker $\mathrm{y}, \delta_{\mathrm{xy}}$ being the expected distance between marker x and y based on the model and $\mathrm{e}_{\mathrm{xy}}$ the error corresponding to the distance between marker x and y

One can imagine that this set of equations becomes increasing more complicated when more markers are added to the given order. However, this is not the case, since the basic structure of the equations stays the same if the equations are put in matrix-format (Equation 49). The equation in matrix-format is a standard linear model with more known parameters than unknown parameters.

Equation $49\left(\begin{array}{l}d A B \\ d B C \\ d C D \\ d A C \\ d B D \\ d A D\end{array}\right)=\left(\begin{array}{lll}1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 1 & 1\end{array}\right)\left(\begin{array}{l}\delta A B \\ \delta B C \\ \delta C D\end{array}\right)+\left(\begin{array}{c}e A B \\ e B C \\ e C D \\ e A C \\ e B D \\ e A D\end{array}\right)$

[^3]One standard assumption of linear regression is that the standard errors have equal variances. However, this is not the case since small distances are more precisely estimated than large distances. To adjust for these unequal variances, a weighted least squares method is used (Van Ooijen \& Jansen, 2013b). JoinMap (version 1) initially did this by using the LOD-score (Stam, 1993; Liu, 1997d), and in later versions the square of the LODscore is used (Van Ooijen, 2006). In this thesis the LOD ${ }^{2}$ was used as weight in correspondence with the current version of JoinMap (version 4.1). Another advantage of using the LOD-scores as weight is that the amount of individuals (or missing values) is automatically accounted for and non-informative pairings do not contribute very much to the map estimation.

Another assumption is that the residuals of the pairwise distances, or pairwise recombination frequencies, are independent of each other (Assumption 10). From computer simulations dependency of the residuals of distances did not appear to be a problem (Van Ooijen \& Jansen, 2013b).

The parameters $(\delta \mathrm{AB}, \delta \mathrm{BC}$ and $\delta \mathrm{CD})$ in the linear model represent the final map distances. These parameters can be estimated by minimizing the SSE (Equation 50; Stam, 1993). This formula can be differentiated with respect to $\delta \mathrm{AB}, \delta \mathrm{BC}$ and $\delta \mathrm{CD}$ and estimates for these parameters can be obtained. The estimated parameters ( $\delta \mathrm{AB}, \delta \mathrm{BC}$ and $\delta \mathrm{CD}$ ) represent the final map distances. The matrix equation can easily be extended to contain more markers.

Equation $50 S S E=L O D_{A B}{ }^{2} *(\delta A B-d A B)^{2}+L O D_{B C}{ }^{2} *(\delta B C-d B C)^{2}+L O D_{C D}{ }^{2} *(\delta C D-d C D)^{2}+$ $L O D_{A C}{ }^{2} *(\delta A C-d A B-d B C)^{2}+L O D_{B D}{ }^{2} *(\delta B D-d B C-d C D)^{2}+L O D_{A D}{ }^{2} *(\delta A D-d A B-d B C-$ $d C D)^{2}$
*With $\mathrm{d}_{\mathrm{xy}}$ being the observed distance (based on recombination frequency) between marker x and marker $\mathrm{y}, \delta_{\mathrm{xy}}$ being the expected distance between marker x and y based on the model and $\mathrm{LOD}_{\mathrm{xy}}$ the LOD/score between marker x and y

## Selecting the markers

A careful reader might have noted that the map can be estimated with the linear regression method for any given order, but that linear regression does not present a way to find the optimal order. The best order has to be chosen based on other criteria and during this thesis several possible criteria were used.

The first obvious step in regression mapping is finding the first pair. In the regression method of JoinMap, this is done by considering the marker pair that is most informative (Van Ooijen, 2006).

Informativeness is reflected in the LOD-score and therefore the pair with the highest LOD-score was used as the starting pair in this thesis.

The next marker to be added is selected based on the sum of LOD-scores between this marker and the markers already in the order. Consider the following example in which the order consists of marker A-B-C and there are two markers, D and E , yet unmapped. The LOD-score of A-D is $8, \mathrm{~B}-\mathrm{D}$ is $5, \mathrm{C}-\mathrm{D}$ is 6 , $\mathrm{A}-\mathrm{E}$ is $4, \mathrm{~B}-\mathrm{E}$ is 4 and $\mathrm{C}-\mathrm{E}$ is 7. The next marker to be added in the mapping procedure is then D , since the sum of LOD-scores is higher for this marker $(8+5+6=19)$ than for marker $E(4+4+7=15)$. LOD-scores between markers that are not yet in the order (in this example the LOD-score between marker D and E ) are neglected in this procedure.

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After the next marker is selected, the best fitting position is determined. The new marker is considered at every position of the marker order without changing the current map order (Stam, 1993). Consider again the order of marker A-B-C. The next marker, D, can fit at the following positions: D-A-B-C, A-D-B-C, A-B-D-C and A-B-C-D. The linear model, as described above, is applied to these different marker orders. From this, the residual sum of squares ( SSE ) is calculated automatically, since this is minimized by the least square method. The smaller the SSE is the better the model (the order of markers) fits the data. The marker order with the lowest SSE is the order with the best fit (Van Ooijen \& Jansen, 2013c) and this new order contains the new marker.

After the next marker is fitted into the order, a reshuffling, or ripple, is performed. The ripple is considering all the possible orders within a moving window (of usually three markers) (Van Ooijen, 2006). Consider the previous example again with markers A-B-C-D being ordered. The ripple will look at all permutations within a moving window of three markers. Thus marker orders of A-B-C-D, A-C-B-D,C-A-B-D,C-B-A-D, B-C-A-D (for the first moving window) and A-B-C-D, A-B-D-C, A-D-B-C, A-D-C-B, A-C-D-B and A-C-B-D (for the second moving window). Based on all these orders, the most optimal order is determined again by the lowest SSE. As one can imagine from seeing the many possibilities of the ripple, the ripple is a timeconsuming process (Stam, 1993; see below), but is needed to find the best global order instead of a local order

## Evaluation of markers

To see if the optimal map order is actually any good, the map distances are transformed back to recombination frequencies with the reverse of the Haldane mapping function (Van Ooijen, 2006; Vinod, 2011; Equation 51).

Equation $51 r=\frac{1}{2} *\left(1-e^{-2 d_{\text {Haldane }}}\right)$

When there is a negative recombination frequency (either observed or expected) between 0 and -0.001 the recombination frequency is considered to be 0 . This will lead to a poorer fit, since the observed and expected recombination frequency have a larger difference, but the marker order is still evaluated. When there is a negative recombination frequency below -0.001 it is considered to be a negative recombination frequency. Negative recombination frequencies (or distances) cannot happen in reality and therefore the order with the next marker is rejected.

After this step, the goodness-of-fit Chi-square is calculated (Set of equations 52; Van Ooijen (personal communication). The goodness-of-fit is a likelihood ratio test. The degrees of freedom of this test are roughly equal to the number of pairs with a direct estimate (the number of parameters in the model) minus the number of map distances (Van Ooijen, 2006). When the test statistic is not significant it means that the expected and observed recombination frequencies are not different and the linear model (the order) is considered to be good. On the other hand, when the Chi-square statistic is significant, the order is considered to have a poor fit and the new marker is rejected from the order.

Set of equations 52:

$$
\chi 2=\sum R * \ln \left(\frac{r_{o b s}}{r_{\text {exp }}}\right) \sim \chi_{d f}^{2}
$$

with $R=N *$ robs
with $N=\frac{L O D}{s * \log 10(s)+r_{o b s} * \log 10\left(r_{o b s}\right)+\log 10(2)}$
with $s=1-r_{o b s}$
with $d f \approx$ number of pairs with a direct estimate - number of total map distances
${ }^{*} \mathrm{r}_{\text {obs }}$ is the observed recombination frequency, $\mathrm{r}_{\mathrm{exp}}$ is the recombination frequency from the model, $\chi^{2}$ is the Chi-Square value, df is the degrees of freedom, R is the number of recombinants, N is the number of individuals, LOD is the logarithm of odds ratio.

The goodness-of-fit Chi-square indicates whether the added marker is at a likely position and doesn't create a conflicting order. However, this does not tell if the order with the added marker is better than the order without the added marker. To compare the order with and without the added marker, the goodness-of-fit Chisquare is also used. In the so called jump-test, two Chi-square values (one for the order without the new marker and one for the order with the new marker), are compared (Van Ooijen, personal communication). However, since the Chi-square values originated from different degrees of freedom, the Chi-square values need to be normalized first (Equation 53; Ooijen personal communication). When the jump test is larger than 3, the result is significant and the new marker is rejected (Van Ooijen, 2006). When the test is not significant, the new marker fits well and the search continues for a next marker and the procedure is repeated until all markers are considered. The idea behind this is that a poor marker will cause conflicts in the newly estimated order and thus cause a poorer fit (Van Ooijen \& Jansen, 2013d)

Equation 53 Jump $=\left(\chi_{\text {after }}^{2}-\chi_{\text {before }}^{2}\right) /\left(2 *\left(d f_{\text {after }}-d f_{\text {before }}\right)^{2}\right)^{>3}$

* $\chi^{2}$ is the Chi-Square value, df is the degrees of freedom,

The markers that are removed from the ordering, either by negative distances, significant Chi-square values or significant jump-tests, are considered again in a so-called second round (Van Ooijen, 2006). This may prove to be useful, since there are now more markers in the model and therefore it is still possible that a marker can be placed.

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## Time-efficiency and co-segregating markers

As mentioned above, the rippling function is a time-consuming process. A way to reduce the amount of time spend by rippling is to reduce the amount of markers to be mapped. This might sound conflicting since the goal is a marker dense map. However, there are many markers that can be mapped without actually using them in the mapping procedure. Those markers are co-segregating markers. For every marker pair with zero recombination, one of the two markers is taken out before the ordering and put back at end of the ordering procedure. For example, when the ordering time of SxN markers only, without taking out co-segregating markers is considered, the time it takes to order markers appears to be exponential (Figure 11). When cosegregating markers are taken out, the time-increase is tremendous. This proves that it is time can be gain by taking out co-segregating markers. It should be mentioned that the markers used in the actual ordering still follow an exponential function.

When different marker types are considered, it is wise to keep the marker types with the highest information content in the ordering procedure. Therefore the marker type is considered when taking out one of the two co-segregating markers in a pair. Whenever a SxN marker with any other marker type has a recombination frequency of 0 , the $\operatorname{SxN}$ marker is kept in. When a $S x N$ marker is co-segregating with another SxN marker, the marker with the smallest number of missing values is kept. When a SxS marker is cosegregating with DxN marker, the SxS marker is kept. When a SxS marker is co-segregating with SxT marker, both markers are kept since the co-segregation condition ( $\mathrm{r}=0$ ) might be caused by some situation in which the phase is highly uninformative. When a SxS marker is co-segregating with another SxS marker, which maker to be taken out is based on the number of missing values. Whenever a DxN marker is co-segregating with a SxT marker, the DxN marker is taken out. When a DxN marker is co-segregating with a marker of the same type, again the number of missing values is taken as a criterion to take the marker out. When a SxT marker is cosegregating with another SxT marker, the marker to be taken out is also determined by the amount of missing values. In this way, the most informative markers are used in the mapping procedure.


Figure 11. Time for ordering SxN markers with and without taking out co-segregating markers. The plot on the left shows the time in minutes the linear regression takes to calculate SxN homolog maps with cosegregating markers included. The plot on the right show the time in minutes linear regression takes to calculate SxN homolog maps when co-segregating markers are taken out based on missing values.

## Conclusion Chapter 5:

The linear regression approach is a straightforward and deterministic method of linkage mapping. By converting the recombination frequencies into distances, practically any marker type can be ordered. However, the time to order markers is exponential with the number of markers. Therefore, co-segregating markers are taken out of the mapping procedure.

## Chapter 6: Homolog maps

## Summary Chapter 6:

In the previous chapter, ordering markers by means of the linear regression method is explained. In this chapter, homolog maps, based on SxN markers only, are compared with maps estimated by JoinMap's maximum likelihood method. Both methods were very comparable. Furthermore, the SxN maps, as well as DxN maps (based on SxN and DxN markers), SxS maps (based on SxN, DxN and SxS markers) and SxT maps (based on SxN, DxN, SxS and SxT markers), were compared with the physical positions. The physical positions and the map positions were comparable and the maps clearly showed the centromere and chromosome arms. In addition, two methods of map evaluation are provided, namely a heatmap-method based on the recombination frequencies and the LOD-scores, and a method of evaluating the observed versus the expected distances.

## Types of maps

In the previous chapter, the theory behind ordering markers by means of linear regression was explained. In accordance with that procedure, the SNP markers were ordered for each homolog. First only SxN markers were ordered in a map (called the SxN map), next SxN and DxN markers (called the DxN map), followed by SxN, DxN and SxS markers (called the SxS map) and finally maps were created with these three marker types and SxT markers (called the SxT map). This was done to study the effect of the different marker types on the ordering. However, in practice, one would like to map all marker types in one go. In total 95 SxN maps were created (homolog 3 of chromosome 10 of P2 had 3 or less unique markers). 96 DxN maps and 96 SxS maps were created. 88 SxT maps were completed (because there was an unknown error in the ordering procedure of homolog 2 of chromosome 2 of P 2 , homolog 3 of chromosome 3 of P 1 , homolog 2 of chromosome 3 of P2, homolog 1 of chromosome 6 of P1, homolog 2 of chromosome 10 of P1, homolog 2 and 3 of chromosome 10 of P 2 and homolog 2 of chromosome 11 of P 2 ). Due to these errors, 14 SxT markers assigned to homologs were never considered in the ordering procedure.

## SxN maps

Since the SxN markers can also be ordered by software that is developed for diploid organisms, it is wise to compare the linear regression method (described in Chapter 5) with methods developed for diploids. When homolog 1 of chromosome 11 of P 2 is ordered with the linear regression method of this thesis and with the maximum likelihood and linear regression method (Round 2) of JoinMap, the ordering is similar (Figure 12). There are no internal map inversions. The distances are not equal, but distances of the linear regression method of this thesis are very similar to the maximum likelihood approach of JoinMap.

Another way of looking at the similarity between two mapping approach is by plotting the map positions of common markers against each other as was proposed to compare map positions of different maps of tomato (Sim et al., 2012). If both mapping methods are similar, the map positions of both maps should follow a straight line when plotted against each other. Therefore, the SxN map of homolog 1 of chromosome 11 of P2 by the linear regression method is compared with SxN maps from Bourke et al. (2015) by the maximum likelihood approach of JoinMap. Indeed we see a very straight line with a Pearson correlation of 0.9995 (Figure 13). Of course, such quantification is easy to generate for all the 95 SxN maps.

As can be seen from Figure 14, the vast majority of the SxN maps generated by the linear regression approach in this thesis (except 1 map) are significantly correlated with the maximum likelihood approach of JoinMap. This gives confidence that ordering with the linear regression approach described in this thesis works for SxN markers.

Comparing the results of linear regression in this thesis with other mapping methods is only part of the story, since there is another comparison to be made, namely with the physical position. When the physical positions are compared with order of $S x N$ markers estimated by the linear regression method, there is a strong Spearman correlation (Figure 15). The reason why a Spearman correlation is used instead of a Pearson correlation, is because there is no linear relationship between the physical positions and map positions and therefore a Pearson correlation, based on ranks, is more suitable. Also this is good evidence that the linear regression works in the mapping of SxN markers.


Figure 12. Comparison of three mapping methods on homolog 1 of chromosome 11 of $\mathbf{P} 2$ with only SxN markers. Linear regression (Round 2) of JoinMap (left), linear regression method in this thesis (middle) and maximum likelihood of JoinMap (right) are shown. The map positions of the markers are given in cM. Between the same marker on different maps, lines are drawn.

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Figure 13. Map positions of common markers from the maximum likelihood map of JoinMap and the linear regression map for homolog 1 for chromosome 11 of P2. The markers map at almost the same positions in both ordering methods as can be seen from the straight line. Both maps are in the reverse orientation when compared to Figure 12. The maximum likelihood maps of JoinMap were considered from the work of Bourke et al., (2015).


Figure 14. Pearson correlations between map positions of the maximum likelihood method and the linear regression approach of SxN maps. The left plot shows the p-value of the Pearson correlation, which is significant in all cases except one. The right plot shows the Pearson correlations of the maps. Many maps appear to be oriented in the inverse direction, but since the assignment of the starting position $(0 \mathrm{cM})$ is arbitrary, this does not matter.


Figure 15. Spearman correlations between maps positions the linear regression approach and physical positions of SxN markers. The left plot shows the p-value of the Spearman correlation. The right plot shows the Spearman correlation of map order with the physical positions.

## Maps including other marker types

So far, only SxN markers are considered, but there are more marker types. Therefore the physical position is compared with the ordering of multiple marker types. When the example of homolog 1 of chromosome 11 of P2 is considered again, it can be noted that there is already a decent coverage of the physical chromosome by the SxN markers on the SxN map (Figure 16). The centromere is visible as a region where hardly any recombination happens and the chromosome arms are present as the regions where recombination occurs often. When the DxN maps are calculated, the coverage is already higher and the length of the map is not increased so much. Thereafter, the SxS maps can be calculated. Here there is an increase in map length. It should also be noted that the total map is now inverted, but since the orientation of the maps can be switched, this does not matter. Furthermore, due to the extra information provided by the SxS markers, more DxN markers are now present in the map when compared to the DxN map itself (Table 9). After this, the SxT map was calculated. Again there is a slight increase in map length. Still the relationship between map distances and physical distances is present and clear.


Figure 16. The different map orders are compared with the physical positions of the marker. The top left plot compares the ordering of the SxN map with the new physical positions, which has some small and some large changes when compared to the old physical data (Data; Appendix 10). The top right plot compares the ordering of the DxN map with the new physical positions. The bottom left plot compares the ordering of the SxSmap with the new physical positions. The bottom right plot compares the ordering of the SxT map with the new physical positions. The grey sigmoid line represents a correlation, based on visual inspection (and thus bears no statistical significance), between the physical positions and the map positions. The other homologs of this chromosome and other chromosomes can be found in Appendix 6.

Table 9. Different marker numbers of the four maps of homolog 1 of chromosome $\mathbf{1 1} \mathbf{~ o f ~ P 2 . ~ T h e ~ n u m b e r ~ o f ~}$ markers per marker type appears to be more or less stable in the different marker type maps.

| Map | Markers |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
|  | $S x N$ | $D x N$ | $S x S$ | SxT |
|  | 34 |  |  |  |
| $D x N$ | 34 | 14 |  |  |
| $S x S$ | 34 | 16 | 11 |  |
| SxT | 34 | 16 | 10 | 3 |

## New map evaluation methods

Apart from looking at the physical positions for map evaluation, some other methods for map evaluation are used as well. The first method is map evaluation by the use of a heatmap (Van Ooijen, personal communication). In the heatmap (Figure 17), the recombination frequencies and LOD-scores are plotted against the order of the markers. In such a plot, every square represents a recombination frequency or LOD-score of a marker with another marker. The diagonal means nothing, since these are LOD-scores or recombination frequencies from a marker with itself. The low recombination frequencies are correlated with the marker order, since a green patch (low recombination frequencies) follows the diagonal. There is a similar pattern with the LOD-scores, although the pattern is less clear. Furthermore some markers have in general lower LOD-scores than others, which can be due to the marker type. Another thing that can be seen from Figure 17 is that taking markers out on basis on the criterion of having a zero recombination event between two markers is a good criterion. This can be seen by big squares of both recombination frequencies and LOD-scores in Figure 17 below.

Furthermore, the heatmap evaluation can also be used to spot ordering errors. In Figure 18, the heatmap of the recombination frequency, used in mapping of homolog 2 of chromosome 2 of parent 2 , is shown. The plot on the left shows the correct order, while the plot on the right contains an artificial wrong marker (Potvar0089282). This incorrect marker was introduced by preventing the removal of markers that failed the Chi-square or jump test in the ordering step (Chapter 5). This heatmap shows that this marker does not fit well in the ordering as can be seen from the high recombination frequency (red line) in an area were all the other markers have a low recombination frequency (green square).

Another method of evaluation is plotting the observed versus the expected distances. In Figure 19, the expected adjacent distances (from the ordering model) are plotted against the observed distances (based on the calculated recombination frequencies) and a straight line can be seen. This is a good indication that the linear model worked. Furthermore, all the expected and observed distances are plotted as well. Here also a straight line can be observed, however, the larger the distance the more it deviates from the line. This is in line with the fact that larger distances have a large error (Hans Jansen, personal communication).

All the maps can be and are evaluated by the three methods proposed here: plotting the map distances against the physical positions (Appendix 5), plotting heatmaps of recombination frequencies and LOD-scores and plotting the observed versus the expected distances (results not shown).


Figure 17. Heatmap of LOD scores and recombination frequencies of all marker pairs of homolog $\mathbf{1}$ of chromosome 11 of P2. The markers used in the ordering are shown in the two plots above, while all the markers are shown in the plot below.


Figure 18. Heatmap of the recombination frequencies used in the ordering of homolog $\mathbf{2}$ of chromosome 2 of P2. The plot on the right is the correct order, while the plot on the left contains one artificial incorrect marker (Potvar0089282), introduced by not allowing for marker removal during the ordering of markers. From the heatmap it can clearly be seen that this marker is incorrectly mapped.


Figure 19. Plot of observed versus the expected distances of homolog $\mathbf{1}$ of chromosome $\mathbf{1 1}$ of $\mathbf{P 2}$. The plot on the left presents the adjacent distances only, while the plot on the right presents distances of all marker pairs on the homolog.

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## Conclusion Chapter 6:

The SxN maps, estimated by the linear regression method described in this thesis, were compared with the maximum likelihood method of JoinMap. Both methods gave comparable results. In addition, the physical positions were also comparable with the map order. Combining these two finding with the new map evaluation tools, leads to the conclusion that the linear regression method used here is capable of mapping different marker types.

## Chapter 7: Integration

## Summary Chapter 7:

The homolog maps, estimated in the previous chapter, are integrated in this chapter. LPmerge is used for the integrated of the homolog maps. LPmerge uses a graph-theory approach to integrate and solve conflicting orders. This is in contrast to JoinMap, which uses a statistical pooled approach. The timing difference between the two methods is tremendous. The integrated chromosomes maps of LPmerge gave good correlation with the underlying homolog maps and the physical positions. The integrated maps covered in total 1406.13 cM for 12 chromosomes and contained 5165 markers.

## Programmes to integrate maps

In the previous chapter, the maps of the homologs are calculated. For effective QTL-analysis, an integrated map of those homologs is desired. There are several programmes that can integrate maps of different populations into one consensus map. In this chapter, the homologs are thus treated as if they came from different populations.

Currently, different approaches have been developed to make a consensus map based on maps of different populations. The first approach is to visually align the maps by hand (Yap et al., 2003). Of course this proves to be very unpractical for large datasets. Luckily, the other approaches are automated.

The second approach relies on the recombination frequencies and LOD-scores and is thus directly based on the genotypes and this is called a statistical pooled approach (Jackson et al., 2005). JoinMap uses this approach. In JoinMap all the pairwise recombination frequencies are used to create an integrated map with the linear regression approach (Van Ooijen, 2006). This also requires the repulsion estimates for markers on different homologs. As was already mentioned in Chapter 1, some recombination frequencies for repulsion can be negative, which are then set to zero. Doing so is a loss of information and might shorten the integrated map (Hackett et al., 1998). Furthermore, the approach by JoinMap proves to be time-consuming with a large number of markers, for example JoinMap took 3 months of calculations for the construction of a consensus map of 1800 markers (Wu et al., 2008). Even due to the drawback of timing, JoinMap is used for the integration of linkage maps of certain species, for example pineapple (de Sousa et al., 2013). Another programme, MetaQTL, which also uses the weighted regression approach, was used for the construction of an integrated map of potato (Danan et al., 2011).

Another approach to integrate maps is to use the maps themselves, rather than the underlying recombination frequencies and LOD scores. This approach is used by MergeMap (Yap et al., 2003) and uses graph-theory and regards the maps as a directed graph.

In graph-theory, the markers are represented as nodes and the distances as edges. In the approach proposed by Yap et al., (2003), the individual linkage maps are scanned for bridge-markers. In case of a tetraploid, the bridge markers are the DxN markers (bridge for homologs) and SxT and SxS markers (both a bridge for parents).

Thereafter, the bridge markers are used as anchors and merged. Once the maps are merged based on bridge-markers, the software looks for inconsistencies and presents them as cycles (non-linear paths) in the graph. The software presents the integrated maps as a graph which connects the well-ordered (or merged) markers with lines and the inconsistencies as cycles. The reason that the software presents it in such a way instead of a single linkage map is that presenting the consensus map as a single linkage map may hide inconsistencies with the underlying homolog maps (Yap et al., 2003). Although such a graph-map is useful to spot inconsistencies easily, it is not very useful for QTL-analysis since it does not present a single integrated linkage map. Thus it is useful to solve the inconsistencies of the integrated graph by linearization or simplification to a linear graph (Endelman, 2011). However, by doing so, it might create an order in the consensus map that is not present in any of the individual linkage maps.

Therefore, new software, such as DAGGER (Endelman et al., 2014), has been developed to cope with this problem. DAGGER finds the best consensus map by minimizing the residual mean sum error (RMSE) between the individual linkage maps and the consensus map. However, one practical disadvantage of DAGGER is that it shrinks the consensus maps considerably and another disadvantage of DAGGER is that it cannot handle ordering conflicts.

Its successor, LPmerge, solved these problems (Endelman \& Plomion, 2014). One advantage of LPmerge in comparison to other merging programmes is that is removes constrains rather than markers when there are inconsistencies between the underlying linkage maps. By using LPmerge and MergeMap to integrate different maps of maritime pine it was found out that MergeMap gave longer consensus maps than LPmerge, while the ordering was similar (Plomion et al., 2014). Furthermore, LPmerge has been used in other species, such as cassava (International Cassava Genetic Map Consortium, 2014). Although LPmerge has been used to integrate populations of tetraploid wheat (Yu et al., 2014), it has not been used yet for the integration of homologs. Here LPmerge was used for the development of an integrated map of the 8 homolog maps per chromosome.

LPmerge minimises the RMSE, residual mean square error, by means of linear programming between the individual homolog maps and the integrated map to find the best order of markers for the integrated map (Endelman \& Plomion, 2014). It is advised to select the consensus map with the lowest RMSE. The error terms of the consensus map are based on the interval size. The interval ranges from 1 to the maximum interval size and LPmerge allows the user to change the maximum interval size (with a default value of 1 to 3 ). An interval size of 1 means that only adjacent pairs on the original maps are considered for the error estimation while higher interval sizes mean that also markers further away are considered.

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## Integration of homolog maps

For chromosome 1 the SxS map of homolog 1 of P1 was used since the SxT map showed an increase of 50 cM when compared to the SxS map, furthermore, for homolog 4 of P 2 the SxS map was used since there was an error during the ordering of the SxT map, for the other homologs the SxT map was used. For chromosome 2, the SxS map of homolog 1 of P2 was used since there was an error during the ordering of the SxT map, for the other homologs the SxT map was used. For chromosome 3, the SxS map of homolog 3 of P1 and homolog 1 of P2 were used since there was an error during the ordering of the SxT map, also for homolog 4 of P1 the SxS map was used since the SxT map was not consistent with the SxS map, for the other homologs the SxT map was used. For chromosome 4 the SxT maps were used for all homologs. For chromosome 5, the SxS map of homolog 2 of P2 was used since there the SxT map lost an entire chromosome arm when compared to the SxT map, for the other homologs the SxT map was used. For chromosome 6, the SxS map of homolog 1 of P1 was used since there was an error during the ordering of the SxT map, for the other homologs the SxT map was used. For chromosome 7 the SxS map of homolog 4 of P1 was used since the SxT map showed an increase of 40 cM when compared to the SxS map, for the other homologs the SxT map was used. For chromosome 8 the SxT maps were used for all homologs. For chromosome 9 the SxT maps were used for all homologs. For chromosome 10, the SxS map of homolog 2 of P1 and homolog 2 and 3 of P2 were used since there was an error during the ordering of the SxT map, for the other homologs the SxT map was used. For chromosome 11, the SxS map of homolog 2 of P2 was used since there was an error during the ordering of the SxT map, for the other homologs the SxT map was used. For chromosome 12 the SxT maps were used for all homologs.

The individual homolog maps were put in the correct orientation with respect to each other, since LPmerge is orientation-dependent (personal observation; results not shown). This is done based on the (Spearman) correlation of the order of the homolog map with the physical position. When a correlation larger than 0 is found, the map is already in the good orientation, but when a correlation lower than 0 is found, the map should be reversed. It should be noted that the Pearson correlation between maps themselves could also be used to put the maps into the right orientation. During integration the maximum interval size was varied from 1 to 4 and the best consensus map was selected based on the lowest RMSE and the smallest consensus map length (Endelman, 2011). In practice, a maximum interval size of 1 was selected for all chromosomes.

## Evaluation of the integration process

A way to visualize the quality of the integrated map is to plot the underlying homolog maps against the integrated map, which gave a good correlation between the maps, for the example of chromosome 11 (Figure 20). This means that the order between the markers on the homologs is maintained on the integrated map. More importantly than a general correlation are potential switches between the positions of markers. No large rearrangements of marker order are found (Figure 20). This means that the constraints that were removed by LPmerge to make the consensus map are in correspondence with the underlying homolog maps. The Pearson correlation can be calculated for all the homolog maps against the integrated maps. For all the chromosomes there is a good correlation between the homolog maps and the integrated map (Figure 21; Appendix 16).


Figure 20. The map positions of the markers on the homolog maps are plotted against the map positions in the integrated map of chromosome 11. The homolog maps have a good correlation with the integrated map. The plots of the individual homolog maps against the integrated maps of other chromosomes can be found in Appendix 16.


Figure 21. The Pearson correlations between map positions of the underlying homolog maps and the integrated map. The left plot shows the p-value of the Pearson correlation, which is significant in all cases. The right plot shows the Pearson correlation of the maps.

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When the integrated map of homolog 11 is plotted against the physical positions together with the homolog maps (Figure 22), a number of things can be noted. The first thing that comes to mind is the coverage of the markers in the plot. All the regions (centromere and the arms) are covered well by markers. The second thing that can be noted is the relative smoothness of the curve, when considering that 8 homolog maps were integrated. Another thing that can be noticed is that the physical position of one marker, from homolog 2 of P2, around 70 cM on the integrated map is out of range of all the other markers. This can indicate that the physical position of this marker is not good (and probably unrealistic) and needs to be revised. In addition, markers that did not have any physical information were treated as if they had a physical position of 0 bp . By plotting those markers, there relative physical position can be figured out based on the integrated map. Such an example can be found around 100 cM , meaning that the relative position of this marker should be at about $4 * 10^{7} \mathrm{bp}$.

Figure 22 is only one example, but the other integrated chromosomes can be evaluated in a similar fashion (Table 10; Figure 23). The first thing that comes to mind when looking at all the integrated chromosomes is that some integrated maps appear to have two centromeres. This can pinpoint to conflicting homolog maps or a lack of bridge markers in the centromere.

Furthermore, literature on previous linkage maps can be compared with the integrated chromosome maps. Chromosome 6 is known for its short arm (Van Os et al., 2006), which can be seen from Figure 23. Chromosome 5 is metacentric (Van Os et al., 2006), which means that both arms are equally long. Chromosome 2 is telocentric (Park et al., 2007), which is indicated with a centromere in the telomere and thus one long arm. Chromosome 12 is also telocentric according to Park et al., (2007), but cytogenetic studies suggest that this is not the case (Gavrilenko, 2007), which is in correspondence with the integrated map.

Another way of looking at the quality of the integrated map, is by looking at the markers that are actually loci of the same gene. The 6 loci of D_locus_(DFR) are all located on chromosome 2 at 80.43 cM , the two R2 loci are both located on chromosome 4 around 30 cM , the 6 solcap_TUBER markers are all located on chromosome 10 around 56 cM and the three Plocus_F35H are all located on chromosome 11 at 102.37 cM (Appendix 9). The fact that all the loci of different genes are mapped together on the integrated map indicates that the mapping of the homolog maps in combination with integration performed well.

Based on the Pearson correlation between the homolog maps and the integrated map, the comparison between the integrated map with the physical information, the comparison with literature, and mapped loci of the same genes, it can be concluded that the integrated maps are of good quality. The integrated maps covered in total 1406.13 cM for 12 chromosomes and contained 5165 markers (Table 10; Figure 23). The majority of the markers were SxN markers and the other marker types were used as bridge markers. The coverage ( N markers / map length in cM ) was on average 3.71. This is a major increase in marker coverage when considering the previous integrated map (Hackett et al., 2013), which had a coverage of only 1.22 (Appendix 13).

## Chromosome 11



Figure 22. Map positions of the integrated map and homolog maps against the physical positions of chromosome 11. The map positions of the integrated map are plotted against the physical positions. The original map positions of markers on the individual homolog maps are plotted against the physical positions as well.

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Table 10. Overview of integrated chromosomes. This table shows the Residual Mean Square Error (RMSE) and standard deviation (sd) from the integration of 8 homologs into an integrated map per chromosome by LPmerge. The number of markers and total map length are shown together with the size of gaps. The coverage of markers per map distance and base pairs is shown as well. The physical position of the markers come from the sequence information (Vos et al., 2014;The Potato Genome Sequencing Consortium, 2011). The Spearman correlation between the physical positions and the integrated map positions is shown as well. The number of markers per integrated chromosome per marker segregation type is presented in this table.

| Chromosome | Mean RMSE | sd | Markers | Map length in $\mathbf{c M}$ | $\begin{gathered} \hline \text { Gaps > } \\ 10 \mathrm{cM} \end{gathered}$ | $\begin{array}{r} \hline \text { Gaps> } \\ \mathbf{1 c M} \end{array}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 20.44 | 10.58 | 624 | 141.7 |  | 44 |  |
| 2 | 24.89 | 15.04 | 544 | 118.9 | 1 | 30 |  |
| 3 | 16.71 | 8.33 | 459 | 125.57 |  | 38 |  |
| 4 | 23.88 | 15.78 | 478 | 151.26 |  | 42 |  |
| 5 | 14.9 | 10.06 | 545 | 101.75 |  | 29 |  |
| 6 | 18.99 | 9.91 | 352 | 121.2 |  | 33 |  |
| 7 | 8.24 | 4.39 | 447 | 94.78 |  | 22 |  |
| 8 | 11.08 | 8.33 | 450 | 102.85 |  | 27 |  |
| 9 | 16.2 | 10.35 | 369 | 119.06 |  | 39 |  |
| 10 | 15.38 | 4.24 | 213 | 109.83 | 1 | 33 |  |
| 11 | 20.11 | 11.27 | 396 | 136.1 |  | 39 |  |
| 12 | 13.91 | 11.95 | 288 | 83.13 |  | 30 |  |
| Total (sum or average) | 17.0608333 | 10.01917 | 5165 | 1406.13 | 2 | 406 |  |
| Chromosome | Coverage N/cM | Coverage <br> N/MB | Spearmancorrelation | p-value | SxN | DxN | SxS |
| 1 | 4.40366973 | 9.984 | 0.981313 | 0 | 338 | 95 | 129 |
| 2 | 4.57527334 | 12.65116 | 0.981313 | $6.83 \mathrm{e}-259$ | 359 | 46 | 118 |
| 3 | 3.65533169 | 18 | 0.975320 | $6.092 \mathrm{e}-302$ | 262 | 95 | 65 |
| 4 | 3.16012165 | 9.192308 | 0.977070 | $6.32 \mathrm{e}-322$ | 267 | 74 | 103 |
| 5 | 5.35626536 | 15.13889 | 0.935467 | $1.90 \mathrm{e}-247$ | 353 | 93 | 55 |
| 6 | 2.90429043 | 8.8 | 0.979327 | $5.28 \mathrm{e}-245$ | 219 | 45 | 78 |
| 7 | 4.71618485 | 14.19048 | 0.968993 | $2.55 \mathrm{e}-272$ | 227 | 93 | 91 |
| 8 | 4.37530384 | 16.36364 | 0.960020 | $7.44 \mathrm{e}-250$ | 228 | 46 | 78 |
| 9 | 3.09927768 | 12.09836 | 0.955169 | $4.31 \mathrm{e}-196$ | 197 | 72 | 72 |
| 10 | 1.93936083 | 5.195122 | 0.902943 | $2.47 \mathrm{e}-79$ | 110 | 48 | 38 |
| 11 | 2.90962528 | 12.375 | 0.947498 | $3.37 \mathrm{e}-197$ | 229 | 57 | 66 |
| 12 | 3.46445327 | 7.384615 | 0.975454 | $5.38 \mathrm{e}-190$ | 165 | 64 | 39 |
| Total (sum or average) | 3.71326316 | 11.78113 | 0.96165725 | $2.24 \mathrm{e}-80$ | 2954 | 828 | 932 |



Figure 23. Integrated map positions per chromosome plotted against the physical positions. The marker segregation types are shown with their corresponding map positions and physical positions. Physical positions with missing values were set at 0 bp to allow those markers to be plotted. In this way one could estimate very roughly the physical position based on the genetic position on the integrated map.


Figure 23. Continued

Chromosome 9


Physical position in bp

Chromosome 11


Physical position in bp

Chromosome 10


Physical position in bp

Chromosome 12


Physical position in bp

Figure 23. Continued

## Conclusion Chapter 7:

LPmerge was used to integrate the homolog maps. Integration of homolog maps with LPmerge was extremely fast in terms of computational time. The integrated map covered in total 1406.13 cM for 12 chromosomes and contained 5165 markers. The integrated map showed good correlation with the individual homolog maps. Furthermore, it showed a good correlation with the physical positions. In addition, it can allow for a rough estimation of the physical position for markers with no assigned physical position.

## Discussion and future prospects

## Linkage mapping pipeline in $R$

Currently genetic and statistical tools to analyze polyploids species are either lacking, very basic (Dufresne et al., 2014) or cannot handle large number of markers (Hackett \& Luo, 2003). However, it is important that genetic analysis on polyploidy organisms can be performed, since many crop species, such as potato, are polyploids. Therefore there is a desire to make a pipeline that covers all the steps from marker development to QTLs in polyploids. In this thesis, a mapping pipeline in R was built from dosage scored marker data to an integrated map for tetraploid potato. The strategy to build the integrated map involved several steps, starting from the calculation of the recombination frequencies between SxN markers and ending in integrating homolog maps. In the Discussion and Future Prospects, all the steps of the mapping pipeline are discussed with relation to the performance, literature or other programmes, and speculation with regards to errors and violation of the assumptions. Finally, the significance of the thesis overall is explained with regards to future developments in tetraploids.

## Mode of inheritance

In Chapter 1, the recombination frequencies and LOD-scores between SxN markers were calculated. Many SxN markers were evaluated with respect towards the mode of inheritance. Based on the repulsion recombination frequency estimates, it could be concluded that potato is an autopolyploid, as indicated by Bradshaw (1994) and no preferential pairing occurs (Assumption 7). Although, other methods for testing the mode of inheritance could be used (Vukosavljev et al., 2014), this method worked well for potato.

The method presented here can be applied to other tetraploid species as well and was used for Alstroemeria. The preliminary results of Alstroemeria indicated that a certain degree of preferential pairing is present (Appendix 15). Other lines of evidence, such as the inheritance of DxS markers, indicate that indeed preferential pairing occurs (Shahin, personal communication), however, on which chromosome(s) and to what degree preferential pairing occurs is not known yet.

Since the recombination frequencies between SxN markers are needed for most software, the method to investigate the mode of inheritance via SxN markers is a desirable method. Another way of investigating the mode of inheritance within this pipeline would be to check the ratio between coupling and repulsion linkages, which might provide a crude estimate for the amount of preferential pairing (Wu et al., 1992).

The mode of inheritance was investigated based on repulsion recombination frequency estimates. Under the tetrasomic model, as used for autotetraploid species, the repulsion estimate of the recombination frequency can be negative. In some cases the recombination frequency of both repulsion and coupling phase were out of the 0 to 0.5 range for recombination frequency estimates. It is common practice to estimate the phase as repulsion between the two SxN markers and set the recombination frequency at 0 (Hackett et al., 1998), which is essentially a loss of information. Wu et al., (1992) indicated that negative recombination frequency estimates might indicate a violation of the assumed number of homologs. Another possible explanation for the phenomena of negative recombination frequency estimates could be the huge standard error that repulsion linkages have regardless of the population size (Hackett et al., 1998).

A way of illustrating the low information content of repulsion linkages, due to large standard errors, is that the repulsion recombination frequencies have a much lower LOD-score when compared to coupling linkages. Combining the large standard error with a low LOD-score, it can therefore be concluded that it is not wise to use these estimates in the map integration process, which does happen in the statistical pooled approach of JoinMap for example. In this thesis, the repulsion estimates are not used in the map construction and integration (see below).

## Clustering SxN markers into linkage groups

In Chapter 2, the LOD-score of linkage was used to cluster the $\operatorname{SxN}$ markers into linkage groups. The algorithm described by Van Ooijen \& Jansen (2013a) was used in this thesis as well as by JoinMap. Both programmes gave identical results, although in JoinMap the LOD of independence was used instead the LOD of linkage. Whether the algorithm will cluster the markers in the same way when other linkage thresholds, such as the test of linkage of Mather (described in Chapter 1) or the $\mathrm{G}^{2}$-test of JoinMap, are used, is currently unknown.

When the same method was applied to Alstroemeria, the SxN markers did not cluster until SxN markers with more than $10 \%$ missing values were excluded from the data. This indicates that this method used here is vulnerable to single (or multiple) unreliable markers. Ronin et al., (2010) recognize this problem as pseudolinkage, which means that two markers of different linkage groups have lower recombination frequencies (or higher LOD-scores) than markers on the same linkage group. In the approach of Ronin et al., (2010) markers are clustered in linkage groups for different LOD-score thresholds and at the same time ordered. Jansen (personal communication) suggested to use another method of clustering SxN markers into linkage groups, namely based on the recombination frequency. In this approach, markers with a low recombination frequency are grouped together while markers with a high recombination frequency are excluded. Whether clustering markers based on the recombination frequency is less vulnerable to single marker deviations is currently not known. For the clustering of markers into linkage groups only SxN markers were used. However, whether it is possible to use the same approach for all the marker types at once is currently not known.

In addition to comparing the clustering method of this thesis with the clustering method of JoinMap, the clustering method was also compared with the information of the physical chromosomes. The physical chromosomes and the clustering method were not identical. This could indicate that some markers are wrongfully assigned to chromosomes. Another explanation is that markers are duplicated in the genome and thus are located on two chromosomes (a violation of assumption 6). If indeed markers are located on two chromosomes, the calculation of the recombination frequencies and LOD-scores will be wrong for those markers, since the dosage scores are actually a mixture of two markers. It is therefore likely that in those situations the markers will not map well. Although it was not investigated if such markers are present on the current SNP array, it is very unlikely that the violation of this assumption will have an effect on the integrated map, since there are only a few markers that are wrongfully assigned to linkage groups based on the physical chromosomes (and only a fraction of those are likely to be a duplicated marker).

## Clustering SxN markers into homologs

In Chapter 3, the SxN markers were assigned to homologs. Currently, software to assign SxN markers to homologs is not available. Previously, homolog assignment of $\operatorname{SxN}$ markers was based on the ordering of SxN markers of a linkage map with JoinMap (or other diploid mapping programmes) and identifying the correct phase from the order (Maliepaard, personal communication; Hackett et al., 2013). In this thesis a method to assign SxN markers to homologs was developed and this method uses the phase information (coupling or repulsion) of SxN markers. This method produces a phase-tree which a user can cut into four or more homologs (or sub clusters). For most chromosomes this led to four distinctive homologs. However, for some homologs the distinction was not clear and therefore the phase-tree was cut in five sub clusters (or artificial homologs). To put two sub clusters together into one biologically meaningful homolog, another source of information was used, namely the linkage between SxN and DxN markers. The SxN with DxN linkages contained enough information to put two sub clusters together into one real homolog for most chromosomes except two. For these two chromosomes, other sources of information were used, such as the physical positions of the SxN markers. The phase-tree and SxN with DxN linkage proved to be useful methods to separate the homologs from each other. Although this methodology is not perfect yet, it is a step in the good direction, especially when considering previous methods to separate the homologs did not exist before.

Currently, it has not yet been investigated how the phase-tree approach will work under different degrees of preferential pairing. In species with a degree of preferential pairing, the homologs are not as distinctive as in autotetraploid potato. This might prove to be a problem in terms of the formation of sub clusters in the phase-tree. However, a true allotetraploid (complete preferential pairing) species, such as wheat, could be handled as a diploid and therefore this problem will only exist from species with a degree of preferential pairing.

## Other marker types

In Chapter 4, the recombination frequencies, LOD-scores and the phase was estimated for all marker segregation types (SxN, DxN, SxS, SxT) combinations. The SxT markers were assigned to chromosomes and homologs in this chapter, while $S x S$ and DxN markers were already assigned to chromosomes and homologs in the previous chapter. Hackett et al., (2013) simulated the recombination frequencies of the different marker combinations. In this study the simulated recombination frequency of a SxS marker with a SxT marker differed greatly from the actual recombination frequency and had the lowest LOD-score. This corresponds with the fact that the LOD-scores of SxS with Sxt markers were very low in some phases (Appendix 7). In addition to the low LOD-scores, Meyer et al., (1998) found that SxS markers in mixed phase with each other had a high standard error, but on the other hand SxS markers or SxT markers in coupling phase show a high LOD-score (Hackett et al., 2013; Appendix 7). The same was found for SxS with SxN markers in repulsion (Meyer et al., 1998). Additionally, Hackett et al., (1998) found that also DxN with DxN markers in mixed and repulsion phase had a high standard error. This is another indication that the recombination frequency estimates of markers in mixed and repulsion phase may not be reliable, although in some cases the repulsion estimates might be useful (Mester et al., 2003b). A recommendation by Bourke (personal communication) was to set the LOD-score of uninformative phase situations at 0 . What the effect of setting the LOD-score at 0 in the mapping procedure will be when implemented has yet to be investigated.

The two marker types that are not considered in this thesis, DxS and DxD, need such an implementation since also here the LOD-scores are low (Hackett et al., 2013) and are not informative (Meyer et al., 1998). Although these marker types could be useful for map integration and provide extra coverage to interesting regions, such as QTL regions, with the current approach I would say that those marker types are too uninformative to be mapped well. Furthermore, it is doubtful if these marker types would be beneficial since the marker density of the integrated map is already high.

## Adjusting estimators of the recombination frequencies

When the recombination frequencies are calculated, it is good to keep possible violation of the assumptions and possible errors into account. For example, it is known that double reduction occurs in potato (Bourke et al., 2015; Haynes \& Douches, 1993), but one of the assumptions is that this not happen or does not influence the mapping of markers much (Assumption 8). What the effect is of the violation of such an assumption is currently not known and it would be interesting to see its effect in both simulation and real data studies. Preliminary results show that the formation of quadrivalents, leading to double reduction, does not influence the estimation of recombination frequency of SxN markers in coupling (Bourke, personal communication).

A way of accounting for errors is to adjust the recombination frequency estimators for the errors and violations of the assumptions. For example, Liu (1997b) developed a method to adjust the estimator of the recombination frequency for skewedness in a diploid F2 population by introducing two distortion parameters. Without doubt, a similar method can be applied to tetraploids as well. Currently, no software available can handle these kind of skewedness models, however it would be relatively straightforward to implement a similar model for tetraploids in the pipeline of linkage mapping described in this thesis

Apart from adjusting for skewed markers in the recombination frequency calculation, other deviations can be handled when the estimator of the recombination frequency is adjusted. For example, a model has been developed to account for degrees of preferential pairing and double reduction by introducing extra parameters into the recombination estimator (Wu et al., 2002b; Wu et al., 2004b). In this way, the pairwise recombination frequency for allotetraploids can be calculated. Such recombination frequency estimators could allow the linkage mapping pipeline, described in this thesis, to be expanded to allotetraploids as well. In addition, Rhemsmeier (2013) includes five parameters, including preferential pairing and multivalent formation, into the calculation of the recombination frequency. Göring \& Terwilliger (2000) developed estimators for the recombination frequencies in diploids that allow for the presence of genotyping errors (see below), which could potentially also be implemented in the recombination frequency estimators of tetraploids. Furthermore, there are several other deviations that could be implemented, such as unequal recombination rates in both parents (Assumption 11; Plomion \& O'Malley, 1996). However, so far, this is not done and this is a challenge for the future.

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## Ordering with linear regression, time-efficiency and co-segregating markers

In Chapter 5, the ordering of markers by the linear regression approach was explained. The linear regression uses the recombination frequencies between markers to estimate the map distances. The squared LOD-score functions as a weight in the linear regression. The time the linear regression method approach takes to map all the markers increases exponentially with the number of unique (not co-segregating) markers to be mapped. This can be problematic in the future, since there is a tendency to use more markers (see below) or in case of large populations (less co-segregating markers due to many recombination events). It is therefore needed to also implement other mapping algorithms within the same pipeline as presented here. Not only will this very likely speed up the process of mapping, but will allow the user to choose a method he or she desires.
Furthermore, another beneficial effect of having two (or more) mapping algorithms that can be selected within the same pipeline is that the orders estimated by different mapping algorithms can be compared for (in)consistencies.

In addition, efficient programming in R might speed up the computational process in R (Visser et al., 2015). The code written in R can be optimized by an experienced programmer and this is definitely a challenge for the future.

Another way of improving the speed of the linear regression method is by taking out co-segregating markers. In this thesis, a marker was considered co-segregating with another marker when the recombination frequency was zero. However, as was noted above, this might lead to false positives when there are marker type and phase combinations which are uninformative and thus another way of taking out co-segregating markers is desired. Another viewpoint on taking out co-segregating markers is that currently the number of markers is surpassing the mapping resolution (based on the population size as well as other parameters) and therefore only a few markers can be genuinely mapped (Ronin et al., 2010). According to the authors it is therefore necessary to bin markers. The question then becomes how to select the right markers for the estimation of a skeleton map. Wenzl et al., (2006) for example bin markers based on the so-called segregation signatures of markers, while Van Os et al., (2006) use a different but similar approach with a bin signature. A method for successfully binning marker has yet to be implemented in the R pipeline.

Furthermore, during the mapping procedure thresholds are considered, such as a value of 3 for the jump-test. What the effect of these thresholds is on the map order is currently not known and is worth investigating. A simulation study with a known marker order might reveal the sensitivity for the different threshold used in this thesis.

Although the points mentioned above, linear regression has the advantage that it only needs the distances, which are converted from recombination frequencies, and the LOD-scores. This indirectly means that the linear regression approach is not only suitable for tetraploids, but also for higher ploidy levels, as long as the recombination frequencies and LOD-scores are calculated. So far this has been done for hexaploid sweet potato (Kriegner et al., 2003) and octoploid sugarcane (Aitken et al., 2007) with JoinMap's regression approach for example. Similarly, mapping those species could easily be done with the linear regression method proposed here in R when the recombination frequencies between markers from higher polyploidy levels are calculated.

## Homolog maps and map evaluation

In Chapter 6, the marker types, SxN, DxN, SxS and SxT, were ordered and presented as homolog maps. One SxN map was compared with both ordering methods, linear regression and maximum likelihood, of JoinMap. The three ordering methods produced the same order although there were small differences in the map distances. The maximum likelihood method was the fastest of the three ordering methods considered in this example. The order of the regression method presented in this thesis was most similar with the order of the maximum likelihood method of JoinMap. When all the SxN homolog maps were compared with the order estimated by the maximum likelihood approach of JoinMap, it was found that both methods produced maps which are comparable in order and size. In addition, the physical positions were used as a verification of the map order.

Furthermore, the other marker segregation types were mapped. These maps were compared with the physical positions. The physical map positions and the linkage map positions were strongly correlated. This is an indication that the ordering by the linear regression method works for the other marker segregation types as well. One note should be made that the map length appears to increase, although not quantified, when more marker and marker types are added (see below). An explanation for this could be that markers in the mixed phase are not very informative as previously discussed, but are used in the ordering.

Apart from comparison with JoinMap and the physical positions, the homolog maps were also evaluated by two new methods. The first method is plotting the LOD-scores and recombination frequencies by means of a heatmap. The second method is plotting the observed distances, the transformed recombination frequencies, against the expected distances from the order. The observed and expected distances should roughly be equal. Both methods allow the user to visually check the ordering process.

## Integration of homolog maps with LPmerge

In Chapter 7, the homolog maps were integrated with the R-package LPmerge. LPmerge uses a graphtheory approach to integrate individual maps. The graph-theory approach is incredibly fast, especially when compared to JoinMap, where the integration takes a long time when the marker number is high (Wu et al., 2008). The integrated maps showed a high correlation when compared to the individual homolog maps. Furthermore, the physical positions showed a good correlation with the integrated map too.

The integrated map with a cumulative length of 1406.13 cM for 12 chromosomes and contained 5165 markers, and thus has a high coverage. Furthermore, it has very few gaps. According to Watanabe (1994) the ultimate goal of marker development is the saturation of the genome with a maximum gap size of 1 cM . Although, the integrated map has gaps larger than 1 cM and thus saturation is not final yet, it is getting close (Table 21; Appendix 17).

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## Comparison of the integrated map and maps found in literature

Isidore et al., (2003) estimated that the cumulative length of the potato genetic map should be between 600 cM and 1100 cM , while on the other hand Gebhart et al., (1991) estimated that the cumulative length should be between 1200 cM and 1300 cM . Still, the integrated map presented here with 1406 cM surpasses both estimates. To evaluate the integrated map length, the genetic map presented here is compared with genetic maps in the literature (Table 11). The first tetraploid map was estimated by Meyer et al., (1998) and covered 909 cM and 486 cM for the respective parents (which could indicate that the recombination frequencies in both parents are not equal; assumption 11). The most recent tetraploid map in the literature is the integrated map of Hackett et al., (2013). This map covers 1087 cM and misses some homologs. Prashaw et al., (2014) estimated the most recent diploid map, which covers only 753.9 cM , which is a decrease in map length when compared to previous diploid potato maps. Furthermore, recently a consensus map has been estimated based on different maps present in the literature and covers 1260 cM (Danan et al., 2012). What can be noted is that the length of all these maps differs. It can therefore be said that there is no fixed estimate for the total length of a genetic map of potato and that the quest for the true genetic map still continues. Still the map presented here is the longest potato map, but not in the Solanum genus, for which diploid tomato has the longest map (Table 11).

One of the reasons why the map presented here is the longest potato map, can be due to the fact that the population size is the largest. During simulation studies it is found that when the population size decreases, the cumulative map length also decreases (Hackett et al.,, 1998). In addition, the difference in the true position and the map position increases when the population size increases. The limited number of informative meiosis in a small population could cause errors (DeWan et al., 2002). This appears not to be the case in this particular population, since the mapping population is large. Based on the past literature, there was no correlation of total potato map length (including the map of this thesis) and the population size (Pearson correlation 0.247, p-value 0.464 ; Table 11). What is causing the conflict between the simulation study and the published genetic maps is currently not known.

What can be seen in Table 11 though, is that there is a correlation between the number of markers used and the total map length (Pearson correlation 0.665, p-value 0.0094), between the number of markers and the publication year (Pearson correlation 0.639 , p-value 0.0138 ) and between the population size and the publication year (Pearson correlation 0.639 , p -value 0.0139 ). It appears that the number of markers in the map is more a measurement for the cumulative map length than the population size. Consequently, correctly binning of markers shortens linkage maps (Ronin et al., 2010).

Table 11. Overview of linkage maps of potato found in literature, the integrated map of this thesis and linkage maps of other Solanum species. The type of the map, population size, length and the number of markers are used as a statistic for comparing the maps. Furthermore, authors and the publication years are included in the table as well.

| Authors | Publication year | Type | Population size | $\begin{aligned} & \text { Total } \\ & \text { length }(\mathrm{cM}) \end{aligned}$ | N <br> Markers |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Potatoes |  |  |  |  |  |
| Gebhardt et al. | 1991 | diploid | 67 | 1034 | 304 |
| Tanksley et al. | 1992 | diploid | 155 | 684 | 134 |
| Jacobs et al. | 1994 | diploid | 67 | 1120 | 270 |
| Meyer et al. | 1998 | tetraploid | 94 | 909.9 | 231 |
| Meyer et al. | 1998 | tetraploid | 94 | 486.6 | 106 |
| Menéndez et al. | 2002 | diploid | 189 | 750 | 447 |
| Feingold et al. | 2005 | tetraploid | 42 | 792 | 55 |
| Luo et al. | 2006 | tetraploid | 228 | 888 | 201 |
| Danan et al. | 2011 | consensus | - | 1260 | 2141 |
| Felcher et al. | 2012 | diploid | ? | 965.3 | 944 |
| Felcher et al. | 2012 | diploid | ? | 792.1 | 637 |
| Hackett et al. | 2013 | tetraploid | 190 | 1087.5 | 1301 |
| Prashar et al. | 2014 | diploid | 186 | 753.99 | 2157 |
| This thesis | 2015 | tetraploid | 237 | 1406.13 | 5165 |
| Other Solanum species |  |  |  |  |  |
| Sim et al. | 2012 | Tomato (diploid) | 79 | 1669.9 | 3503 |
| Sim et al. | 2012 | Tomato (diploid) | 160 | 1154.6 | 3687 |
| Sim et al. | 2012 | Tomato (diploid) | 183 | 1049.2 | 4491 |
| Gramazio et al. | 2014 | Eggplant (diploid) | 91 | 1085 | 234 |
| Iorizzo et al. | 2014 | S. Bulbocastanum (diploid) | ? | 644.9 | 409 |

## Effect of errors and violation of assumptions on mapping

One of the reasons that more markers might increase the map length is because with more markers there is a higher change on errors. One of these errors is assigning a wrong dosage to a marker which can have a huge impact on the accuracy of the map by inflating the map length (Cheema \& Dicks, 2009). Cartwright et al. (2007) explain that every $1 \%$ error rate inflates the map with 2 cM . Brzustowicz et al. (1993) even found that a $3 \%$ error rate can double the map length. It is good to note that the error rate can be estimated for a specific SNP array (Saunders et al., 2007), although estimating the error rate for a specific marker is often labour intensive, it is possible (Hoffman \& Amos, 2005). When the global error rate, for a specific SNP array, is known, the true map length can be estimated from the estimated length and the number of mapped markers (Brzustowicz et al., 1993).

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In addition to wrong dosage scoring, missing data can lead to incorrect marker orders, especially in regions with a high marker coverage (Hackett \& Broadfoot, 2003). Even though, on a local level the marker order might be wrong due to missing data, it is doubtful that it will distort the global order (Maliepaard, personal communication). Markers with many missing values were not removed before ordering or before calculation of the recombination frequency during this thesis. Considering that markers with missing values can lead to an incorrect order, it may be wise to have a pre-selection of the markers (Pompanon et al., 2005) before the markers enter the mapping pipeline described in this thesis. An example of a pre-selection is a $10 \%$ missing value threshold, as was used in Alstroemeria (see above; Appendix 15), meaning that markers with more than $10 \%$ missing values are excluded prior to the analysis.

Hackett \& Broadfoot (2003) mention that missing data in combination with segregation distortion (violation of Assumption 3) will shorten the map when the linear regression method of JoinMap is used, however this is in contrast to my personal observations (results not shown). Although, under normal conditions, the linear regression method of JoinMap is longer than the linear regression method used in this thesis and the maximum llikelihood method of JoinMap (Figure 12). Furthermore, Hackett \& Broadfoot (2003) also mention that segregation distortion does not affect the map order much, but this is in contrast with other studies (Cheema \& Dicks, 2009). Liu (1997b) showed that small recombination frequencies have a larger bias for segregation distortion while for larger distances the tolerance against skewedness goes up. Small recombination frequencies are of most importance in the linear regression approach and thus these findings could be worrying. However, one would still want to use the small distances in the linear regression approach, since those are most informative and large map distances are more prone to errors when compared to small map distances (Jansen, personal communication).

Another reason for the difference in map length could be that the integrated map presented in this thesis does cover more bits of the genome and previous maps are missing regions, for example telomeric regions. However, if the previous maps are missing certain genomic regions is not known since no comparison between those genetic maps and the physical positions has been made yet.

In addition, during genetic mapping a lot of tests are performed. Although during this thesis multipletesting was taken into account, errors due to multiple testing are likely to have occurred and this could also lead to inconsistencies on the map (Ripol et al., 1999). Furthermore, ordering errors of bridge markers could be problematic in some cases, although LPmerge is able to remove ordering conflicts quite easily (Endelman \& Plomion, 2014).

The reasons why errors in the map order are troublesome is because it could complicate the ability to map QTLs or isolate genes (DeWan et al., 2002). However, a side note should be made here that small local errors in the order would likely not influence the ability to detect QTLs, but map inversions at a larger distance might. It is not very likely that there are many errors in the integrated map, since there is a good correlation between the physical positions and the linkage map, a good correlation between the SxN maps with the previous SxN map (Bourke et al., 2015), the homolog maps are corresponding with the integrated map and the other evaluation methods gave no indication that the ordering might be wrong. Still, it would be interesting to see the source of possible errors and the effect on the map ordering procedure presented in this thesis. This could be done, for example, by simulating tetraploid populations with PedigreeSim (Voorrips \& Maliepaard, 2012) and deliberately introduce different kind of errors.

## QTL analysis

As was mentioned in the Introduction, the estimation of an integrated linkage map is one step towards QTL analysis on the tetraploid level. The advantage of doing a QTL analysis on an integrated map instead of homolog maps itself, is that the QTL analysis based on the integrated map has greater power and higher accuracy. An estimated position of a QTL with a low accuracy is a major obstacle in the application of the results of the QTL analysis (Korol et al., 2012). The QTL mapping with only homolog maps need larger populations to detect the same QTL effects (Hackett et al., 2001). Therefore, progress was made to estimate integrated linkage map of potato. With the marker dense linkage map made in this thesis, QTL analysis can be done and it may provide detailed information about the location of QTLs (Hackett et al., 2014).

QTL mapping is a combination of linkage mapping and traditional quantitative genetics (Liu, 1997e). During QTL analysis, a significant association between traits and markers is searched for. Significant association between traits and markers may be evidence that a QTL is located nearby. The integrated marker information of the consensus map is combined in the calculation of haplotype probabilities along with the map positions to be used in the QTL analysis. This leads to greater power to find QTLs. Wu et al., (2004a) developed a model for QTL analysis in outcrossing tetraploids, such as potato.

Hackett et al. (2014) presents a method to do integrated QTL analysis on 12 potato chromosomes. The QTL analysis was done by a combination of a Hidden Markov Model, to estimate the haplotype probabilities, and weighted regression on those genotype probabilities. Several options for the modelling of QTLs are possible in autotetraploids, such as a main effect model (Hackett et al., 2013) or a mixture model (Bradshaw et al., 2004). Further research will very likely show what kind of approach is most suitable for certain QTLs in potato.

A way to make QTL analysis even more powerful is to use pedigree-information (Bink et al., 2002). The dosages of 3 grandparents and 1 great-grandparent are available for this population (Maliepaard et al., n.d.). When more information is required, this can possible be found in public databases (Van Berloo et al., 2007). By combining the integrated map with pedigree-information it will be possible to find QTLs with higher power and precision.

In addition to the ability to map QTLs, it is also possible to map Segregation Distortion Loci (SDL), such as the self-incompatibility locus located on chromosome 1 (Gebhardt et al., 1991), with a similar method as mapping QTLs (Vogl \& Xu, 2000).

## Conclusion

In this thesis, a mapping pipeline was developed for autotetraploid species such a potato. Four different marker types were assigned to chromosomes and homologs. The markers on homologs were mapped with a linear regression approach. The homolog maps showed good correlation with the physical positions. In addition, the SxN maps showed a high correlation with the maps estimated by JoinMap. The homolog maps were integrated with the R-package LPmerge. LPmerege was extremely fast and uses a graph-theory approach. The methods were applied to a SNP dataset of tetraploid potato. From the comparison of the integrated map with the maps of other species, the genome sequence and other evaluation methods, it can be concluded that the integrated map presented here has a good quality. The integrated map presented in this thesis has a high coverage and can be used for haplotyping, QTL analysis and as a reference linkage map. The methods to estimate the map are working well for tetraploid potato and can therefore be applied to other autotetraploids as well.

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## Recommendations

In the Discussion and Future Prospects possibilities were discussed to improve the linkage mapping procedure described in this thesis. In the Recommendations, these possibilities and opportunities are summarized.

- Implement methods to test for degrees of preferential pairing within the pipeline from marker development to QTL-analysis for tetraploids.
- Develop a method to deal with and investigate the cause of recombination frequencies out of the 0-0.5 range (negative recombination frequencies).
- Investigate how the clustering of markers in linkage groups works when other thresholds than the LOD of linkage are used.
- Investigate what the effect is of single pseudo-linkage marker is on the clustering of markers into linkage groups.
- Investigate if the clustering of markers into linkage groups still works when other marker types than SxN are used.
- Investigate what the effect is of duplicated markers on the calculation of the recombination frequencies and LOD-scores.
- Investigate how the clustering of markers into homologs performs under degrees of preferential pairing.
- Investigate what the effect of setting the LOD-score at 0 when the phase is uninformative.
- Investigate a good way to deal with uninformative marker types, such as DxD and DxS
- Implement parameters for preferential pairing, formation of multivalents, skewedness, unequal recombination frequencies, etc. into the estimator of the recombination frequency.
- Implement more ordering algorithms in the linkage mapping pipeline.
- Investigate how to properly deal with co-segregating markers or how to implement binning in a descent way.
- Investigate the sensitivity of the thresholds used in the whole mapping pipeline.
- Investigate the effect of segregation distortion, missing values, genotyping errors, multiple testing, etc. on the ordering.
- Estimate the (genotype) error rate of the SNP array used.
- Investigate why the integrated map is one of the longest maps in the Solanum genus.
- Investigate what kind of pre-selection is necessary for linkage mapping.
- Implement a haplotyping and QTL-analysis in the pipeline that spans from marker development to QTL-analysis.
- Make the R-scripts more time-efficient and turn the R-scripts into a freely available package.


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## Appendix 1: Editing the datasets

As mentioned in Programmes, Data and Assumptions, the initial datasets have been edited slightly in Excel for practical reasons. How the datasets are edited is mentioned for each dataset here below:

The SxN dataset for P1 (P1_Allsimxnull.xlsx) is edited by converting the dosages 2 to 0 for markers for which the parents have dosages of 3 and 0 (triplex $x$ nulliplex) and converting the dosage 2 to 0 for markers for which the parents have dosages of 4 and 1 (quadruplex $x$ simplex). Furthermore, the markers that have 1 as physical chromosome are converted to ST4.01ch01 as physical chromosome. In the same way 4 is converted to ST4.01ch04, 5 is converted to ST4.01ch05, 8 is converted to ST4.01ch08, 9 is converted to ST4.01ch09, chr02 is converted to ST4.01ch02, chr04 is converted to ST4.01ch04, chr11 is converted to ST4.01ch11 and Chr5 is converted to ST4.01ch05. Thereafter, the file was saved as "P1_all_simxnull.csv."

The SxN dataset for P2 (P2_Allsimxnull.xlsx) is edited by converting uu and - to NA, converting the dosages 3 to 1 and 2 to 0 for markers for which have parents have dosages of 4 and 1 (quadruplex $x$ simplex), converting the dosage 2 to 0 for markers for which the parents have dosages of 3 and 0 (triplex x nulliplex), converting the dosages 4 to 0 and 3 to 1 for markers for which the parents have a dosages of 4 and 3 (quadruplex x triplex). Four markers PotVar0009488, PotVar0090283, PotVar0078532, solcap_snp_c2_37622) were removed from the dataset, since the parental dosages were missing and this made it hard to estimate to which dosages these markers should have been converted. Furthermore, the columns which contained information about the missing values were removed. In addition, the markers that have chr04 as physical chromosome are converted to ST4.01ch04 as physical chromosome. Also, markers that had Unknown as physical chromosome were converted to NA. After the editing, the file was saved as "P2_all_simxnull.csv."

The DxN dataset (P1_P2_All_DxN.xlsx) consisted of two sheets, one for each parent. Sheet 1 contains information of the duplex x nulliplex data of P 1 , which is edited by which is edited by converting uu and - to NA and converting the dosages 4 to 2,3 to 1 and 2 to 0 for markers for which have parents have dosages of 4 and 2 (quadruplex x duplex). Furthermore, the columns which contained information about the missing values were removed. In addition to that, three markers (PotVar0029408, Potvar0068142 and Potvar0088599) were removed from the dataset since the parental dosages were missing and this made it hard to estimate to which dosages these markers should have been converted. . Furthermore, the markers that have chr10 as physical chromosome are converted to ST4.01ch10 as physical chromosome. Also chr07 is converted to ST4.01ch07. Furthermore, markers that had Unknown as physical chromosome were converted to NA. After the editing, the file was saved as P1_All_DxN.csv.

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Sheet 2 is the DxN data for P2, which is edited by converting uu and - to NA and converting the dosages 4 to 2 , 3 to 1 and 2 to 0 for markers for which have parents have dosages of 4 and 2 (quadruplex $x$ duplex). Furthermore, the columns which contained information about the missing values were removed. In addition, the markers that have Chr09 as physical chromosome are converted to ST4.01ch09 as physical chromosome. After the editing, the file was saved as "P2_All_DxN.csv."

The SxS dataset for both parents (P1_P2_All_sim_x_sim.xlsx) is edited by converting Unknown to NA as physical chromosome. In the same way Chr9 is converted to ST4.01ch09. PotVar0102642 and PotVar0131737 were removed from the dataset because almost all dosages were missing values. After the editing, the file was saved as "P1_P2_All_sim_x_sim.csv."

In the dataset with the new physical position, the physical positions which were missing ( $\mathrm{\# N} / \mathrm{B}$ ) were set as 0 . The advantage of this is, is that the missing physical position could potentially be inferred from the linkage maps positions. Another reason is that R will systematically fail when it encounters a non-numeric value (\#N/B) in a place where there should be a numeric value. After editing, the file was saved as "Position info all infinium markers_NBRemoved.csv."

## Appendix 2: Preferential pairing

In Chapter 1 the mode of inheritance of potato was investigated. It was concluded that potato indeed has tetrasomic inheritance. However, a few marker pairs tested significantly for the preferential test and of course it is interesting to see why. One hypothesis is that a skewed marker could be pulling the other markers in the pairs towards testing significant for preferential pairing. Therefore, the markers in the preferential pairing pairs are tested for skewedness by using a Binomial test (with $\mathrm{H}_{0}=\mathrm{n} 1 /(\mathrm{n} 0+\mathrm{n} 1)=0.5$; Table 12). From Table 12 it can be concluded that only a few markers are skewed. This is even more clear, when the frequency of the occurrence of a SxN marker in a preferential pair is plotted against the p -value for skewedness per physical chromosome (Figure 24). The preferential pairing markers of chromosome 2 of P 1 are not skewed, but abundant, while the preferential pairing markers of chromosome 1 and 10 are few but skewed. The same pattern holds for P2, where the markers of chromosome 11 are not skewed and the marker pair of a marker on chromosome 4 and 10 contains a skewed marker (one of these markers is wrongfully assigned to the physical chromosome and this can be seen in Appendix 3). From this it can be concluded that the hypothesis, a single skewed marker is pulling other markers towards a situation that looks like preferential pairing, is not true in all preferential pairing cases. What can be seen however, is that single markers are pulling other markers. However, why this happens is currently unknown and not investigated further in this thesis.

Table 12. SxN markers that tested significantly for preferential pairing. This table included the marker name, the p-value for skewedness, the frequency of occurrence in a "preferential pairing" pair, the physical chromosome and the physical position in base pair.

| Marker Name | p-value | Frequency | Parent | Physical chromosome | Physical positions (in bp( |
| :---: | :---: | :---: | :---: | :---: | :---: |
| PotVar0039036 | 0.18809044 | 6 | P1 | 2 | 22151711 |
| PotVar0039050 | 0.103459235 | 6 | P1 | 2 | 22005405 |
| PotVar0039021 | 0.134177819 | 5 | P1 | 1 | 64376174 |
| solcap_snp_c1_12024 | 0.007799616 | 4 | P1 | 10 | 45944735 |
| PotVar0032906 | 0.371980256 | 3 | P1 | 1 | 64376110 |
| PotVar0038914 | 0.068716964 | 3 | P1 | 2 | 22153416 |
| PotVar0039112 | 0.068716964 | 3 | P1 | 2 | 22001826 |
| PotVar0039162 | 0.118818527 | 3 | P1 | 2 | 20906832 |
| PotVar0039293 | 0.152838641 | 3 | P1 | 2 | 20903543 |
| PotVar0039503 | 0.214123258 | 3 | P1 | 2 | 20838296 |
| PotVar0039524 | 0.423773691 | 2 | P1 | 2 | 20838027 |
| PotVar0010678 | 0.224546142 | 1 | P1 | 2 | 38654566 |
| PotVar0010735 | 0.845223367 | 1 | P1 | 2 | 38503391 |
| PotVar0032910 | 0.037428085 | 1 | P1 | 2 | 22151971 |
| PotVar0032928 | 0.037428085 | 1 | P1 | 1 | 64376527 |
| PotVar0119199 | 0.603397237 | 1 | P1 | 10 | 49584903 |
| solcap_snp_c1_11535 | 0.603397237 | 1 | P1 | 10 | 49553136 |
| solcap_snp_c2_13751 | 0.026349714 | 1 | P1 | 1 | 64614014 |
| solcap_snp_c2_19223 | 0.210176728 | 1 | P1 | 10 | 38722264 |
| solcap_snp_c2_19225 | 0.103459235 | 1 | P1 | 10 | 38723959 |
| PotVar0054060 | 0.70637084 | 5 | P2 | 11 | 14227149 |
| PotVar0021602 | 0.69559142 | 1 | P2 | 11 | 18319898 |
| PotVar0054058 | 0.89623426 | 1 | P2 | 11 | 14227218 |
| PotVar0058240 | 0.02487583 | 1 | P2 | 10 | 57479587 |
| PotVar0101542 | 0.69559142 | 1 | P2 | 4 | 4925258 |
| PotVar0101550 | 0.69559142 | 1 | P2 | 4 | 4925336 |
| PotVar0109580 | 0.16967645 | 1 | P2 | 4 | 6336502 |
| PotVar0113358 | 0.60030616 | 1 | P2 | 11 | 28638721 |



Figure 24. The frequency of occurrence of a $S x N$ marker in a preferential pairing plotted against the $p$ value for skewedness per physical chromosome. It can be noted that not all preferential pairing markers on a certain chromosome are skewed.

## Appendix 3: Clustering of SxN markers along linkage groups

In Chapter 2 the SxN markers were assigned to chromosomes (or linkage groups). Thereafter, the clustering method was compared with the physical chromosomes and the clustering of JoinMap. This appendix presents the consistencies and inconsistencies of the clustering method.

The SxN markers of P1 were clustered at a LOD of 5. Two markers were not clustered (PotVar0079248 and PotVar0059901). The comparison with the physical chromosomes is good (Table 13) and the comparison with JoinMap clustering (Table 14) is perfect. The SxN markers of P2 were clustered at a LOD of 5.15. Two markers were not clustered (PotVar0055484 and PotVar0077706). The comparison with the physical chromosomes is good (Table 15), however, 7 markers were not used in the comparison since those were not assigned yet to physical chromosomes. Between the physical chromosomes and the clustering methods, some inconsistencies exist. Therefore, these SxN markers are investigated a bit further (Table 16). However, most markers were located at the same chromosome in the updated physical chromosomes and public databases.

Table 13. Comparison of clustering of SxN markers of P1 with the physical chromosomes. Both methods of clustering markers are similar, although some inconsistencies exist.

|  | Cluster |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Chromosomes | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | Total |
| 1 | 2 | 156 |  |  |  |  |  |  |  |  |  |  | 158 |
| 2 |  |  | 153 |  |  |  |  |  |  |  |  |  | 153 |
| 3 |  |  |  | 109 |  |  |  |  |  |  |  |  | 109 |
| 4 |  |  |  |  | 144 |  |  |  | 1 |  |  |  | 145 |
| 5 |  |  |  |  |  | 191 |  |  |  |  |  | 1 | 192 |
| 6 |  |  |  |  |  |  | 76 |  |  |  |  |  | 76 |
| 7 |  |  |  |  |  |  |  | 105 | 1 |  |  |  | 106 |
| 8 | 182 |  | 1 |  |  |  |  |  |  |  |  | 2 | 185 |
| 9 |  |  |  |  |  |  |  |  | 115 |  |  |  | 115 |
| 10 |  | 2 |  |  |  |  |  |  |  | 83 |  |  | 85 |
| 11 | 2 | 1 |  |  |  |  |  |  |  |  | 137 |  | 140 |
| 12 |  |  | 1 |  |  | 1 |  |  |  |  |  | 79 | 81 |
| Total | 186 | 159 | 155 | 109 | 144 | 192 | 76 | 105 | 117 | 83 | 137 | 82 | 1545 |

Table 14. Comparison of clustering of SxN markers of P1 with the JoinMap clustering. Both methods of clustering markers are similar.

|  | Cluster |  |  |  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | Total |
| JM Chromosomes |  | 159 |  |  |  |  |  |  |  |  |  |  | 159 |
| 1 |  |  | 155 |  |  |  |  |  |  |  |  |  | 155 |
| 2 |  |  |  | 109 |  |  |  |  |  |  |  |  | 109 |
| 3 |  |  |  |  | 144 |  |  |  |  |  |  |  | 144 |
| 4 |  |  |  |  |  | 192 |  |  |  |  |  |  | 192 |
| 5 |  |  |  |  |  |  | 76 |  |  |  |  |  | 76 |
| 6 |  |  |  |  |  |  |  | 105 |  |  |  |  | 105 |
| 7 |  |  |  |  |  |  |  |  | 117 |  |  |  | 117 |
| 8 |  |  |  |  |  |  |  |  |  | 83 |  |  | 83 |
| 9 |  |  |  |  |  |  |  |  |  | 137 |  | 137 |  |
| 10 |  |  |  |  |  |  |  |  |  |  |  | 82 | 82 |
| 11 | 186 | 159 | 155 | 109 | 144 | 192 | 76 | 105 | 117 | 83 | 137 | 82 | $\mathbf{1 5 4 5}$ |
| 12 |  |  |  |  |  |  |  |  |  | 186 |  |  |  |
| Total |  |  |  |  |  |  |  |  |  |  |  |  |  |

Table 15. Comparison of clustering of SxN markers of P21 with the physical chromosomes. Both methods of clustering markers are similar, although some inconsistencies exist.

|  | Cluster |  |  |  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Chromosomes | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | Total |
| 1 |  |  |  |  | 181 |  |  |  | 1 |  |  |  | 182 |
| 2 | 234 |  |  |  |  |  |  |  |  |  |  |  | 234 |
| 3 |  | 224 |  |  |  |  |  |  |  |  |  |  | 224 |
| 4 |  |  | 4 |  |  |  |  | 132 | 2 | 2 |  |  | 140 |
| 5 |  |  |  |  |  |  |  |  |  | 188 |  |  | 188 |
| 6 |  | 1 |  | 1 |  |  | 152 |  |  |  |  |  | 154 |
| 7 |  |  | 129 |  |  | 1 |  |  |  |  |  |  | 130 |
| 8 |  |  |  | 103 |  |  |  |  |  |  |  |  | 103 |
| 9 |  |  |  |  | 1 |  |  | 1 |  |  | 1 | 43 | 46 |
| 10 |  |  |  |  |  |  |  | 126 | 1 |  |  | 127 |  |
| 11 |  |  | 1 |  |  | 85 |  |  |  |  |  |  | 86 |
| 12 | 234 | 225 | 134 | 104 | 182 | 86 | 152 | 133 | 129 | 191 | 107 | 43 | $\mathbf{1 7 2 0}$ |
| Total |  |  |  |  |  |  |  |  |  |  |  |  |  |

Table 16. SxN markers with inconsistencies between clustering and physical chromosomes. The markers were searched for in a public database and those results are presented under note.

| Marker name | Parent | Physical <br> Chromosome | Clustering <br> Chromosome | Note |
| :---: | :---: | :---: | :---: | :---: |
| PotVar0081045 | P1 | 1 | 8 |  |
| solcap_snp_c2_54581 | P1 | 1 | 8 | Still on chromosome 1* |
| solcap_snp_c2_32337 | P2 | 1 | 11 | On chromosome 1 and 11* |
| PotVar0050913 | P1 | 4 | 9 |  |
| PotVar0032614 | P2 | 4 | 7 |  |
| PotVar0032617 | P2 | 4 | 7 |  |
| PotVar0032700 | P2 | 4 | 7 |  |
| PotVar0032779 | P2 | 4 | 7 |  |
| PotVar0101542 | P2 | 4 | 11 |  |
| PotVar0101550 | P2 | 4 | 11 |  |
| PotVar0084430 | P2 | 4 | 5 |  |
| PotVar0084432 | P2 | 4 | 5 |  |
| PotVar0125939 | P1 | 5 | 12 |  |
| PotVar0085038 | P2 | 6 | 3 |  |
| PotVar0069362 | P2 | 6 | 8 |  |
| solcap_snp_c2_4567 | P1 | 7 | 9 | Still on chromosome 7* |
| PotVar0022107 | P2 | 7 | 12 |  |
| PotVar0125072 | P1 | 8 | 2 |  |
| PotVar0124931 | P1 | 8 | 12 |  |
| PotVar0124993 | P1 | 8 | 12 |  |
| PotVar0014240 | P1 | 10 | 1 |  |
| PotVar0118576 | P1 | 10 | 1 |  |
| PotVar0014615 | P2 | 10 | 1 |  |
| PotVar0058240 | P2 | 10 | 4 | Skewed preferential pairing marker: Table 13 |
| PotVar0118577 | P2 | 10 | 9 |  |
| PotVar0118200 | P1 | 11 | 8 |  |
| PotVar0118202 | P1 | 11 | 8 |  |
| PotVar0071270 | P1 | 11 | 1 |  |
| PotVar0047235 | P2 | 11 | 5 |  |
| solcap_snp_c2_42265 | P1 | 12 | 2 | On chromosome 12 and 2* |
| PotVar0007814 | P1 | 12 | 5 |  |
| PotVar0037615 | P2 | 12 | 7 |  |

## Appendix 4: Hierarchical phase trees

In Chapter 3, the SxN markers were assigned to homologs based on a phase-tree, DxN linkage and sometimes other information sources. Only the phase-tree of chromosome 11 of P2 was shown. Therefore, the phase-trees are presented here for further information (Figure 25).

Figure 25. Hierarchical phase-trees of all the chromosomes. Most chromosomes split nicely in four chromosomes.




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## Appendix 5: Comparison of ordering by JoinMap and ordering of this

## thesis

In Chapter 6, the SxN maps were compared between two mapping methods, namely the maximum likelihood method of JoinMap and the linear regression approach of this thesis. This appendix expands further on the comparison of JoinMap and the ordering method used during this thesis. The number of SxN markers mapped by the maximum likelihood method of JoinMap and the linear regression method used in this thesis are roughly equal (Table 16), although some inconsistencies exist. Furthermore, when the map distances of the common markers are plotted against each there is a good correlation of the two (Figure 26).

Table 16, Next page. Number of SxN markers ordering by the maximum likelihood method of JoinMap and the ordering by the method used in this thesis. The numbers of the homolog ( 1 to 4 ) are translated to letters (A to D) because the assignment of homologs was different between JoinMap and the clustering method here.


Figure 26. Map positions of common SxN markers in both SxN map of the linear regression method of this thesis and the maximum likelihood method of JoinMap. The map positions are plotted against each other.





## Appendix 6: Comparison between the physical positions and map positions

In Chapter 6, different maps were estimated. The SxN map contains only SxN markers, the DxN map contains SxN and DxN markers, the SxS map contains SxN, DxN and SxS markers and the SxT map contains all marker types considered in this thesis. In this thesis, those maps are compared with the physical positions for further information.

## SxN maps

The SxN maps, containing only SxN markers, are compared with the physical positions (Figure 27).

Figure 27. The comparison of the map position of the SxN map with the physical positions. The old and new physical positions are compared with the map. In some cases, the comparison between the map and the old physical positions is wrongfully presented as a vertical line. This means that a non-numerical value is present as physical position.

| - Homolog 1 <br> - Homolog 2 <br> - Homolog 3 <br> - Homolog 4 |  |
| :---: | :---: |
| P1 Chromosome 1 <br> Old physical position <br> New physical position <br> Physical position in bp <br> Physical position in bp | P2 Chromosome 1 <br> Old physical position: <br> New physical position <br> Physical position in bp <br> Physical position in bp |


| P1 Chromosome 2 <br> New physical position | P2 Chromosome 2 |
| :---: | :---: |
| P1 Chromosome 3 <br> Old physical position: New physical position | P2 Chromosome 3 <br> Old physical position: <br> New physical position |
| P1 Chromosome 4 | P2 Chromosome 4 |



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## DxN maps

The DxN maps, containing SxN and DxN markers, are compared with the physical positions (Figure 28).

Figure 28. The comparison of the map position of the DxN map with the physical positions. The old and new physical positions are compared with the map. In some cases, the comparison between the map and the old physical positions is wrongfully presented as a vertical line. This means that a non-numerical value is present as physical position.


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## SxS maps

The SxS maps, containing SxN, DxN and SxS markers, are compared with the physical positions (Figure 29).

Figure 29. The comparison of the map position of the $S x S$ map with the physical positions. The old and new physical positions are compared with the map. In some cases, the comparison between the map and the old physical positions is wrongfully presented as a vertical line. This means that a non-numerical value is present as physical position.


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| P1 chromosome 2 | New physical positions | P2 chromosome 2 <br> Old physical positions | New physical positions |
| :---: | :---: | :---: | :---: |
| P1 chromosome 3 <br> Old physical positions | New physical positions | P2 chromosome 3 <br> Old physical positions | New physical positions |
| P1 chromosome 4 <br> Old physical positions | New physical positions | P2 chromosome 4 <br> Old physical positions | New physical positions |

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| P1 chromosome 5 <br> Old physical positions <br> New physical positions | P2 chromosome 5 <br> Old physical positions <br> New physical positions |
| :---: | :---: |
|  |   |
| P1 chromosome 6 <br> New physical positions | P2 chromosome 6 |
| P1 chromosome 7 <br> New physical positions | P2 chromosome 7 |



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| P1 chromosome 11 <br> Old physical positions <br> New physical positions | P2 chromosome 11 <br> Old physical positions | New physical positions |
| :---: | :---: | :---: |
|  |  |  |
| P1 chromosome 12 <br> New physical positions | P2 chromosome 12 <br> Old physical positions | New physical positions |

## SxT maps

The SxT maps, containing all marker types considered in this thesis, are compared with the physical positions (Figure 30).

Figure 30. The comparison of the map position of the SxT map with the physical positions. The old and new physical positions are compared with the map. In some cases, the comparison between the map and the old physical positions is wrongfully presented as a vertical line. This means that a non-numerical value is present as physical position.


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| P1 chromosome 5 <br> Old physical positions <br> New physical positions | P2 chromosome 5 <br> Old physical positions <br> New physical positions |
| :---: | :---: |
|   |   |
| P1 chromosome 6 <br> New physical positions | P2 chromosome 6 <br> New physical positions |
| P1 chromosome 7 <br> New physical positions | P2 chromosome 7 |

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## Appendix 7: Relationship between LOD-scores and recombination frequencies

In Chapters 1 to 4, the recombination frequencies and LOD-scores for different marker types and phases are calculated. In Figure 31, the recombination frequencies are plotted against the LOD-scores to give an impression of the information content.

Figure 31. The recombination frequencies of the different marker types and the corresponding LODscore. Some marker type and phase combination are very informative while some other are not informative at all.


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## Appendix 8: Removed markers from ordering

During the ordering of markers in Chapter 6, markers were removed by the ordering procedure for different reasons. In Table 18, the markers that were removed are presented. The markers come from the ordering of the same homolog maps that are used in the integration procedure. The reason of removal is shown together with the missing values and the p -value for skewedness.

Table 18. Markers that are removed by the ordering procedure together with some additional statistics.
The parent, chromosome, homolog and marker type are shown. The reason of removal is also shown together with the missing values and the p -value for skewedness for each marker.

| Marker Name |  |  |  |
| :--- | :--- | ---: | ---: | :--- | :--- | :--- | :--- |


| solcap_snp_c1_8113 | P1 | 2 | 3 | SxS | Negative distance | 6 | 0.580834136 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| solcap_snp_c1_7341 | P1 | 2 | 3 | SxS | Negative distance | 5 | 0.06703193 |
| PotVar0120627 | P1 | 3 | 1 | DxN | Jump | 2 | 0.754337881 |
| PotVar0056918 | P1 | 3 | 1 | DxN | Jump | 32 | 0.193932736 |
| PotVar0121928 | P1 | 3 | 2 | SxN | Jump | 17 | 0.091665418 |
| PotVar0106413 | P1 | 3 | 2 | SxN | Negative distance | 2 | 0.077332376 |
| PotVar0013242 | P1 | 3 | 2 | DxN | Jump | 1 | 0.032902886 |
| PotVar0121927 | P1 | 3 | 2 | SxT | Negative distance | 3 | 0.400704947 |
| PotVar0019184 | P1 | 3 | 2 | SxN | Jump | 30 | 0.108823554 |
| PotVar0019460 | P1 | 3 | 2 | DxN | Jump | 6 | 0.100715603 |
| PotVar0019343 | P1 | 3 | 2 | DxN | Jump | 0 | 0.019145335 |
| PotVar0013592 | P1 | 3 | 3 | DxN | Jump | 2 | 0.928237098 |
| PotVar0019343 | P1 | 3 | 3 | DxN | Jump | 0 | 0.019145335 |
| PotVar0043186 | P1 | 3 | 4 | DxN | Jump | 28 | 0.630951478 |
| PotVar0084554 | P1 | 3 | 4 | DxN | Jump | 1 | 0.07809821 |
| solcap_snp_c2_21590 | P1 | 4 | 1 | SxS | Negative distance | 1 | 0.632783385 |
| solcap_snp_c2_21578 | P1 | 4 | 1 | SxS | Negative distance | 3 | 0.692448531 |
| solcap_snp_c1_6748 | P1 | 4 | 1 | SxS | Negative distance | 2 | 0.89716935 |
| PotVar0101164 | P1 | 4 | 1 | SxN | Negative distance | 1 | 0.896234257 |
| PotVar0101048 | P1 | 4 | 1 | SxN | Negative distance | 9 | 0.506955687 |
| PotVar0076875 | P1 | 4 | 1 | SxN | Negative distance | 6 | 0.552979217 |
| solcap_snp_c2_55090 | P1 | 4 | 1 | SxT | Negative distance | 0 | 0.420173059 |
| solcap_snp_c2_26794 | P1 | 4 | 1 | SxT | Negative distance | 1 | 0.543258784 |
| solcap_snp_c2_26800 | P1 | 4 | 1 | SxT | Negative distance | 1 | 0.593815603 |
| solcap_snp_c2_36957 | P1 | 4 | 1 | SxN | Negative distance | 2 | 0.844572164 |
| solcap_snp_c1_11008 | P1 | 4 | 1 | SxN | Negative distance | 2 | 1 |
| PotVar0026570 | P1 | 4 | 1 | SxN | Negative distance | 27 | 0.240681858 |
| PotVar0076646 | P1 | 4 | 1 | SxS | Negative distance | 3 | 0.024702404 |
| solcap_snp_c1_12564 | P1 | 4 | 1 | DxN | Jump | 0 | 0.829685255 |
| solcap_snp_c1_11391 | P1 | 4 | 1 | DxN | Jump | 0 | 0.712762086 |
| PotVar0071109 | P1 | 4 | 1 | DxN | Negative distance | 3 | 0.911240229 |
| solcap_snp_c1_11722 | P1 | 4 | 1 | DxN | Negative distance | 1 | 0.888123856 |
| solcap_snp_c1_10715 | P1 | 4 | 1 | DxN | Jump | 0 | 0.033841211 |
| solcap_snp_c2_34017 | P1 | 4 | 2 | SxS | Negative distance | 5 | 0.856267532 |
| solcap_snp_c1_12564 | P1 | 4 | 2 | DxN | Jump | 0 | 0.829685255 |
| PotVar0070965 | P1 | 4 | 2 | DxN | Jump | 30 | 0.024651968 |
| solcap_snp_c2_26771 | P1 | 4 | 3 | SxT | Negative distance | 4 | 0.635851839 |
| solcap_snp_c2_48810 | P1 | 4 | 3 | SxT | Negative distance | 6 | 0.835559533 |
| PotVar0071109 | P1 | 4 | 3 | DxN | Jump | 3 | 0.911240229 |
| PotVar0016775 | P1 | 4 | 4 | SxT | Negative distance | 5 | 0.588503495 |
| PotVar0075324 | P1 | 4 | 4 | SxT | Negative distance | 7 | 0.174152124 |
| PotVar0017293 | P1 | 4 | 4 | SxT | Negative distance | 9 | 0.268262453 |
| PotVar0109579 | P1 | 4 | 4 | SxT | Jump | 5 | 0.630522211 |
| solcap_snp_c2_11568 | P1 | 4 | 4 | SxT | Negative distance | 1 | 0.56199002 |
| PotVar0100820 | P1 | 4 | 4 | SxT | Jump | 12 | 0.683861409 |

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| PotVar0100941 | P1 | 4 | 4 | SxT | Jump | 13 | 0.642772591 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PotVar0107009 | P1 | 4 | 4 | SxT | Jump | 5 | 0.652643567 |
| PotVar0100919 | P1 | 4 | 4 | SxS | Jump | 1 | 0.922647085 |
| PotVar0100767 | P1 | 4 | 4 | SxS | Jump | 5 | 0.890137521 |
| PotVar0106843 | P1 | 4 | 4 | SxS | Jump | 0 | 0.981191782 |
| PotVar0076503 | P1 | 4 | 4 | SxS | Jump | 1 | 0.98736859 |
| PotVar0076511 | P1 | 4 | 4 | SxS | Jump | 9 | 0.647775867 |
| PotVar0076621 | P1 | 4 | 4 | SxS | Jump | 2 | 0.98103324 |
| PotVar0076666 | P1 | 4 | 4 | SxS | Jump | 1 | 0.922647085 |
| solcap_snp_c1_11626 | P1 | 4 | 4 | SxN | Jump | 1 | 0.601860667 |
| solcap_snp_c1_3740 | P1 | 4 | 4 | DxN | Jump | 3 | 0.487751747 |
| solcap_snp_c1_15513 | P1 | 4 | 4 | DxN | Jump | 0 | 0.42552551 |
| solcap_snp_c1_11356 | P1 | 4 | 4 | DxN | Jump | 0 | 0.712762086 |
| PotVar0070856 | P1 | 4 | 4 | DxN | Negative distance | 17 | 0.727470509 |
| solcap_snp_c1_7569 | P1 | 4 | 4 | DxN | Jump | 0 | 0.156047483 |
| PotVar0070965 | P1 | 4 | 4 | DxN | Significance | 30 | 0.024651968 |
| PotVar0075687 | P1 | 4 | 4 | DxN | Jump | 7 | 0.620534601 |
| solcap_snp_c2_23593 | P1 | 4 | 4 | DxN | Negative distance | 1 | 0.49964575 |
| PotVar0034716 | P1 | 5 | 1 | SxN | Negative distance | 1 | 0.03148605 |
| PotVar0034469 | P1 | 5 | 1 | SxN | Negative distance | 2 | 0.026349714 |
| solcap_snp_c2_11685 | P1 | 5 | 1 | DxN | Negative distance | 0 | 0.63000639 |
| solcap_snp_c2_11707 | P1 | 5 | 1 | DxN | Negative distance | 0 | 0.418845499 |
| PotVar0048673 | P1 | 5 | 1 | DxN | Negative distance | 24 | 0.360188865 |
| PotVar0081633 | P1 | 5 | 3 | SxS | Negative distance | 2 | 0.08861942 |
| solcap_snp_c2_50302 | P1 | 5 | 3 | DxN | Negative distance | 5 | 0.593598731 |
| PotVar0123135 | P1 | 5 | 4 | SxS | Negative distance | 10 | 0.140498978 |
| PotVar0081647 | P1 | 5 | 4 | SxT | Negative distance | 8 | 0.532057152 |
| PotVar0048577 | P1 | 5 | 4 | SxN | Jump | 36 | 0.158165345 |
| solcap_snp_c2_33509 | P1 | 5 | 4 | SxS | Jump | 8 | 0.548572033 |
| solcap_snp_c2_23834 | P1 | 5 | 4 | SxS | Jump | 0 | 0.977060455 |
| solcap_snp_c2_24066 | P1 | 6 | 3 | DxN | Jump | 13 | 0.115242775 |
| PotVar0057091 | P1 | 6 | 4 | DxN | Jump | 3 | 1 |
| solcap_snp_c2_9202 | P1 | 6 | 4 | DxN | Jump | 0 | 0.909430492 |
| PotVar0085050 | P1 | 6 | 4 | DxN | Jump | 25 | 0.115826676 |
| PotVar0082855 | P1 | 6 | 4 | DxN | Jump | 3 | 0.056597251 |
| solcap_snp_c2_28212 | P1 | 7 | 1 | DxN | Negative distance | 1 | 0.200065559 |
| PotVar0036843 | P1 | 7 | 1 | SxS | Negative distance | 1 | 0.581367099 |
| PotVar0102524 | P1 | 7 | 1 | SxS | Negative distance | 0 | 0.58147105 |
| solcap_snp_c2_26239 | P1 | 7 | 1 | SxS | Negative distance | 0 | 0.459102853 |
| PotVar0132155 | P1 | 7 | 1 | SxS | Negative distance | 22 | 0.054513749 |
| PotVar0022288 | P1 | 7 | 1 | SxS | Jump | 4 | 0.026663398 |
| solcap_snp_c2_38828 | P1 | 7 | 1 | SxS | Negative distance | 5 | 0.269727031 |
| PotVar0102724 | P1 | 7 | 1 | DxN | Jump | 2 | 0.086110178 |
| solcap_snp_c1_8601 | P1 | 7 | 2 | SxN | Negative distance | 21 | 0.219511208 |

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| PotVar0132077 | P1 | 7 | 2 | SxN | Negative distance | 0 | 0.845223367 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PotVar0095593 | P1 | 7 | 2 | SxN | Negative distance | 1 | 0.794212476 |
| PotVar0095619 | P1 | 7 | 2 | SxN | Negative distance | 5 | 0.94767273 |
| solcap_snp_c1_16221 | P1 | 7 | 2 | SxN | Negative distance | 0 | 0.696813997 |
| solcap_snp_c2_36838 | P1 | 7 | 2 | SxN | Negative distance | 0 | 0.744901949 |
| PotVar0102362 | P1 | 7 | 2 | SxN | Negative distance | 0 | 0.948117129 |
| PotVar0102547 | P1 | 7 | 2 | SxN | Negative distance | 0 | 0.845223367 |
| solcap_snp_c2_52663 | P1 | 7 | 2 | SxT | Negative distance | 6 | 0.993527531 |
| PotVar0095580 | P1 | 7 | 2 | SxS | Negative distance | 1 | 0.724673625 |
| PotVar0015345 | P1 | 7 | 3 | SxS | Significance | 85 | 0.005946217 |
| solcap_snp_c2_49379 | P1 | 8 | 1 | DxN | Jump | 0 | 0.464951219 |
| solcap_snp_c1_8282 | P1 | 8 | 3 | DxN | Jump | 1 | 0.015741054 |
| PotVar0088739 | P1 | 8 | 3 | SxT | Negative distance | 9 | 0.344455809 |
| solcap_snp_c2_51957 | P1 | 8 | 3 | SxT | Jump | 4 | 0.59365364 |
| PotVar0063333 | P1 | 8 | 4 | DxN | Negative distance | 1 | 0.33265958 |
| PotVar0012337 | P1 | 9 | 1 | DxN | Jump | 2 | 0.773845546 |
| PotVar0012284 | P1 | 9 | 1 | DxN | Jump | 16 | 0.126884299 |
| PotVar0012007 | P1 | 9 | 1 | DxN | Jump | 15 | 0.437052173 |
| solcap_snp_c1_3597 | P1 | 9 | 1 | DxN | Jump | 1 | 0.654601377 |
| PotVar0061732 | P1 | 9 | 2 | SxS | Jump | 3 | 0.17943384 |
| solcap_snp_c2_43241 | P1 | 9 | 4 | SxT | Jump | 5 | 0.40273248 |
| solcap_snp_c2_3063 | P1 | 9 | 4 | DxN | Significance | 1 | 0.476386669 |
| PotVar0123577 | P1 | 10 | 2 | DxN | Jump | 7 | 0.218569295 |
| PotVar0065848 | P1 | 10 | 2 | SxS | Jump | 8 | 0.11794291 |
| solcap_snp_c2_950 | P1 | 10 | 2 | DxN | Jump | 0 | 0.811508223 |
| PotVar0057421 | P1 | 10 | 3 | SxS | Negative distance | 4 | 0.614390559 |
| PotVar0057635 | P1 | 10 | 3 | SxS | Negative distance | 4 | 0.840448381 |
| PotVar0057721 | P1 | 10 | 3 | SxS | Negative distance | 25 | 0.626891918 |
| PotVar0057860 | P1 | 10 | 3 | SxS | Negative distance | 4 | 0.840448381 |
| PotVar0058227 | P1 | 10 | 3 | SxN | Negative distance | 2 | 0.433812405 |
| PotVar0005597 | P1 | 10 | 3 | SxN | Negative distance | 1 | 0.695591422 |
| PotVar0005576 | P1 | 10 | 3 | SxN | Negative distance | 1 | 0.558068429 |
| PotVar0005103 | P1 | 10 | 3 | SxN | Negative distance | 2 | 0.94789635 |
| solcap_snp_c2_40823 | P1 | 10 | 3 | SxN | Negative distance | 0 | 0.516056364 |
| solcap_snp_c2_41394 | P1 | 10 | 3 | SxN | Negative distance | 1 | 0.648726044 |
| solcap_snp_c2_40764 | P1 | 10 | 3 | SxN | Negative distance | 0 | 0.896670248 |
| solcap_snp_c2_45603 | P1 | 10 | 3 | SxT | Negative distance | 4 | 0.660893157 |
| PotVar0132240 | P1 | 10 | 3 | SxT | Negative distance | 4 | 0.745282889 |
| solcap_snp_c1_14236 | P1 | 10 | 3 | SxS | Negative distance | 2 | 0.084566864 |
| PotVar0120165 | P1 | 10 | 3 | SxS | Jump | 3 | 0.596250727 |
| solcap_snp_c2_1263 | P1 | 10 | 3 | SxS | Jump | 4 | 0.563853184 |
| PotVar0104285 | P1 | 10 | 3 | SxS | Jump | 4 | 0.275353495 |
| PotVar0104021 | P1 | 10 | 3 | SxS | Jump | 39 | 0.167314703 |
| PotVar0065380 | P1 | 10 | 4 | SxN | Negative distance | 4 | 0.793351627 |
| solcap_snp_c1_16585 | P1 | 11 | 2 | SxT | Negative distance | 10 | 0.642279779 |

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| solcap_snp_c2_4957 | P1 | 11 | 2 | SxT | Negative distance | 13 | 0.741479961 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| solcap_snp_c1_16586 | P1 | 11 | 2 | SxT | Negative distance | 8 | 0.976268657 |
| PotVar0005899 | P1 | 11 | 2 | SxT | Negative distance | 5 | 0.856267532 |
| solcap_snp_c2_44633 | P1 | 11 | 2 | SxT | Negative distance | 9 | 0.853939666 |
| PotVar0059121 | P1 | 11 | 2 | SxT | Negative distance | 6 | 0.306057378 |
| PotVar0134712 | P1 | 11 | 2 | SxN | Negative distance | 0 | 0.948117129 |
| solcap_snp_c1_14683 | P1 | 11 | 2 | SxN | Negative distance | 1 | 0.896234257 |
| solcap_snp_c2_54586 | P1 | 11 | 2 | SxN | Negative distance | 11 | 0.641575228 |
| solcap_snp_c2_3737 | P1 | 11 | 2 | SxN | Negative distance | 2 | 0.94789635 |
| PotVar0112309 | P1 | 11 | 2 | SxN | Negative distance | 5 | 0.792479885 |
| solcap_snp_c1_4926 | P1 | 11 | 2 | SxN | Negative distance | 2 | 0.55639128 |
| solcap_snp_c1_9183 | P1 | 11 | 2 | SxN | Negative distance | 1 | 0.514276192 |
| solcap_snp_c2_57106 | P1 | 11 | 2 | SxN | Negative distance | 0 | 0.397473921 |
| solcap_snp_c2_56626 | P1 | 11 | 2 | SxN | Negative distance | 3 | 0.600306158 |
| solcap_snp_c2_33905 | P1 | 11 | 2 | SxN | Negative distance | 12 | 0.204163755 |
| PotVar0059873 | P1 | 11 | 2 | SxN | Negative distance | 3 | 0.55639128 |
| solcap_snp_c2_53683 | P1 | 11 | 2 | SxN | Negative distance | 5 | 0.742790582 |
| solcap_snp_c2_12334 | P1 | 11 | 2 | SxN | Negative distance | 3 | 0.512476402 |
| PotVar0058735 | P1 | 11 | 2 | SxN | Negative distance | 1 | 0.514276192 |
| solcap_snp_c2_15340 | P1 | 11 | 2 | SxS | Negative distance | 6 | 0.880112422 |
| solcap_snp_c2_23921 | P1 | 11 | 2 | SxT | Negative distance | 7 | 0.928752451 |
| PotVar0105987 | P1 | 11 | 2 | SxS | Negative distance | 3 | 0.270443437 |
| solcap_snp_c2_54589 | P1 | 11 | 2 | DxN | Negative distance | 5 | 0.093416279 |
| solcap_snp_c2_20948 | P1 | 11 | 2 | SxT | Negative distance | 5 | 0.288985342 |
| PotVar0066299 | P1 | 11 | 3 | DxN | Jump | 3 | 0.574366733 |
| PotVar0064140 | P1 | 11 | 3 | DxN | Jump | 4 | 0.696569307 |
| solcap_snp_c2_18836 | P1 | 12 | 1 | SxS | Negative distance | 4 | 0.379913699 |
| PotVar0030960 | P1 | 12 | 1 | SxS | Negative distance | 10 | 0.006321008 |
| PotVar0107233 | P1 | 12 | 3 | DxN | Jump | 8 | 0.04657954 |
| solcap_snp_c1_13697 | P1 | 12 | 3 | DxN | Jump | 4 | 0.154926128 |
| PotVar0052458 | P1 | 12 | 3 | DxN | Jump | 2 | 0.23682696 |
| PotVar0069011 | P1 | 12 | 3 | DxN | Significance | 26 | 0.79558866 |
| PotVar0098373 | P1 | 12 | 4 | SxS | Jump | 6 | 0.050766455 |
| PotVar0050696 | P2 | 1 | 1 | SxS | Negative distance | 2 | 0.549980564 |
| solcap_snp_c2_9892 | P2 | 1 | 1 | SxS | Negative distance | 2 | 0.722143133 |
| solcap_snp_c2_4896 | P2 | 1 | 1 | SxS | Negative distance | 3 | 0.616987828 |
| PotVar0035753 | P2 | 1 | 1 | SxS | Negative distance | 1 | 0.805653367 |
| PotVar0035852 | P2 | 1 | 1 | SxS | Negative distance | 2 | 0.786293197 |
| PotVar0036054 | P2 | 1 | 1 | SxS | Negative distance | 1 | 0.778800783 |
| solcap_snp_c1_15123 | P2 | 1 | 1 | DxN | Jump | 0 | 0.42552551 |
| PotVar0061044 | P2 | 1 | 1 | DxN | Jump | 0 | 0.333503718 |
| PotVar0050201 | P2 | 1 | 1 | DxN | Jump | 2 | 0.165650962 |
| solcap_snp_c2_27894 | P2 | 1 | 1 | SxS | Negative distance | 1 | 0.72775079 |
| PotVar0045420 | P2 | 1 | 1 | DxN | Jump | 14 | 0.003808089 |

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| PotVar0071966 | P2 | 1 | 1 | SxT | Jump | 1 | 0.574023613 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PotVar0071853 | P2 | 1 | 1 | SxS | Jump | 2 | 0.547645193 |
| PotVar0029356 | P2 | 1 | 2 | DxN | Jump | 37 | 0.560598677 |
| solcap_snp_c1_2519 | P2 | 1 | 3 | SxS | Negative distance | 3 | 0.345037365 |
| PotVar0042445 | P2 | 1 | 3 | SxS | Negative distance | 2 | 0.417083814 |
| PotVar0041272 | P2 | 1 | 3 | SxS | Negative distance | 2 | 0.260068945 |
| solcap_snp_c1_3895 | P2 | 1 | 3 | SxS | Negative distance | 1 | 0.043658559 |
| PotVar0006268 | P2 | 1 | 3 | SxS | Negative distance | 7 | 0.107481689 |
| PotVar0029221 | P2 | 1 | 3 | SxS | Negative distance | 2 | 0.88578892 |
| solcap_snp_c2_20502 | P2 | 1 | 3 | SxT | Negative distance | 0 | 0.028706465 |
| PotVar0041226 | P2 | 1 | 3 | DxN | Negative distance | 0 | 0.993690873 |
| PotVar0006051 | P2 | 1 | 3 | DxN | Negative distance | 17 | 0.695934314 |
| PotVar0044821 | P2 | 1 | 4 | SxT | Negative distance | 1 | 0.954459402 |
| solcap_snp_c2_17539 | P2 | 1 | 4 | DxN | Jump | 3 | 0.253651279 |
| PotVar0050306 | P2 | 1 | 4 | DxN | Significance | 1 | 0.125396923 |
| PotVar0050855 | P2 | 1 | 4 | DxN | Jump | 4 | 0.330096878 |
| PotVar0060676 | P2 | 1 | 4 | DxN | Significance | 1 | 0.407690993 |
| PotVar0126809 | P2 | 1 | 4 | DxN | Jump | 0 | 0.152628741 |
| PotVar0036238 | P2 | 1 | 4 | DxN | Jump | 31 | 0.413837641 |
| PotVar0041660 | P2 | 1 | 4 | DxN | Negative distance | 0 | 0.944629941 |
| solcap_snp_c2_14274 | P2 | 1 | 4 | DxN | Jump | 1 | 0.958512303 |
| PotVar0120130 | P2 | 1 | 4 | SxT | Jump | 12 | 0.750761941 |
| PotVar0071945 | P2 | 1 | 4 | SxS | Jump | 17 | 0.459657916 |
| PotVar0009857 | P2 | 2 | 1 | SxT | Jump | 8 | 0.688415675 |
| solcap_snp_c2_27271 | P2 | 2 | 1 | DxN | Jump | 2 | 0.065025308 |
| solcap_snp_c2_17415 | P2 | 2 | 1 | DxN | Jump | 33 | 0.004665095 |
| PotVar0094352 | P2 | 2 | 2 | SxN | Jump | 0 | 0.152838641 |
| PotVar0094561 | P2 | 2 | 2 | SxN | Jump | 2 | 0.089661905 |
| PotVar0088857 | P2 | 2 | 2 | SxS | Jump | 5 | 0.181427972 |
| PotVar0009867 | P2 | 2 | 2 | SxS | Jump | 16 | 0.300785628 |
| solcap_snp_c1_8113 | P2 | 2 | 2 | SxS | Jump | 6 | 0.580834136 |
| PotVar0124339 | P2 | 2 | 2 | SxN | Jump | 0 | 0.051100537 |
| PotVar0002139 | P2 | 2 | 2 | DxN | Jump | 5 | 0.633245845 |
| PotVar0001573 | P2 | 2 | 2 | DxN | Jump | 1 | 0.290170054 |
| PotVar0001694 | P2 | 2 | 2 | DxN | Jump | 1 | 0.230823554 |
| PotVar0117579 | P2 | 2 | 2 | SxN | Jump | 2 | 0.067544047 |
| solcap_snp_c2_53818 | P2 | 2 | 2 | SxN | Jump | 0 | 0.091031106 |
| PotVar0029477 | P2 | 2 | 2 | SxN | Jump | 0 | 0.091031106 |
| solcap_snp_c1_12354 | P2 | 2 | 2 | SxS | Jump | 2 | 0.125089799 |
| PotVar0123873 | P2 | 2 | 2 | SxS | Jump | 1 | 0.153030406 |
| solcap_snp_c2_42059 | P2 | 2 | 2 | SxS | Jump | 3 | 0.100774312 |
| solcap_snp_c1_11553 | P2 | 2 | 2 | SxS | Jump | 16 | 0.036849804 |
| solcap_snp_c2_47765 | P2 | 2 | 2 | SxN | Jump | 2 | 0.361135437 |
| solcap_snp_c1_868 | P2 | 2 | 2 | SxN | Jump | 2 | 0.433812405 |
| solcap_snp_c2_41884 | P2 | 2 | 2 | SxN | Jump | 1 | 0.397473921 |

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| solcap_snp_c2_41874 | P2 | 2 | 2 | SxN | Jump | 25 | 0.010875333 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| solcap_snp_c2_32237 | P2 | 2 | 2 | SxN | Jump | 1 | 0.397473921 |
| PotVar0109750 | P2 | 2 | 2 | SxN | Jump | 8 | 0.290350496 |
| solcap_snp_c2_45311 | P2 | 2 | 2 | SxS | Jump | 0 | 0.019145335 |
| PotVar0089282 | P2 | 2 | 2 | SxN | Jump | 61 | 0.001914064 |
| solcap_snp_c2_55863 | P2 | 2 | 2 | SxS | Jump | 4 | 0.808603695 |
| solcap_snp_c2_805 | P2 | 2 | 2 | DxN | Jump | 7 | 0.129718144 |
| PotVar0116077 | P2 | 2 | 3 | SxS | Jump | 2 | 0.53157292 |
| PotVar0046789 | P2 | 2 | 3 | SxS | Negative distance | 5 | 0.720661163 |
| solcap_snp_c1_16540 | P2 | 2 | 3 | SxS | Negative distance | 3 | 0.704387005 |
| solcap_snp_c1_10493 | P2 | 2 | 3 | SxT | Jump | 6 | 0.911126445 |
| PotVar0119058 | P2 | 2 | 3 | SxT | Jump | 6 | 0.835559533 |
| PotVar0009178 | P2 | 2 | 3 | SxS | Jump | 7 | 0.320097246 |
| solcap_snp_c2_41963 | P2 | 2 | 3 | SxS | Jump | 32 | 0.123055236 |
| PotVar0109718 | P2 | 2 | 3 | SxN | Jump | 1 | 0.948117129 |
| solcap_snp_c2_27271 | P2 | 2 | 3 | DxN | Jump | 2 | 0.065025308 |
| solcap_snp_c2_735 | P2 | 2 | 3 | DxN | Jump | 1 | 0.346690775 |
| solcap_snp_c2_32467 | P2 | 2 | 3 | SxT | Significance | 8 | 0.170951473 |
| solcap_snp_c1_2350 | P2 | 2 | 3 | SxT | Significance | 11 | 0.072199758 |
| solcap_snp_c2_805 | P2 | 2 | 3 | DxN | Jump | 7 | 0.129718144 |
| PotVar0010377 | P2 | 2 | 4 | DxN | Negative distance | 4 | 0.561438399 |
| solcap_snp_c2_9497 | P2 | 3 | 1 | SxN | Negative distance | 36 | 0.39737829 |
| PotVar0013867 | P2 | 3 | 1 | SxT | Negative distance | 6 | 0.590979455 |
| PotVar0013866 | P2 | 3 | 1 | SxT | Negative distance | 5 | 0.588503495 |
| PotVar0021187 | P2 | 3 | 1 | SxT | Negative distance | 6 | 0.357672138 |
| PotVar0113388 | P2 | 3 | 1 | DxN | Negative distance | 0 | 0.087448183 |
| solcap_snp_c2_46605 | P2 | 3 | 1 | DxN | Negative distance | 0 | 0.062725492 |
| PotVar0129499 | P2 | 3 | 1 | DxN | Negative distance | 1 | 0.233034726 |
| PotVar0095322 | P2 | 3 | 1 | DxN | Negative distance | 0 | 0.309112301 |
| PotVar0094840 | P2 | 3 | 1 | DxN | Negative distance | 4 | 0.224330427 |
| PotVar0021338 | P2 | 3 | 1 | SxN | Jump | 22 | 0.495333072 |
| solcap_snp_c1_15839 | P2 | 3 | 1 | DxN | Significance | 0 | 0.965788776 |
| PotVar0019272 | P2 | 3 | 1 | DxN | Negative distance | 0 | 0.993690873 |
| solcap_snp_c1_5388 | P2 | 3 | 1 | DxN | Significance | 0 | 0.895154013 |
| solcap_snp_c1_15783 | P2 | 3 | 1 | DxN | Significance | 1 | 0.899485628 |
| solcap_snp_c2_17218 | P2 | 3 | 1 | DxN | Significance | 0 | 0.965788776 |
| PotVar0084678 | P2 | 3 | 1 | DxN | Significance | 2 | 0.882027614 |
| solcap_snp_c2_36231 | P2 | 3 | 1 | DxN | Significance | 2 | 0.663932715 |
| PotVar0068047 | P2 | 3 | 2 | SxN | Jump | 1 | 0.397473921 |
| PotVar0070350 | P2 | 3 | 2 | SxN | Jump | 1 | 0.268427312 |
| solcap_snp_c2_37991 | P2 | 3 | 2 | SxN | Jump | 4 | 1 |
| PotVar0095449 | P2 | 3 | 2 | SxN | Jump | 0 | 0.795062658 |
| PotVar0094878 | P2 | 3 | 2 | SxN | Jump | 0 | 0.896670248 |
| PotVar0085735 | P2 | 3 | 2 | SxN | Jump | 2 | 0.896234257 |

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| solcap_snp_c1_167 | P2 | 3 | 2 | SxN | Jump | 2 | 0.794212476 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PotVar0056335 | P2 | 3 | 2 | SxN | Jump | 1 | 0.216078094 |
| PotVar0055974 | P2 | 3 | 2 | SxN | Jump | 1 | 0.328866863 |
| solcap_snp_c2_1835 | P2 | 3 | 2 | SxN | Jump | 5 | 0.554694997 |
| PotVar0027440 | P2 | 3 | 2 | SxN | Jump | 1 | 0.474044299 |
| solcap_snp_c2_57258 | P2 | 3 | 2 | SxN | Jump | 2 | 0.601860667 |
| PotVar0030069 | P2 | 3 | 2 | SxN | Jump | 2 | 0.361135437 |
| PotVar0121236 | P2 | 3 | 2 | SxN | Jump | 3 | 0.472161104 |
| PotVar0013408 | P2 | 3 | 2 | SxN | Jump | 3 | 0.55639128 |
| PotVar0013895 | P2 | 3 | 2 | SxN | Jump | 4 | 0.512476402 |
| PotVar0014057 | P2 | 3 | 2 | SxN | Jump | 3 | 0.266389411 |
| PotVar0014208 | P2 | 3 | 2 | SxN | Jump | 4 | 0.359081609 |
| solcap_snp_c2_1579 | P2 | 3 | 2 | SxS | Jump | 9 | 0.003006383 |
| solcap_snp_c2_20259 | P2 | 3 | 2 | SxS | Jump | 1 | 0.571596456 |
| solcap_snp_c2_1722 | P2 | 3 | 2 | DxN | Jump | 0 | 0.447625887 |
| PotVar0055776 | P2 | 3 | 2 | DxN | Jump | 0 | 0.541222911 |
| PotVar0030088 | P2 | 3 | 2 | DxN | Jump | 1 | 0.830787398 |
| solcap_snp_c2_18271 | P2 | 3 | 2 | DxN | Jump | 2 | 0.663932715 |
| solcap_snp_c2_35553 | P2 | 3 | 2 | DxN | Jump | 1 | 0.970774554 |
| solcap_snp_c2_5286 | P2 | 3 | 2 | DxN | Jump | 1 | 0.305306015 |
| solcap_snp_c1_1909 | P2 | 3 | 2 | DxN | Jump | 91 | 0.01564609 |
| PotVar0021136 | P2 | 3 | 2 | DxN | Jump | 0 | 0.211443497 |
| solcap_snp_c1_15839 | P2 | 3 | 2 | DxN | Jump | 0 | 0.965788776 |
| PotVar0019272 | P2 | 3 | 2 | DxN | Jump | 0 | 0.993690873 |
| PotVar0019302 | P2 | 3 | 2 | DxN | Jump | 1 | 0.992612171 |
| solcap_snp_c1_5388 | P2 | 3 | 2 | DxN | Jump | 0 | 0.895154013 |
| solcap_snp_c1_15783 | P2 | 3 | 2 | DxN | Jump | 1 | 0.899485628 |
| solcap_snp_c2_17218 | P2 | 3 | 2 | DxN | Jump | 0 | 0.965788776 |
| PotVar0084678 | P2 | 3 | 2 | DxN | Jump | 2 | 0.882027614 |
| solcap_snp_c2_36231 | P2 | 3 | 2 | DxN | Jump | 2 | 0.663932715 |
| PotVar0120484 | P2 | 3 | 3 | SxT | Jump | 20 | 0.58457724 |
| solcap_snp_c1_6332 | P2 | 3 | 3 | SxS | Negative distance | 27 | 0.045480292 |
| solcap_snp_c1_9292 | P2 | 3 | 3 | SxS | Negative distance | 1 | 0.703494715 |
| PotVar0094922 | P2 | 3 | 3 | SxS | Negative distance | 1 | 0.805653367 |
| PotVar0029778 | P2 | 3 | 3 | SxS | Negative distance | 5 | 0.953692684 |
| PotVar0121499 | P2 | 3 | 3 | SxN | Negative distance | 3 | 0.844572164 |
| PotVar0014077 | P2 | 3 | 3 | SxN | Negative distance | 2 | 0.601860667 |
| solcap_snp_c2_5263 | P2 | 3 | 3 | SxN | Negative distance | 2 | 0.794212476 |
| solcap_snp_c2_26402 | P2 | 3 | 3 | DxN | Jump | 4 | 0.714739663 |
| PotVar0029727 | P2 | 3 | 4 | SxN | Negative distance | 2 | 0.117256565 |
| solcap_snp_c1_5794 | P2 | 3 | 4 | SxN | Negative distance | 1 | 0.171499463 |
| solcap_snp_c1_7111 | P2 | 3 | 4 | SxN | Negative distance | 3 | 0.042479994 |
| PotVar0121403 | P2 | 3 | 4 | SxN | Negative distance | 9 | 0.097575937 |
| solcap_snp_c1_151 | P2 | 3 | 4 | SxN | Negative distance | 3 | 0.101991434 |
| solcap_snp_c2_616 | P2 | 3 | 4 | SxN | Negative distance | 2 | 0.151099073 |

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| PotVar0021118 | P2 | 3 | 4 | SxN | Negative distance | 3 | 0.214123258 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PotVar0021255 | P2 | 3 | 4 | DxN | Jump | 0 | 0.001766761 |
| PotVar0020884 | P2 | 3 | 4 | DxN | Jump | 0 | 0.008069851 |
| PotVar0021083 | P2 | 3 | 4 | DxN | Jump | 6 | 0.053996764 |
| solcap_snp_c2_18268 | P2 | 3 | 4 | SxS | Negative distance | 5 | 0.6843332 |
| solcap_snp_c2_18271 | P2 | 3 | 4 | DxN | Jump | 2 | 0.663932715 |
| PotVar0055776 | P2 | 3 | 4 | DxN | Jump | 0 | 0.541222911 |
| solcap_snp_c2_16722 | P2 | 4 | 1 | SxS | Negative distance | 0 | 0.745836445 |
| PotVar0000514 | P2 | 4 | 2 | SxT | Negative distance | 3 | 0.423596317 |
| PotVar0017609 | P2 | 4 | 2 | SxS | Jump | 9 | 0.367879441 |
| solcap_snp_c1_3461 | P2 | 4 | 2 | SxS | Jump | 6 | 0.432720897 |
| PotVar0058240 | P2 | 4 | 2 | SxN | Negative distance | 100 | 0.016432262 |
| PotVar0075700 | P2 | 4 | 3 | DxN | Jump | 62 | 0.004086771 |
| solcap_snp_c2_55793 | P2 | 4 | 3 | DxN | Jump | 2 | 0.120006093 |
| PotVar0000759 | P2 | 4 | 3 | DxN | Jump | 1 | 0.04464066 |
| solcap_snp_c1_8330 | P2 | 4 | 3 | DxN | Jump | 14 | 0.00145046 |
| PotVar0118472 | P2 | 4 | 3 | DxN | Jump | 13 | 0.411316266 |
| solcap_snp_c2_11490 | P2 | 4 | 3 | DxN | Jump | 7 | 0.426486778 |
| solcap_snp_c2_39322 | P2 | 4 | 3 | DxN | Jump | 19 | 0.005871679 |
| solcap_snp_c2_36993 | P2 | 4 | 4 | SxT | Jump | 8 | 0.85266491 |
| solcap_snp_c2_36941 | P2 | 4 | 4 | SxS | Negative distance | 2 | 0.226960628 |
| PotVar0034970 | P2 | 5 | 1 | SxT | Negative distance | 6 | 0.658527552 |
| PotVar0081707 | P2 | 5 | 4 | SxT | Negative distance | 3 | 0.220287776 |
| solcap_snp_c2_42451 | P2 | 5 | 4 | SxT | Negative distance | 3 | 0.357037475 |
| PotVar0117367 | P2 | 5 | 4 | DxN | Negative distance | 1 | 0.677889363 |
| PotVar0117324 | P2 | 5 | 4 | DxN | Jump | 0 | 0.788721679 |
| PotVar0129937 | P2 | 5 | 4 | DxN | Jump | 1 | 0.762474327 |
| PotVar0080320 | P2 | 5 | 4 | DxN | Negative distance | 1 | 0.598869322 |
| PotVar0080026 | P2 | 5 | 4 | DxN | Jump | 0 | 0.706027376 |
| PotVar0080800 | P2 | 5 | 4 | DxN | Jump | 6 | 0.653557557 |
| solcap_snp_c2_11747 | P2 | 5 | 4 | DxN | Jump | 14 | 0.539780918 |
| solcap_snp_c1_1126 | P2 | 5 | 4 | SxN | Negative distance | 3 | 0.214123258 |
| solcap_snp_c2_51765 | P2 | 6 | 1 | DxN | Jump | 1 | 0.360167369 |
| PotVar0040162 | P2 | 6 | 1 | DxN | Jump | 3 | 0.273932982 |
| PotVar0086012 | P2 | 6 | 2 | SxN | Negative distance | 1 | 0.268427312 |
| PotVar0069582 | P2 | 6 | 2 | SxT | Negative distance | 2 | 0.208443948 |
| PotVar0104586 | P2 | 6 | 2 | SxN | Negative distance | 1 | 0.845223367 |
| solcap_snp_c2_43080 | P2 | 6 | 2 | SxN | Negative distance | 18 | 0.176407874 |
| PotVar0090367 | P2 | 6 | 2 | SxN | Negative distance | 2 | 1 |
| solcap_snp_c1_3125 | P2 | 6 | 3 | SxT | Negative distance | 8 | 0.993471188 |
| solcap_snp_c2_56590 | P2 | 6 | 3 | DxN | Jump | 0 | 0.231766399 |
| solcap_snp_c2_37358 | P2 | 6 | 3 | DxN | Jump | 2 | 0.278688788 |
| solcap_snp_c2_37329 | P2 | 6 | 3 | DxN | Jump | 1 | 0.258801243 |
| solcap_snp_c1_16128 | P2 | 6 | 3 | SxS | Jump | 5 | 0.034070944 |

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| PotVar0065903 | P2 | 6 | 3 | DxN | Jump | 5 | 0.091918455 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PotVar0015345 | P2 | 7 | 1 | SxS | Significance | 85 | 0.005946217 |
| PotVar0102371 | P2 | 7 | 2 | SxS | Negative distance | 6 | 0.769584314 |
| PotVar0134970 | P2 | 7 | 2 | DxN | Jump | 1 | 0.264622988 |
| PotVar0093025 | P2 | 7 | 3 | SxS | Negative distance | 3 | 0.614356754 |
| solcap_snp_c1_2404 | P2 | 7 | 4 | SxT | Negative distance | 3 | 0.535833595 |
| solcap_snp_c2_33488 | P2 | 7 | 4 | SxS | Negative distance | 1 | 0.63547036 |
| PotVar0093776 | P2 | 7 | 4 | SxS | Negative distance | 2 | 0.61694295 |
| PotVar0093742 | P2 | 7 | 4 | DxN | Jump | 2 | 0.514328241 |
| PotVar0102773 | P2 | 7 | 4 | DxN | Jump | 35 | 0.336516226 |
| PotVar0047739 | P2 | 7 | 4 | DxN | Jump | 0 | 0.895154013 |
| PotVar0103342 | P2 | 8 | 1 | SxT | Negative distance | 2 | 0.049681251 |
| solcap_snp_c2_28433 | P2 | 8 | 1 | DxN | Jump | 0 | 0.567533389 |
| solcap_snp_c2_47905 | P2 | 8 | 2 | SxS | Negative distance | 25 | 0.066073922 |
| PotVar0124889 | P2 | 8 | 2 | DxN | Significance | 70 | 0.016103116 |
| solcap_snp_c1_10384 | P2 | 8 | 4 | SxT | Negative distance | 1 | 0.593815603 |
| solcap_snp_c1_8297 | P2 | 8 | 4 | SxT | Negative distance | 2 | 0.540698413 |
| PotVar0011929 | P2 | 9 | 1 | DxN | Negative distance | 2 | 0.215891627 |
| solcap_snp_c2_46431 | P2 | 9 | 2 | SxN | Negative distance | 2 | 0.240256334 |
| solcap_snp_c2_46427 | P2 | 9 | 2 | SxN | Negative distance | 0 | 0.43575911 |
| PotVar0132972 | P2 | 9 | 2 | SxN | Negative distance | 0 | 0.43575911 |
| PotVar0034273 | P2 | 9 | 2 | SxN | Negative distance | 6 | 0.292450194 |
| solcap_snp_c1_4248 | P2 | 9 | 2 | SxN | Negative distance | 0 | 0.516056364 |
| solcap_snp_c1_4282 | P2 | 9 | 2 | SxN | Negative distance | 2 | 0.361135437 |
| solcap_snp_c1_1000 | P2 | 9 | 2 | SxS | Negative distance | 4 | 0.68397882 |
| PotVar0012446 | P2 | 9 | 2 | DxN | Negative distance | 4 | 0.255978725 |
| PotVar0101835 | P2 | 9 | 2 | SxN | Negative distance | 2 | 0.601860667 |
| PotVar0103657 | P2 | 9 | 2 | SxN | Negative distance | 2 | 0.695591422 |
| PotVar0103791 | P2 | 9 | 2 | SxN | Negative distance | 5 | 0.94767273 |
| PotVar0103920 | P2 | 9 | 2 | SxN | Negative distance | 1 | 0.648726044 |
| PotVar0103891 | P2 | 9 | 2 | SxN | Negative distance | 1 | 0.744901949 |
| PotVar0107741 | P2 | 9 | 2 | SxN | Negative distance | 1 | 0.744901949 |
| PotVar0107499 | P2 | 9 | 2 | SxN | Negative distance | 2 | 0.514276192 |
| solcap_snp_c2_42964 | P2 | 9 | 2 | SxT | Significance | 7 | 0.061341152 |
| solcap_snp_c1_16414 | P2 | 9 | 2 | SxT | Significance | 5 | 0.052656504 |
| PotVar0131150 | P2 | 9 | 2 | DxN | Negative distance | 0 | 0.464951219 |
| PotVar0054644 | P2 | 9 | 2 | DxN | Negative distance | 1 | 0.388712511 |
| PotVar0012077 | P2 | 9 | 2 | DxN | Jump | 6 | 0.148697066 |
| PotVar0012114 | P2 | 9 | 2 | DxN | Negative distance | 13 | 0.028147056 |
| PotVar0011657 | P2 | 9 | 2 | DxN | Negative distance | 71 | 0.030933869 |
| solcap_snp_c2_4196 | P2 | 9 | 2 | DxN | Negative distance | 3 | 0.937908799 |
| solcap_snp_c1_975 | P2 | 9 | 2 | DxN | Negative distance | 14 | 0.008309476 |
| solcap_snp_c2_3323 | P2 | 9 | 2 | DxN | Negative distance | 5 | 0.340416229 |
| PotVar0130658 | P2 | 9 | 2 | DxN | Negative distance | 1 | 0.268861387 |
| solcap_snp_c1_1053 | P2 | 9 | 2 | DxN | Negative distance | 1 | 0.300493094 |

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| PotVar0103876 | P2 | 9 | 3 | SxT | Jump | 4 | 0.234922912 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PotVar0097335 | P2 | 9 | 3 | SxT | Jump | 7 | 0.403049598 |
| PotVar0101947 | P2 | 9 | 3 | DxN | Jump | 23 | 0.094437873 |
| PotVar0105170 | P2 | 9 | 3 | SxS | Jump | 7 | 0.703157823 |
| PotVar0105349 | P2 | 9 | 3 | SxS | Jump | 7 | 0.679120621 |
| solcap_snp_c2_3949 | P2 | 9 | 4 | SxS | Negative distance | 8 | 0.31367789 |
| solcap_snp_c2_3323 | P2 | 9 | 4 | DxN | Jump | 5 | 0.340416229 |
| PotVar0130658 | P2 | 9 | 4 | DxN | Jump | 1 | 0.268861387 |
| PotVar0065848 | P2 | 10 | 2 | SxS | Jump | 8 | 0.11794291 |
| solcap_snp_c2_56515 | P2 | 10 | 2 | DxN | Significance | 2 | 0.754337881 |
| solcap_snp_c2_27827 | P2 | 10 | 2 | DxN | Significance | 9 | 0.041821609 |
| solcap_snp_c1_307 | P2 | 10 | 4 | DxN | Significance | 0 | 0.132789868 |
| PotVar0105750 | P2 | 11 | 1 | SxS | Negative distance | 25 | 0.242902697 |
| PotVar0063968 | P2 | 11 | 1 | SxN | Jump | 8 | 0.354916224 |
| PotVar0067438 | P2 | 11 | 3 | SxS | Negative distance | 7 | 0.264362296 |
| PotVar0067013 | P2 | 11 | 3 | SxT | Negative distance | 4 | 0.103050905 |
| solcap_snp_c2_20948 | P2 | 11 | 3 | SxT | Negative distance | 5 | 0.288985342 |
| PotVar0064771 | P2 | 11 | 3 | DxN | Jump | 4 | 0.002240943 |
| PotVar0064519 | P2 | 11 | 3 | DxN | Jump | 24 | 0.016479571 |
| solcap_snp_c2_50977 | P2 | 11 | 4 | SxS | Jump | 3 | 0.216554175 |
| PotVar0130698 | P2 | 11 | 4 | SxS | Jump | 9 | 0.164864463 |
| PotVar0047372 | P2 | 11 | 4 | SxS | Jump | 3 | 0.576210605 |
| PotVar0058600 | P2 | 11 | 4 | SxS | Jump | 14 | 0.12456101 |
| PotVar0105566 | P2 | 11 | 4 | SxN | Jump | 1 | 0.558068429 |
| PotVar0106057 | P2 | 11 | 4 | SxN | Jump | 3 | 0.55639128 |
| solcap_snp_c2_6256 | P2 | 11 | 4 | SxN | Jump | 1 | 0.474044299 |
| PotVar0067017 | P2 | 11 | 4 | SxN | Jump | 1 | 0.216078094 |
| PotVar0110432 | P2 | 11 | 4 | SxN | Jump | 10 | 0.001389865 |
| PotVar0067764 | P2 | 11 | 4 | SxN | Jump | 21 | 0.117389103 |
| solcap_snp_c1_2162 | P2 | 11 | 4 | SxN | Jump | 0 | 0.298647087 |
| PotVar0112755 | P2 | 11 | 4 | DxN | Jump | 3 | 0.340642044 |
| PotVar0066337 | P2 | 11 | 4 | DxN | Jump | 4 | 0.689875153 |
| PotVar0064787 | P2 | 11 | 4 | DxN | Jump | 16 | 0.069117612 |
| PotVar0064771 | P2 | 11 | 4 | DxN | Jump | 4 | 0.002240943 |
| PotVar0064519 | P2 | 11 | 4 | DxN | Jump | 24 | 0.016479571 |
| PotVar0008553 | P2 | 11 | 4 | DxN | Negative distance | 6 | 0.916070147 |
| solcap_snp_c2_18788 | P2 | 12 | 4 | SxS | Negative distance | 0 | 0.155226615 |
| solcap_snp_c2_24595 | P2 | 12 | 4 | DxN | Jump | 1 | 0.476386669 |
| PotVar0098059 | P2 | 12 | 4 | DxN | Negative distance | 1 | 0.377752164 |

## Appendix 9: The integrated map or the final orders

In Chapter 7, the individual homolog maps were integrated. The map positions of all the markers on the integrated map are shown in Table 19.

Table 19. Map position in cM of all the markers on the integrated map. Every chromosome has a sub-table with its own markers and map positions.

| Chromosome 1 |  |
| :---: | :---: |
| Name | cM |
| PotVar0120126 | 0 |
| PotVar0120075 | 0.43 |
| PotVar0119913 | 0.43 |
| PotVar0119973 | 0.43 |
| PotVar0044821 | 2.31 |
| PotVar0044815 | 2.31 |
| PotVar0071852 | 2.58 |
| solcap_snp_c2_21099 | 3.62 |
| PotVar0120088 | 5.83 |
| PotVar0119912 | 6.26 |
| solcap_snp_c1_6674 | 6.26 |
| solcap_snp_c2_6906 | 6.53 |
| PotVar0072072 | 6.53 |
| PotVar0119989 | 6.68 |
| PotVar0119975 | 6.68 |
| solcap_snp_c2_21234 | 7.11 |
| PotVar0071853 | 7.72 |
| PotVar0120034 | 8.23 |
| PotVar0120004 | 8.66 |
| PotVar0119813 | 8.66 |
| solcap_snp_c1_10930 | 9.03 |
| solcap_snp_c2_36658 | 9.03 |
| solcap_snp_c2_36660 | 9.46 |
| PotVar0071925 | 9.46 |
| PotVar0120070 | 9.46 |
| PotVar0044985 | 9.55 |
| PotVar0044829 | 9.55 |
| PotVar0072052 | 9.55 |
| PotVar0071924 | 9.95 |
| PotVar0072063 | 10.81 |
| PotVar0071966 | 12.01 |
| PotVar0072033 | 12.14 |
| PotVar0044840 | 12.14 |
| PotVar0072076 | 12.9 |


| PotVar0071846 | 13.69 |
| :---: | :---: |
| solcap_snp_c2_6683 | 15.08 |
| solcap_snp_c2_6713 | 17.44 |
| solcap_snp_c2_21247 | 18.09 |
| PotVar0044864 | 18.82 |
| PotVar0044823 | 18.84 |
| solcap_snp_c2_21227 | 20.13 |
| solcap_snp_c2_21233 | 20.13 |
| PotVar0045000 | 20.13 |
| PotVar0045260 | 26.02 |
| PotVar0045340 | 26.02 |
| PotVar0045502 | 26.02 |
| PotVar0045662 | 26.02 |
| PotVar0045167 | 27.03 |
| PotVar0045459 | 27.03 |
| PotVar0045210 | 28.48 |
| PotVar0045404 | 28.48 |
| PotVar0045339 | 28.48 |
| PotVar0045505 | 28.48 |
| PotVar0045145 | 28.48 |
| solcap_snp_c1_6114 | 28.61 |
| solcap_snp_c2_51800 | 33.68 |
| solcap_snp_c2_55012 | 33.78 |
| PotVar0114875 | 33.78 |
| solcap_snp_c1_13296 | 34.02 |
| solcap_snp_c2_48051 | 34.11 |
| solcap_snp_c2_27918 | 34.12 |
| PotVar0045460 | 34.61 |
| PotVar0122300 | 37.63 |
| PotVar0045420 | 37.8 |
| solcap_snp_c2_52705 | 41.04 |
| solcap_snp_c2_2332 | 41.49 |
| solcap_snp_c2_53521 | 43.13 |
| solcap_snp_c2_43984 | 43.13 |
| solcap_snp_c1_12937 | 43.13 |
| solcap_snp_c2_43973 | 43.13 |


| solcap_snp_c2_686 | 43.44 |
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| PotVar0102233 | 43.44 |
| solcap_snp_c2_54303 | 44.48 |
| solcap_snp_c2_54306 | 44.48 |
| PotVar0088430 | 44.48 |
| solcap_snp_c2_45395 | 44.48 |
| solcap_snp_c2_53763 | 44.48 |
| PotVar0100708 | 44.48 |
| solcap_snp_c1_5477 | 44.48 |
| solcap_snp_c2_2873 | 44.48 |
| solcap_snp_c2_55618 | 44.48 |
| PotVar0071270 | 44.48 |
| PotVar0014900 | 44.48 |
| PotVar0102229 | 44.8 |
| solcap_snp_c1_14649 | 44.8 |
| PotVar0102234 | 44.96 |
| PotVar0102148 | 45.53 |
| PotVar0109024 | 45.53 |
| solcap_snp_c2_694 | 45.53 |
| solcap_snp_c2_49719 | 45.53 |
| solcap_snp_c1_12152 | 45.91 |
| PotVar0088385 | 46.12 |
| PotVar0095087 | 46.12 |
| PotVar0095116 | 46.12 |
| PotVar0122548 | 46.12 |
| solcap_snp_c1_15612 | 46.12 |
| solcap_snp_c1_15853 | 46.12 |
| solcap_snp_c1_16423 | 46.12 |
| solcap_snp_c1_16690 | 46.12 |
| solcap_snp_c1_6795 | 46.12 |
| solcap_snp_c2_27681 | 46.12 |
| solcap_snp_c2_2871 | 46.12 |
| PotVar0122472 | 46.12 |
| PotVar0132283 | 46.12 |
| PotVar0132289 | 46.12 |
| PotVar0132309 | 46.12 |

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| solcap_snp_c1_15855 | 46.12 |
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| solcap_snp_c1_16425 | 46.12 |
| solcap_snp_c1_8535 | 46.12 |
| solcap_snp_c2_2874 | 46.12 |
| solcap_snp_c2_32111 | 46.12 |
| solcap_snp_c2_55113 | 46.12 |
| solcap_snp_c2_55621 | 46.12 |
| solcap_snp_c2_56843 | 46.12 |
| solcap_snp_c2_54307 | 46.12 |
| PotVar0000042 | 46.46 |
| solcap_snp_c1_12938 | 46.9 |
| solcap_snp_c2_43970 | 46.9 |
| PotVar0102174 | 46.96 |
| solcap_snp_c2_35601 | 47.39 |
| PotVar0102161 | 48.16 |
| solcap_snp_c2_49722 | 48.16 |
| solcap_snp_c2_41438 | 48.16 |
| solcap_snp_c2_49724 | 48.16 |
| solcap_snp_c2_49726 | 48.16 |
| PotVar0118576 | 48.71 |
| PotVar0102189 | 48.81 |
| PotVar0102258 | 48.81 |
| solcap_snp_c2_49732 | 48.81 |
| solcap_snp_c1_14648 | 49.16 |
| solcap_snp_c1_8362 | 49.16 |
| PotVar0028605 | 49.16 |
| PotVar0100622 | 49.16 |
| PotVar0102235 | 49.18 |
| solcap_snp_c2_2653 | 49.18 |
| PotVar0114310 | 49.18 |
| PotVar0037326 | 49.6 |
| PotVar0122454 | 49.6 |
| PotVar0000062 | 49.6 |
| PotVar0122549 | 49.6 |
| PotVar0095159 | 49.6 |
| solcap_snp_c2_40112 | 49.6 |
| PotVar0071533 | 49.6 |
| PotVar0124795 | 49.81 |
| solcap_snp_c2_35518 | 49.81 |
| PotVar0088355 | 50.16 |
| PotVar0122473 | 50.16 |
| PotVar0088290 | 50.16 |
| PotVar0122550 | 50.48 |
| PotVar0014240 | 50.48 |


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| PotVar0122493 | 50.48 |
| PotVar0081107 | 50.48 |
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| PotVar0081102 | 50.48 |
| PotVar0132314 | 50.48 |
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| solcap_snp_c2_45626 | 50.51 |
| solcap_snp_c2_45627 | 50.51 |
| PotVar0071625 | 50.51 |
| PotVar0071645 | 50.51 |
| solcap_snp_c2_56842 | 50.74 |
| solcap_snp_c2_35532 | 50.74 |
| solcap_snp_c2_40131 | 50.74 |
| PotVar0095162 | 50.74 |
| solcap_snp_c1_16169 | 50.74 |
| PotVar0006081 | 50.74 |
| solcap_snp_c2_48549 | 50.74 |
| solcap_snp_c2_45623 | 50.74 |
| solcap_snp_c2_57284 | 50.74 |
| solcap_snp_c1_15521 | 50.74 |
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| solcap_snp_c2_35220 | 50.74 |
| PotVar0095169 | 50.74 |
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| PotVar0095184 | 50.74 |
| PotVar0132333 | 50.74 |
| solcap_snp_c2_27677 | 50.74 |
| PotVar0000406 | 50.74 |
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| solcap_snp_c1_14249 | 50.97 |
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| PotVar0100729 | 51.02 |
| PotVar0114353 | 51.02 |
| PotVar0100762 | 51.02 |
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| solcap_snp_c2_45621 | 51.37 |
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| PotVar0018985 | 52.22 |
| PotVar0018968 | 52.22 |
| PotVar0071624 | 52.22 |
| PotVar0071575 | 52.22 |


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| PotVar0018848 | 52.22 |
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| PotVar0049628 | 52.4 |
| PotVar0018685 | 52.57 |
| PotVar0049426 | 52.83 |
| PotVar0049351 | 52.83 |
| PotVar0049273 | 52.83 |
| PotVar0049427 | 52.83 |
| solcap_snp_c1_14633 | 53.11 |
| PotVar0049291 | 53.26 |
| PotVar0018833 | 53.58 |
| PotVar0132267 | 53.59 |
| PotVar0095172 | 53.59 |
| solcap_snp_c2_35503 | 54.02 |
| PotVar0018687 | 54.02 |
| solcap_snp_c2_41339 | 54.11 |
| solcap_snp_c2_35536 | 54.45 |
| solcap_snp_c1_13430 | 54.45 |
| PotVar0018694 | 54.45 |
| solcap_snp_c2_35537 | 54.45 |
| solcap_snp_c2_2591 | 54.45 |
| PotVar0018693 | 54.45 |
| PotVar0006125 | 54.45 |
| PotVar0018832 | 54.5 |
| PotVar0049174 | 54.54 |
| solcap_snp_c1_12131 | 54.54 |
| PotVar0018996 | 54.56 |
| PotVar0071554 | 54.56 |
| PotVar0049691 | 55.75 |
| PotVar0049692 | 55.75 |
| PotVar0049754 | 56.17 |
| PotVar0049777 | 56.17 |
| PotVar0006142 | 56.57 |
| PotVar0049542 | 57.03 |
| solcap_snp_c2_38404 | 57.03 |
| PotVar0049593 | 57.03 |
| solcap_snp_c2_56359 | 57.4 |
| solcap_snp_c1_16515 | 57.4 |
| solcap_snp_c2_45622 | 57.4 |
| PotVar0005994 | 58.2 |
| PotVar0005918 | 59.67 |
| PotVar0049567 | 60 |

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| PotVar0049564 | 60 |
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| solcap_snp_c2_20798 | 60 |
| solcap_snp_c2_13671 | 60 |
| solcap_snp_c2_20799 | 60.63 |
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| PotVar0033081 | 61.11 |
| PotVar0032877 | 61.11 |
| PotVar0014615 | 61.11 |
| PotVar0033046 | 61.64 |
| PotVar0126047 | 62.21 |
| PotVar0072127 | 62.38 |
| PotVar0072239 | 62.38 |
| PotVar0072439 | 62.38 |
| PotVar0072169 | 62.38 |
| PotVar0072448 | 62.38 |
| PotVar0126146 | 62.49 |
| solcap_snp_c1_4415 | 62.62 |
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| PotVar0032928 | 63.05 |
| PotVar0049199 | 63.34 |
| PotVar0049037 | 63.34 |
| solcap_snp_c2_32367 | 63.34 |
| PotVar0049005 | 63.34 |
| PotVar0126052 | 63.34 |
| PotVar0126035 | 63.34 |
| solcap_snp_c1_13686 | 63.34 |
| solcap_snp_c2_40954 | 63.34 |
| PotVar0033086 | 63.34 |
| solcap_snp_c2_13751 | 63.48 |
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| PotVar0032879 | 63.51 |
| PotVar0033013 | 63.51 |
| PotVar0032875 | 63.51 |
| PotVar0033007 | 63.51 |
| PotVar0032984 | 63.51 |
| PotVar0032987 | 64.42 |
| PotVar0032926 | 64.42 |
| PotVar0032887 | 64.44 |
| PotVar0032906 | 64.44 |
| PotVar0033135 | 64.71 |
| PotVar0049099 | 65.89 |
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| solcap_snp_c2_13650 | 67.86 |
| solcap_snp_c1_4757 | 69.19 |
| PotVar0033411 | 69.61 |


| PotVar0033735 | 69.61 |
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| PotVar0033409 | 69.61 |
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| solcap_snp_c2_14489 | 69.61 |
| solcap_snp_c2_14580 | 69.61 |
| solcap_snp_c1_4752 | 69.61 |
| solcap_snp_c2_14589 | 69.61 |
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| PotVar0129827 | 69.61 |
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| PotVar0098709 | 69.61 |
| PotVar0098530 | 69.61 |
| PotVar0098422 | 69.61 |
| PotVar0098430 | 69.61 |
| solcap_snp_c2_20521 | 69.61 |
| PotVar0072262 | 69.61 |
| PotVar0072139 | 69.61 |
| PotVar0043708 | 69.61 |
| PotVar0098727 | 69.61 |
| PotVar0129853 | 69.61 |
| solcap_snp_c1_4745 | 69.61 |
| PotVar0129817 | 69.61 |
| solcap_snp_c2_20569 | 69.61 |
| PotVar0098524 | 69.61 |
| solcap_snp_c2_20522 | 69.61 |
| solcap_snp_c2_20501 | 69.61 |
| solcap_snp_c2_20513 | 69.61 |
| solcap_snp_c1_6501 | 69.61 |
| PotVar0006051 | 69.61 |
| solcap_snp_c2_20506 | 70.04 |
| PotVar0098389 | 70.04 |
| PotVar0098497 | 70.04 |
| solcap_snp_c2_20517 | 70.04 |
| solcap_snp_c2_20530 | 70.04 |


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| PotVar0043650 | 70.39 |
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| solcap_snp_c2_31821 | 73.5 |
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| PotVar0043665 | 74.6 |
| PotVar0072433 | 74.95 |
| PotVar0072443 | 74.95 |
| PotVar0043513 | 75.42 |
| PotVar0043404 | 75.42 |
| PotVar0043821 | 75.52 |
| PotVar0043814 | 75.52 |
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| PotVar0041585 | 77.11 |
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| PotVar0043296 | 78.52 |
| solcap_snp_c2_17539 | 78.52 |
| solcap_snp_c2_17537 | 79.62 |
| PotVar0043484 | 79.62 |
| PotVar0043426 | 79.62 |
| solcap_snp_c2_17529 | 79.62 |
| PotVar0043347 | 79.62 |
| PotVar0043570 | 79.62 |
| solcap_snp_c2_14274 | 81.22 |
| PotVar0041660 | 82.85 |
| solcap_snp_c1_3895 | 83.41 |
| PotVar0006158 | 83.41 |
| solcap_snp_c1_5653 | 83.41 |
| PotVar0041488 | 84.24 |
| solcap_snp_c1_5656 | 86.08 |
| solcap_snp_c2_17191 | 86.08 |
| PotVar0041226 | 86.26 |
| PotVar0041271 | 86.26 |
| PotVar0041241 | 86.26 |
| PotVar0041233 | 86.26 |
| PotVar0041397 | 87.96 |

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| PotVar0041586 | 87.96 |
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| PotVar0041674 | 88.39 |
| PotVar0006246 | 88.49 |
| PotVar0006265 | 89.3 |
| PotVar0006356 | 89.36 |
| PotVar0006243 | 90.02 |
| PotVar0006198 | 90.31 |
| solcap_snp_c1_3852 | 90.9 |
| solcap_snp_c1_3851 | 90.9 |
| solcap_snp_c2_17192 | 91.99 |
| solcap_snp_c1_3853 | 92.08 |
| solcap_snp_c1_3854 | 92.08 |
| solcap_snp_c2_12215 | 92.08 |
| PotVar0041919 | 93.73 |
| PotVar0042300 | 93.73 |
| PotVar0006395 | 94.12 |
| PotVar0028758 | 94.18 |
| solcap_snp_c2_2506 | 94.39 |
| PotVar0041859 | 94.48 |
| PotVar0041901 | 94.48 |
| solcap_snp_c1_5295 | 94.48 |
| PotVar0042036 | 94.48 |
| PotVar0041272 | 95.13 |
| PotVar0041319 | 95.13 |
| PotVar0041415 | 95.13 |
| PotVar0041439 | 95.13 |
| solcap_snp_c1_4604 | 95.13 |
| PotVar0041571 | 95.13 |
| PotVar0041593 | 95.13 |
| PotVar0006384 | 95.13 |
| PotVar0041677 | 95.23 |
| PotVar0042489 | 96.75 |
| PotVar0029118 | 96.79 |
| PotVar0042709 | 97.19 |
| PotVar0006430 | 97.21 |
| solcap_snp_c1_601 | 97.22 |
| solcap_snp_c1_4617 | 98.76 |
| solcap_snp_c1_573 | 101.13 |
| solcap_snp_c2_2291 | 101.13 |
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| PotVar0042358 | 101.65 |
| PotVar0042350 | 101.65 |
| PotVar0049903 | 102.27 |


| PotVar0049914 | 102.27 |
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| solcap_snp_c1_2458 | 102.28 |
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| PotVar0042497 | 102.29 |
| PotVar0049886 | 102.71 |
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| solcap_snp_c1_5281 | 102.71 |
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| solcap_snp_c2_16424 | 102.71 |
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| PotVar0041748 | 102.71 |
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| PotVar0029382 | 102.71 |
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| PotVar0049919 | 107.05 |
| PotVar0049790 | 107.84 |
| PotVar0029356 | 108.47 |
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| PotVar0049792 | 109.36 |
| PotVar0050056 | 110.23 |
| PotVar0050009 | 110.23 |
| PotVar0049974 | 110.23 |
| PotVar0050140 | 110.67 |
| PotVar0050116 | 110.67 |
| PotVar0050638 | 111.1 |
| PotVar0050484 | 111.1 |
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| PotVar0049948 | 111.8 |
| PotVar0096787 | 112.05 |


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| PotVar0049906 | 112.93 |
| PotVar0049853 | 113.37 |
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| PotVar0050061 | 114.28 |
| solcap_snp_c2_7059 | 114.71 |
| solcap_snp_c2_7056 | 114.71 |
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| PotVar0050406 | 115.15 |
| PotVar0050409 | 115.15 |
| PotVar0050432 | 115.15 |
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| PotVar0050453 | 115.15 |
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| PotVar0050401 | 115.15 |
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| PotVar0096805 | 115.98 |
| PotVar0050806 | 116.04 |
| solcap_snp_c2_9988 | 116.04 |
| PotVar0050814 | 116.04 |
| PotVar0050773 | 116.04 |
| PotVar0061225 | 116.11 |
| PotVar0061136 | 116.11 |
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| PotVar0061243 | 117.14 |
| PotVar0060673 | 117.81 |
| PotVar0060854 | 118.66 |
| PotVar0060695 | 118.88 |
| PotVar0035449 | 119.37 |
| PotVar0035721 | 120.62 |
| PotVar0050306 | 121.17 |

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| solcap_snp_c2_6990 | 121.32 |
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| PotVar0050855 | 122.13 |
| PotVar0049982 | 122.69 |
| PotVar0050316 | 122.69 |
| PotVar0050601 | 122.69 |
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| PotVar0050824 | 122.69 |
| PotVar0050864 | 122.69 |
| solcap_snp_c2_9925 | 122.69 |
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| PotVar0060952 | 123.19 |
| PotVar0061206 | 124.3 |
| PotVar0050829 | 124.3 |
| PotVar0035136 | 124.3 |
| solcap_snp_c1_1645 | 124.51 |
| PotVar0061197 | 124.63 |
| PotVar0061119 | 124.63 |
| PotVar0061100 | 124.63 |
| PotVar0061268 | 124.63 |
| PotVar0050696 | 124.63 |
| solcap_snp_c2_4799 | 125.43 |
| solcap_snp_c2_4860 | 125.43 |
| solcap_snp_c1_1638 | 125.43 |
| PotVar0035248 | 127.96 |
| PotVar0061043 | 127.96 |
| solcap_snp_c2_9892 | 127.96 |
| PotVar0060753 | 127.96 |
| PotVar0060667 | 127.96 |
| PotVar0060678 | 127.96 |
| PotVar0035605 | 127.96 |
| PotVar0035780 | 127.96 |
| solcap_snp_c2_4896 | 127.96 |
| solcap_snp_c2_4910 | 127.96 |
| PotVar0035238 | 127.96 |
| solcap_snp_c2_4906 | 127.96 |
| PotVar0035451 | 127.96 |
| solcap_snp_c2_4709 | 127.96 |
| PotVar0035693 | 127.96 |
| solcap_snp_c2_4707 | 127.96 |
| PotVar0035883 | 127.96 |


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| solcap_snp_c2_34547 | 127.96 |
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| solcap_snp_c2_24 | 127.96 |
| PotVar0126918 | 127.96 |
| PotVar0126768 | 127.96 |
| PotVar0127072 | 127.96 |
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| solcap_snp_c2_14709 | 127.96 |
| solcap_snp_c2_14708 | 127.96 |
| solcap_snp_c2_14841 | 127.96 |
| solcap_snp_c2_37816 | 127.96 |
| PotVar0099836 | 127.96 |
| PotVar0122409 | 127.96 |
| PotVar0036058 | 127.96 |
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| solcap_snp_c1_1737 | 127.96 |
| solcap_snp_c2_4614 | 127.96 |
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| PotVar0060740 | 127.96 |
| PotVar0060676 | 127.96 |
| PotVar0035697 | 127.96 |
| solcap_snp_c2_36571 | 127.96 |
| PotVar0035595 | 127.96 |
| PotVar0126676 | 127.96 |
| PotVar0126593 | 127.96 |
| PotVar0036150 | 127.96 |
| PotVar0036238 | 127.96 |
| PotVar0126809 | 127.96 |
| PotVar0099900 | 127.96 |
| PotVar0061044 | 127.96 |
| solcap_snp_c1_15123 | 127.96 |
| PotVar0035546 | 127.96 |
| PotVar0035378 | 128.74 |
| solcap_snp_c2_30963 | 129.73 |
| PotVar0036191 | 129.75 |
| PotVar0036085 | 129.75 |


| solcap_snp_c2_735 | 0 |
| :--- | ---: |
| solcap_snp_c2_55863 | 1.11 |
| PotVar0075207 | 1.36 |


| PotVar0126645 | 130.23 |
| :---: | :---: |
| PotVar0126891 | 130.23 |
| PotVar0126574 | 130.23 |
| PotVar0126772 | 130.23 |
| PotVar0127026 | 130.46 |
| PotVar0035753 | 131.29 |
| PotVar0124628 | 131.56 |
| PotVar0035852 | 131.72 |
| PotVar0036149 | 133.4 |
| PotVar0126587 | 133.4 |
| PotVar0126685 | 133.6 |
| PotVar0099829 | 134.05 |
| PotVar0126769 | 134.29 |
| PotVar0036054 | 134.72 |
| PotVar0127038 | 134.72 |
| solcap_snp_c2_49917 | 136.9 |
| solcap_snp_c2_49911 | 136.9 |
| PotVar0124515 | 136.9 |
| PotVar0124464 | 136.9 |
| PotVar0124552 | 136.92 |
| solcap_snp_c2_49906 | 136.92 |
| PotVar0124463 | 136.92 |
| PotVar0099321 | 139.11 |
| PotVar0099426 | 139.11 |
| PotVar0099782 | 140.78 |
| PotVar0099756 | 140.78 |
| solcap_snp_c2_30961 | 141.7 |
| solcap_snp_c2_30958 | 141.7 |
| solcap_snp_c2_30956 | 141.7 |
| solcap_snp_c2_30955 | 141.7 |
| PotVar0122386 | 141.7 |
| PotVar0122388 | 141.7 |
| solcap_snp_c2_31041 | 141.7 |
| PotVar0122414 | 141.7 |
| PotVar0122353 | 141.7 |
| PotVar0122423 | 141.7 |
| PotVar0099652 | 141.7 |
| PotVar0099578 | 141.7 |
| solcap_snp_c1_9401 | 141.7 |


| solcap_snp_c2_730 | 1.8 |
| :--- | ---: |
| PotVar0109627 | 1.8 |
| PotVar0039162 | 2.94 |

Methods for mapping and linkage map integration in tetraploid potato

| PotVar0039524 | 2.94 |
| :---: | :---: |
| PotVar0039293 | 3.39 |
| PotVar0039273 | 3.39 |
| PotVar0039503 | 3.39 |
| solcap_snp_c2_4505 | 3.57 |
| PotVar0109716 | 3.57 |
| solcap_snp_c2_30952 | 3.6 |
| solcap_snp_c2_41879 | 3.6 |
| PotVar0032158 | 4.23 |
| PotVar0039416 | 4.23 |
| solcap_snp_c 1_15873 | 4.23 |
| solcap_snp_c2_17424 | 4.23 |
| solcap_snp_c2_30164 | 4.23 |
| solcap_snp_c2_785 | 4.23 |
| PotVar0032441 | 4.23 |
| PotVar0032521 | 4.23 |
| PotVar0039373 | 4.23 |
| PotVar0039384 | 4.23 |
| PotVar0054564 | 4.23 |
| PotVar0075203 | 4.23 |
| PotVar0099232 | 4.23 |
| solcap_snp_c1_4792 | 4.23 |
| solcap_snp_c2_17427 | 4.23 |
| PotVar0054547 | 4.23 |
| solcap_snp_c2_40336 | 4.67 |
| solcap_snp_c2_16347 | 5.39 |
| PotVar0038914 | 5.58 |
| PotVar0039112 | 5.58 |
| solcap_snp_c2_16362 | 6.48 |
| solcap_snp_c2_30926 | 7.36 |
| solcap_snp_c2_30914 | 7.36 |
| solcap_snp_c2_30929 | 7.36 |
| PotVar0054490 | 8.21 |
| PotVar0054559 | 8.21 |
| PotVar0054438 | 9 |
| PotVar0054546 | 9 |
| solcap_snp_c2_30915 | 9 |
| solcap_snp_c2_47096 | 9 |
| solcap_snp_c1_15973 | 9.87 |
| PotVar0039456 | 13.38 |
| PotVar0039219 | 13.38 |
| solcap_snp_c2_17415 | 13.38 |
| PotVar0039036 | 14.73 |
| PotVar0039005 | 17.17 |


| PotVar0039021 | 17.17 |
| :---: | :---: |
| solcap_snp_c1_11344 | 17.17 |
| solcap_snp_c2_32400 | 17.17 |
| solcap_snp_c2_32415 | 17.17 |
| PotVar0039004 | 17.17 |
| PotVar0039094 | 17.17 |
| PotVar0039050 | 17.6 |
| solcap_snp_c2_32425 | 18.14 |
| solcap_snp_c2_37248 | 18.57 |
| solcap_snp_c2_39705 | 18.57 |
| PotVar0029524 | 19.43 |
| solcap_snp_c2_32406 | 20.28 |
| solcap_snp_c2_52630 | 20.28 |
| PotVar0029505 | 21.18 |
| solcap_snp_c2_50889 | 21.41 |
| PotVar0117650 | 21.57 |
| solcap_snp_c2_21717 | 21.57 |
| PotVar0117640 | 21.57 |
| solcap_snp_c2_21721 | 21.57 |
| PotVar0029506 | 22.32 |
| PotVar0088857 | 22.49 |
| solcap_snp_c2_21746 | 23.18 |
| PotVar0089300 | 23.58 |
| PotVar0117601 | 24.04 |
| PotVar0029531 | 25.09 |
| PotVar0029568 | 25.95 |
| solcap_snp_c2_45323 | 25.97 |
| solcap_snp_c1_12305 | 25.97 |
| PotVar0089006 | 26.66 |
| solcap_snp_c1_12330 | 26.96 |
| solcap_snp_c2_41963 | 26.96 |
| PotVar0039003 | 28.08 |
| PotVar0062655 | 29.99 |
| PotVar0124338 | 30.79 |
| PotVar0124219 | 30.79 |
| solcap_snp_c2_45319 | 30.79 |
| PotVar0124142 | 30.79 |
| PotVar0124128 | 30.79 |
| PotVar0124165 | 30.79 |
| solcap_snp_c2_48239 | 30.86 |
| solcap_snp_c1_5091 | 30.86 |
| solcap_snp_c1_9363 | 31.57 |
| solcap_snp_c2_45311 | 31.57 |
| PotVar0062569 | 31.72 |


| PotVar0062136 | 32.17 |
| :---: | :---: |
| PotVar0062180 | 32.17 |
| PotVar0062276 | 32.17 |
| solcap_snp_c2_51113 | 32.17 |
| PotVar0062231 | 32.17 |
| PotVar0062385 | 32.17 |
| solcap_snp_c2_51115 | 32.17 |
| PotVar0117656 | 33.35 |
| PotVar0062628 | 34.78 |
| PotVar0088875 | 35.58 |
| solcap_snp_c2_48194 | 35.64 |
| PotVar0089071 | 36.23 |
| PotVar0062568 | 36.5 |
| PotVar0062484 | 36.94 |
| PotVar0062566 | 36.94 |
| PotVar0089083 | 37.32 |
| PotVar0062335 | 37.38 |
| PotVar0089235 | 37.54 |
| PotVar0089338 | 37.54 |
| PotVar0089350 | 37.54 |
| PotVar0062308 | 37.81 |
| PotVar0062079 | 37.81 |
| PotVar0062004 | 37.81 |
| PotVar0062472 | 37.81 |
| PotVar0062277 | 37.81 |
| PotVar0062114 | 37.81 |
| PotVar0062077 | 37.81 |
| PotVar0062142 | 37.81 |
| solcap_snp_c1_9356 | 37.98 |
| PotVar0082241 | 39.02 |
| PotVar0082281 | 39.02 |
| PotVar0094274 | 39.02 |
| PotVar0094547 | 39.02 |
| PotVar0082429 | 39.02 |
| PotVar0082458 | 39.02 |
| PotVar0094234 | 39.02 |
| PotVar0082531 | 39.02 |
| PotVar0094604 | 40.22 |
| PotVar0082552 | 40.44 |
| PotVar0082313 | 41.8 |
| PotVar0082438 | 41.8 |
| PotVar0125072 | 41.8 |
| solcap_snp_c2_45307 | 42.16 |
| PotVar0124264 | 42.16 |

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| solcap_snp_c1_12320 | 43.46 |
| :---: | :---: |
| solcap_snp_c1_12354 | 43.46 |
| PotVar0123873 | 43.46 |
| PotVar0123826 | 43.46 |
| solcap_snp_c2_42059 | 43.46 |
| solcap_snp_c1_11553 | 43.46 |
| PotVar0124100 | 43.46 |
| PotVar0038032 | 46.48 |
| PotVar0038002 | 46.48 |
| PotVar0082442 | 48.11 |
| PotVar0094414 | 48.32 |
| PotVar0094582 | 48.32 |
| PotVar0082550 | 48.32 |
| PotVar0094224 | 49.13 |
| PotVar0094537 | 49.13 |
| PotVar0094171 | 49.13 |
| PotVar0094115 | 49.14 |
| PotVar0094276 | 49.14 |
| PotVar0082332 | 49.14 |
| PotVar0094218 | 49.14 |
| PotVar0111837 | 49.25 |
| solcap_snp_c1_13233 | 49.25 |
| PotVar0082226 | 49.94 |
| PotVar0082166 | 49.94 |
| solcap_snp_c2_23192 | 50.38 |
| solcap_snp_c2_41495 | 50.69 |
| PotVar0094383 | 50.69 |
| PotVar0094361 | 51.11 |
| PotVar0131484 | 51.42 |
| solcap_snp_c2_51986 | 51.84 |
| PotVar0111702 | 52 |
| PotVar0111704 | 52 |
| solcap_snp_c1_13887 | 52 |
| PotVar0131512 | 52 |
| solcap_snp_c2_39175 | 52 |
| PotVar0038035 | 52.27 |
| PotVar0038033 | 52.27 |
| PotVar0094371 | 52.36 |
| PotVar0038345 | 56.12 |
| PotVar0038256 | 56.12 |
| solcap_snp_c2_44768 | 57.13 |
| PotVar0120925 | 57.13 |
| PotVar0120894 | 57.13 |
| PotVar0120885 | 57.13 |
| PotVar0038096 | 57.13 |


| PotVar0038136 | 57.13 |
| :---: | :---: |
| solcap_snp_c1_12257 | 57.13 |
| PotVar0120910 | 57.13 |
| solcap_snp_c1_12287 | 57.13 |
| PotVar0094229 | 57.13 |
| PotVar0038755 | 57.13 |
| PotVar0128369 | 57.13 |
| PotVar0045713 | 57.13 |
| solcap_snp_c2_17937 | 57.13 |
| solcap_snp_c2_17935 | 57.13 |
| solcap_snp_c2_17921 | 57.13 |
| PotVar0045967 | 57.13 |
| PotVar0131510 | 57.13 |
| PotVar0120737 | 57.13 |
| PotVar0037994 | 57.13 |
| solcap_snp_c2_33108 | 57.14 |
| solcap_snp_c1_4192 | 57.61 |
| PotVar0038674 | 57.79 |
| PotVar0119003 | 57.79 |
| PotVar0120697 | 57.82 |
| PotVar0038855 | 57.92 |
| PotVar0038592 | 57.92 |
| PotVar0038830 | 57.92 |
| PotVar0038662 | 57.92 |
| PotVar0038423 | 57.96 |
| PotVar0038425 | 57.96 |
| PotVar0038389 | 57.96 |
| PotVar0038395 | 58.4 |
| PotVar0038427 | 58.4 |
| PotVar0038759 | 58.4 |
| PotVar0038673 | 58.83 |
| PotVar0038624 | 58.83 |
| solcap_snp_c2_17914 | 59.59 |
| PotVar0046773 | 59.6 |
| solcap_snp_c1_12264 | 59.6 |
| PotVar0038876 | 59.69 |
| PotVar0038880 | 59.69 |
| PotVar0038859 | 59.69 |
| PotVar0128492 | 61.03 |
| PotVar0046016 | 61.39 |
| PotVar0128490 | 61.43 |
| solcap_snp_c2_40167 | 61.59 |
| PotVar0046427 | 62.3 |
| PotVar0046364 | 62.73 |
| PotVar0046249 | 62.94 |


| PotVar0046234 | 63.28 |
| :---: | :---: |
| PotVar0046114 | 63.28 |
| PotVar0046535 | 63.6 |
| PotVar0046724 | 63.6 |
| PotVar0046900 | 63.6 |
| PotVar0046141 | 63.61 |
| PotVar0045853 | 63.69 |
| PotVar0046115 | 63.69 |
| PotVar0045730 | 63.69 |
| PotVar0046193 | 63.69 |
| PotVar0046194 | 63.69 |
| PotVar0045695 | 63.69 |
| PotVar0046418 | 63.94 |
| PotVar0045784 | 63.95 |
| PotVar0045938 | 63.95 |
| PotVar0046722 | 64.03 |
| PotVar0046608 | 64.03 |
| PotVar0046903 | 64.03 |
| PotVar0046065 | 64.6 |
| PotVar0046178 | 64.6 |
| PotVar0046109 | 64.6 |
| solcap_snp_c2_17930 | 64.6 |
| PotVar0045735 | 64.6 |
| PotVar0046179 | 64.6 |
| PotVar0046292 | 64.6 |
| solcap_snp_c2_17809 | 64.63 |
| solcap_snp_c1_16172 | 64.82 |
| solcap_snp_c2_17858 | 64.82 |
| PotVar0046789 | 64.9 |
| PotVar0046968 | 64.9 |
| PotVar0047042 | 65.33 |
| PotVar0045734 | 65.56 |
| PotVar0045743 | 65.56 |
| solcap_snp_c2_17926 | 65.56 |
| PotVar0045952 | 65.56 |
| PotVar0045976 | 65.72 |
| PotVar0046782 | 65.97 |
| PotVar0047112 | 65.97 |
| PotVar0046549 | 65.97 |
| PotVar0046936 | 65.97 |
| PotVar0046605 | 65.97 |
| solcap_snp_c2_42265 | 66.2 |
| PotVar0046575 | 67.04 |
| PotVar0046916 | 67.04 |
| PotVar0046640 | 67.04 |

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| solcap_snp_c2_40635 | 67.86 |
| :---: | :---: |
| PotVar0046637 | 68.73 |
| PotVar0115838 | 69.24 |
| PotVar0046422 | 70.3 |
| PotVar0046462 | 70.3 |
| PotVar0046419 | 70.3 |
| PotVar0010943 | 70.4 |
| PotVar0115882 | 70.4 |
| PotVar0115831 | 70.41 |
| PotVar0047107 | 70.72 |
| PotVar0046902 | 70.72 |
| PotVar0047075 | 70.72 |
| PotVar0010676 | 70.84 |
| solcap_snp_c1_10494 | 70.84 |
| PotVar0115923 | 70.84 |
| solcap_snp_c1_12373 | 70.84 |
| solcap_snp_c2_42169 | 71.15 |
| PotVar0116077 | 71.95 |
| PotVar0119034 | 72.05 |
| solcap_snp_c1_10492 | 72.05 |
| PotVar0038744 | 72.62 |
| PotVar0118971 | 72.97 |
| PotVar0010377 | 73.59 |
| PotVar0128434 | 73.7 |
| PotVar0010082 | 74.21 |
| PotVar0128389 | 74.35 |
| PotVar0010835 | 74.67 |
| PotVar0010677 | 74.67 |
| PotVar0010948 | 74.67 |
| PotVar0010076 | 74.72 |
| solcap_snp_c2_25766 | 75.15 |
| PotVar0010550 | 75.15 |
| PotVar0010106 | 75.15 |
| PotVar0010664 | 75.66 |
| solcap_snp_c2_42132 | 75.66 |
| PotVar0119004 | 75.66 |
| PotVar0010618 | 75.66 |
| PotVar0010869 | 75.66 |
| PotVar0010684 | 75.66 |
| PotVar0010629 | 75.66 |
| PotVar0010133 | 75.66 |
| solcap_snp_c1_15481 | 75.66 |
| PotVar0010851 | 75.66 |
| PotVar0010535 | 75.66 |


| solcap_snp_c2_53034 | 75.66 |
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| PotVar0010668 | 75.66 |
| PotVar0045674 | 75.89 |
| PotVar0115971 | 76.1 |
| PotVar0115988 | 76.1 |
| PotVar0119013 | 76.1 |
| solcap_snp_c2_53033 | 76.1 |
| solcap_snp_c2_17925 | 76.1 |
| solcap_snp_c1_10493 | 76.1 |
| PotVar0118945 | 76.1 |
| PotVar0119053 | 76.1 |
| PotVar0119058 | 76.1 |
| PotVar0010928 | 76.1 |
| PotVar0010874 | 76.1 |
| PotVar0010934 | 76.1 |
| PotVar0010735 | 76.1 |
| PotVar0010547 | 76.1 |
| PotVar0010400 | 76.1 |
| PotVar0010195 | 76.1 |
| PotVar0010303 | 76.1 |
| PotVar0010331 | 76.1 |
| PotVar0010351 | 76.1 |
| PotVar0010350 | 76.1 |
| PotVar0010145 | 76.1 |
| PotVar0010080 | 76.1 |
| PotVar0010072 | 76.1 |
| PotVar0009928 | 76.1 |
| PotVar0009943 | 76.1 |
| PotVar0009802 | 76.1 |
| PotVar0009955 | 76.1 |
| PotVar0009408 | 76.1 |
| PotVar0009568 | 76.1 |
| PotVar0009279 | 76.1 |
| PotVar0009159 | 76.1 |
| solcap_snp_c1_7957 | 76.1 |
| PotVar0090166 | 76.1 |
| solcap_snp_c2_7559 | 76.1 |
| PotVar0010183 | 76.25 |
| PotVar0010353 | 76.47 |
| PotVar0010345 | 76.47 |
| solcap_snp_c2_42133 | 76.47 |
| PotVar0010270 | 76.47 |
| PotVar0010926 | 76.48 |
| PotVar0115953 | 76.49 |


| PotVar0115816 | 76.49 |
| :---: | :---: |
| PotVar0010703 | 76.49 |
| solcap_snp_c2_40610 | 76.49 |
| PotVar0010678 | 76.49 |
| PotVar0010401 | 77.67 |
| PotVar0010077 | 78.43 |
| PotVar0010033 | 79.55 |
| D_locus_(DFR)_A_LG02 | 80.43 |
| D_locus_(DFR)_C_LG02 | 80.43 |
| D_locus_(DFR)_E_LG02 | 80.43 |
| D_locus_(DFR)_G_LG02 | 80.43 |
| D_locus_(DFR)_H_LG02 | 80.43 |
| PotVar0009951 | 80.43 |
| PotVar0009747 | 80.43 |
| solcap_snp_c1_7964 | 80.43 |
| PotVar0009505 | 80.43 |
| PotVar0009466 | 80.43 |
| PotVar0009844 | 80.43 |
| PotVar0009827 | 80.43 |
| PotVar0009483 | 80.43 |
| D_locus_(DFR)_D_LG02 | 80.43 |
| solcap_snp_c2_25044 | 80.86 |
| PotVar0010007 | 80.86 |
| PotVar0010024 | 81.38 |
| PotVar0009282 | 82.17 |
| PotVar0009178 | 82.17 |
| PotVar0009171 | 82.17 |
| PotVar0090084 | 82.79 |
| PotVar0090045 | 82.79 |
| PotVar0090077 | 82.79 |
| solcap_snp_c1_7342 | 82.92 |
| solcap_snp_c2_22894 | 82.92 |
| solcap_snp_c1_7341 | 82.92 |
| PotVar0010500 | 82.94 |
| PotVar0009548 | 82.94 |
| PotVar0009474 | 82.94 |
| PotVar0009867 | 82.94 |
| PotVar0009567 | 82.94 |
| PotVar0009857 | 82.94 |
| PotVar0090139 | 82.94 |
| PotVar0009673 | 83.18 |
| PotVar0009808 | 83.18 |
| PotVar0009651 | 83.18 |
| PotVar0009460 | 83.63 |

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| PotVar0009411 | 83.63 |
| :---: | :---: |
| PotVar0089984 | 83.65 |
| solcap_snp_c1_2656 | 83.65 |
| solcap_snp_c2_7631 | 83.94 |
| solcap_snp_c1_15746 | 84.52 |
| PotVar0118927 | 85.39 |
| solcap_snp_c2_7423 | 86.17 |
| solcap_snp_c2_7424 | 86.17 |
| solcap_snp_c2_7501 | 86.26 |
| PotVar0006700 | 86.56 |
| PotVar0006735 | 86.56 |
| PotVar0090074 | 87.09 |
| solcap_snp_c1_2641 | 87.09 |
| solcap_snp_c1_16540 | 87.09 |
| PotVar0118925 | 87.42 |
| solcap_snp_c2_7422 | 87.5 |
| PotVar0006761 | 87.5 |
| PotVar0089995 | 88.41 |
| PotVar0006851 | 88.71 |
| PotVar0006826 | 88.71 |
| solcap_snp_c1_2574 | 88.86 |
| PotVar0006863 | 89.47 |
| PotVar0006684 | 89.47 |
| PotVar0006870 | 90.69 |
| PotVar0006747 | 90.69 |
| solcap_snp_c1_16542 | 90.86 |
| PotVar0006913 | 91.57 |
| PotVar0006934 | 91.57 |
| PotVar0007012 | 92.45 |
| PotVar0007054 | 92.45 |
| PotVar0007051 | 92.45 |
| PotVar0007146 | 92.8 |
| PotVar0007182 | 92.8 |
| PotVar0007178 | 92.88 |
| PotVar0001581 | 93.2 |
| PotVar0001799 | 94.34 |
| PotVar0006916 | 94.69 |
| PotVar0006948 | 94.69 |
| PotVar0001571 | 94.69 |
| PotVar0006681 | 94.69 |
| PotVar0006947 | 96.25 |
| PotVar0006881 | 96.33 |
| PotVar0007040 | 97.63 |
| PotVar0003459 | 97.99 |
| PotVar0003645 | 97.99 |


| solcap_snp_c2_43350 | 99.71 |
| :---: | :---: |
| PotVar0001550 | 99.92 |
| PotVar0001625 | 99.92 |
| solcap_snp_c2_27268 | 99.92 |
| solcap_snp_c2_27372 | 99.92 |
| PotVar0001686 | 99.92 |
| solcap_snp_c2_43408 | 99.92 |
| solcap_snp_c1_4860 | 99.92 |
| PotVar0002114 | 99.92 |
| PotVar0002440 | 99.92 |
| PotVar0002607 | 99.92 |
| PotVar0002530 | 99.92 |
| PotVar0002800 | 99.92 |
| solcap_snp_c1_10593 | 99.92 |
| PotVar0001694 | 99.92 |
| PotVar0001573 | 99.92 |
| solcap_snp_c1_12771 | 99.93 |
| PotVar0002139 | 100.04 |
| solcap_snp_c1_5931 | 100.23 |
| PotVar0003452 | 100.23 |
| PotVar0001749 | 100.36 |
| PotVar0001789 | 100.36 |
| PotVar0001921 | 100.36 |
| solcap_snp_c1_12509 | 100.36 |
| solcap_snp_c2_42570 | 100.36 |
| PotVar0001704 | 100.36 |
| PotVar0006989 | 100.36 |
| PotVar0002132 | 102.08 |
| PotVar0002188 | 102.08 |
| PotVar0002196 | 102.08 |
| solcap_snp_c1_7871 | 102.08 |
| solcap_snp_c2_15066 | 102.08 |
| solcap_snp_c2_15067 | 102.08 |
| PotVar0002627 | 102.47 |
| PotVar0002507 | 102.47 |
| PotVar0002438 | 102.56 |
| PotVar0002461 | 102.56 |
| PotVar0002481 | 102.56 |
| solcap_snp_c2_24869 | 102.56 |
| PotVar0002433 | 102.56 |
| PotVar0002715 | 103 |
| PotVar0002556 | 103 |
| PotVar0002594 | 103 |
| PotVar0002504 | 103 |
| PotVar0002736 | 103.8 |


| PotVar0002934 | 104.24 |
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| PotVar0002940 | 104.24 |
| PotVar0002954 | 104.24 |
| PotVar0003017 | 104.24 |
| PotVar0003379 | 104.67 |
| PotVar0003253 | 105.1 |
| solcap_snp_c2_47199 | 105.53 |
| solcap_snp_c2_47200 | 105.85 |
| PotVar0003529 | 105.95 |
| PotVar0003444 | 106.47 |
| PotVar0003791 | 106.47 |
| PotVar0003792 | 106.47 |
| PotVar0003627 | 106.47 |
| PotVar0002770 | 107.07 |
| PotVar0002772 | 107.07 |
| PotVar0002892 | 107.51 |
| solcap_snp_c2_47196 | 107.51 |
| solcap_snp_c2_47201 | 107.51 |
| solcap_snp_c2_47163 | 107.51 |
| solcap_snp_c1_11459 | 107.95 |
| PotVar0002976 | 107.95 |
| PotVar0002948 | 107.95 |
| PotVar0003078 | 107.95 |
| PotVar0003105 | 107.95 |
| PotVar0003151 | 107.95 |
| PotVar0003427 | 107.95 |
| PotVar0003313 | 107.95 |
| PotVar0003054 | 107.95 |
| solcap_snp_c1_5908 | 107.95 |
| solcap_snp_c2_35689 | 107.95 |
| solcap_snp_c2_35693 | 107.95 |
| solcap_snp_c2_35694 | 107.95 |
| PotVar0002935 | 107.95 |
| PotVar0003004 | 107.95 |
| PotVar0003084 | 107.95 |
| PotVar0003442 | 107.95 |
| PotVar0003462 | 107.95 |
| PotVar0003546 | 107.95 |
| solcap_snp_c1_5909 | 107.95 |
| solcap_snp_c1_5924 | 107.95 |
| solcap_snp_c2_35691 | 107.95 |
| solcap_snp_c2_35695 | 107.95 |
| solcap_snp_c2_35698 | 107.95 |
| solcap_snp_c2_35701 | 107.95 |
| solcap_snp_c2_35702 | 107.95 |

Methods for mapping and linkage map integration in tetraploid potato

| PotVar0003761 | 107.95 |
| :--- | :--- |


| solcap_snp_c2_15047 | 108.06 |
| :--- | :--- |


| PotVar0002908 | 118.9 |
| :--- | :--- |


| Chromosome 3 |  |
| :---: | :---: |
| Name | cM |
| PotVar0084575 | 0 |
| PotVar0084566 | 0 |
| solcap_snp_c1_12825 | 0 |
| solcap_snp_c2_52806 | 0 |
| solcap_snp_c2_52813 | 0 |
| PotVar0084741 | 0 |
| solcap_snp_c2_54290 | 0.05 |
| solcap_snp_c2_54286 | 0.05 |
| PotVar0019336 | 2.23 |
| PotVar0019456 | 4.71 |
| PotVar0019201 | 4.71 |
| PotVar0084666 | 4.85 |
| PotVar0084730 | 4.85 |
| PotVar0084556 | 5.28 |
| PotVar0084554 | 5.38 |
| solcap_snp_c2_52815 | 6.52 |
| solcap_snp_c1_15782 | 6.52 |
| solcap_snp_c2_51389 | 6.52 |
| PotVar0019302 | 8.35 |
| PotVar0019259 | 9.19 |
| solcap_snp_c2_17279 | 10.5 |
| PotVar0019680 | 10.7 |
| solcap_snp_c1_13059 | 11.59 |
| PotVar0019460 | 12.78 |
| PotVar0021474 | 14.33 |
| solcap_snp_c1_1914 | 14.33 |
| solcap_snp_c2_5269 | 14.33 |
| PotVar0055456 | 14.33 |
| solcap_snp_c1_8969 | 14.33 |
| solcap_snp_c2_29441 | 14.33 |
| solcap_snp_c2_5289 | 14.33 |
| solcap_snp_c2_5292 | 14.33 |
| solcap_snp_c2_57638 | 14.33 |
| PotVar0021479 | 14.33 |
| PotVar0019554 | 15.05 |
| solcap_snp_c1_13052 | 15.05 |
| PotVar0021288 | 15.23 |
| solcap_snp_c1_7144 | 15.23 |
| solcap_snp_c2_14424 | 15.23 |


| solcap_snp_c2_5736 | 15.23 |
| :---: | :---: |
| PotVar0085038 | 16.22 |
| PotVar0106434 | 16.22 |
| PotVar0106457 | 16.22 |
| PotVar0121921 | 16.22 |
| PotVar0121932 | 16.22 |
| PotVar0132195 | 16.22 |
| PotVar0132206 | 16.22 |
| solcap_snp_c1_3347 | 16.22 |
| solcap_snp_c2_10088 | 16.22 |
| solcap_snp_c2_11269 | 16.22 |
| solcap_snp_c2_35563 | 16.22 |
| solcap_snp_c2_37411 | 16.22 |
| PotVar0085563 | 16.22 |
| PotVar0085679 | 16.22 |
| PotVar0106337 | 16.22 |
| PotVar0106377 | 16.22 |
| solcap_snp_c 1_16052 | 16.22 |
| solcap_snp_c1_16382 | 16.22 |
| solcap_snp_c2_37431 | 16.22 |
| solcap_snp_c2_41163 | 16.22 |
| solcap_snp_c2_41178 | 16.22 |
| solcap_snp_c2_10087 | 16.22 |
| solcap_snp_c2_50636 | 17.75 |
| solcap_snp_c2_50635 | 17.75 |
| solcap_snp_c2_54530 | 17.75 |
| solcap_snp_c2_53606 | 17.97 |
| PotVar0021457 | 19.74 |
| PotVar0121927 | 21.08 |
| PotVar0113278 | 21.11 |
| PotVar0021445 | 21.53 |
| solcap_snp_c1_12751 | 21.98 |
| PotVar0085575 | 21.98 |
| PotVar0085799 | 21.98 |
| PotVar0131468 | 21.98 |
| PotVar0094670 | 21.98 |
| solcap_snp_c2_43182 | 21.98 |
| PotVar0094679 | 21.98 |
| PotVar0129473 | 22.48 |
| PotVar0129536 | 22.48 |
| solcap_snp_c2_5286 | 23.75 |


| solcap_snp_c2_54674 | 24.22 |
| :---: | :---: |
| solcap_snp_c2_5300 | 24.44 |
| solcap_snp_c1_1918 | 24.87 |
| solcap_snp_c2_5226 | 24.87 |
| solcap_snp_c1_15204 | 27.22 |
| solcap_snp_c2_5732 | 27.22 |
| solcap_snp_c1_3662 | 27.63 |
| PotVar0026680 | 27.63 |
| PotVar0106352 | 28.59 |
| PotVar0094787 | 28.64 |
| PotVar0085747 | 29.52 |
| PotVar0094713 | 29.52 |
| PotVar0085802 | 29.52 |
| PotVar0085581 | 29.72 |
| solcap_snp_c2_35553 | 29.88 |
| PotVar0131462 | 30.18 |
| solcap_snp_c2_35354 | 30.18 |
| PotVar0094922 | 30.39 |
| solcap_snp_c1_9292 | 30.81 |
| PotVar0085797 | 31.03 |
| PotVar0085748 | 31.03 |
| PotVar0094840 | 31.54 |
| PotVar0094886 | 32.55 |
| PotVar0094925 | 32.55 |
| solcap_snp_c2_30730 | 32.55 |
| PotVar0094857 | 32.55 |
| solcap_snp_c1_9268 | 32.59 |
| PotVar0095450 | 33.25 |
| solcap_snp_c2_36469 | 33.52 |
| PotVar0095271 | 33.52 |
| solcap_snp_c2_49970 | 33.52 |
| solcap_snp_c2_48378 | 33.59 |
| PotVar0129579 | 33.59 |
| solcap_snp_c2_52495 | 35.1 |
| solcap_snp_c1_4814 | 35.1 |
| PotVar0095473 | 35.1 |
| solcap_snp_c1_7139 | 35.1 |
| PotVar0129442 | 35.1 |
| PotVar0129720 | 35.1 |
| solcap_snp_c2_48362 | 35.1 |
| solcap_snp_c2_48363 | 35.1 |

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| solcap_snp_c2_48381 | 35.1 |
| :---: | :---: |
| PotVar0095451 | 35.1 |
| solcap_snp_c2_38068 | 35.1 |
| solcap_snp_c2_48390 | 35.1 |
| solcap_snp_c1_14316 | 35.1 |
| PotVar0129474 | 35.1 |
| PotVar0129705 | 35.1 |
| solcap_snp_c1_11350 | 35.1 |
| solcap_snp_c2_48368 | 35.1 |
| solcap_snp_c1_16679 | 35.65 |
| solcap_snp_c2_37989 | 35.65 |
| PotVar0095322 | 36.34 |
| solcap_snp_c2_49976 | 36.78 |
| solcap_snp_c2_55729 | 36.78 |
| solcap_snp_c2_48359 | 37.3 |
| PotVar0129499 | 37.61 |
| PotVar0068140 | 39.7 |
| PotVar0068122 | 39.7 |
| PotVar0068152 | 39.7 |
| PotVar0115488 | 39.82 |
| PotVar0115519 | 39.82 |
| PotVar0115783 | 39.82 |
| solcap_snp_c2_42312 | 39.82 |
| PotVar0115449 | 39.82 |
| solcap_snp_c2_38047 | 40.37 |
| PotVar0068173 | 40.64 |
| PotVar0115703 | 41.28 |
| PotVar0115750 | 41.28 |
| PotVar0115775 | 41.28 |
| PotVar0115570 | 41.28 |
| PotVar0068141 | 41.72 |
| solcap_snp_c2_46592 | 41.78 |
| solcap_snp_c1_7882 | 41.99 |
| solcap_snp_c2_24983 | 41.99 |
| solcap_snp_c2_45699 | 42 |
| PotVar0068033 | 43.25 |
| solcap_snp_c2_46605 | 44.46 |
| PotVar0067935 | 44.59 |
| PotVar0113388 | 46.63 |
| PotVar0068174 | 46.82 |
| solcap_snp_c2_42306 | 47.28 |
| solcap_snp_c2_57349 | 48.19 |
| PotVar0068133 | 48.5 |
| PotVar0070260 | 48.82 |
| PotVar0055399 | 48.82 |


| PotVar0120627 | 48.82 |
| :---: | :---: |
| PotVar0129496 | 49.95 |
| solcap_snp_c2_48385 | 49.95 |
| solcap_snp_c1_13847 | 50.98 |
| PotVar0056918 | 51.16 |
| PotVar0068149 | 51.47 |
| PotVar0068134 | 51.9 |
| PotVar0042853 | 52.27 |
| PotVar0042845 | 52.27 |
| solcap_snp_c2_13825 | 52.51 |
| PotVar0113509 | 53.12 |
| PotVar0055361 | 53.31 |
| solcap_snp_c2_55465 | 54.04 |
| solcap_snp_c1_9161 | 54.04 |
| solcap_snp_c2_46603 | 54.04 |
| PotVar0070258 | 55.42 |
| PotVar0070245 | 55.42 |
| PotVar0070248 | 55.42 |
| PotVar0043163 | 57.09 |
| solcap_snp_c1_6869 | 59.66 |
| PotVar0070335 | 59.7 |
| PotVar0055353 | 60.94 |
| PotVar0055210 | 60.94 |
| PotVar0055234 | 60.94 |
| PotVar0055248 | 60.94 |
| PotVar0055339 | 60.94 |
| PotVar0055105 | 60.94 |
| PotVar0055756 | 61.85 |
| solcap_snp_c1_6864 | 62.27 |
| PotVar0055556 | 62.28 |
| PotVar0055722 | 62.28 |
| solcap_snp_c2_1567 | 64.39 |
| PotVar0056354 | 64.69 |
| PotVar0070281 | 66.7 |
| PotVar0113506 | 66.85 |
| PotVar0113511 | 66.85 |
| PotVar0113398 | 66.85 |
| PotVar0070299 | 66.85 |
| solcap_snp_c2_20347 | 66.85 |
| PotVar0056884 | 67.09 |
| PotVar0121873 | 68.09 |
| PotVar0120554 | 68.09 |
| PotVar0120452 | 68.09 |
| PotVar0043186 | 68.09 |
| solcap_snp_c2_57865 | 68.09 |


| solcap_snp_c2_17552 | 68.09 |
| :---: | :---: |
| PotVar0043196 | 68.09 |
| solcap_snp_c2_25560 | 69.05 |
| PotVar0055403 | 69.48 |
| solcap_snp_c2_14017 | 69.51 |
| PotVar0027434 | 69.51 |
| PotVar0113472 | 69.9 |
| solcap_snp_c2_55276 | 69.92 |
| PotVar0055120 | 70.35 |
| PotVar0070334 | 71.12 |
| solcap_snp_c1_6332 | 71.12 |
| solcap_snp_c2_54785 | 71.21 |
| PotVar0043187 | 71.21 |
| PotVar0055394 | 71.21 |
| solcap_snp_c1_8069 | 71.21 |
| solcap_snp_c2_55279 | 71.21 |
| solcap_snp_c2_55284 | 71.21 |
| solcap_snp_c2_55285 | 71.21 |
| PotVar0042968 | 71.21 |
| PotVar0042948 | 71.21 |
| solcap_snp_c1_9025 | 71.21 |
| PotVar0043256 | 71.21 |
| solcap_snp_c2_29678 | 71.21 |
| PotVar0043210 | 71.21 |
| PotVar0056507 | 72.08 |
| PotVar0056231 | 72.08 |
| solcap_snp_c2_55283 | 72.09 |
| PotVar0055003 | 72.09 |
| PotVar0055362 | 72.09 |
| PotVar0054961 | 72.09 |
| PotVar0042852 | 72.09 |
| PotVar0055831 | 72.5 |
| PotVar0042846 | 72.52 |
| PotVar0054986 | 72.52 |
| PotVar0055130 | 72.52 |
| solcap_snp_c2_57860 | 72.52 |
| PotVar0055205 | 72.52 |
| PotVar0056253 | 72.69 |
| solcap_snp_c2_1579 | 72.69 |
| solcap_snp_c1_3637 | 72.95 |
| PotVar0042829 | 72.95 |
| PotVar0043145 | 72.96 |
| PotVar0043197 | 72.96 |
| PotVar0043007 | 72.96 |
| solcap_snp_c1_3638 | 73.4 |

Methods for mapping and linkage map integration in tetraploid potato

| PotVar0042906 | 73.4 |
| :---: | :---: |
| PotVar0043199 | 73.4 |
| PotVar0043211 | 73.4 |
| PotVar0030088 | 73.6 |
| PotVar0120608 | 74.26 |
| PotVar0120301 | 74.26 |
| PotVar0120444 | 74.26 |
| PotVar0120279 | 74.26 |
| PotVar0120480 | 74.26 |
| PotVar0121744 | 74.26 |
| PotVar0120489 | 74.26 |
| PotVar0055916 | 74.26 |
| solcap_snp_c2_1722 | 74.26 |
| PotVar0120478 | 74.26 |
| PotVar0120613 | 74.26 |
| PotVar0120283 | 74.26 |
| PotVar0121756 | 74.26 |
| PotVar0121761 | 74.26 |
| PotVar0121805 | 74.26 |
| solcap_snp_c2_20176 | 74.26 |
| PotVar0043245 | 74.26 |
| PotVar0120252 | 74.26 |
| PotVar0120600 | 74.26 |
| solcap_snp_c2_55072 | 74.26 |
| PotVar0120595 | 74.26 |
| PotVar0120488 | 74.26 |
| PotVar0055692 | 74.69 |
| PotVar0056242 | 76.31 |
| PotVar0120531 | 76.31 |
| PotVar0120487 | 76.31 |
| PotVar0120416 | 76.31 |
| PotVar0120323 | 76.31 |
| PotVar0121869 | 76.31 |
| solcap_snp_c2_20113 | 76.31 |
| solcap_snp_c2_20097 | 76.31 |
| PotVar0120242 | 76.31 |
| PotVar0120555 | 76.31 |
| solcap_snp_c2_20175 | 76.74 |
| solcap_snp_c2_1688 | 76.84 |
| PotVar0056881 | 77.03 |
| PotVar0121803 | 77.03 |
| PotVar0070435 | 77.16 |
| PotVar0056835 | 77.16 |
| PotVar0055694 | 77.17 |


| PotVar0056297 | 77.59 |
| :---: | :---: |
| solcap_snp_c2_1556 | 77.59 |
| PotVar0056380 | 77.59 |
| PotVar0056911 | 77.93 |
| PotVar0070449 | 77.93 |
| PotVar0070532 | 77.93 |
| PotVar0056921 | 77.93 |
| PotVar0056200 | 79.17 |
| PotVar0056554 | 79.17 |
| PotVar0056273 | 79.17 |
| PotVar0056042 | 79.39 |
| PotVar0056453 | 79.39 |
| solcap_snp_c2_20259 | 79.46 |
| PotVar0056506 | 79.85 |
| PotVar0056116 | 79.85 |
| PotVar0056464 | 79.85 |
| PotVar0014120 | 79.88 |
| PotVar0027609 | 80.5 |
| solcap_snp_c1_7096 | 80.5 |
| PotVar0029778 | 80.5 |
| PotVar0029786 | 80.5 |
| PotVar0029784 | 80.5 |
| PotVar0029844 | 80.5 |
| PotVar0055583 | 81.23 |
| solcap_snp_c2_18268 | 82.01 |
| PotVar0030288 | 82.01 |
| PotVar0055978 | 82.32 |
| PotVar0055885 | 82.32 |
| PotVar0055804 | 82.32 |
| PotVar0055999 | 82.32 |
| PotVar0055755 | 82.32 |
| PotVar0056019 | 82.32 |
| solcap_snp_c2_1720 | 82.32 |
| solcap_snp_c2_1718 | 83.28 |
| solcap_snp_c1_7112 | 84.5 |
| PotVar0029965 | 84.5 |
| solcap_snp_c 1_4509 | 85.19 |
| solcap_snp_c2_22466 | 86.65 |
| PotVar0122174 | 87.73 |
| solcap_snp_c2_1724 | 88.68 |
| solcap_snp_c2_17631 | 88.68 |
| PotVar0020948 | 88.68 |
| solcap_snp_c2_14064 | 88.68 |
| solcap_snp_c1_4542 | 88.68 |


| PotVar0055603 | 88.68 |
| :---: | :---: |
| solcap_snp_c2_1725 | 88.68 |
| PotVar0055568 | 88.68 |
| PotVar0030875 | 88.89 |
| PotVar0121169 | 89 |
| solcap_snp_c2_14155 | 89.47 |
| solcap_snp_c2_57263 | 89.56 |
| PotVar0027485 | 89.56 |
| PotVar0121351 | 89.63 |
| PotVar0013242 | 89.63 |
| solcap_snp_c1_16234 | 90 |
| PotVar0029733 | 90.43 |
| PotVar0029816 | 90.43 |
| PotVar0029766 | 90.43 |
| PotVar0030743 | 91.07 |
| PotVar0021019 | 91.16 |
| PotVar0020971 | 91.59 |
| PotVar0030033 | 91.76 |
| PotVar0029865 | 91.76 |
| PotVar0030066 | 91.76 |
| solcap_snp_c1_7115 | 91.76 |
| PotVar0029968 | 91.76 |
| PotVar0030874 | 91.88 |
| PotVar0030504 | 92.64 |
| PotVar0030330 | 92.64 |
| PotVar0030456 | 93.22 |
| solcap_snp_c1_5951 | 93.22 |
| solcap_snp_c2_18308 | 93.22 |
| PotVar0121328 | 93.51 |
| PotVar0121124 | 93.51 |
| PotVar0013238 | 93.96 |
| PotVar0013245 | 93.96 |
| PotVar0030909 | 93.96 |
| PotVar0121530 | 93.96 |
| solcap_snp_c1_8203 | 93.96 |
| PotVar0121399 | 93.96 |
| solcap_snp_c1_8194 | 93.96 |
| solcap_snp_c2_18428 | 93.96 |
| PotVar0121402 | 93.96 |
| PotVar0014009 | 94.18 |
| PotVar0013943 | 94.18 |
| PotVar0121139 | 94.96 |
| solcap_snp_c1_111 | 95.51 |
| PotVar0013322 | 96.26 |

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| PotVar0030768 | 96.53 |
| :--- | ---: |
| PotVar0121290 | 98.49 |
| PotVar0013592 | 98.49 |
| PotVar0013766 | 98.49 |
| PotVar0013866 | 98.49 |
| PotVar0013867 | 98.49 |
| PotVar0013496 | 98.55 |
| PotVar0013434 | 98.76 |
| PotVar0013544 | 98.76 |
| PotVar0013533 | 98.76 |
| PotVar0013345 | 98.76 |
| PotVar0013816 | 98.76 |
| PotVar0014106 | 98.76 |
| solcap_snp_c2_26402 | 98.76 |
| PotVar0014097 | 98.76 |
| PotVar0014107 | 98.76 |
| PotVar0013845 | 98.76 |
| PotVar0014087 | 98.76 |
| PotVar0014196 | 98.76 |
| PotVar0014192 | 98.76 |
| PotVar0021255 | 100.74 |
| PotVar0021251 | 100.74 |
| PotVar0021083 | 100.74 |
| PotVar0020884 |  |
|  |  |


| Chromosome 4 |  |
| :--- | ---: |
| Name | cM |
| solcap_snp_c1_11030 | 0 |
| solcap_snp_c2_36955 | 0 |
| solcap_snp_c2_36993 | 0.67 |
| PotVar0026619 | 2.44 |
| solcap_snp_c2_36951 | 6.23 |
| solcap_snp_c2_23611 | 6.48 |
| solcap_snp_c1_7570 | 6.48 |
| solcap_snp_c1_7571 | 6.48 |
| solcap_snp_c2_54463 | 10.97 |
| solcap_snp_c2_29872 | 10.99 |
| PotVar0076761 | 10.99 |
| PotVar0076759 | 10.99 |
| PotVar0076872 | 10.99 |
| solcap_snp_c2_36941 | 14.95 |
| solcap_snp_c2_23596 | 15 |
| solcap_snp_c1_7574 | 18.15 |
| solcap_snp_c2_31719 | 21.4 |


| PotVar0014217 | 100.74 |
| :--- | ---: |
| solcap_snp_c2_578 | 100.74 |
| PotVar0014025 | 100.93 |
| PotVar0013510 | 101.37 |
| solcap_snp_c2_326 | 101.37 |
| PotVar0013907 | 101.84 |
| PotVar0021209 | 102.7 |
| PotVar0021026 | 108.7 |
| PotVar0021098 | 108.7 |
| PotVar0021166 | 108.7 |
| PotVar0021182 | 109.59 |
| PotVar0020803 | 110.42 |
| PotVar0020656 | 110.85 |
| PotVar0020782 | 111.92 |
| PotVar0020802 | 111.96 |
| PotVar0020426 | 112.39 |
| PotVar0020507 | 113.24 |
| PotVar0020213 | 113.34 |
| PotVar0021136 | 114.48 |
| PotVar0019945 | 114.48 |
| PotVar0019908 | 114.48 |
| PotVar0019861 |  |
| PotVar0019800 | 14.48 |
| solcap_snp_c2_37121 |  |
|  | 103 |


| PotVar0106844 | 21.4 |
| :--- | ---: |
| solcap_snp_c1_7569 | 27.51 |
| solcap_snp_c2_39322 | 27.63 |
| solcap_snp_c2_29850 | 28.49 |
| solcap_snp_c2_29851 | 28.49 |
| PotVar0076654 | 28.92 |
| solcap_snp_c1_13626 | 29.35 |
| PotVar0076557 | 29.35 |
| PotVar0076616 | 29.35 |
| solcap_snp_c2_31688 | 29.35 |
| solcap_snp_c2_21915 | 29.35 |
| R2_E_LG04 | 29.35 |
| solcap_snp_c2_11564 | 29.35 |
| solcap_snp_c2_48871 | 29.35 |
| PotVar0039597 | 29.35 |
| PotVar0076646 | 29.35 |
| PotVar0106655 | 30.21 |
| PotVar0106745 | 30.21 |
| PotVar0076666 | 30.45 |


| PotVar0020074 | 114.73 |
| :--- | :---: |
| solcap_snp_c2_37139 | 114.95 |
| PotVar0020457 | 114.95 |
| PotVar0020402 | 114.95 |
| PotVar0021131 | 121.05 |
| PotVar0020249 | 123.73 |
| PotVar0020227 | 123.73 |
| PotVar0020451 | 123.73 |
| PotVar0020808 | 123.82 |
| PotVar0020653 | 123.82 |
| PotVar0020171 | 124.17 |
| PotVar0020716 | 124.25 |
| solcap_snp_c2_9531 | 124.25 |
| PotVar0020079 | 125.04 |
| PotVar0019703 | 125.48 |
| PotVar0019900 | 125.48 |
| PotVar0019827 | 125.48 |
| PotVar0019773 | 125.48 |
| PotVar0020037 | 125.48 |
| PotVar0020552 | 125.57 |
| PotVar0020485 | 125.57 |
| PotVar0020566 | 125.57 |
| PotVar0020413 |  |


| PotVar0076621 | 30.45 |
| :--- | ---: |
| PotVar0106922 | 30.66 |
| solcap_snp_c1_9546 | 30.66 |
| PotVar0106917 | 30.66 |
| PotVar0106871 | 30.66 |
| solcap_snp_c2_31732 | 30.66 |
| PotVar0106851 | 30.66 |
| PotVar0127847 | 30.66 |
| solcap_snp_c2_11432 | 30.66 |
| solcap_snp_c2_11435 | 30.66 |
| PotVar0076873 | 30.66 |
| PotVar0076511 | 31.03 |
| PotVar0076503 | 31.25 |
| PotVar0106843 | 31.68 |
| PotVar0100848 | 31.87 |
| PotVar0101108 | 31.87 |
| PotVar0076554 | 31.87 |
| PotVar0100790 | 31.87 |
| PotVar0101074 | 31.87 |

Methods for mapping and linkage map integration in tetraploid potato

| PotVar0106727 | 31.87 |
| :---: | :---: |
| PotVar0106974 | 31.87 |
| R2_D_LG04 | 31.87 |
| PotVar0100916 | 31.87 |
| PotVar0076901 | 31.91 |
| PotVar0109580 | 32.23 |
| PotVar0109408 | 32.31 |
| PotVar0109406 | 32.31 |
| PotVar0100767 | 33 |
| PotVar0127735 | 33.17 |
| PotVar0127894 | 33.21 |
| PotVar0100919 | 33.21 |
| solcap_snp_c2_11490 | 33.21 |
| PotVar0076636 | 33.21 |
| solcap_snp_c2_39624 | 33.63 |
| solcap_snp_c2_21858 | 34.35 |
| solcap_snp_c1_13859 | 35.42 |
| PotVar0076517 | 35.84 |
| PotVar0106874 | 36.28 |
| PotVar0106780 | 36.76 |
| PotVar0076874 | 38.05 |
| PotVar0100934 | 38.19 |
| solcap_snp_c1_3722 | 38.46 |
| PotVar0076628 | 38.48 |
| PotVar0100792 | 38.72 |
| PotVar0109404 | 39.19 |
| solcap_snp_c1_3740 | 39.93 |
| solcap_snp_c2_11534 | 40.05 |
| solcap_snp_c2_11488 | 41.34 |
| PotVar0127881 | 42.31 |
| PotVar0127732 | 42.62 |
| PotVar0106766 | 42.93 |
| PotVar0007646 | 43.24 |
| solcap_snp_c2_48864 | 43.91 |
| PotVar0101281 | 44.62 |
| solcap_snp_c1_8341 | 44.77 |
| solcap_snp_c2_26814 | 44.77 |
| solcap_snp_c2_26791 | 44.77 |
| solcap_snp_c2_51637 | 45.51 |
| solcap_snp_c1_16079 | 45.72 |
| solcap_snp_c2_16720 | 46.28 |
| solcap_snp_c2_38729 | 47.89 |
| solcap_snp_c2_56253 | 47.89 |
| solcap_snp_c2_14930 | 47.89 |


| solcap_snp_c2_56052 | 47.89 |
| :---: | :---: |
| solcap_snp_c1_11406 | 47.89 |
| solcap_snp_c2_38243 | 47.89 |
| PotVar0008082 | 47.89 |
| PotVar0008075 | 47.89 |
| solcap_snp_c2_18221 | 47.89 |
| PotVar0073568 | 47.89 |
| PotVar0073629 | 47.89 |
| PotVar0014872 | 47.89 |
| PotVar0014738 | 47.89 |
| solcap_snp_c1_13125 | 47.89 |
| solcap_snp_c2_26884 | 47.89 |
| solcap_snp_c2_47244 | 47.89 |
| solcap_snp_c1_14038 | 47.89 |
| solcap_snp_c1_6127 | 47.89 |
| solcap_snp_c2_54090 | 47.89 |
| solcap_snp_c2_51176 | 47.89 |
| solcap_snp_c2_51549 | 47.89 |
| solcap_snp_c1_15085 | 47.89 |
| PotVar0121064 | 47.89 |
| solcap_snp_c2_56254 | 47.89 |
| solcap_snp_c2_56255 | 47.89 |
| solcap_snp_c2_56256 | 47.89 |
| solcap_snp_c1_16261 | 47.89 |
| solcap_snp_c2_18225 | 47.89 |
| solcap_snp_c2_18223 | 47.89 |
| solcap_snp_c2_39961 | 47.89 |
| PotVar0073731 | 47.89 |
| PotVar0073743 | 47.89 |
| solcap_snp_c1_9839 | 47.89 |
| solcap_snp_c1_12887 | 47.89 |
| PotVar0007768 | 47.89 |
| PotVar0007750 | 47.89 |
| solcap_snp_c 1_6157 | 47.89 |
| PotVar0007732 | 47.89 |
| PotVar0014770 | 47.89 |
| solcap_snp_c2_19422 | 47.89 |
| solcap_snp_c1_13124 | 47.89 |
| solcap_snp_c1_6126 | 47.89 |
| solcap_snp_c1_10941 | 47.89 |
| solcap_snp_c2_14924 | 47.89 |
| solcap_snp_c2_53248 | 47.89 |
| PotVar0007761 | 47.89 |
| solcap_snp_c2_26780 | 50.67 |


| solcap_snp_c2_26801 | 50.67 |
| :---: | :---: |
| solcap_snp_c2_26779 | 50.67 |
| solcap_snp_c2_26842 | 50.67 |
| solcap_snp_c2_31403 | 50.67 |
| solcap_snp_c1_8353 | 50.67 |
| solcap_snp_c2_26796 | 53.52 |
| solcap_snp_c2_26793 | 53.52 |
| solcap_snp_c2_26795 | 53.52 |
| solcap_snp_c1_16643 | 53.52 |
| solcap_snp_c2_26794 | 53.52 |
| solcap_snp_c2_26800 | 53.52 |
| PotVar0091972 | 53.74 |
| PotVar0092188 | 54.17 |
| solcap_snp_c2_51560 | 55.04 |
| PotVar0121097 | 55.04 |
| solcap_snp_c2_44601 | 56.75 |
| solcap_snp_c2_56758 | 57.65 |
| PotVar0009086 | 58.63 |
| solcap_snp_c1_3310 | 59.44 |
| solcap_snp_c2_16722 | 59.44 |
| PotVar0076076 | 59.59 |
| solcap_snp_c2_16712 | 60.96 |
| solcap_snp_c2_55090 | 60.96 |
| solcap_snp_c2_55711 | 62.58 |
| solcap_snp_c2_55710 | 62.58 |
| solcap_snp_c2_39856 | 63.03 |
| PotVar0076174 | 63.03 |
| PotVar0076126 | 63.03 |
| PotVar0076291 | 63.46 |
| solcap_snp_c1_15530 | 65.72 |
| PotVar0076127 | 66.5 |
| PotVar0076251 | 66.57 |
| solcap_snp_c1_13396 | 67 |
| PotVar0076322 | 67 |
| solcap_snp_c1_16534 | 67.01 |
| PotVar0076141 | 67.43 |
| solcap_snp_c2_54533 | 67.43 |
| PotVar0076084 | 67.43 |
| PotVar0076175 | 67.43 |
| PotVar0076311 | 67.43 |
| solcap_snp_c1_11791 | 67.43 |
| PotVar0076312 | 67.43 |
| solcap_snp_c1_6033 | 67.43 |
| solcap_snp_c2_58078 | 68.29 |

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| solcap_snp_c1_15982 | 68.29 |
| :---: | :---: |
| solcap_snp_c2_48694 | 70.71 |
| PotVar0074748 | 70.71 |
| solcap_snp_c2_48693 | 70.71 |
| solcap_snp_c2_48691 | 70.71 |
| solcap_snp_c2_1499 | 70.71 |
| solcap_snp_c2_53566 | 71.36 |
| solcap_snp_c1_6905 | 71.55 |
| PotVar0130958 | 71.69 |
| PotVar0074876 | 72.91 |
| PotVar0133113 | 74.18 |
| solcap_snp_c2_45035 | 74.27 |
| PotVar0075104 | 74.27 |
| PotVar0074959 | 74.27 |
| solcap_snp_c1_16625 | 75.13 |
| solcap_snp_c1_12945 | 75.13 |
| solcap_snp_c2_54887 | 75.13 |
| PotVar0074809 | 75.13 |
| PotVar0075042 | 75.13 |
| solcap_snp_c2_45040 | 75.13 |
| PotVar0075008 | 75.13 |
| PotVar0075013 | 75.13 |
| PotVar0075056 | 75.13 |
| PotVar0074712 | 75.13 |
| solcap_snp_c2_48810 | 75.13 |
| PotVar0116182 | 76.43 |
| PotVar0116232 | 76.43 |
| PotVar0116335 | 76.43 |
| PotVar0116179 | 76.43 |
| PotVar0100515 | 77.19 |
| solcap_snp_c1_11758 | 79.05 |
| solcap_snp_c2_55849 | 79.58 |
| solcap_snp_c2_36059 | 79.91 |
| solcap_snp_c2_55854 | 79.91 |
| solcap_snp_c2_36027 | 79.91 |
| PotVar0116492 | 79.91 |
| PotVar0100544 | 80.79 |
| PotVar0084388 | 80.79 |
| solcap_snp_c2_51234 | 80.89 |
| solcap_snp_c2_51232 | 80.89 |
| solcap_snp_c1_11391 | 82.18 |
| solcap_snp_c2_34948 | 83.26 |
| PotVar0084331 | 83.26 |
| solcap_snp_c1_10750 | 83.26 |
| PotVar0116499 | 83.26 |


| PotVar0084519 | 83.26 |
| :---: | :---: |
| solcap_snp_c2_38116 | 83.39 |
| solcap_snp_c1_11356 | 83.39 |
| solcap_snp_c2_48290 | 85.92 |
| solcap_snp_c2_52884 | 87.58 |
| solcap_snp_c2_36060 | 88.27 |
| PotVar0118472 | 88.27 |
| PotVar0100536 | 89.01 |
| PotVar0070877 | 89.04 |
| PotVar0071120 | 89.94 |
| PotVar0071127 | 89.94 |
| solcap_snp_c2_39342 | 90.8 |
| PotVar0070856 | 91.82 |
| PotVar0099137 | 92.36 |
| PotVar0099182 | 92.36 |
| PotVar0000820 | 92.54 |
| PotVar0098992 | 92.57 |
| PotVar0071025 | 98.88 |
| PotVar0070881 | 98.88 |
| solcap_snp_c2_32543 | 98.88 |
| solcap_snp_c2_32550 | 98.88 |
| PotVar0000459 | 99.07 |
| solcap_snp_c2_50004 | 99.1 |
| solcap_snp_c2_39453 | 100.18 |
| PotVar0000812 | 100.28 |
| PotVar0000774 | 100.28 |
| PotVar0000759 | 100.28 |
| PotVar0113773 | 101.78 |
| solcap_snp_c2_43748 | 101.78 |
| PotVar0113891 | 101.78 |
| PotVar0113797 | 101.78 |
| solcap_snp_c1_11639 | 102.02 |
| PotVar0087115 | 103.2 |
| PotVar0087136 | 103.2 |
| solcap_snp_c1_8330 | 103.2 |
| solcap_snp_c2_55784 | 103.55 |
| solcap_snp_c2_55774 | 103.55 |
| solcap_snp_c2_55793 | 103.55 |
| solcap_snp_c2_39463 | 103.76 |
| PotVar0000732 | 103.76 |
| PotVar0000760 | 103.76 |
| solcap_snp_c1_6749 | 104.61 |
| PotVar0000474 | 104.61 |
| PotVar0000512 | 104.61 |
| solcap_snp_c2_21590 | 104.61 |


| PotVar0000615 | 104.61 |
| :---: | :---: |
| solcap_snp_c1_6748 | 104.61 |
| solcap_snp_c2_21578 | 104.61 |
| PotVar0000800 | 104.61 |
| PotVar0000495 | 104.61 |
| PotVar0000460 | 104.61 |
| solcap_snp_c2_26675 | 104.61 |
| PotVar0000484 | 104.61 |
| PotVar0000619 | 104.82 |
| PotVar0000579 | 104.82 |
| PotVar0000481 | 104.82 |
| PotVar0000514 | 104.82 |
| solcap_snp_c2_26758 | 105.93 |
| solcap_snp_c1_8328 | 105.93 |
| PotVar0000542 | 105.93 |
| solcap_snp_c2_26731 | 105.93 |
| PotVar0123717 | 106.78 |
| solcap_snp_c2_55791 | 107.22 |
| PotVar0087118 | 107.41 |
| PotVar0123633 | 108.78 |
| solcap_snp_c2_55777 | 108.78 |
| PotVar0123624 | 108.78 |
| PotVar0087222 | 109.15 |
| PotVar0087243 | 109.76 |
| PotVar0087323 | 109.76 |
| PotVar0087064 | 109.76 |
| PotVar0087312 | 110.02 |
| PotVar0015560 | 110.93 |
| PotVar0015617 | 110.93 |
| PotVar0015713 | 110.93 |
| PotVar0015711 | 110.93 |
| PotVar0015907 | 111.8 |
| PotVar0015743 | 111.8 |
| PotVar0111404 | 112.39 |
| PotVar0111409 | 112.39 |
| PotVar0075291 | 112.39 |
| PotVar0075409 | 112.39 |
| solcap_snp_c2_34812 | 112.39 |
| PotVar0087234 | 112.39 |
| PotVar0075324 | 112.39 |
| PotVar0076006 | 112.39 |
| PotVar0016524 | 113.21 |
| PotVar0016743 | 113.21 |
| PotVar0017079 | 113.21 |
| PotVar0017285 | 113.21 |

Methods for mapping and linkage map integration in tetraploid potato

| solcap_snp_c2_10798 | 113.21 |
| :---: | :---: |
| PotVar0016521 | 113.21 |
| PotVar0075251 | 114.33 |
| PotVar0075236 | 114.33 |
| PotVar0075516 | 114.6 |
| PotVar0075331 | 114.78 |
| PotVar0017413 | 115.1 |
| PotVar0017380 | 115.1 |
| PotVar0017497 | 115.97 |
| PotVar0017942 | 115.97 |
| PotVar0017463 | 115.97 |
| PotVar0111515 | 116.45 |
| PotVar0111414 | 116.45 |
| solcap_snp_c1_13172 | 117.58 |
| PotVar0111537 | 118.47 |
| solcap_snp_c2_52205 | 120.85 |
| PotVar0075295 | 121.63 |
| solcap_snp_c1_4140 | 122.39 |
| solcap_snp_c1_10424 | 123.16 |
| solcap_snp_c2_34876 | 123.16 |
| solcap_snp_c1_9614 | 123.16 |
| solcap_snp_c1_9613 | 123.16 |
| PotVar0111553 | 123.16 |
| solcap_snp_c1_9619 | 123.16 |
| PotVar0075793 | 123.16 |
| PotVar0076032 | 123.16 |
| PotVar0075888 | 123.16 |
| PotVar0130793 | 123.16 |
| PotVar0130846 | 123.16 |
| solcap_snp_c2_12959 | 123.16 |
| PotVar0130835 | 123.16 |
| solcap_snp_c1_10435 | 123.16 |
| PotVar0075293 | 123.16 |
| PotVar0075407 | 123.16 |
| solcap_snp_c2_34873 | 123.16 |
| PotVar0075700 | 123.16 |
| solcap_snp_c1_13085 | 123.16 |
| solcap_snp_c1_13077 | 123.16 |
| solcap_snp_c2_12954 | 123.16 |
| solcap_snp_c1_4178 | 123.16 |
| PotVar0130789 | 123.16 |
| solcap_snp_c2_52196 | 123.16 |
| PotVar0111367 | 123.16 |
| PotVar0111470 | 123.16 |


| solcap_snp_c2_32099 | 123.16 |
| :---: | :---: |
| solcap_snp_c2_52203 | 123.16 |
| solcap_snp_c1_15237 | 123.16 |
| solcap_snp_c2_12947 | 123.26 |
| PotVar0075590 | 123.6 |
| solcap_snp_c2_12956 | 123.7 |
| solcap_snp_c2_12957 | 123.7 |
| solcap_snp_c2_12953 | 123.7 |
| solcap_snp_c2_12958 | 123.7 |
| PotVar0130885 | 123.7 |
| solcap_snp_c2_12924 | 123.87 |
| PotVar0015039 | 124.2 |
| solcap_snp_c2_12936 | 124.69 |
| solcap_snp_c2_34019 | 127.27 |
| solcap_snp_c2_35970 | 127.27 |
| PotVar0015370 | 127.27 |
| solcap_snp_c2_12937 | 127.71 |
| solcap_snp_c2_12921 | 128.57 |
| solcap_snp_c2_12930 | 128.57 |
| PotVar0015456 | 128.93 |
| PotVar0015535 | 128.93 |
| solcap_snp_c1_4175 | 129 |
| solcap_snp_c1_4162 | 129 |
| solcap_snp_c1_4172 | 129 |
| PotVar0015063 | 129.43 |
| PotVar0015087 | 129.43 |
| PotVar0015108 | 129.43 |
| PotVar0015043 | 129.43 |
| PotVar0016703 | 130.24 |
| solcap_snp_c1_4109 | 130.29 |
| PotVar0016173 | 130.71 |
| solcap_snp_c1_10670 | 130.72 |
| solcap_snp_c1_10668 | 130.72 |
| PotVar0015174 | 131.15 |
| PotVar0015207 | 131.15 |
| solcap_snp_c1_10196 | 131.15 |
| PotVar0015145 | 131.15 |
| PotVar0015152 | 131.58 |
| PotVar0015291 | 131.58 |
| solcap_snp_c1_10178 | 134.33 |
| solcap_snp_c2_34017 | 134.33 |
| PotVar0015639 | 134.89 |
| PotVar0016414 | 137.39 |
| solcap_snp_c1_3545 | 137.64 |


| PotVar0015848 | 137.64 |
| :---: | :---: |
| PotVar0015898 | 137.64 |
| solcap_snp_c2_35959 | 137.64 |
| PotVar0016394 | 138.04 |
| PotVar0016316 | 138.04 |
| solcap_snp_c1_10667 | 138.04 |
| PotVar0015940 | 138.04 |
| PotVar0015998 | 138.04 |
| solcap_snp_c2_35995 | 138.04 |
| solcap_snp_c1_10713 | 138.04 |
| PotVar0016706 | 138.04 |
| PotVar0016270 | 138.04 |
| PotVar0016172 | 138.04 |
| PotVar0017157 | 138.04 |
| PotVar0016800 | 138.04 |
| PotVar0016863 | 138.04 |
| PotVar0017188 | 138.04 |
| PotVar0016906 | 138.04 |
| PotVar0016819 | 138.04 |
| solcap_snp_c2_10614 | 138.04 |
| PotVar0017371 | 138.04 |
| solcap_snp_c1_10202 | 138.04 |
| solcap_snp_c2_10693 | 138.04 |
| PotVar0016775 | 138.04 |
| PotVar0016403 | 138.04 |
| PotVar0016397 | 138.04 |
| PotVar0017149 | 138.04 |
| PotVar0017260 | 138.04 |
| solcap_snp_c2_10690 | 138.04 |
| PotVar0016968 | 138.04 |
| PotVar0017276 | 138.04 |
| PotVar0017024 | 138.04 |
| PotVar0015513 | 138.04 |
| PotVar0015583 | 138.04 |
| PotVar0015728 | 138.04 |
| PotVar0015864 | 138.04 |
| solcap_snp_c1_10679 | 138.04 |
| PotVar0015588 | 138.04 |
| PotVar0015597 | 138.04 |
| solcap_snp_c2_35958 | 138.04 |
| solcap_snp_c1_10677 | 138.04 |
| PotVar0015899 | 138.04 |
| PotVar0015433 | 138.04 |
| PotVar0015419 | 138.04 |

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| PotVar0017710 | 138.48 |
| :--- | ---: |
| solcap_snp_c1_3462 | 138.48 |
| PotVar0017842 | 138.48 |
| solcap_snp_c1_3461 | 138.48 |
| PotVar0017609 | 138.7 |
| PotVar0017293 | 138.97 |
| solcap_snp_c1_3522 | 138.97 |
| PotVar0017171 | 138.97 |


| Chromosome 5 |  |
| :---: | :---: |
| Name | cM |
| PotVar0048675 | 0 |
| PotVar0048610 | 0 |
| PotVar0048582 | 0 |
| PotVar0048835 | 0 |
| PotVar0048790 | 0 |
| solcap_snp_c2_23735 | 0 |
| PotVar0048467 | 0 |
| PotVar0048925 | 0 |
| solcap_snp_c2_23834 | 0 |
| solcap_snp_c2_33509 | 0.86 |
| solcap_snp_c2_33532 | 0.86 |
| solcap_snp_c2_52070 | 0.86 |
| PotVar0114697 | 1.29 |
| PotVar0114766 | 1.29 |
| solcap_snp_c2_11758 | 1.29 |
| solcap_snp_c2_11605 | 1.29 |
| PotVar0048155 | 1.54 |
| PotVar0048673 | 3.32 |
| solcap_snp_c1_7632 | 5.95 |
| PotVar0048854 | 6.38 |
| PotVar0025938 | 6.47 |
| PotVar0025923 | 6.47 |
| PotVar0048301 | 7.26 |
| PotVar0048303 | 7.26 |
| PotVar0025983 | 7.61 |
| PotVar0025773 | 7.61 |
| PotVar0025592 | 8.14 |
| PotVar0025762 | 8.56 |
| PotVar0025753 | 9.42 |
| PotVar0026021 | 10.85 |
| PotVar0025449 | 10.85 |
| PotVar0025320 | 12.28 |
| PotVar0025959 | 12.28 |


| PotVar0017084 | 139.42 |
| :--- | ---: |
| PotVar0017411 | 141.24 |
| solcap_snp_c1_3497 | 141.24 |
| solcap_snp_c2_10615 | 141.68 |
| PotVar0017377 | 141.68 |
| solcap_snp_c2_10612 | 142.45 |
| PotVar0017372 | 142.45 |
| PotVar0017726 | 142.91 |


| solcap_snp_c2_23803 | 13.71 |
| :---: | :---: |
| solcap_snp_c2_33518 | 13.94 |
| PotVar0048921 | 14.25 |
| solcap_snp_c1_10042 | 15.22 |
| solcap_snp_c2_33517 | 15.22 |
| PotVar0048229 | 15.37 |
| PotVar0114686 | 16.44 |
| PotVar0114705 | 16.44 |
| solcap_snp_c2_23831 | 16.67 |
| solcap_snp_c2_23828 | 16.88 |
| PotVar0048171 | 16.88 |
| PotVar0048114 | 17.1 |
| PotVar0024773 | 17.1 |
| PotVar0025052 | 17.1 |
| PotVar0025609 | 17.1 |
| PotVar0025348 | 17.1 |
| PotVar0026049 | 17.1 |
| solcap_snp_c2_11707 | 17.16 |
| PotVar0024686 | 18.5 |
| PotVar0024709 | 18.5 |
| PotVar0024728 | 18.5 |
| solcap_snp_c2_11685 | 18.75 |
| PotVar0024528 | 19.61 |
| PotVar0025140 | 19.8 |
| PotVar0024602 | 19.82 |
| PotVar0024611 | 19.82 |
| PotVar0026091 | 19.84 |
| PotVar0026113 | 19.84 |
| PotVar0026057 | 20.08 |
| PotVar0024744 | 20.33 |
| PotVar0024936 | 21.26 |
| PotVar0024781 | 21.26 |
| PotVar0025065 | 21.26 |
| PotVar0025139 | 21.26 |
| PotVar0025527 | 21.72 |


| PotVar0017806 | 142.91 |
| :--- | :---: |
| PotVar0017501 | 142.91 |
| PotVar0017828 | 142.91 |
| solcap_snp_c2_10567 | 142.91 |
| PotVar0017868 | 143.43 |
| PotVar0017895 | 143.87 |
| PotVar0017531 | 143.87 |
| PotVar0016416 | 151.26 |


| PotVar0025740 | 21.72 |
| :---: | :---: |
| PotVar0025764 | 21.72 |
| PotVar0025780 | 21.72 |
| solcap_snp_c2_11924 | 21.72 |
| PotVar0026051 | 21.72 |
| PotVar0025053 | 22.45 |
| PotVar0024816 | 22.45 |
| PotVar0026317 | 23.46 |
| PotVar0078044 | 23.48 |
| PotVar0078215 | 23.48 |
| PotVar0078683 | 23.48 |
| PotVar0078882 | 23.48 |
| PotVar0079450 | 23.48 |
| PotVar0079612 | 23.48 |
| solcap_snp_c2_22959 | 23.48 |
| PotVar0077849 | 23.48 |
| PotVar0078927 | 23.48 |
| PotVar0079086 | 23.48 |
| PotVar0079250 | 23.48 |
| PotVar0079251 | 23.48 |
| PotVar0079591 | 23.48 |
| PotVar0079570 | 23.48 |
| PotVar0025179 | 24.21 |
| PotVar0079948 | 25.01 |
| PotVar0025350 | 25.97 |
| PotVar0079378 | 25.97 |
| PotVar0080850 | 25.97 |
| PotVar0080789 | 25.97 |
| PotVar0130000 | 25.97 |
| PotVar0080275 | 25.97 |
| PotVar0117065 | 25.97 |
| PotVar0117352 | 25.97 |
| solcap_snp_c1_14840 | 25.97 |
| PotVar0117419 | 25.97 |
| PotVar0089832 | 25.97 |

Methods for mapping and linkage map integration in tetraploid potato

| PotVar0079940 | 25.97 |
| :---: | :---: |
| PotVar0079782 | 25.97 |
| PotVar0080614 | 25.97 |
| PotVar0080670 | 25.97 |
| PotVar0080048 | 25.97 |
| PotVar0080122 | 25.97 |
| PotVar0080575 | 25.97 |
| PotVar0080883 | 25.97 |
| PotVar0089637 | 26.91 |
| PotVar0089842 | 26.91 |
| PotVar0117221 | 26.91 |
| PotVar0089709 | 26.91 |
| PotVar0078469 | 28.08 |
| PotVar0078533 | 28.08 |
| PotVar0078025 | 28.08 |
| PotVar0026274 | 28.59 |
| PotVar0026316 | 28.59 |
| PotVar0079955 | 28.59 |
| solcap_snp_c2_50302 | 28.59 |
| PotVar0078411 | 28.59 |
| PotVar0078439 | 28.59 |
| PotVar0079038 | 28.59 |
| PotVar0079085 | 28.59 |
| PotVar0079110 | 28.59 |
| PotVar0079157 | 28.59 |
| PotVar0079489 | 28.59 |
| PotVar0079577 | 28.59 |
| PotVar0079585 | 28.59 |
| PotVar0079877 | 28.59 |
| PotVar0026238 | 28.59 |
| PotVar0078060 | 28.59 |
| PotVar0079430 | 28.59 |
| PotVar0078520 | 28.59 |
| PotVar0078561 | 28.59 |
| PotVar0079406 | 28.59 |
| PotVar0079428 | 28.59 |
| PotVar0079652 | 28.59 |
| PotVar0078045 | 28.59 |
| PotVar0078769 | 28.59 |
| PotVar0079027 | 28.59 |
| PotVar0079081 | 28.59 |
| PotVar0079374 | 28.59 |
| PotVar0079376 | 28.59 |
| PotVar0026556 | 28.59 |


| PotVar0079653 | 28.59 |
| :---: | :---: |
| PotVar0080867 | 28.59 |
| PotVar0078609 | 28.59 |
| PotVar0117366 | 28.59 |
| solcap_snp_c2_51478 | 28.59 |
| PotVar0117354 | 28.59 |
| PotVar0089662 | 28.59 |
| PotVar0089604 | 28.59 |
| solcap_snp_c2_38193 | 28.59 |
| PotVar0079737 | 28.59 |
| solcap_snp_c2_38163 | 28.89 |
| PotVar0080026 | 29.54 |
| PotVar0080320 | 29.85 |
| PotVar0080800 | 30.5 |
| PotVar0117437 | 31.02 |
| PotVar0025360 | 31.02 |
| PotVar0025579 | 31.02 |
| solcap_snp_c1_3795 | 31.02 |
| solcap_snp_c2_11923 | 31.02 |
| PotVar0079966 | 31.02 |
| PotVar0080476 | 31.02 |
| PotVar0117192 | 31.02 |
| solcap_snp_c2_38167 | 31.02 |
| PotVar0025607 | 31.02 |
| solcap_snp_c2_47284 | 31.02 |
| PotVar0116903 | 31.02 |
| PotVar0025980 | 31.02 |
| PotVar0025599 | 31.02 |
| PotVar0078229 | 31.02 |
| PotVar0078648 | 31.02 |
| PotVar0078670 | 31.02 |
| PotVar0078972 | 31.02 |
| PotVar0079124 | 31.02 |
| PotVar0078022 | 31.02 |
| PotVar0080027 | 31.02 |
| PotVar0079860 | 31.02 |
| PotVar0080686 | 31.02 |
| PotVar0116897 | 31.02 |
| PotVar0079901 | 31.02 |
| PotVar0080213 | 31.02 |
| PotVar0080365 | 31.02 |
| PotVar0080570 | 31.02 |
| PotVar0117073 | 31.02 |
| PotVar0117095 | 31.02 |


| solcap_snp_c2_22995 | 31.02 |
| :---: | :---: |
| PotVar0079820 | 31.02 |
| PotVar0117047 | 31.02 |
| PotVar0117275 | 31.02 |
| PotVar0117190 | 31.02 |
| PotVar0080004 | 31.02 |
| PotVar0117280 | 31.02 |
| PotVar0129937 | 31.16 |
| PotVar0117324 | 31.79 |
| PotVar0117438 | 32.1 |
| PotVar0117367 | 32.1 |
| PotVar0026053 | 32.87 |
| PotVar0025817 | 32.87 |
| PotVar0089374 | 33.42 |
| solcap_snp_c2_52084 | 33.42 |
| solcap_snp_c2_11747 | 33.42 |
| PotVar0026355 | 33.42 |
| PotVar0078379 | 33.42 |
| PotVar0079403 | 33.42 |
| PotVar0079611 | 33.42 |
| PotVar0026425 | 33.42 |
| PotVar0077822 | 33.42 |
| PotVar0078126 | 33.42 |
| PotVar0079063 | 33.42 |
| PotVar0079368 | 33.42 |
| PotVar0026211 | 33.42 |
| PotVar0083808 | 34.84 |
| PotVar0083817 | 35.94 |
| solcap_snp_c2_45517 | 36.35 |
| PotVar0084178 | 37.24 |
| PotVar0083684 | 37.34 |
| PotVar0084089 | 37.69 |
| PotVar0084163 | 37.98 |
| solcap_snp_c2_37719 | 37.98 |
| PotVar0085303 | 38.44 |
| PotVar0125832 | 38.45 |
| solcap_snp_c1_11267 | 39.53 |
| PotVar0084164 | 39.53 |
| PotVar0125947 | 39.53 |
| solcap_snp_c2_55452 | 39.88 |
| PotVar0089376 | 40.26 |
| PotVar0125819 | 40.45 |
| PotVar0047235 | 40.74 |
| PotVar0085501 | 41.53 |

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| PotVar0084190 | 42.7 |
| :---: | :---: |
| PotVar0085312 | 43.68 |
| PotVar0085401 | 43.68 |
| PotVar0085405 | 43.68 |
| PotVar0085531 | 43.68 |
| PotVar0085459 | 43.68 |
| PotVar0125830 | 43.81 |
| solcap_snp_c2_37692 | 43.99 |
| PotVar0014494 | 44.47 |
| PotVar0014510 | 44.47 |
| PotVar0014440 | 44.47 |
| PotVar0091638 | 44.62 |
| PotVar0091918 | 44.62 |
| PotVar0091929 | 44.62 |
| PotVar0091364 | 44.62 |
| PotVar0014380 | 44.9 |
| PotVar0090934 | 44.91 |
| solcap_snp_c2_56464 | 45.33 |
| PotVar0014357 | 45.33 |
| PotVar0091038 | 45.48 |
| solcap_snp_c2_53298 | 45.55 |
| solcap_snp_c2_53306 | 45.55 |
| solcap_snp_c2_53307 | 45.55 |
| PotVar0109994 | 45.55 |
| PotVar0085259 | 45.78 |
| PotVar0085257 | 45.78 |
| PotVar0091177 | 45.91 |
| PotVar0001033 | 46.34 |
| PotVar0084120 | 46.42 |
| solcap_snp_c2_38748 | 46.47 |
| solcap_snp_c2_54725 | 46.47 |
| PotVar0104925 | 46.47 |
| PotVar0104911 | 46.47 |
| solcap_snp_c2_49286 | 46.47 |
| PotVar0104871 | 46.47 |
| solcap_snp_c1_15292 | 46.76 |
| PotVar0083923 | 46.76 |
| PotVar0084086 | 46.76 |
| PotVar0091259 | 46.76 |
| PotVar0091740 | 46.76 |
| PotVar0091619 | 47.11 |
| PotVar0091465 | 47.11 |
| PotVar0091464 | 47.11 |
| PotVar0091432 | 47.11 |
| PotVar0091575 | 47.11 |


| PotVar0091625 | 47.56 |
| :---: | :---: |
| PotVar0091668 | 47.56 |
| PotVar0134951 | 47.58 |
| solcap_snp_c2_49385 | 47.58 |
| PotVar0001247 | 47.58 |
| PotVar0001272 | 47.58 |
| PotVar0001295 | 47.58 |
| PotVar0001317 | 47.58 |
| PotVar0001451 | 47.58 |
| solcap_snp_c1_15192 | 47.58 |
| solcap_snp_c1_15690 | 47.58 |
| PotVar0001495 | 47.58 |
| PotVar0001507 | 47.58 |
| PotVar0001074 | 47.58 |
| solcap_snp_c2_50226 | 47.58 |
| solcap_snp_c2_47967 | 47.58 |
| solcap_snp_c2_48587 | 47.58 |
| solcap_snp_c2_57245 | 47.58 |
| PotVar0001227 | 47.58 |
| solcap_snp_c2_15722 | 47.58 |
| solcap_snp_c2_52397 | 47.58 |
| PotVar0001360 | 47.58 |
| solcap_snp_c1_14645 | 47.66 |
| PotVar0091229 | 47.66 |
| solcap_snp_c1_11078 | 48.23 |
| PotVar0090998 | 48.23 |
| PotVar0091176 | 48.23 |
| solcap_snp_c2_32854 | 48.23 |
| PotVar0091126 | 48.23 |
| PotVar0014571 | 48.23 |
| solcap_snp_c2_43663 | 48.23 |
| PotVar0083756 | 48.23 |
| PotVar0090986 | 48.23 |
| PotVar0001530 | 48.23 |
| PotVar0000967 | 48.23 |
| solcap_snp_c2_52053 | 48.23 |
| solcap_snp_c2_40089 | 48.23 |
| solcap_snp_c1_11868 | 48.23 |
| PotVar0001438 | 48.23 |
| solcap_snp_c2_49666 | 48.23 |
| PotVar0125811 | 48.23 |
| PotVar0001271 | 48.23 |
| PotVar0014379 | 49.77 |
| PotVar0014299 | 50.2 |
| PotVar0001415 | 50.31 |


| PotVar0024151 | 50.31 |
| :---: | :---: |
| PotVar0084430 | 50.31 |
| PotVar0001283 | 50.31 |
| PotVar0024137 | 50.31 |
| PotVar0084432 | 50.31 |
| PotVar0001195 | 50.31 |
| solcap_snp_c2_54598 | 50.63 |
| PotVar0001310 | 50.76 |
| PotVar0109880 | 51.06 |
| PotVar0055481 | 51.06 |
| PotVar0104798 | 51.06 |
| solcap_snp_c2_44034 | 51.06 |
| solcap_snp_c2_54741 | 52 |
| PotVar0014475 | 52.13 |
| PotVar0104886 | 52.31 |
| solcap_snp_c2_48821 | 54.35 |
| PotVar0123241 | 54.35 |
| PotVar0123263 | 54.35 |
| PotVar0001525 | 54.35 |
| PotVar0001067 | 54.35 |
| PotVar0001163 | 54.35 |
| solcap_snp_c2_54576 | 54.35 |
| solcap_snp_c2_48422 | 54.35 |
| PotVar0001318 | 54.35 |
| solcap_snp_c2_52058 | 54.35 |
| solcap_snp_c2_38365 | 54.35 |
| solcap_snp_c2_38364 | 54.35 |
| solcap_snp_c2_40092 | 54.35 |
| PotVar0001147 | 54.35 |
| solcap_snp_c2_51980 | 54.91 |
| PotVar0104796 | 55.01 |
| solcap_snp_c2_54743 | 55.01 |
| solcap_snp_c2_54742 | 55.01 |
| solcap_snp_c 1_12966 | 55.43 |
| PotVar0104857 | 55.86 |
| PotVar0104802 | 55.86 |
| PotVar0001239 | 56.3 |
| solcap_snp_c1_5058 | 56.43 |
| PotVar0001513 | 56.74 |
| PotVar0001214 | 56.74 |
| solcap_snp_c2_38252 | 57.67 |
| solcap_snp_c2_47405 | 57.77 |
| solcap_snp_c2_5214 | 57.77 |
| solcap_snp_c2_5006 | 57.77 |
| solcap_snp_c2_5003 | 57.77 |

Methods for mapping and linkage map integration in tetraploid potato

| solcap_snp_c2_5217 | 57.77 |
| :---: | :---: |
| solcap_snp_c1_1802 | 57.87 |
| PotVar0001290 | 58.09 |
| PotVar0001324 | 58.09 |
| solcap_snp_c2_48820 | 58.09 |
| solcap_snp_c2_52056 | 58.09 |
| PotVar0001270 | 58.09 |
| PotVar0018043 | 58.09 |
| solcap_snp_c2_52055 | 58.09 |
| PotVar0001413 | 58.09 |
| PotVar0014413 | 58.54 |
| solcap_snp_c1_14700 | 58.57 |
| PotVar0134955 | 58.57 |
| solcap_snp_c2_44073 | 58.57 |
| PotVar0001015 | 58.57 |
| solcap_snp_c2_47389 | 58.74 |
| solcap_snp_c2_47390 | 58.74 |
| solcap_snp_c2_50231 | 59.04 |
| PotVar0001436 | 59.14 |
| PotVar0106493 | 59.19 |
| solcap_snp_c2_5150 | 59.19 |
| PotVar0106489 | 60.07 |
| PotVar0106504 | 60.07 |
| solcap_snp_c2_5154 | 60.07 |
| PotVar0106500 | 60.07 |
| PotVar0033995 | 61.23 |
| PotVar0018022 | 61.77 |
| PotVar0034046 | 63.07 |
| PotVar0106514 | 63.07 |
| solcap_snp_c2_15676 | 63.47 |
| PotVar0001127 | 63.47 |
| PotVar0034048 | 65.9 |
| PotVar0034098 | 65.9 |
| solcap_snp_c 1_15965 | 66.84 |
| PotVar0033952 | 66.93 |
| PotVar0123233 | 68.14 |
| PotVar0123271 | 68.69 |
| PotVar0106516 | 69.56 |
| PotVar0033946 | 69.66 |
| solcap_snp_c2_40775 | 69.66 |
| PotVar0106494 | 69.66 |
| PotVar0033999 | 70 |
| solcap_snp_c1_1875 | 70 |
| PotVar0106501 | 70 |


| PotVar0034096 | 71.73 |
| :---: | :---: |
| PotVar0034089 | 71.73 |
| solcap_snp_c1_12414 | 72.69 |
| solcap_snp_c2_42374 | 72.69 |
| solcap_snp_c2_49653 | 73.74 |
| PotVar0126177 | 75.52 |
| PotVar0081337 | 75.64 |
| solcap_snp_c2_49116 | 75.95 |
| PotVar0081577 | 76.52 |
| PotVar0081379 | 76.97 |
| PotVar0007814 | 76.97 |
| PotVar0081513 | 77.7 |
| solcap_snp_c2_49128 | 78.3 |
| solcap_snp_c1_11996 | 78.95 |
| PotVar0081356 | 79.05 |
| PotVar0081357 | 79.06 |
| PotVar0123209 | 79.32 |
| solcap_snp_c1_12439 | 79.56 |
| PotVar0081571 | 79.56 |
| PotVar0081369 | 79.56 |
| solcap_snp_c2_10338 | 79.56 |
| solcap_snp_c2_10341 | 79.56 |
| PotVar0081647 | 79.56 |
| PotVar0081633 | 79.56 |
| PotVar0081749 | 79.56 |
| PotVar0082012 | 79.56 |
| PotVar0082125 | 79.56 |
| PotVar0123108 | 80.03 |
| PotVar0123086 | 80.46 |
| PotVar0081707 | 81.34 |
| PotVar0081723 | 81.34 |
| PotVar0081615 | 81.34 |
| PotVar0081622 | 81.34 |
| PotVar0122968 | 81.34 |
| PotVar0123135 | 81.34 |
| PotVar0128000 | 81.76 |
| solcap_snp_c2_10287 | 81.85 |
| PotVar0081678 | 82.8 |
| PotVar0081681 | 82.8 |
| PotVar0081987 | 82.9 |
| PotVar0082001 | 82.9 |
| PotVar0081821 | 82.9 |
| PotVar0082011 | 82.9 |
| PotVar0082064 | 82.9 |


| PotVar0081993 | 82.9 |
| :---: | :---: |
| PotVar0082095 | 82.9 |
| PotVar0082074 | 82.9 |
| PotVar0082079 | 83.24 |
| PotVar0082142 | 83.24 |
| solcap_snp_c2_42451 | 83.24 |
| solcap_snp_c2_42542 | 83.24 |
| PotVar0123127 | 83.24 |
| PotVar0128071 | 83.24 |
| solcap_snp_c2_8302 | 83.24 |
| PotVar0034986 | 83.24 |
| solcap_snp_c2_8510 | 83.24 |
| PotVar0034903 | 83.24 |
| PotVar0034892 | 83.24 |
| PotVar0128222 | 83.24 |
| solcap_snp_c2_8256 | 83.24 |
| PotVar0081880 | 83.24 |
| PotVar0081936 | 83.24 |
| PotVar0034964 | 83.24 |
| PotVar0082094 | 83.67 |
| PotVar0081674 | 84.11 |
| PotVar0082112 | 84.11 |
| PotVar0081632 | 84.11 |
| PotVar0123144 | 84.21 |
| PotVar0123062 | 84.21 |
| PotVar0081696 | 84.53 |
| PotVar0081566 | 84.81 |
| PotVar0081536 | 85.03 |
| PotVar0128198 | 85.62 |
| PotVar0123145 | 86.27 |
| PotVar0123206 | 87.38 |
| PotVar0082093 | 88.01 |
| PotVar0082108 | 88.01 |
| PotVar0082107 | 88.01 |
| PotVar0082096 | 88.11 |
| PotVar0128203 | 88.47 |
| PotVar0128174 | 88.47 |
| PotVar0128205 | 88.47 |
| PotVar0128091 | 88.47 |
| PotVar0127929 | 88.9 |
| PotVar0128038 | 88.9 |
| PotVar0123022 | 89.85 |
| PotVar0123092 | 89.85 |
| solcap_snp_c2_42481 | 90.28 |

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| PotVar0034970 | 90.61 |
| :--- | ---: |
| PotVar0128021 | 90.71 |
| PotVar0034886 | 91.55 |
| PotVar0123117 | 91.63 |
| PotVar0123083 | 91.63 |
| solcap_snp_c2_42452 | 91.63 |
| solcap_snp_c2_8210 | 91.8 |
| PotVar0035035 | 91.8 |
| solcap_snp_c2_55239 | 92.05 |
| solcap_snp_c2_8295 | 94.72 |
| PotVar0128234 | 94.72 |
| PotVar0128144 | 94.72 |
| solcap_snp_c2_8428 | 94.72 |
| PotVar0034966 | 94.72 |
| solcap_snp_c1_1219 | 94.72 |


| Chromosome 6 |  |
| :--- | ---: |
| Name | cM |
| PotVar0083563 | 0 |
| PotVar0083583 | 0 |
| PotVar0083604 | 0 |
| PotVar0083550 | 0 |
| solcap_snp_c2_30595 | 0.09 |
| PotVar0083339 | 0.86 |
| PotVar0083062 | 0.86 |
| solcap_snp_c2_36400 | 1.29 |
| PotVar0083053 | 1.55 |
| solcap_snp_c1_9224 | 3.5 |
| PotVar0083246 | 3.5 |
| solcap_snp_c2_30495 | 3.5 |
| PotVar0082855 | 3.5 |
| PotVar0027035 | 5.74 |
| PotVar0026839 | 6.16 |
| PotVar0027076 | 17.31 |
| PotVar0026902 | 12.58 |
| PotVar0027050 | 12.58 |
| solcap_snp_c2_55553 | 12.58 |
| solcap_snp_c1_16128 | 12.71 |
| PotVar0026688 | 13.71 |
| PotVar0026864 | 15.36 |
| PotVar0083630 | 15.69 |
| PotVar0027032 | 17.31 |
| solcap_snp_c2_27620 | 070 |
|  |  |


| solcap_snp_c1_1125 | 94.72 |
| :--- | ---: |
| PotVar0034812 | 94.72 |
| solcap_snp_c1_2865 | 95.13 |
| PotVar0034971 | 95.13 |
| PotVar0034941 | 95.13 |
| PotVar0034768 | 95.13 |
| PotVar0034599 | 95.13 |
| solcap_snp_c2_3449 | 95.13 |
| PotVar0034566 | 95.13 |
| PotVar0034978 | 95.57 |
| PotVar0034973 | 95.57 |
| PotVar0035034 | 95.57 |
| PotVar0034467 | 96.72 |
| PotVar0034404 | 96.72 |
| PotVar0034649 | 96.72 |


| solcap_snp_c2_36709 | 18.41 |
| :--- | ---: |
| solcap_snp_c1_10939 | 18.83 |
| solcap_snp_c1_10938 | 18.83 |
| solcap_snp_c1_15811 | 19.68 |
| solcap_snp_c2_49638 | 22.29 |
| solcap_snp_c1_13871 | 22.72 |
| solcap_snp_c2_50183 | 24.4 |
| PotVar0131893 | 24.4 |
| PotVar0131873 | 24.62 |
| PotVar0004038 | 25.23 |
| PotVar0004060 | 25.23 |
| PotVar0069488 | 25.23 |
| PotVar0069491 | 25.23 |
| PotVar0069492 | 25.23 |
| PotVar0004013 | 25.23 |
| PotVar0027083 | 26.12 |
| PotVar0026695 | 26.34 |
| PotVar0090366 | 27.82 |
| PotVar0090406 | 27.82 |
| PotVar0090338 | 27.82 |
| PotVar0131889 | 27.85 |
| solcap_snp_c2_36590 | 27.85 |
| PotVar0131863 | 27.85 |
| solcap_snp_c2_36595 | 27.85 |
| PotVar0131880 | 29.75 |
| solcap_snp_c1_16656 | 2003983 |
| solcap_snp_c2_17378 | 2.75 |


| PotVar0034950 | 96.83 |
| :--- | ---: |
| PotVar0034862 | 96.83 |
| PotVar0034580 | 97.64 |
| solcap_snp_c1_1123 | 97.64 |
| PotVar0034466 | 97.92 |
| PotVar0034730 | 97.94 |
| solcap_snp_c2_3512 | 98 |
| solcap_snp_c2_3452 | 99.3 |
| PotVar0034578 | 99.3 |
| PotVar0034688 | 99.3 |
| PotVar0034395 | 100.47 |
| PotVar0034408 | 100.53 |
| solcap_snp_c1_1163 | 101.75 |


| solcap_snp_c2_4590 | 29.75 |
| :---: | :---: |
| PotVar0036573 | 29.75 |
| PotVar0090345 | 29.75 |
| PotVar0093229 | 29.75 |
| PotVar0131933 | 29.75 |
| solcap_snp_c2_27867 | 29.75 |
| PotVar0131882 | 29.75 |
| PotVar0096888 | 29.75 |
| PotVar0093232 | 29.75 |
| PotVar0090320 | 30.47 |
| solcap_snp_c2_24297 | 30.9 |
| PotVar0093261 | 30.9 |
| solcap_snp_c2_42354 | 31.33 |
| PotVar0093114 | 31.76 |
| PotVar0104638 | 31.78 |
| PotVar0104705 | 31.78 |
| PotVar0133873 | 31.84 |
| solcap_snp_c2_32893 | 32.61 |
| solcap_snp_c1_10560 | 32.61 |
| solcap_snp_c2_24050 | 32.61 |
| PotVar0090309 | 32.61 |
| solcap_snp_c2_42351 | 32.61 |
| solcap_snp_c2_40266 | 32.61 |
| PotVar0104660 | 32.61 |
| PotVar0131877 | 32.61 |
| solcap_snp_c2_51762 | 32.61 |
| solcap_snp_c2_51768 | 32.61 |
| solcap_snp_c2_51766 | 32.61 |

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| solcap_snp_c1_15233 | 32.61 |
| :---: | :---: |
| solcap_snp_c2_33302 | 32.61 |
| solcap_snp_c2_33365 | 32.61 |
| solcap_snp_c2_56058 | 32.61 |
| PotVar0133869 | 32.61 |
| PotVar0104694 | 32.71 |
| solcap_snp_c2_37603 | 33.04 |
| solcap_snp_c2_32952 | 33.04 |
| solcap_snp_c2_43068 | 33.74 |
| PotVar0104703 | 34.17 |
| solcap_snp_c2_51760 | 34.17 |
| solcap_snp_c2_51771 | 34.17 |
| PotVar0133895 | 34.6 |
| solcap_snp_c2_33314 | 34.6 |
| solcap_snp_c2_54220 | 34.6 |
| solcap_snp_c2_57016 | 34.6 |
| solcap_snp_c2_57019 | 34.6 |
| solcap_snp_c2_43123 | 34.6 |
| PotVar0127129 | 34.6 |
| PotVar0127210 | 34.6 |
| solcap_snp_c1_11275 | 34.6 |
| solcap_snp_c2_37766 | 34.6 |
| solcap_snp_c2_32918 | 34.6 |
| solcap_snp_c1_10157 | 34.6 |
| PotVar0093231 | 34.6 |
| PotVar0104776 | 34.99 |
| PotVar0133948 | 35.54 |
| solcap_snp_c2_33346 | 36.25 |
| PotVar0054869 | 36.25 |
| PotVar0054938 | 37.03 |
| PotVar0087364 | 37.55 |
| PotVar0134018 | 38.32 |
| solcap_snp_c2_31648 | 38.74 |
| solcap_snp_c2_40242 | 38.99 |
| PotVar0133549 | 38.99 |
| solcap_snp_c2_37756 | 39.7 |
| solcap_snp_c2_40236 | 39.94 |
| PotVar0127164 | 40.18 |
| PotVar0127225 | 40.18 |
| PotVar0127196 | 40.18 |
| PotVar0127331 | 40.18 |
| PotVar0127104 | 40.18 |
| PotVar0127224 | 40.61 |
| PotVar0054901 | 41.4 |


| PotVar0119434 | 41.92 |
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| PotVar0119420 | 41.92 |
| solcap_snp_c2_56132 | 46.31 |
| solcap_snp_c2_49052 | 46.77 |
| solcap_snp_c2_49053 | 47.19 |
| PotVar0087403 | 47.19 |
| PotVar0127240 | 48.05 |
| PotVar0133545 | 48.15 |
| solcap_snp_c2_37762 | 48.15 |
| PotVar0119498 | 48.15 |
| solcap_snp_c2_49885 | 48.15 |
| PotVar0070225 | 51.31 |
| PotVar0070228 | 51.31 |
| PotVar0070189 | 51.31 |
| PotVar0070203 | 51.31 |
| PotVar0070124 | 52.21 |
| PotVar0070014 | 53.5 |
| solcap_snp_c2_25929 | 54.31 |
| PotVar0070093 | 54.39 |
| solcap_snp_c2_16777 | 54.39 |
| PotVar0069973 | 54.39 |
| PotVar0090695 | 54.74 |
| PotVar0090703 | 54.74 |
| PotVar0070227 | 55.61 |
| solcap_snp_c2_31893 | 55.61 |
| PotVar0070150 | 55.61 |
| PotVar0085941 | 55.7 |
| PotVar0090673 | 55.7 |
| PotVar0090556 | 55.7 |
| solcap_snp_c2_54195 | 56.48 |
| PotVar0086011 | 56.91 |
| PotVar0090783 | 58.56 |
| solcap_snp_c2_5858 | 59.66 |
| PotVar0090705 | 60.41 |
| PotVar0090785 | 60.41 |
| PotVar0090474 | 60.41 |
| PotVar0090465 | 60.41 |
| PotVar0090460 | 60.41 |
| PotVar0090449 | 60.41 |
| PotVar0090458 | 60.41 |
| PotVar0085050 | 60.55 |
| PotVar0090868 | 60.62 |
| solcap_snp_c 1_10646 | 60.83 |
| PotVar0084850 | 60.83 |


| solcap_snp_c2_31180 | 61.26 |
| :---: | :---: |
| solcap_snp_c2_41412 | 61.4 |
| solcap_snp_c2_31144 | 61.49 |
| PotVar0084854 | 61.49 |
| solcap_snp_c2_41405 | 61.83 |
| PotVar0073982 | 62.26 |
| PotVar0074004 | 62.26 |
| PotVar0073911 | 62.26 |
| PotVar0073971 | 62.26 |
| PotVar0073985 | 62.26 |
| PotVar0074079 | 62.26 |
| solcap_snp_c2_41406 | 62.26 |
| solcap_snp_c2_56145 | 62.26 |
| PotVar0073953 | 62.26 |
| solcap_snp_c1_13135 | 62.69 |
| PotVar0074175 | 63.12 |
| solcap_snp_c1_2960 | 63.12 |
| PotVar0074119 | 63.12 |
| solcap_snp_c1_2953 | 63.12 |
| solcap_snp_c1_3003 | 63.12 |
| solcap_snp_c2_8867 | 63.12 |
| PotVar0074198 | 63.12 |
| solcap_snp_c2_8790 | 63.55 |
| PotVar0085064 | 64.11 |
| PotVar0085088 | 64.11 |
| solcap_snp_c2_5772 | 64.11 |
| solcap_snp_c1_2065 | 64.11 |
| solcap_snp_c1_2116 | 64.11 |
| solcap_snp_c1_2117 | 64.11 |
| solcap_snp_c2_5771 | 64.11 |
| solcap_snp_c2_5835 | 64.11 |
| solcap_snp_c2_5868 | 64.11 |
| solcap_snp_c2_8793 | 64.33 |
| solcap_snp_c1_2979 | 64.33 |
| solcap_snp_c2_33777 | 65.15 |
| solcap_snp_c2_33891 | 65.58 |
| solcap_snp_c2_33830 | 65.58 |
| PotVar0085035 | 65.58 |
| PotVar0040610 | 66.09 |
| PotVar0040630 | 66.09 |
| PotVar0040651 | 66.09 |
| PotVar0040658 | 66.09 |
| solcap_snp_c2_9010 | 66.19 |
| solcap_snp_c1_10109 | 67.6 |

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| solcap_snp_c2_9009 | 70.64 |
| :---: | :---: |
| solcap_snp_c1_2944 | 71.29 |
| solcap_snp_c2_8663 | 71.29 |
| solcap_snp_c2_8966 | 73.21 |
| PotVar0040682 | 73.21 |
| solcap_snp_c2_9001 | 73.21 |
| solcap_snp_c2_9005 | 73.21 |
| solcap_snp_c2_8652 | 73.21 |
| solcap_snp_c2_8786 | 73.63 |
| solcap_snp_c2_9002 | 73.67 |
| solcap_snp_c2_8904 | 74.53 |
| solcap_snp_c2_8999 | 74.86 |
| PotVar0040680 | 74.86 |
| PotVar0040538 | 75.38 |
| solcap_snp_c2_22289 | 75.81 |
| solcap_snp_c1_7005 | 76.24 |
| PotVar0040499 | 76.24 |
| PotVar0040249 | 76.24 |
| solcap_snp_c1_6994 | 76.24 |
| PotVar0040507 | 76.24 |
| solcap_snp_c2_22336 | 76.24 |
| PotVar0040397 | 76.24 |
| solcap_snp_c2_9011 | 76.24 |
| solcap_snp_c1_6997 | 76.24 |
| PotVar0040162 | 77.94 |
| PotVar0040532 | 78.93 |
| PotVar0040491 | 80.87 |
| PotVar0056976 | 81.71 |
| PotVar0040236 | 81.77 |
| PotVar0040125 | 81.79 |
| PotVar0040426 | 82.21 |
| PotVar0040161 | 82.21 |
| PotVar0040122 | 82.21 |
| PotVar0039905 | 82.21 |
| PotVar0039962 | 82.21 |
| PotVar0040351 | 82.21 |
| PotVar0040358 | 82.21 |
| PotVar0040287 | 82.21 |
| PotVar0040388 | 82.21 |
| PotVar0040366 | 82.21 |
| PotVar0039988 | 82.21 |
| PotVar0040135 | 82.21 |
| PotVar0039982 | 82.21 |
| PotVar0039725 | 82.21 |
| PotVar0039963 | 82.21 |


| PotVar0039835 | 82.21 |
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| PotVar0041181 | 82.21 |
| solcap_snp_c2_56590 | 82.21 |
| solcap_snp_c2_37358 | 82.21 |
| PotVar0127622 | 82.21 |
| solcap_snp_c2_37329 | 82.21 |
| PotVar0040257 | 83.94 |
| PotVar0127585 | 83.94 |
| solcap_snp_c1_3074 | 84.07 |
| solcap_snp_c2_9039 | 84.69 |
| PotVar0040137 | 84.89 |
| PotVar0040182 | 84.89 |
| solcap_snp_c2_24066 | 84.89 |
| PotVar0041150 | 84.89 |
| PotVar0039950 | 84.89 |
| PotVar0039686 | 84.89 |
| solcap_snp_c2_24229 | 84.89 |
| PotVar0039692 | 84.89 |
| PotVar0039687 | 84.89 |
| PotVar0039697 | 84.89 |
| solcap_snp_c2_9308 | 84.89 |
| PotVar0041167 | 84.89 |
| PotVar0041190 | 84.89 |
| PotVar0041021 | 84.89 |
| PotVar0041040 | 84.89 |
| PotVar0041041 | 84.89 |
| PotVar0127625 | 84.89 |
| PotVar0041048 | 84.89 |
| PotVar0041079 | 84.89 |
| PotVar0040999 | 84.89 |
| PotVar0056982 | 84.89 |
| PotVar0057082 | 84.89 |
| PotVar0057065 | 84.89 |
| PotVar0057368 | 84.89 |
| solcap_snp_c1_7029 | 84.89 |
| solcap_snp_c1_7040 | 84.89 |
| solcap_snp_c1_7688 | 84.89 |
| PotVar0039728 | 84.89 |
| solcap_snp_c2_24245 | 84.89 |
| PotVar0039939 | 84.89 |
| PotVar0039998 | 84.89 |
| solcap_snp_c1_7031 | 84.89 |
| solcap_snp_c1_7041 | 84.89 |
| solcap_snp_c2_22404 | 84.89 |
| PotVar0040289 | 84.89 |


| PotVar0041199 | 84.89 |
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| PotVar0040540 | 84.89 |
| PotVar0056998 | 84.99 |
| solcap_snp_c2_9137 | 85.81 |
| PotVar0057119 | 86.28 |
| PotVar0057170 | 86.71 |
| PotVar0057370 | 87.02 |
| PotVar0132843 | 87.24 |
| solcap_snp_c2_9043 | 87.45 |
| PotVar0132862 | 88.43 |
| PotVar0132845 | 88.74 |
| PotVar0057041 | 89.36 |
| PotVar0057120 | 89.78 |
| solcap_snp_c2_37339 | 90.8 |
| PotVar0040975 | 90.8 |
| PotVar0066091 | 91.83 |
| PotVar0057091 | 92.49 |
| PotVar0056996 | 96.33 |
| solcap_snp_c1_8679 | 96.94 |
| PotVar0132863 | 96.94 |
| PotVar0132754 | 96.94 |
| solcap_snp_c2_50798 | 96.94 |
| solcap_snp_c2_50802 | 97.21 |
| solcap_snp_c1_16127 | 97.37 |
| PotVar0057192 | 99.42 |
| PotVar0057365 | 100.29 |
| PotVar0065888 | 101.6 |
| solcap_snp_c2_29187 | 104.15 |
| PotVar0065920 | 104.96 |
| solcap_snp_c2_1950 | 105.46 |
| solcap_snp_c1_7679 | 107.89 |
| PotVar0057109 | 107.89 |
| solcap_snp_c2_9193 | 107.89 |
| PotVar0132784 | 107.89 |
| PotVar0057090 | 107.89 |
| PotVar0132831 | 107.89 |
| PotVar0066099 | 107.89 |
| PotVar0065875 | 107.89 |
| PotVar0065921 | 107.89 |
| solcap_snp_c2_9247 | 109.73 |
| solcap_snp_c1_3130 | 109.73 |
| solcap_snp_c2_9202 | 110.23 |
| PotVar0065852 | 111.49 |
| solcap_snp_c 1_15061 | 116.25 |
| PotVar0065992 | 116.25 |

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| PotVar0065896 | 116.25 |
| :--- | :--- |


| PotVar0065903 | 116.25 |
| :--- | :--- |


| solcap_snp_c1_14614 | 121.2 |
| :--- | :--- |


| Chromosome 7 |  |
| :---: | :---: |
| Name | cM |
| solcap_snp_c1_13663 | 0 |
| solcap_snp_c2_46102 | 0 |
| PotVar0023044 | 0 |
| PotVar0022689 | 0.43 |
| PotVar0022751 | 0.43 |
| PotVar0022656 | 1.31 |
| PotVar0022397 | 2.1 |
| PotVar0022472 | 2.74 |
| PotVar0022817 | 3.25 |
| solcap_snp_c2_38828 | 3.25 |
| PotVar0022437 | 4.16 |
| PotVar0022654 | 4.2 |
| PotVar0022114 | 5.02 |
| PotVar0022108 | 5.02 |
| solcap_snp_c1_15462 | 5.17 |
| PotVar0023049 | 5.21 |
| PotVar0022595 | 5.21 |
| PotVar0022249 | 5.33 |
| solcap_snp_c2_36067 | 5.33 |
| PotVar0022526 | 6.52 |
| PotVar0022452 | 6.52 |
| PotVar0022711 | 6.99 |
| PotVar0022288 | 7.2 |
| PotVar0022541 | 7.22 |
| PotVar0022266 | 7.38 |
| PotVar0022225 | 7.38 |
| PotVar0022443 | 7.43 |
| PotVar0095725 | 7.43 |
| PotVar0023040 | 7.43 |
| PotVar0022997 | 7.43 |
| solcap_snp_c2_43960 | 7.43 |
| PotVar0022712 | 7.43 |
| solcap_snp_c2_52663 | 7.43 |
| solcap_snp_c2_26239 | 7.43 |
| PotVar0102524 | 7.43 |
| solcap_snp_c2_45643 | 7.53 |
| solcap_snp_c2_26154 | 7.95 |
| PotVar0130023 | 7.95 |
| PotVar0022083 | 8.25 |


| PotVar0022139 | 8.25 |
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| solcap_snp_c2_26145 | 8.38 |
| PotVar0022653 | 8.41 |
| solcap_snp_c2_26197 | 9.99 |
| PotVar0130025 | 9.99 |
| PotVar0130054 | 9.99 |
| PotVar0130051 | 9.99 |
| PotVar0130068 | 9.99 |
| PotVar0130024 | 9.99 |
| solcap_snp_c2_26182 | 10.12 |
| PotVar0022442 | 10.15 |
| PotVar0130065 | 12.76 |
| PotVar0022264 | 12.84 |
| PotVar0022115 | 12.84 |
| PotVar0022369 | 12.84 |
| solcap_snp_c2_26162 | 13.19 |
| PotVar0102528 | 13.96 |
| PotVar0130091 | 14.11 |
| PotVar0102374 | 14.39 |
| PotVar0102533 | 14.93 |
| PotVar0095701 | 15.76 |
| solcap_snp_c1_16225 | 15.76 |
| PotVar0095825 | 15.76 |
| solcap_snp_c1_16222 | 15.76 |
| solcap_snp_c2_46736 | 16.51 |
| PotVar0102540 | 16.51 |
| PotVar0095918 | 16.51 |
| PotVar0132140 | 16.51 |
| PotVar0132139 | 16.51 |
| PotVar0095833 | 16.51 |
| solcap_snp_c2_46752 | 16.51 |
| PotVar0095580 | 16.51 |
| PotVar0132011 | 16.51 |
| PotVar0102342 | 17.05 |
| PotVar0132707 | 17.37 |
| PotVar0132489 | 17.37 |
| solcap_snp_c2_55830 | 17.56 |
| PotVar0095739 | 17.56 |
| solcap_snp_c2_55832 | 17.56 |
| solcap_snp_c2_55837 | 17.56 |
| PotVar0095883 | 17.56 |


| PotVar0097757 | 17.8 |
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| PotVar0097696 | 17.8 |
| PotVar0095511 | 18.15 |
| PotVar0102371 | 18.26 |
| solcap_snp_c2_42640 | 18.67 |
| PotVar0103609 | 18.67 |
| PotVar0095632 | 19.19 |
| solcap_snp_c2_43588 | 19.19 |
| PotVar0095478 | 19.19 |
| PotVar0095628 | 19.35 |
| PotVar0127530 | 19.54 |
| PotVar0127427 | 19.54 |
| PotVar0097752 | 19.54 |
| PotVar0097761 | 19.54 |
| PotVar0127381 | 19.97 |
| PotVar0095645 | 20.19 |
| PotVar0028319 | 20.85 |
| PotVar0028351 | 20.85 |
| PotVar0028271 | 21.06 |
| PotVar0028147 | 21.06 |
| solcap_snp_c2_46379 | 21.3 |
| PotVar0132155 | 21.3 |
| solcap_snp_c2_48715 | 21.71 |
| PotVar0132505 | 22.14 |
| solcap_snp_c2_55986 | 22.14 |
| solcap_snp_c2_6601 | 22.14 |
| solcap_snp_c2_55985 | 22.14 |
| PotVar0097692 | 22.14 |
| solcap_snp_c2_52374 | 22.14 |
| PotVar0027925 | 22.57 |
| PotVar0028053 | 22.57 |
| solcap_snp_c2_52376 | 22.98 |
| solcap_snp_c2_52377 | 22.98 |
| solcap_snp_c2_31373 | 23.91 |
| solcap_snp_c2_2856 | 23.91 |
| solcap_snp_c2_49853 | 23.91 |
| solcap_snp_c1_15484 | 23.93 |
| solcap_snp_c1_15485 | 23.93 |
| PotVar0032760 | 24.35 |
| PotVar0012599 | 24.35 |
| PotVar0086506 | 24.35 |

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| solcap_snp_c2_7712 | 24.35 |
| :---: | :---: |
| solcap_snp_c2_7735 | 24.35 |
| solcap_snp_c1_512 | 24.35 |
| solcap_snp_c2_7715 | 24.35 |
| solcap_snp_c1_14735 | 24.75 |
| PotVar0132627 | 24.75 |
| PotVar0132568 | 24.85 |
| PotVar0132538 | 24.85 |
| PotVar0097715 | 24.85 |
| PotVar0086423 | 25.2 |
| PotVar0032700 | 25.2 |
| PotVar0037615 | 25.2 |
| PotVar0086488 | 25.2 |
| PotVar0086524 | 25.2 |
| PotVar0032779 | 25.2 |
| PotVar0097697 | 25.57 |
| solcap_snp_c2_13908 | 25.65 |
| PotVar0127459 | 25.68 |
| solcap_snp_c2_52104 | 25.68 |
| PotVar0028432 | 25.99 |
| PotVar0103477 | 25.99 |
| PotVar0028391 | 25.99 |
| PotVar0027924 | 26.86 |
| solcap_snp_c2_6622 | 26.86 |
| PotVar0027937 | 26.86 |
| solcap_snp_c2_6600 | 26.86 |
| solcap_snp_c2_6617 | 26.86 |
| solcap_snp_c2_6619 | 26.86 |
| solcap_snp_c2_6620 | 26.86 |
| PotVar0027956 | 26.86 |
| solcap_snp_c2_6609 | 26.89 |
| PotVar0134230 | 27.56 |
| PotVar0127439 | 28.11 |
| PotVar0127372 | 28.54 |
| PotVar0127400 | 28.54 |
| solcap_snp_c2_4530 | 28.96 |
| solcap_snp_c2_13889 | 29.06 |
| PotVar0028383 | 29.42 |
| PotVar0028350 | 29.42 |
| PotVar0028392 | 29.42 |
| PotVar0069893 | 29.78 |
| PotVar0069612 | 29.78 |
| PotVar0069680 | 29.78 |
| solcap_snp_c1_3153 | 29.78 |
| PotVar0069827 | 29.78 |


| solcap_snp_c1_10855 | 31.23 |
| :---: | :---: |
| solcap_snp_c2_49836 | 31.23 |
| PotVar0069919 | 31.29 |
| PotVar0134260 | 31.29 |
| PotVar0134371 | 31.29 |
| solcap_snp_c2_4475 | 31.29 |
| PotVar0069647 | 31.51 |
| solcap_snp_c2_23391 | 31.52 |
| PotVar0092761 | 31.52 |
| solcap_snp_c1_15700 | 31.52 |
| PotVar0092409 | 31.52 |
| solcap_snp_c2_23396 | 31.52 |
| PotVar0128797 | 31.52 |
| PotVar0069634 | 32.4 |
| PotVar0115368 | 32.4 |
| PotVar0115281 | 32.4 |
| PotVar0092426 | 32.4 |
| PotVar0092775 | 32.4 |
| PotVar0128906 | 32.4 |
| solcap_snp_c1_7399 | 32.4 |
| PotVar0128887 | 32.4 |
| PotVar0093018 | 32.4 |
| PotVar0092990 | 32.4 |
| PotVar0093016 | 32.4 |
| solcap_snp_c1_2404 | 33.13 |
| PotVar0128900 | 33.4 |
| PotVar0092660 | 33.4 |
| solcap_snp_c1_5112 | 33.4 |
| solcap_snp_c1_5126 | 33.4 |
| PotVar0128963 | 33.4 |
| PotVar0028081 | 33.4 |
| solcap_snp_c2_6616 | 33.4 |
| PotVar0028036 | 33.4 |
| PotVar0028024 | 33.4 |
| PotVar0027940 | 33.4 |
| solcap_snp_c1_2405 | 33.4 |
| PotVar0028084 | 33.4 |
| PotVar0086496 | 33.4 |
| solcap_snp_c1_2672 | 33.4 |
| PotVar0032614 | 33.4 |
| PotVar0032617 | 33.4 |
| PotVar0134361 | 33.4 |
| PotVar0069668 | 33.4 |
| solcap_snp_c2_9357 | 33.48 |
| solcap_snp_c1_16194 | 33.94 |


| PotVar0092903 | 33.94 |
| :---: | :---: |
| PotVar0092913 | 33.94 |
| PotVar0115139 | 33.94 |
| solcap_snp_c2_44120 | 33.94 |
| PotVar0069620 | 33.94 |
| PotVar0069656 | 33.94 |
| PotVar0069878 | 33.94 |
| solcap_snp_c2_9354 | 33.94 |
| solcap_snp_c2_9355 | 33.94 |
| solcap_snp_c2_47671 | 33.94 |
| PotVar0115319 | 34.16 |
| PotVar0115246 | 34.16 |
| PotVar0115416 | 34.39 |
| PotVar0115101 | 34.39 |
| solcap_snp_c1_16193 | 34.39 |
| PotVar0092875 | 34.39 |
| PotVar0115020 | 34.39 |
| solcap_snp_c2_15929 | 34.39 |
| solcap_snp_c1_12976 | 34.39 |
| PotVar0115415 | 34.39 |
| PotVar0115039 | 34.39 |
| PotVar0115344 | 34.39 |
| PotVar0093655 | 34.39 |
| PotVar0093742 | 34.39 |
| PotVar0086359 | 35.02 |
| solcap_snp_c2_19696 | 35.02 |
| solcap_snp_c2_19698 | 35.02 |
| PotVar0012598 | 35.02 |
| solcap_snp_c1_9478 | 35.02 |
| solcap_snp_c2_8193 | 35.02 |
| solcap_snp_c2_34558 | 35.02 |
| solcap_snp_c2_1975 | 35.02 |
| solcap_snp_c2_1980 | 35.02 |
| solcap_snp_c2_9359 | 35.02 |
| solcap_snp_c1_7521 | 35.02 |
| PotVar0012608 | 35.02 |
| PotVar0092421 | 35.02 |
| PotVar0092448 | 35.02 |
| PotVar0092628 | 35.02 |
| PotVar0128886 | 35.02 |
| solcap_snp_c2_23075 | 35.02 |
| PotVar0092298 | 35.02 |
| solcap_snp_c1_3141 | 35.02 |
| PotVar0115014 | 35.02 |
| solcap_snp_c1_5115 | 35.02 |

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| solcap_snp_c1_5113 | 35.02 |
| :---: | :---: |
| PotVar0092872 | 35.02 |
| PotVar0093790 | 35.49 |
| solcap_snp_c2_33495 | 35.49 |
| solcap_snp_c2_33492 | 35.49 |
| solcap_snp_c2_44095 | 35.49 |
| PotVar0092770 | 35.5 |
| PotVar0092830 | 35.5 |
| solcap_snp_c2_45461 | 35.83 |
| PotVar0119733 | 35.83 |
| PotVar0115046 | 35.91 |
| PotVar0093632 | 36.42 |
| solcap_snp_c2_33488 | 36.79 |
| PotVar0093025 | 36.83 |
| PotVar0093776 | 37 |
| PotVar0133600 | 37.42 |
| solcap_snp_c2_25250 | 38.04 |
| solcap_snp_c1_7405 | 38.26 |
| PotVar0093572 | 38.43 |
| solcap_snp_c2_15908 | 39.24 |
| solcap_snp_c2_15923 | 39.67 |
| PotVar0093555 | 40.6 |
| PotVar0093513 | 40.6 |
| PotVar0093634 | 40.6 |
| solcap_snp_c2_33493 | 41.03 |
| solcap_snp_c2_45445 | 44.21 |
| PotVar0119736 | 44.21 |
| solcap_snp_c1_6228 | 44.67 |
| PotVar0133616 | 44.72 |
| PotVar0088454 | 45.76 |
| PotVar0093777 | 46.1 |
| solcap_snp_c2_33491 | 46.1 |
| solcap_snp_c2_45176 | 46.21 |
| PotVar0133592 | 46.21 |
| PotVar0133588 | 46.21 |
| PotVar0133614 | 46.21 |
| PotVar0119757 | 46.98 |
| solcap_snp_c2_33429 | 46.98 |
| PotVar0119730 | 46.98 |
| PotVar0119726 | 46.98 |
| solcap_snp_c1_7973 | 48.13 |
| PotVar0134970 | 49.25 |
| solcap_snp_c2_45181 | 50.59 |
| solcap_snp_c2_38787 | 50.65 |


| PotVar0134084 | 51.55 |
| :---: | :---: |
| solcap_snp_c2_46329 | 51.76 |
| solcap_snp_c1_6244 | 51.76 |
| solcap_snp_c2_19748 | 53.72 |
| PotVar0134031 | 53.72 |
| solcap_snp_c1_6238 | 54.16 |
| PotVar0133636 | 56.38 |
| solcap_snp_c2_25207 | 56.38 |
| solcap_snp_c2_35078 | 56.38 |
| PotVar0104502 | 57.18 |
| solcap_snp_c2_35110 | 57.57 |
| PotVar0134105 | 57.57 |
| solcap_snp_c2_35055 | 58.02 |
| solcap_snp_c2_35058 | 58.79 |
| PotVar0134065 | 59.66 |
| PotVar0134990 | 60.09 |
| solcap_snp_c1_10461 | 60.96 |
| solcap_snp_c2_35053 | 61.26 |
| solcap_snp_c2_35051 | 62.13 |
| solcap_snp_c2_26006 | 62.71 |
| solcap_snp_c2_26014 | 62.71 |
| PotVar0134030 | 62.78 |
| PotVar0134999 | 62.78 |
| solcap_snp_c2_26041 | 63.05 |
| PotVar0047676 | 64.42 |
| PotVar0047482 | 64.85 |
| Gro14_a_Paal_LG07 | 64.85 |
| PotVar0047713 | 66.5 |
| solcap_snp_c2_26015 | 67.14 |
| PotVar0047739 | 67.14 |
| PotVar0047767 | 67.14 |
| PotVar0047816 | 67.24 |
| PotVar0047993 | 67.29 |
| PotVar0047949 | 67.29 |
| PotVar0047836 | 67.29 |
| PotVar0134086 | 68.33 |
| PotVar0048010 | 68.59 |
| PotVar0048065 | 69.38 |
| solcap_snp_c2_28212 | 69.38 |
| PotVar0044409 | 70.24 |
| PotVar0044179 | 70.87 |
| PotVar0044126 | 72.51 |
| PotVar0044653 | 72.59 |
| solcap_snp_c2_26040 | 72.81 |


| PotVar0047616 | 72.81 |
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| solcap_snp_c2_26003 | 73.47 |
| solcap_snp_c2_26011 | 73.47 |
| solcap_snp_c2_33038 | 73.47 |
| solcap_snp_c2_50620 | 74.1 |
| PotVar0047901 | 74.11 |
| PotVar0047847 | 74.11 |
| solcap_snp_c2_26007 | 74.11 |
| solcap_snp_c2_26012 | 74.11 |
| solcap_snp_c2_28174 | 74.11 |
| PotVar0047551 | 74.11 |
| PotVar0044685 | 74.11 |
| solcap_snp_c2_12420 | 74.16 |
| PotVar0043929 | 74.47 |
| PotVar0102878 | 74.47 |
| PotVar0047595 | 75.26 |
| PotVar0047459 | 75.26 |
| PotVar0047829 | 75.26 |
| PotVar0047976 | 75.26 |
| solcap_snp_c2_33019 | 75.26 |
| solcap_snp_c1_9918 | 75.26 |
| solcap_snp_c2_28310 | 75.26 |
| solcap_snp_c2_28195 | 75.26 |
| PotVar0048050 | 75.26 |
| PotVar0048012 | 75.36 |
| solcap_snp_c2_28309 | 75.36 |
| solcap_snp_c1_8709 | 75.36 |
| solcap_snp_c1_8713 | 75.36 |
| solcap_snp_c2_28167 | 75.36 |
| solcap_snp_c2_28176 | 75.36 |
| solcap_snp_c2_28186 | 75.36 |
| PotVar0043885 | 75.46 |
| PotVar0102788 | 76.13 |
| solcap_snp_c2_12596 | 76.13 |
| PotVar0102837 | 76.13 |
| PotVar0102773 | 76.51 |
| PotVar0044133 | 77.04 |
| PotVar0044416 | 77.04 |
| PotVar0048011 | 77.04 |
| solcap_snp_c2_28171 | 77.04 |
| PotVar0044024 | 77.04 |
| PotVar0043970 | 77.04 |
| PotVar0047769 | 77.04 |
| PotVar0047982 | 77.04 |

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| solcap_snp_c2_42756 | 77.47 |
| :--- | :---: |
| PotVar0044651 | 77.47 |
| PotVar0044551 | 77.93 |
| solcap_snp_c2_42807 | 77.93 |
| solcap_snp_c2_16846 | 78.18 |
| solcap_snp_c2_30416 | 78.21 |
| PotVar0128563 | 78.21 |
| PotVar0102649 | 78.21 |
| PotVar0044169 | 78.39 |
| solcap_snp_c2_12405 | 78.82 |
| PotVar0044131 | 78.82 |
| PotVar0044090 | 78.87 |
| PotVar0044591 | 80.07 |
| solcap_snp_c2_51513 | 80.16 |
| PotVar0102784 | 80.16 |
| solcap_snp_c2_51536 | 80.59 |
| PotVar0044156 | 81.03 |
| PotVar0044278 | 81.13 |
| solcap_snp_c1_12597 | 81.13 |
| PotVar0044411 | 81.13 |


| Chromosome 8 | cM |
| :--- | ---: |
| Name | 0 |
| PotVar0113745 | 0 |
| PotVar0113742 | 0.21 |
| PotVar0113635 | 0.36 |
| solcap_snp_c2_27452 | 0.43 |
| PotVar0113623 | 1.3 |
| solcap_snp_c2_51957 | 3.19 |
| PotVar0088789 | 3.19 |
| PotVar0088709 | 4.1 |
| PotVar0088803 | 5.15 |
| PotVar0118200 | 5.15 |
| PotVar0118202 | 5.46 |
| PotVar0108990 | 5.46 |
| solcap_snp_c2_57750 | 5.46 |
| PotVar0110053 | 5.93 |
| PotVar0110028 | 6.02 |
| solcap_snp_c2_29025 | 6.02 |
| solcap_snp_c2_29020 | 7.54 |
| PotVar0088684 | 7.96 |
| PotVar0088692 | 7.96 |
| solcap_snp_c1_14884 |  |
| PotVar0088757 |  |
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| PotVar0128566 | 81.36 |
| :--- | ---: |
| PotVar0044305 | 81.62 |
| solcap_snp_c2_18573 | 82.34 |
| PotVar0043954 | 82.78 |
| solcap_snp_c2_12411 | 82.78 |
| PotVar0102877 | 82.78 |
| PotVar0044087 | 83.93 |
| solcap_snp_c2_18685 | 85.1 |
| solcap_snp_c2_18667 | 85.1 |
| solcap_snp_c2_18684 | 85.1 |
| PotVar0037125 | 85.53 |
| PotVar0037122 | 85.53 |
| solcap_snp_c2_30428 | 86.35 |
| solcap_snp_c2_30460 | 86.35 |
| solcap_snp_c2_18745 | 86.4 |
| PotVar0037035 | 86.4 |
| PotVar0036819 | 86.79 |
| solcap_snp_c2_12526 | 87.01 |
| PotVar0037236 | 87.66 |
| PotVar0102724 | 88.05 |


| PotVar0088714 | 7.96 |
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| PotVar0088710 | 7.96 |
| PotVar0088766 | 7.96 |
| PotVar0110149 | 7.96 |
| PotVar0110157 | 7.96 |
| PotVar0088806 | 7.96 |
| solcap_snp_c2_53516 | 7.96 |
| PotVar0088738 | 7.96 |
| PotVar0088760 | 7.96 |
| PotVar0088739 | 8.02 |
| PotVar0108992 | 8.71 |
| PotVar0088783 | 8.78 |
| PotVar0110066 | 8.89 |
| solcap_snp_c2_24404 | 8.89 |
| PotVar0110096 | 8.89 |
| PotVar0110161 | 9.21 |
| PotVar0063780 | 9.44 |
| solcap_snp_c2_24410 | 9.83 |
| solcap_snp_c1_7739 | 10.04 |
| PotVar0110060 | 10.04 |
| PotVar0108807 | 10.27 |
| PotVar0108825 | 10.27 |
| PotVar0109013 |  |
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| PotVar0102815 | 90.1 |
| :--- | ---: |
| PotVar0036750 | 92.01 |
| PotVar0036643 | 92.01 |
| PotVar0036821 | 92.01 |
| PotVar0036731 | 92.01 |
| PotVar0036644 | 92.01 |
| solcap_snp_c1_8830 | 92.01 |
| solcap_snp_c2_28850 | 92.45 |
| PotVar0037157 | 92.45 |
| PotVar0037090 | 92.45 |
| PotVar0037039 | 92.45 |
| PotVar0036843 | 92.47 |
| solcap_snp_c2_33279 | 92.67 |
| solcap_snp_c2_33278 | 92.67 |
| solcap_snp_c2_28851 | 92.9 |
| solcap_snp_c2_28848 | 92.9 |
| solcap_snp_c2_28846 | 92.9 |
| solcap_snp_c2_33276 | 92.9 |
| solcap_snp_c2_33273 | 94.78 |


| PotVar0108833 | 10.27 |
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| PotVar0108899 | 10.27 |
| PotVar0108902 | 10.5 |
| PotVar0110136 | 10.96 |
| solcap_snp_c2_44855 | 11.87 |
| PotVar0063749 | 12.06 |
| solcap_snp_c2_34142 | 12.82 |
| PotVar0108896 | 12.82 |
| PotVar0108913 | 12.82 |
| PotVar0063725 | 12.89 |
| PotVar0063904 | 13.04 |
| PotVar0063940 | 13.04 |
| solcap_snp_c2_48951 | 13.53 |
| PotVar0063845 | 13.53 |
| solcap_snp_c2_34124 | 13.91 |
| solcap_snp_c2_30037 | 13.91 |
| PotVar0063938 | 13.91 |
| PotVar0063693 | 13.96 |
| PotVar0063692 | 13.96 |
| PotVar0063624 | 13.96 |
| solcap_snp_c2_34121 | 14.34 |
| solcap_snp_c2_26893 | 14.77 |
| PotVar0063591 |  |
|  | 143 |

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| PotVar0063939 | 15.86 |
| :---: | :---: |
| solcap_snp_c2_19533 | 15.86 |
| solcap_snp_c2_19534 | 15.86 |
| solcap_snp_c2_34179 | 15.86 |
| solcap_snp_c2_30104 | 15.86 |
| PotVar0063844 | 15.86 |
| solcap_snp_c2_48953 | 15.86 |
| PotVar0063766 | 15.86 |
| PotVar0063756 | 15.86 |
| PotVar0063704 | 15.86 |
| solcap_snp_c1_8380 | 15.86 |
| PotVar0063755 | 15.86 |
| solcap_snp_c2_26938 | 15.86 |
| solcap_snp_c2_19638 | 15.86 |
| solcap_snp_c2_47904 | 15.86 |
| solcap_snp_c2_47905 | 15.86 |
| solcap_snp_c2_19437 | 15.95 |
| solcap_snp_c2_37599 | 15.95 |
| solcap_snp_c2_47920 | 15.95 |
| solcap_snp_c2_47923 | 15.95 |
| solcap_snp_c2_57588 | 15.95 |
| solcap_snp_c2_57589 | 15.95 |
| solcap_snp_c2_37600 | 15.95 |
| solcap_snp_c2_57591 | 15.95 |
| solcap_snp_c2_54581 | 15.95 |
| PotVar0081045 | 15.95 |
| solcap_snp_c2_57849 | 15.95 |
| solcap_snp_c2_2103 | 15.95 |
| solcap_snp_c2_2102 | 15.95 |
| solcap_snp_c2_19951 | 15.95 |
| solcap_snp_c2_19940 | 15.95 |
| PotVar0076488 | 15.95 |
| solcap_snp_c2_2844 | 15.95 |
| solcap_snp_c2_2843 | 15.95 |
| solcap_snp_c2_2842 | 15.95 |
| solcap_snp_c2_2837 | 15.95 |
| solcap_snp_c1_846 | 15.95 |
| solcap_snp_c2_8167 | 15.95 |
| solcap_snp_c2_5909 | 15.95 |
| solcap_snp_c2_29284 | 15.95 |
| solcap_snp_c2_29283 | 15.95 |
| solcap_snp_c2_19426 | 15.95 |
| solcap_snp_c1_6130 | 15.95 |
| solcap_snp_c1_6131 | 15.95 |


| solcap_snp_c1_6138 | 15.95 |
| :---: | :---: |
| solcap_snp_c2_30255 | 15.95 |
| solcap_snp_c1_11442 | 15.95 |
| solcap_snp_c2_30904 | 15.95 |
| solcap_snp_c2_30907 | 15.95 |
| solcap_snp_c1_2686 | 15.95 |
| solcap_snp_c1_2687 | 15.95 |
| PotVar0088658 | 15.95 |
| solcap_snp_c1_15689 | 15.95 |
| solcap_snp_c2_34078 | 15.95 |
| solcap_snp_c2_34565 | 15.95 |
| solcap_snp_c2_34564 | 15.95 |
| solcap_snp_c2_42290 | 15.95 |
| solcap_snp_c2_2178 | 15.95 |
| PotVar0076384 | 15.95 |
| solcap_snp_c2_19942 | 15.95 |
| solcap_snp_c2_2840 | 15.95 |
| solcap_snp_c2_2826 | 15.95 |
| solcap_snp_c2_8169 | 15.95 |
| solcap_snp_c2_8172 | 15.95 |
| solcap_snp_c2_5915 | 15.95 |
| solcap_snp_c2_29494 | 15.95 |
| solcap_snp_c2_29498 | 15.95 |
| solcap_snp_c2_29286 | 15.95 |
| solcap_snp_c2_29280 | 15.95 |
| solcap_snp_c2_19433 | 15.95 |
| solcap_snp_c1_6136 | 15.95 |
| solcap_snp_c1_6140 | 15.95 |
| solcap_snp_c1_6142 | 15.95 |
| solcap_snp_c1_9169 | 15.95 |
| solcap_snp_c2_30293 | 15.95 |
| solcap_snp_c2_19432 | 15.95 |
| solcap_snp_c2_31354 | 16.42 |
| solcap_snp_c2_12746 | 16.42 |
| solcap_snp_c2_17305 | 16.42 |
| solcap_snp_c2_47900 | 16.42 |
| solcap_snp_c2_17317 | 16.48 |
| solcap_snp_c2_17304 | 16.48 |
| solcap_snp_c2_52253 | 19.12 |
| solcap_snp_c2_52857 | 19.12 |
| solcap_snp_c1_15451 | 19.12 |
| solcap_snp_c2_42293 | 22.89 |
| PotVar0124889 | 23.12 |
| PotVar0076451 | 23.76 |


| PotVar0076467 | 23.76 |
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| PotVar0076367 | 24.19 |
| PotVar0060621 | 24.61 |
| PotVar0076370 | 25.63 |
| solcap_snp_c1_6262 | 25.63 |
| PotVar0029800 | 25.63 |
| PotVar0040861 | 25.63 |
| solcap_snp_c2_49249 | 25.89 |
| solcap_snp_c2_49243 | 25.89 |
| solcap_snp_c2_33774 | 26.05 |
| solcap_snp_c2_19631 | 27.25 |
| solcap_snp_c2_17318 | 27.25 |
| solcap_snp_c1_6252 | 27.35 |
| solcap_snp_c2_19639 | 27.35 |
| solcap_snp_c2_19949 | 27.35 |
| solcap_snp_c2_53177 | 27.35 |
| solcap_snp_c2_33771 | 27.45 |
| solcap_snp_c2_48358 | 27.45 |
| solcap_snp_c2_53880 | 27.45 |
| solcap_snp_c2_19429 | 27.45 |
| solcap_snp_c2_30256 | 27.45 |
| solcap_snp_c1_9167 | 27.45 |
| solcap_snp_c2_34082 | 27.45 |
| solcap_snp_c2_56757 | 28.94 |
| solcap_snp_c2_2746 | 29.27 |
| solcap_snp_c1_822 | 29.82 |
| solcap_snp_c2_2743 | 29.82 |
| solcap_snp_c2_56491 | 30.33 |
| solcap_snp_c2_41463 | 30.65 |
| solcap_snp_c2_41470 | 30.65 |
| solcap_snp_c2_32317 | 30.7 |
| solcap_snp_c1_14542 | 31.57 |
| solcap_snp_c2_2757 | 31.88 |
| solcap_snp_c2_2744 | 31.88 |
| solcap_snp_c1_12163 | 31.88 |
| solcap_snp_c2_45763 | 32.46 |
| PotVar0133433 | 33.31 |
| solcap_snp_c1_14108 | 33.74 |
| solcap_snp_c2_32302 | 35.41 |
| solcap_snp_c2_32280 | 36.56 |
| solcap_snp_c2_32300 | 36.56 |
| PotVar0077284 | 36.7 |
| PotVar0077225 | 36.7 |
| solcap_snp_c2_15803 | 36.7 |

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| solcap_snp_c2_51328 | 36.99 |
| :---: | :---: |
| solcap_snp_c2_40320 | 38.55 |
| PotVar0103294 | 38.98 |
| PotVar0103406 | 38.98 |
| PotVar0103368 | 38.98 |
| PotVar0134854 | 39.27 |
| solcap_snp_c2_45759 | 39.4 |
| solcap_snp_c1_15044 | 39.5 |
| solcap_snp_c2_44334 | 39.5 |
| solcap_snp_c1_16676 | 39.5 |
| PotVar0133394 | 39.5 |
| PotVar0103329 | 39.59 |
| PotVar0134757 | 40.16 |
| PotVar0134733 | 40.16 |
| solcap_snp_c2_44307 | 40.25 |
| solcap_snp_c2_32309 | 40.25 |
| solcap_snp_c2_32310 | 40.25 |
| solcap_snp_c2_32282 | 40.25 |
| solcap_snp_c2_44331 | 41.09 |
| solcap_snp_c1_13586 | 41.09 |
| solcap_snp_c2_51320 | 41.09 |
| PotVar0133361 | 41.09 |
| solcap_snp_c1_15046 | 43.01 |
| solcap_snp_c2_51369 | 43.01 |
| solcap_snp_c2_51367 | 43.01 |
| solcap_snp_c2_51329 | 43.01 |
| solcap_snp_c2_44305 | 43.01 |
| solcap_snp_c2_44304 | 43.01 |
| PotVar0133399 | 43.01 |
| solcap_snp_c2_18892 | 43.01 |
| solcap_snp_c2_47459 | 43.01 |
| PotVar0086641 | 43.01 |
| solcap_snp_c2_33381 | 43.01 |
| PotVar0086640 | 43.01 |
| PotVar0086805 | 43.01 |
| PotVar0086812 | 43.01 |
| PotVar0123452 | 43.01 |
| solcap_snp_c2_18943 | 43.01 |
| PotVar0086745 | 43.01 |
| solcap_snp_c2_47444 | 43.01 |
| PotVar0134851 | 43.43 |
| solcap_snp_c2_41044 | 43.43 |
| solcap_snp_c1_12166 | 44.31 |
| PotVar0134835 | 44.32 |
| PotVar0134764 | 45.19 |


| solcap_snp_c1_14271 | 45.19 |
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| solcap_snp_c2_33386 | 45.19 |
| PotVar0134793 | 45.19 |
| PotVar0134751 | 45.19 |
| PotVar0134734 | 45.19 |
| solcap_snp_c2_48182 | 45.19 |
| PotVar0123397 | 45.19 |
| PotVar0123415 | 45.19 |
| solcap_snp_c1_11562 | 45.19 |
| PotVar0134798 | 45.19 |
| PotVar0086588 | 45.34 |
| PotVar0123481 | 45.46 |
| PotVar0123525 | 45.64 |
| solcap_snp_c2_18894 | 46.28 |
| solcap_snp_c2_18895 | 46.28 |
| PotVar0086703 | 46.28 |
| PotVar0086598 | 46.49 |
| PotVar0086773 | 46.49 |
| solcap_snp_c2_18922 | 47.13 |
| PotVar0086822 | 47.13 |
| PotVar0086646 | 47.13 |
| PotVar0086766 | 47.13 |
| PotVar0086744 | 47.13 |
| PotVar0134786 | 47.58 |
| solcap_snp_c2_48184 | 47.58 |
| PotVar0077030 | 48.12 |
| PotVar0077094 | 48.12 |
| PotVar0077179 | 48.33 |
| PotVar0077330 | 48.99 |
| PotVar0077537 | 48.99 |
| PotVar0077331 | 48.99 |
| PotVar0077015 | 49.71 |
| PotVar0125618 | 50.11 |
| PotVar0125359 | 50.11 |
| PotVar0125664 | 50.11 |
| PotVar0125338 | 50.11 |
| PotVar0077235 | 50.65 |
| PotVar0077582 | 50.88 |
| solcap_snp_c2_50150 | 50.88 |
| solcap_snp_c2_50153 | 50.88 |
| PotVar0076939 | 50.98 |
| PotVar0077095 | 51.4 |
| PotVar0077528 | 52.15 |
| PotVar0077483 | 52.15 |
| PotVar0077540 | 52.15 |


| PotVar0125518 | 52.26 |
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| PotVar0077092 | 52.73 |
| PotVar0077227 | 52.73 |
| PotVar0077151 | 52.73 |
| PotVar0125369 | 53.19 |
| PotVar0077471 | 53.19 |
| PotVar0125390 | 53.19 |
| PotVar0077614 | 53.19 |
| PotVar0125381 | 53.19 |
| PotVar0125546 | 53.19 |
| PotVar0125152 | 53.19 |
| PotVar0077622 | 53.67 |
| solcap_snp_c2_49377 | 54.26 |
| solcap_snp_c2_50151 | 54.48 |
| PotVar0103342 | 55.51 |
| PotVar0103095 | 56.9 |
| PotVar0103097 | 56.9 |
| PotVar0103351 | 57.77 |
| solcap_snp_c2_28555 | 57.9 |
| PotVar0122021 | 58.2 |
| PotVar0103305 | 58.67 |
| PotVar0103303 | 58.67 |
| PotVar0122082 | 58.67 |
| solcap_snp_c2_28580 | 59.11 |
| solcap_snp_c2_28637 | 60.37 |
| PotVar0063401 | 60.86 |
| PotVar0063512 | 60.86 |
| PotVar0063421 | 61.29 |
| solcap_snp_c2_28633 | 61.29 |
| solcap_snp_c2_28634 | 61.29 |
| PotVar0063331 | 61.29 |
| PotVar0063339 | 61.29 |
| PotVar0063157 | 61.29 |
| PotVar0063427 | 63.83 |
| solcap_snp_c2_28632 | 64.48 |
| PotVar0063471 | 65.15 |
| PotVar0063328 | 65.77 |
| solcap_snp_c2_28548 | 65.99 |
| PotVar0069362 | 66.42 |
| PotVar0121994 | 67.38 |
| PotVar0103331 | 67.38 |
| PotVar0096167 | 68.57 |
| PotVar0063060 | 68.57 |
| PotVar0096182 | 68.77 |
| solcap_snp_c1_13116 | 69.3 |

Methods for mapping and linkage map integration in tetraploid potato

| solcap_snp_c2_28635 | 69.3 |
| :---: | :---: |
| PotVar0063169 | 69.3 |
| PotVar0063333 | 69.3 |
| PotVar0063486 | 69.3 |
| PotVar0096216 | 69.41 |
| PotVar0096433 | 69.41 |
| PotVar0063115 | 70.12 |
| PotVar0063501 | 70.3 |
| solcap_snp_c2_34758 | 70.3 |
| solcap_snp_c2_5332 | 70.3 |
| PotVar0096178 | 70.55 |
| PotVar0096223 | 70.55 |
| PotVar0096222 | 70.97 |
| PotVar0096218 | 70.97 |
| PotVar0063283 | 70.98 |
| solcap_snp_c2_52700 | 70.98 |
| solcap_snp_c2_34709 | 70.98 |
| solcap_snp_c2_34698 | 70.98 |
| solcap_snp_c2_34717 | 70.98 |
| PotVar0096416 | 70.98 |
| PotVar0063073 | 70.98 |
| solcap_snp_c2_34710 | 70.98 |
| solcap_snp_c2_16998 | 70.98 |
| solcap_snp_c2_16999 | 70.98 |
| PotVar0096436 | 70.98 |
| PotVar0096290 | 70.98 |
| solcap_snp_c2_36731 | 71.6 |
| PotVar0100204 | 72.06 |
| PotVar0096463 | 72.16 |
| PotVar0100067 | 72.27 |
| solcap_snp_c2_36745 | 72.27 |
| solcap_snp_c2_36777 | 73.36 |
| PotVar0100304 | 73.36 |
| PotVar0100459 | 74.32 |
| PotVar0100389 | 75.11 |
| PotVar0100350 | 75.11 |
| PotVar0100471 | 75.11 |
| PotVar0081240 | 75.11 |
| solcap_snp_c2_19085 | 75.11 |


| PotVar0100388 | 75.27 |
| :---: | :---: |
| PotVar0081131 | 75.64 |
| solcap_snp_c2_56726 | 75.69 |
| PotVar0100045 | 75.69 |
| PotVar0100194 | 75.69 |
| PotVar0100132 | 75.69 |
| PotVar0100303 | 75.69 |
| PotVar0100427 | 75.69 |
| solcap_snp_c2_19080 | 76.79 |
| PotVar0081279 | 77.27 |
| PotVar0119156 | 79.95 |
| PotVar0119174 | 79.95 |
| solcap_snp_c1_10384 | 80.67 |
| PotVar0024022 | 80.72 |
| PotVar0119088 | 80.82 |
| PotVar0119169 | 80.88 |
| PotVar0097448 | 81.12 |
| PotVar0097455 | 81.12 |
| PotVar0097439 | 81.12 |
| solcap_snp_c1_5546 | 81.22 |
| PotVar0119132 | 81.25 |
| solcap_snp_c2_34634 | 81.76 |
| PotVar0119101 | 81.76 |
| solcap_snp_c1_8291 | 81.76 |
| solcap_snp_c1_8235 | 81.76 |
| PotVar0097495 | 82.55 |
| PotVar0097491 | 82.55 |
| PotVar0024073 | 83.01 |
| solcap_snp_c1_8293 | 83.01 |
| PotVar0024020 | 83.01 |
| PotVar0024071 | 83.01 |
| PotVar0097536 | 83.01 |
| PotVar0024064 | 83.01 |
| PotVar0097423 | 83.05 |
| solcap_snp_c1_8297 | 83.05 |
| PotVar0023748 | 83.06 |
| PotVar0023717 | 83.46 |
| PotVar0023875 | 83.46 |
| PotVar0023806 | 83.46 |


| Chromosome 9 |  |
| :--- | :--- |
| Name | cM |


| solcap_snp_c1_5483 | 83.51 |
| :---: | :---: |
| PotVar0097375 | 83.73 |
| solcap_snp_c1_16495 | 85.2 |
| PotVar0024101 | 85.42 |
| PotVar0023678 | 85.64 |
| PotVar0023850 | 85.64 |
| solcap_snp_c1_5499 | 85.85 |
| PotVar0023957 | 86.03 |
| PotVar0024092 | 86.67 |
| solcap_snp_c2_16994 | 86.93 |
| solcap_snp_c1_8282 | 91.93 |
| solcap_snp_c1_5560 | 92.91 |
| PotVar0097615 | 93.18 |
| PotVar0023867 | 93.18 |
| PotVar0023990 | 93.18 |
| PotVar0023981 | 93.18 |
| PotVar0097603 | 93.18 |
| PotVar0023743 | 93.61 |
| PotVar0023689 | 93.61 |
| PotVar0023429 | 94.87 |
| PotVar0023313 | 94.87 |
| solcap_snp_c1_8763 | 94.87 |
| solcap_snp_c1_8760 | 95.09 |
| PotVar0023506 | 95.67 |
| PotVar0023324 | 95.67 |
| solcap_snp_c1_8754 | 95.82 |
| PotVar0023391 | 95.93 |
| PotVar0023563 | 95.93 |
| PotVar0023288 | 95.93 |
| PotVar0023184 | 96.17 |
| PotVar0023583 | 96.29 |
| PotVar0023582 | 96.29 |
| PotVar0023576 | 96.36 |
| PotVar0023409 | 96.36 |
| solcap_snp_c1_5179 | 96.43 |
| PotVar0023140 | 96.8 |
| solcap_snp_c2_28433 | 99.95 |
| PotVar0023579 | 102.85 |


| PotVar0130628 | 4.28 |
| :--- | :--- |
| solcap_snp_c2_48673 | 6.91 |

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| solcap_snp_c1_975 | 6.91 |
| :---: | :---: |
| solcap_snp_c2_48597 | 8.65 |
| solcap_snp_c2_39029 | 9.52 |
| PotVar0114517 | 9.67 |
| PotVar0114492 | 10.33 |
| solcap_snp_c2_39035 | 10.4 |
| solcap_snp_c1_988 | 11.19 |
| PotVar0114434 | 11.41 |
| solcap_snp_c1_1000 | 11.41 |
| solcap_snp_c1_14370 | 11.41 |
| PotVar0011302 | 11.41 |
| PotVar0011714 | 11.75 |
| PotVar0011497 | 12.18 |
| solcap_snp_c2_10966 | 13.01 |
| PotVar0011522 | 13.44 |
| solcap_snp_c2_39091 | 15.76 |
| PotVar0011929 | 18.21 |
| solcap_snp_c2_39084 | 20.88 |
| solcap_snp_c2_39085 | 20.88 |
| PotVar0011885 | 20.92 |
| solcap_snp_c2_39086 | 21.58 |
| solcap_snp_c1_3612 | 25.64 |
| solcap_snp_c2_39082 | 28.03 |
| solcap_snp_c2_39083 | 28.03 |
| solcap_snp_c1_3608 | 29.02 |
| PotVar0011225 | 29.02 |
| PotVar0011713 | 29.02 |
| PotVar0011849 | 29.02 |
| solcap_snp_c2_10958 | 29.02 |
| solcap_snp_c2_10956 | 29.02 |
| PotVar0011481 | 29.02 |
| PotVar0012073 | 30.24 |
| PotVar0012446 | 31.79 |
| PotVar0012077 | 32.42 |
| PotVar0011708 | 32.6 |
| solcap_snp_c2_10906 | 32.6 |
| solcap_snp_c1_3597 | 32.6 |
| PotVar0011839 | 33.28 |
| PotVar0012007 | 33.28 |
| solcap_snp_c2_4165 | 34.49 |
| PotVar0012337 | 35.37 |
| solcap_snp_c2_3962 | 35.6 |
| PotVar0012114 | 36.07 |
| PotVar0012230 | 36.17 |
| PotVar0012274 | 36.17 |


| PotVar0012284 | 36.44 |
| :---: | :---: |
| solcap_snp_c2_3949 | 36.6 |
| solcap_snp_c2_3943 | 36.82 |
| solcap_snp_c2_4192 | 36.82 |
| solcap_snp_c2_10961 | 37.9 |
| PotVar0011361 | 37.9 |
| PotVar0011392 | 37.9 |
| PotVar0011927 | 37.9 |
| solcap_snp_c2_4045 | 37.9 |
| PotVar0011879 | 37.9 |
| PotVar0012050 | 37.9 |
| PotVar0012165 | 37.9 |
| PotVar0012325 | 37.9 |
| PotVar0012533 | 38.21 |
| PotVar0132444 | 38.26 |
| solcap_snp_c2_4415 | 38.78 |
| solcap_snp_c1_13786 | 38.78 |
| solcap_snp_c2_3934 | 39.26 |
| solcap_snp_c2_4048 | 39.5 |
| PotVar0012492 | 39.5 |
| PotVar0073230 | 40.34 |
| PotVar0073342 | 40.34 |
| solcap_snp_c2_52240 | 40.34 |
| solcap_snp_c2_13194 | 41.62 |
| solcap_snp_c1_1420 | 42.36 |
| solcap_snp_c2_3952 | 42.36 |
| solcap_snp_c1_4243 | 42.36 |
| solcap_snp_c2_13188 | 42.36 |
| solcap_snp_c1_4238 | 42.36 |
| PotVar0133733 | 42.36 |
| solcap_snp_c2_13177 | 42.36 |
| PotVar0133858 | 42.36 |
| solcap_snp_c2_13180 | 42.36 |
| PotVar0073321 | 42.36 |
| solcap_snp_c2_35422 | 42.36 |
| solcap_snp_c1_10528 | 42.36 |
| PotVar0133799 | 42.36 |
| PotVar0133086 | 42.36 |
| solcap_snp_c2_3947 | 42.36 |
| solcap_snp_c1_1426 | 42.36 |
| solcap_snp_c2_3953 | 42.36 |
| solcap_snp_c2_3969 | 42.36 |
| PotVar0073418 | 42.36 |
| PotVar0133769 | 42.36 |
| solcap_snp_c2_52241 | 42.43 |


| solcap_snp_c2_13322 | 42.43 |
| :---: | :---: |
| solcap_snp_c2_13317 | 42.43 |
| solcap_snp_c2_35411 | 42.43 |
| solcap_snp_c2_13133 | 43.69 |
| PotVar0133829 | 45.14 |
| solcap_snp_c2_55129 | 45.39 |
| solcap_snp_c1_4228 | 46.51 |
| solcap_snp_c2_13139 | 46.61 |
| solcap_snp_c2_52522 | 47.46 |
| solcap_snp_c2_52519 | 47.46 |
| PotVar0034276 | 48.8 |
| PotVar0034334 | 48.8 |
| PotVar0132961 | 48.8 |
| PotVar0117779 | 49.66 |
| solcap_snp_c2_49770 | 50.49 |
| PotVar0107349 | 50.76 |
| PotVar0012782 | 50.93 |
| PotVar0054648 | 50.93 |
| PotVar0111212 | 50.93 |
| solcap_snp_c2_1484 | 50.93 |
| solcap_snp_c2_21318 | 50.93 |
| solcap_snp_c2_44951 | 50.93 |
| PotVar0054663 | 50.93 |
| PotVar0132977 | 50.93 |
| solcap_snp_c2_50247 | 50.93 |
| solcap_snp_c2_52518 | 50.93 |
| solcap_snp_c2_52521 | 50.93 |
| solcap_snp_c2_52515 | 50.93 |
| solcap_snp_c1_14669 | 50.93 |
| solcap_snp_c2_31988 | 51.42 |
| PotVar0107326 | 51.63 |
| PotVar0007597 | 51.63 |
| solcap_snp_c2_56179 | 51.63 |
| PotVar0131045 | 51.63 |
| PotVar0131220 | 51.63 |
| solcap_snp_c2_21320 | 51.63 |
| PotVar0131152 | 51.63 |
| solcap_snp_c2_53375 | 51.63 |
| PotVar0107313 | 51.63 |
| solcap_snp_c2_58236 | 51.63 |
| solcap_snp_c2_52898 | 51.63 |
| solcap_snp_c2_4381 | 51.63 |
| solcap_snp_c2_4396 | 51.63 |
| solcap_snp_c2_58373 | 51.63 |
| solcap_snp_c2_26515 | 51.63 |

Methods for mapping and linkage map integration in tetraploid potato

| PotVar0054651 | 51.63 |
| :---: | :---: |
| solcap_snp_c2_3205 | 51.63 |
| PotVar0111163 | 51.63 |
| PotVar0111157 | 51.63 |
| solcap_snp_c2_689 | 51.63 |
| PotVar0050913 | 51.63 |
| solcap_snp_c1_14668 | 51.63 |
| solcap_snp_c2_49764 | 51.63 |
| PotVar0051729 | 51.63 |
| PotVar0107348 | 51.63 |
| PotVar0111200 | 51.63 |
| PotVar0131000 | 51.63 |
| PotVar0131102 | 51.63 |
| PotVar0131026 | 51.63 |
| PotVar0007492 | 51.86 |
| solcap_snp_c1_16394 | 51.86 |
| PotVar0007448 | 51.86 |
| PotVar0007613 | 51.86 |
| solcap_snp_c2_23431 | 54.91 |
| solcap_snp_c1_6476 | 55.05 |
| solcap_snp_c2_23439 | 57.46 |
| solcap_snp_c1_7530 | 57.46 |
| solcap_snp_c2_4404 | 57.46 |
| PotVar0054644 | 57.46 |
| PotVar0111226 | 57.46 |
| PotVar0131150 | 57.46 |
| PotVar0131182 | 57.85 |
| solcap_snp_c2_21314 | 57.85 |
| solcap_snp_c2_21331 | 57.85 |
| solcap_snp_c1_8212 | 57.85 |
| solcap_snp_c2_55124 | 57.85 |
| solcap_snp_c2_1514 | 57.85 |
| solcap_snp_c1_364 | 57.85 |
| PotVar0027117 | 57.85 |
| solcap_snp_c2_681 | 57.85 |
| solcap_snp_c1_2319 | 57.85 |
| solcap_snp_c2_6333 | 57.85 |
| solcap_snp_c1_449 | 57.85 |
| solcap_snp_c2_1908 | 57.85 |
| solcap_snp_c2_1511 | 57.85 |
| solcap_snp_c2_680 | 57.85 |
| PotVar0027377 | 57.85 |
| solcap_snp_c1_16738 | 58.39 |
| solcap_snp_c2_4567 | 59.29 |


| solcap_snp_c2_53558 | 59.38 |
| :---: | :---: |
| solcap_snp_c2_22758 | 59.38 |
| solcap_snp_c2_53559 | 59.38 |
| solcap_snp_c2_16276 | 59.85 |
| solcap_snp_c2_20469 | 59.95 |
| PotVar0007465 | 60.19 |
| PotVar0051493 | 60.79 |
| PotVar0051475 | 60.79 |
| PotVar0051101 | 61.08 |
| solcap_snp_c2_20479 | 61.14 |
| PotVar0051195 | 61.29 |
| solcap_snp_c1_12802 | 61.5 |
| solcap_snp_c2_27648 | 61.57 |
| solcap_snp_c2_27644 | 61.57 |
| solcap_snp_c2_27650 | 61.57 |
| PotVar0058507 | 62.29 |
| PotVar0058493 | 63.59 |
| PotVar0058473 | 63.59 |
| PotVar0094024 | 65.81 |
| solcap_snp_c1_11777 | 67.32 |
| solcap_snp_c2_12780 | 67.47 |
| solcap_snp_c2_12761 | 67.47 |
| solcap_snp_c2_44819 | 68.33 |
| solcap_snp_c2_4196 | 69.92 |
| solcap_snp_c 1_4091 | 69.99 |
| solcap_snp_c1_4084 | 69.99 |
| solcap_snp_c2_12781 | 70.43 |
| PotVar0051102 | 70.43 |
| PotVar0051363 | 70.43 |
| PotVar0051027 | 70.43 |
| PotVar0051119 | 70.43 |
| PotVar0051243 | 70.43 |
| PotVar0051276 | 70.43 |
| PotVar0051366 | 70.43 |
| solcap_snp_c1_6192 | 70.43 |
| PotVar0051418 | 70.43 |
| solcap_snp_c1_6176 | 70.43 |
| PotVar0051520 | 70.43 |
| PotVar0051583 | 70.43 |
| PotVar0051499 | 70.43 |
| PotVar0051651 | 70.43 |
| PotVar0051521 | 70.43 |
| solcap_snp_c2_44815 | 70.43 |
| PotVar0082816 | 70.43 |


| solcap_snp_c2_12788 | 70.43 |
| :---: | :---: |
| solcap_snp_c2_12778 | 71.18 |
| solcap_snp_c1_4077 | 71.18 |
| solcap_snp_c2_12779 | 71.18 |
| solcap_snp_c2_12789 | 71.18 |
| solcap_snp_c1_4090 | 71.18 |
| solcap_snp_c2_12760 | 71.18 |
| PotVar0051698 | 71.69 |
| PotVar0051696 | 71.69 |
| PotVar0129337 | 72.55 |
| solcap_snp_c1_13996 | 74 |
| solcap_snp_c2_43032 | 75.18 |
| PotVar0101941 | 75.18 |
| PotVar0058508 | 75.68 |
| solcap_snp_c2_40867 | 77.52 |
| PotVar0129355 | 77.75 |
| PotVar0103851 | 77.83 |
| PotVar0094050 | 79.66 |
| PotVar0093817 | 79.66 |
| solcap_snp_c2_43049 | 80.31 |
| PotVar0094025 | 80.46 |
| PotVar0129259 | 80.46 |
| solcap_snp_c1_16414 | 80.46 |
| PotVar0129270 | 80.46 |
| PotVar0129386 | 80.46 |
| solcap_snp_c1_1425 | 80.46 |
| PotVar0129336 | 81.33 |
| PotVar0118577 | 81.58 |
| PotVar0093997 | 82.9 |
| PotVar0093848 | 82.9 |
| solcap_snp_c1_15041 | 83.32 |
| solcap_snp_c2_26979 | 83.44 |
| solcap_snp_c2_40848 | 83.75 |
| solcap_snp_c2_43031 | 83.75 |
| solcap_snp_c2_26945 | 84.73 |
| PotVar0101691 | 85.92 |
| solcap_snp_c2_42964 | 85.92 |
| PotVar0101814 | 85.92 |
| PotVar0103895 | 86.03 |
| solcap_snp_c2_27054 | 87.66 |
| PotVar0103704 | 87.66 |
| PotVar0103737 | 87.66 |
| PotVar0103788 | 87.66 |
| PotVar0103876 | 90.5 |

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| PotVar0107543 | 90.61 |
| :---: | :---: |
| PotVar0107780 | 92.28 |
| solcap_snp_c1_12178 | 92.49 |
| PotVar0103918 | 92.79 |
| PotVar0118718 | 94.15 |
| solcap_snp_c2_46784 | 94.58 |
| solcap_snp_c1_13886 | 95.44 |
| PotVar0107708 | 95.45 |
| solcap_snp_c2_22003 | 97.43 |
| PotVar0107676 | 97.43 |
| solcap_snp_c1_6936 | 97.43 |
| PotVar0061844 | 98.1 |
| PotVar0061749 | 98.1 |
| PotVar0107475 | 98.31 |
| PotVar0072548 | 99.06 |
| solcap_snp_c2_22040 | 99.4 |
| solcap_snp_c2_22069 | 99.62 |
| PotVar0118727 | 99.85 |
| PotVar0072689 | 100.35 |
| PotVar0072691 | 100.35 |
| PotVar0072578 | 100.35 |
| PotVar0072727 | 101.2 |
| PotVar0072913 | 101.2 |
| PotVar0072996 | 102.05 |
| solcap_snp_c1_12179 | 104.16 |
| solcap_snp_c2_54325 | 104.16 |
| solcap_snp_c2_21992 | 104.97 |
| PotVar0107548 | 104.97 |
| solcap_snp_c2_22076 | 104.97 |
| PotVar0118734 | 104.97 |
| PotVar0061794 | 104.97 |
| PotVar0073127 | 104.97 |
| PotVar0073119 | 104.97 |


| Chromosome 10 |  |
| :--- | ---: |
| Name | cM |
| solcap_snp_c2_950 | 0 |
| solcap_snp_c1_307 | 0 |
| PotVar0065809 | 0 |
| PotVar0065664 | 0 |
| PotVar0116620 | 1.41 |
| PotVar0108387 | 11.87 |
| solcap_snp_c2_24746 | 12.3 |
| PotVar0107947 | 12.3 |


| PotVar0072968 | 104.97 |
| :---: | :---: |
| PotVar0072670 | 104.97 |
| PotVar0011079 | 104.97 |
| PotVar0010985 | 104.97 |
| PotVar0072482 | 104.97 |
| solcap_snp_c 1_11853 | 104.97 |
| solcap_snp_c2_40084 | 104.97 |
| PotVar0105198 | 104.97 |
| PotVar0072477 | 104.97 |
| solcap_snp_c2_29945 | 104.97 |
| PotVar0105291 | 104.97 |
| PotVar0072536 | 104.97 |
| PotVar0072729 | 104.97 |
| PotVar0072917 | 104.97 |
| PotVar0073121 | 104.97 |
| solcap_snp_c1_6585 | 104.97 |
| solcap_snp_c2_20640 | 104.97 |
| PotVar0011160 | 104.97 |
| PotVar0011130 | 104.97 |
| solcap_snp_c1_11866 | 104.97 |
| solcap_snp_c2_40075 | 104.97 |
| PotVar0011129 | 104.97 |
| PotVar0105281 | 104.97 |
| PotVar0105280 | 104.97 |
| PotVar0061732 | 104.97 |
| PotVar0107781 | 104.97 |
| PotVar0107751 | 104.97 |
| solcap_snp_c2_43241 | 105.29 |
| PotVar0011188 | 106.24 |
| PotVar0011164 | 106.24 |
| PotVar0105194 | 106.77 |
| PotVar0108690 | 108.67 |
| solcap_snp_c2_48042 | 108.67 |


| PotVar0107956 | 12.3 |
| :--- | ---: |
| PotVar0116711 | 16.37 |
| PotVar0116629 | 16.37 |
| PotVar0116626 | 17.35 |
| PotVar0065754 | 17.39 |
| solcap_snp_c1_329 | 19.14 |
| solcap_snp_c2_1305 | 19.14 |
| solcap_snp_c2_1101 | 19.33 |
| solcap_snp_c1_289 | 19.33 |
| solcap_snp_c2_1093 | 19.33 |


| PotVar0108699 | 108.67 |
| :---: | :---: |
| solcap_snp_c2_48041 | 109.63 |
| solcap_snp_c2_3079 | 109.78 |
| PotVar0108622 | 110.07 |
| PotVar0108613 | 110.07 |
| PotVar0108629 | 110.07 |
| solcap_snp_c1_914 | 110.65 |
| PotVar0105349 | 110.65 |
| PotVar0105170 | 110.65 |
| PotVar0105228 | 110.65 |
| PotVar0105056 | 110.65 |
| PotVar0108681 | 111.5 |
| PotVar0108689 | 111.5 |
| solcap_snp_c2_47952 | 112.81 |
| PotVar0097335 | 113.13 |
| PotVar0097174 | 113.13 |
| PotVar0097065 | 113.13 |
| PotVar0097245 | 113.13 |
| PotVar0096975 | 113.13 |
| PotVar0108630 | 113.25 |
| solcap_snp_c1_8566 | 113.57 |
| PotVar0122158 | 113.57 |
| solcap_snp_c2_27715 | 113.57 |
| solcap_snp_c2_27765 | 113.57 |
| solcap_snp_c1_8549 | 113.57 |
| solcap_snp_c2_27692 | 113.57 |
| PotVar0097077 | 114.13 |
| PotVar0097004 | 114.13 |
| solcap_snp_c2_27762 | 114.49 |
| solcap_snp_c2_3063 | 115.25 |
| solcap_snp_c2_27719 | 118.19 |
| solcap_snp_c1_8574 | 119.06 |


| PotVar0104004 | 19.76 |
| :--- | :---: |
| PotVar0104010 | 19.76 |
| PotVar0116820 | 20.43 |
| PotVar0116672 | 20.43 |
| solcap_snp_c1_16114 | 20.86 |
| PotVar0120166 | 21.06 |
| PotVar0104285 | 21.09 |
| solcap_snp_c1_9799 | 21.97 |
| solcap_snp_c2_32768 | 22.48 |
| solcap_snp_c1_14048 | 22.48 |

Methods for mapping and linkage map integration in tetraploid potato

| solcap_snp_c1_14053 | 23.49 |
| :---: | :---: |
| solcap_snp_c1_16651 | 23.49 |
| solcap_snp_c2_826 | 23.63 |
| solcap_snp_c1_6068 | 25.72 |
| solcap_snp_c2_33008 | 26.58 |
| solcap_snp_c2_33005 | 26.58 |
| solcap_snp_c1_14531 | 27.02 |
| solcap_snp_c2_24711 | 28.79 |
| PotVar0108182 | 29.1 |
| solcap_snp_c2_24747 | 29.1 |
| PotVar0108271 | 29.1 |
| solcap_snp_c2_24745 | 29.65 |
| solcap_snp_c1_13025 | 30 |
| solcap_snp_c1_13006 | 31.21 |
| PotVar0108442 | 31.53 |
| solcap_snp_c1_12594 | 31.78 |
| solcap_snp_c2_42739 | 31.78 |
| solcap_snp_c2_32790 | 31.97 |
| PotVar0107984 | 32.73 |
| PotVar0108276 | 32.73 |
| PotVar0104021 | 34.02 |
| PotVar0108273 | 34.03 |
| PotVar0108060 | 34.03 |
| solcap_snp_c2_19222 | 34.04 |
| solcap_snp_c2_19223 | 34.04 |
| solcap_snp_c2_19225 | 34.48 |
| PotVar0108199 | 35.06 |
| PotVar0107954 | 35.06 |
| solcap_snp_c2_1263 | 35.06 |
| PotVar0120148 | 35.22 |
| PotVar0120165 | 35.22 |
| PotVar0108099 | 35.34 |
| solcap_snp_c2_57296 | 36.66 |
| PotVar0029603 | 38.4 |
| solcap_snp_c2_55085 | 39.11 |
| PotVar0131630 | 39.72 |
| PotVar0131645 | 40.4 |
| PotVar0131644 | 40.4 |
| solcap_snp_c2_32740 | 40.62 |
| solcap_snp_c1_11801 | 40.62 |
| PotVar0112028 | 40.62 |
| PotVar0112050 | 40.62 |
| PotVar0112053 | 40.62 |
| solcap_snp_c2_40522 | 40.62 |


| PotVar0007417 | 40.62 |
| :---: | :---: |
| PotVar0099300 | 40.62 |
| PotVar0004372 | 40.62 |
| solcap_snp_c2_18265 | 40.62 |
| PotVar0119513 | 40.62 |
| PotVar0119518 | 40.62 |
| PotVar0099304 | 40.62 |
| PotVar0004373 | 40.62 |
| PotVar0085827 | 40.62 |
| PotVar0080928 | 40.62 |
| PotVar0123577 | 40.62 |
| solcap_snp_c1_11806 | 40.62 |
| solcap_snp_c2_48927 | 41.26 |
| solcap_snp_c2_40822 | 41.9 |
| PotVar0096861 | 44.33 |
| PotVar0051881 | 47.78 |
| solcap_snp_c2_48929 | 47.78 |
| solcap_snp_c2_48928 | 47.78 |
| solcap_snp_c1_12027 | 47.78 |
| PotVar0051833 | 47.78 |
| PotVar0051902 | 47.78 |
| PotVar0106287 | 47.78 |
| solcap_snp_c2_38274 | 49.47 |
| PotVar0051879 | 49.57 |
| PotVar0051918 | 49.9 |
| solcap_snp_c2_41395 | 51.76 |
| solcap_snp_c2_41396 | 51.76 |
| solcap_snp_c2_54951 | 51.76 |
| solcap_snp_c2_41393 | 51.99 |
| solcap_snp_c2_56514 | 52.89 |
| solcap_snp_c1_11535 | 54.29 |
| PotVar0119199 | 54.29 |
| solcap_snp_c2_48926 | 54.79 |
| solcap_snp_c1_12024 | 54.79 |
| solcap_snp_c1_11991 | 54.79 |
| solcap_snp_c2_57635 | 54.79 |
| $\begin{aligned} & \text { solcap_TUBER_SHAPE_c2_2 } \\ & 5527 \end{aligned}$ | 54.79 |
| $\begin{aligned} & \text { solcap_TUBER_SHAPE_c2_2 } \\ & 5528 \end{aligned}$ | 54.79 |
| $\begin{aligned} & \text { solcap_TUBER_SHAPE_c2_2 } \\ & 5529 \end{aligned}$ | 54.79 |
| solcap_snp_c2_45611 | 54.79 |
| solcap_snp_c1_8021 | 54.79 |


| solcap_snp_c2_25469 | 54.79 |
| :---: | :---: |
| solcap_snp_c2_40762 | 55.48 |
| solcap_snp_c2_40765 | 55.48 |
| solcap_snp_c2_40763 | 55.48 |
| solcap_snp_c1_16001 | 56.29 |
| PotVar0132240 | 56.63 |
| solcap_snp_c2_27806 | 56.68 |
| solcap_snp_c2_56344 | 56.92 |
| solcap_snp_c1_13524 | 56.92 |
| $\begin{aligned} & \text { solcap_TUBER_SHAPE_c2_2 } \\ & 5532 \end{aligned}$ | 57.56 |
| solcap_snp_c1_8020 | 57.88 |
| solcap_snp_c1_16351 | 57.88 |
| $\begin{aligned} & \text { solcap_TUBER_SHAPE_c2_2 } \\ & 5530 \end{aligned}$ | 57.88 |
| $\begin{aligned} & \text { solcap_TUBER_SHAPE_c2_2 } \\ & 5523 \end{aligned}$ | 58.56 |
| solcap_snp_c2_45603 | 59.35 |
| solcap_snp_c2_56515 | 60.38 |
| solcap_snp_c2_45612 | 61.03 |
| PotVar0111683 | 62.35 |
| PotVar0134570 | 62.52 |
| solcap_snp_c1_15698 | 62.52 |
| solcap_snp_c2_25549 | 63.21 |
| solcap_snp_c1_8018 | 63.21 |
| solcap_snp_c2_51215 | 64.22 |
| solcap_snp_c2_51202 | 65.31 |
| PotVar0004484 | 67.32 |
| solcap_snp_c1_15218 | 72.56 |
| solcap_snp_c2_27827 | 72.56 |
| PotVar0004666 | 73.41 |
| PotVar0004674 | 73.41 |
| PotVar0004562 | 73.41 |
| PotVar0004795 | 75.9 |
| PotVar0004719 | 76.53 |
| PotVar0004792 | 76.96 |
| PotVar0004789 | 76.96 |
| solcap_snp_c1_4989 | 76.96 |
| solcap_snp_c1_14236 | 76.96 |
| PotVar0005549 | 77.11 |
| PotVar0005644 | 77.56 |
| PotVar0005662 | 77.56 |
| PotVar0004885 | 78.71 |
| solcap_snp_c2_48127 | 78.92 |

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| solcap_snp_c1_9059 | 80.23 |
| :---: | :---: |
| solcap_snp_c1_7187 | 80.66 |
| PotVar0005589 | 81.1 |
| PotVar0005681 | 81.31 |
| solcap_snp_c1_7148 | 81.31 |
| solcap_snp_c1_7165 | 81.31 |
| PotVar0058133 | 81.31 |
| PotVar0058175 | 81.31 |
| PotVar0057954 | 81.31 |
| PotVar0058146 | 81.52 |
| PotVar0057984 | 82.39 |
| PotVar0058094 | 82.39 |
| PotVar0057840 | 83.59 |
| PotVar0005590 | 83.71 |
| PotVar0005666 | 83.71 |
| PotVar0057888 | 83.91 |
| PotVar0057846 | 83.91 |
| PotVar0057905 | 84.23 |
| solcap_snp_c1_9058 | 84.56 |
| solcap_snp_c2_45239 | 84.87 |
| PotVar0057605 | 84.87 |
| PotVar0122838 | 84.87 |


| PotVar0122771 | 84.87 |
| :--- | ---: |
| PotVar0005256 | 85.24 |
| PotVar0005016 | 85.5 |
| PotVar0057431 | 85.64 |
| PotVar0122647 | 86.09 |
| PotVar0122661 | 86.09 |
| PotVar0122870 | 86.09 |
| PotVar0122826 | 86.09 |
| PotVar0122866 | 89.6 |
| PotVar0122679 | 90.03 |
| PotVar0122649 | 90.03 |
| PotVar0122859 | 90.03 |
| PotVar0122765 | 90.03 |
| PotVar0057719 | 90.88 |
| PotVar0057860 | 92.07 |
| PotVar0057721 | 92.31 |
| PotVar0057500 | 92.31 |
| PotVar0057635 | 92.74 |
| solcap_snp_c2_28789 | 93.4 |
| PotVar0057421 | 95.38 |
| PotVar0122775 | solcap_snp_c1_13243 |


| Chromosome 11 |  |
| :--- | ---: |
| Name | cM |
| PotVar0064140 | 0 |
| PotVar0064625 | 0 |
| PotVar0063963 | 8.02 |
| solcap_snp_c2_13350 | 8.02 |
| PotVar0063984 | 8.02 |
| PotVar0063965 | 9.18 |
| solcap_snp_c1_4296 | 9.6 |
| PotVar0064617 | 10.04 |
| PotVar0064549 | 10.04 |
| PotVar0064694 | 10.04 |
| PotVar0064699 | 10.04 |
| PotVar0064474 | 10.04 |
| solcap_snp_c1_4322 | 10.47 |
| solcap_snp_c1_4319 | 10.47 |
| PotVar0064182 | 11.16 |
| solcap_snp_c1_4336 | 11.34 |
| solcap_snp_c2_37194 | 12.2 |
| PotVar0064663 | 12.46 |
| PotVar0122617 | 12.63 |
|  |  |


| PotVar0066165 | 12.63 |
| :--- | ---: |
| solcap_snp_c1_4347 | 15.44 |
| solcap_snp_c2_33657 | 19.36 |
| PotVar0066338 | 19.36 |
| PotVar0066186 | 20.67 |
| PotVar0066210 | 20.67 |
| PotVar0066142 | 20.67 |
| PotVar0064787 | 20.81 |
| PotVar0066219 | 22.35 |
| PotVar0064963 | 23.53 |
| PotVar0067013 | 23.53 |
| PotVar0066299 | 23.85 |
| PotVar0064473 | 24.96 |
| PotVar0066476 | 28.21 |
| PotVar0066709 | 28.21 |
| PotVar0067177 | 28.21 |
| PotVar0067029 | 28.21 |
| PotVar0067330 | 29.08 |
| PotVar0067381 | 29.08 |
| PotVar0067565 | 29.52 |
| PotVar0067682 | 29.52 |


| PotVar0122789 | 95.38 |
| :--- | ---: |
| PotVar0122668 | 96.09 |
| PotVar0122690 | 96.09 |
| solcap_snp_c1_12236 | 96.09 |
| solcap_snp_c1_12234 | 96.53 |
| solcap_snp_c1_12229 | 96.53 |
| solcap_snp_c1_12224 | 96.75 |
| PotVar0057515 | 99.74 |
|  | 100.6 |
| PotVar0057514 | 5 |
|  | 100.6 |
| PotVar0057644 | 5 |
|  | 107.4 |
| solcap_snp_c2_28740 | 5 |
|  | 108.7 |
| solcap_snp_c2_28697 | 5 |
| PotVar0122769 | 109.8 |
| PotVar0122635 | 3 |
| solcap_snp_c2_45023 | 309.8 |


| solcap_snp_c2_6173 | 29.94 |
| :--- | ---: |
| PotVar0067403 | 30.37 |
| PotVar0110497 | 30.37 |
| PotVar0067477 | 30.44 |
| PotVar0067345 | 30.44 |
| PotVar0067018 | 30.85 |
| PotVar0067025 | 30.85 |
| PotVar0067303 | 30.85 |
| PotVar0067187 | 30.85 |
| PotVar0067347 | 31.55 |
| PotVar0067438 | 31.55 |
| PotVar0110434 | 32.17 |
| PotVar0105739 | 35.25 |
| PotVar0105649 | 35.25 |
| solcap_snp_c1_2314 | 35.3 |
| PotVar0105481 | 37.1 |
| PotVar0105750 | 37.1 |
| PotVar0106272 | 37.1 |
| PotVar0067664 | 37.1 |
| PotVar0105904 | 37.1 |
| PotVar0106051 | 39.1 |
|  |  |

Methods for mapping and linkage map integration in tetraploid potato

| PotVar0106025 | 39.1 |
| :---: | :---: |
| solcap_snp_c1_14083 | 39.1 |
| solcap_snp_c1_16496 | 39.53 |
| solcap_snp_c1_11246 | 40.41 |
| solcap_snp_c2_20947 | 40.41 |
| solcap_snp_c2_20941 | 40.41 |
| PotVar0106087 | 42.51 |
| solcap_snp_c2_37638 | 42.51 |
| solcap_snp_c2_57917 | 42.73 |
| solcap_snp_c1_16301 | 43.37 |
| PotVar0106089 | 43.37 |
| PotVar0106072 | 43.37 |
| solcap_snp_c2_21053 | 46.1 |
| PotVar0058600 | 46.1 |
| solcap_snp_c1_7658 | 46.44 |
| PotVar0105987 | 47.17 |
| PotVar0058653 | 48.62 |
| solcap_snp_c2_23921 | 48.82 |
| PotVar0105735 | 49.7 |
| PotVar0066337 | 49.7 |
| PotVar0105694 | 50.97 |
| solcap_snp_c2_20946 | 52.27 |
| solcap_snp_c1_6644 | 52.27 |
| PotVar0059041 | 52.47 |
| PotVar0060167 | 52.47 |
| solcap_snp_c2_20953 | 52.79 |
| PotVar0059223 | 53.71 |
| PotVar0059116 | 53.81 |
| solcap_snp_c2_24318 | 53.89 |
| PotVar0059988 | 53.89 |
| PotVar0060007 | 53.89 |
| PotVar0059286 | 54.56 |
| PotVar0059315 | 54.56 |
| PotVar0058597 | 54.93 |
| PotVar0059581 | 55.85 |
| PotVar0059692 | 55.85 |
| PotVar0059736 | 55.85 |
| PotVar0059554 | 55.85 |
| PotVar0059121 | 55.89 |
| solcap_snp_c2_49311 | 56.05 |
| PotVar0059889 | 56.28 |
| PotVar0059714 | 56.92 |
| PotVar0059682 | 56.92 |
| PotVar0059394 | 57.01 |


| PotVar0058763 | 57.16 |
| :---: | :---: |
| solcap_snp_c2_2896 | 57.16 |
| solcap_snp_c2_12297 | 57.78 |
| PotVar0058578 | 58.6 |
| PotVar0058729 | 58.7 |
| PotVar0059284 | 61.49 |
| PotVar0059055 | 61.85 |
| PotVar0059608 | 61.92 |
| PotVar0059886 | 61.92 |
| PotVar0059811 | 61.92 |
| PotVar0059222 | 62.12 |
| PotVar0059351 | 62.12 |
| solcap_snp_c2_12276 | 62.83 |
| PotVar0059951 | 62.83 |
| PotVar0059796 | 64.77 |
| PotVar0059350 | 65.56 |
| PotVar0059593 | 65.56 |
| PotVar0059779 | 65.56 |
| PotVar0060119 | 65.56 |
| PotVar0060181 | 65.56 |
| solcap_snp_c2_32997 | 65.56 |
| solcap_snp_c2_32994 | 65.56 |
| PotVar0060232 | 65.56 |
| PotVar0059280 | 65.56 |
| PotVar0059677 | 66.07 |
| PotVar0059598 | 66.07 |
| PotVar0059401 | 66.62 |
| PotVar0060133 | 67.48 |
| solcap_snp_c2_53682 | 67.48 |
| solcap_snp_c2_56630 | 67.64 |
| solcap_snp_c2_49294 | 67.91 |
| PotVar0060023 | 67.91 |
| solcap_snp_c2_53678 | 67.91 |
| PotVar0059066 | 68.5 |
| PotVar0059128 | 68.93 |
| PotVar0059696 | 70.23 |
| PotVar0060154 | 71.09 |
| solcap_snp_c1_15655 | 71.09 |
| PotVar0060183 | 71.09 |
| solcap_snp_c2_56623 | 73.91 |
| PotVar0060312 | 73.91 |
| solcap_snp_c2_33911 | 73.91 |
| solcap_snp_c2_32337 | 73.91 |
| solcap_snp_c2_29089 | 73.91 |


| solcap_snp_c2_29096 | 73.91 |
| :---: | :---: |
| solcap_snp_c1_3992 | 75.01 |
| PotVar0060365 | 75.18 |
| solcap_snp_c2_12263 | 75.32 |
| PotVar0060051 | 75.32 |
| PotVar0059973 | 75.32 |
| PotVar0060091 | 75.32 |
| solcap_snp_c2_32999 | 75.32 |
| PotVar0060082 | 75.32 |
| solcap_snp_c2_33917 | 76.55 |
| PotVar0130698 | 77.15 |
| PotVar0054040 | 77.46 |
| PotVar0060496 | 77.52 |
| solcap_snp_c2_56629 | 77.57 |
| solcap_snp_c2_56627 | 77.57 |
| solcap_snp_c2_57107 | 77.57 |
| PotVar0059933 | 77.57 |
| solcap_snp_c2_12259 | 77.57 |
| PotVar0054058 | 77.97 |
| PotVar0054079 | 77.97 |
| PotVar0021602 | 78.98 |
| PotVar0101542 | 78.98 |
| PotVar0101550 | 78.98 |
| PotVar0113358 | 78.98 |
| PotVar0061519 | 79.42 |
| solcap_snp_c2_50977 | 79.42 |
| PotVar0060273 | 79.85 |
| solcap_snp_c2_33916 | 79.85 |
| PotVar0060548 | 79.85 |
| solcap_snp_c2_29088 | 79.85 |
| solcap_snp_c2_29113 | 79.85 |
| PotVar0054261 | 80.59 |
| solcap_snp_c2_37586 | 80.84 |
| PotVar0054060 | 80.99 |
| solcap_snp_c2_50332 | 81.02 |
| solcap_snp_c2_29434 | 81.02 |
| PotVar0054073 | 81.27 |
| solcap_snp_c2_11364 | 81.28 |
| solcap_snp_c2_11366 | 81.28 |
| PotVar0061347 | 82.02 |
| PotVar0053942 | 82.12 |
| solcap_snp_c2_57617 | 82.12 |
| solcap_snp_c2_50980 | 82.12 |
| PotVar0113312 | 82.12 |

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| solcap_snp_c2_31444 | 82.29 |
| :---: | :---: |
| PotVar0005842 | 82.44 |
| PotVar0005888 | 82.44 |
| solcap_snp_c2_41084 | 82.78 |
| PotVar0054330 | 82.78 |
| PotVar0054089 | 82.78 |
| PotVar0005899 | 82.78 |
| solcap_snp_c2_31472 | 83.16 |
| solcap_snp_c1_9499 | 83.16 |
| PotVar0021746 | 83.36 |
| PotVar0021631 | 83.36 |
| PotVar0130677 | 83.48 |
| solcap_snp_c1_16325 | 83.48 |
| PotVar0061719 | 83.78 |
| PotVar0061379 | 83.78 |
| solcap_snp_c2_4961 | 83.91 |
| solcap_snp_c1_5940 | 83.91 |
| solcap_snp_c1_16555 | 83.91 |
| solcap_snp_c2_18245 | 83.91 |
| solcap_snp_c2_18526 | 83.91 |
| solcap_snp_c1_14951 | 83.91 |
| PotVar0021694 | 83.91 |
| solcap_snp_c1_1781 | 83.91 |
| solcap_snp_c1_1779 | 83.91 |
| solcap_snp_c1_1778 | 83.91 |
| solcap_snp_c2_44637 | 83.91 |
| solcap_snp_c2_44635 | 83.91 |
| PotVar0022012 | 83.91 |
| solcap_snp_c1_1784 | 84.07 |
| solcap_snp_c1_5411 | 84.07 |
| solcap_snp_c2_16709 | 84.07 |
| solcap_snp_c2_17332 | 84.07 |
| solcap_snp_c2_4989 | 84.07 |
| solcap_snp_c1_1774 | 84.07 |
| PotVar0021898 | 84.07 |
| solcap_snp_c2_4957 | 84.07 |
| solcap_snp_c1_5942 | 84.53 |
| solcap_snp_c1_16586 | 84.53 |
| solcap_snp_c2_4993 | 84.76 |
| PotVar0021994 | 84.76 |
| solcap_snp_c2_2957 | 84.76 |
| solcap_snp_c1_16585 | 84.76 |
| solcap_snp_c2_44633 | 84.86 |
| solcap_snp_c1_5965 | 84.98 |
| PotVar0061673 | 85.78 |


| solcap_snp_c1_12160 | 85.78 |
| :---: | :---: |
| solcap_snp_c1_5716 | 85.78 |
| PotVar0005841 | 85.78 |
| PotVar0061578 | 86.1 |
| PotVar0061301 | 86.22 |
| solcap_snp_c1_1468 | 86.22 |
| solcap_snp_c1_1470 | 86.22 |
| PotVar0061300 | 86.22 |
| solcap_snp_c2_4276 | 86.44 |
| solcap_snp_c2_53718 | 86.44 |
| solcap_snp_c2_30368 | 86.44 |
| solcap_snp_c2_30367 | 86.44 |
| solcap_snp_c1_12078 | 87.16 |
| solcap_snp_c2_36581 | 87.16 |
| solcap_snp_c2_55963 | 87.16 |
| PotVar0110595 | 87.16 |
| PotVar0110592 | 87.16 |
| solcap_snp_c1_4371 | 87.16 |
| solcap_snp_c2_13636 | 87.16 |
| solcap_snp_c2_44269 | 87.33 |
| PotVar0071276 | 87.33 |
| solcap_snp_c2_3841 | 89.18 |
| PotVar0047274 | 89.18 |
| solcap_snp_c1_4359 | 89.18 |
| solcap_snp_c2_41083 | 89.32 |
| solcap_snp_c2_13633 | 89.8 |
| solcap_snp_c2_56243 | 89.8 |
| solcap_snp_c2_13632 | 89.8 |
| solcap_snp_c2_51545 | 90.11 |
| solcap_snp_c2_51544 | 90.11 |
| solcap_snp_c2_49808 | 91.91 |
| solcap_snp_c1_4822 | 92.23 |
| solcap_snp_c2_3805 | 92.57 |
| PotVar0112755 | 92.57 |
| solcap_snp_c2_3679 | 92.67 |
| solcap_snp_c2_54589 | 92.68 |
| PotVar0112934 | 93.13 |
| solcap_snp_c2_13593 | 93.89 |
| solcap_snp_c2_13594 | 94.11 |
| solcap_snp_c2_31433 | 94.11 |
| solcap_snp_c2_31484 | 94.11 |
| solcap_snp_c2_31443 | 94.11 |
| solcap_snp_c2_14952 | 94.11 |
| solcap_snp_c1_15081 | 94.11 |
| solcap_snp_c2_14946 | 94.11 |


| solcap_snp_c1_4376 | 94.98 |
| :---: | :---: |
| solcap_snp_c2_13613 | 96.27 |
| PotVar0110626 | 96.87 |
| solcap_snp_c2_49812 | 97.79 |
| PotVar0047211 | 98.44 |
| PotVar0008666 | 98.64 |
| PotVar0008668 | 98.64 |
| PotVar0008826 | 99.07 |
| PotVar0124397 | 99.5 |
| PotVar0047409 | 100.14 |
| PotVar0118030 | 100.37 |
| PotVar0047229 | 100.93 |
| PotVar0113183 | 101.45 |
| solcap_snp_c2_3691 | 102.27 |
| solcap_snp_c2_3823 | 102.27 |
| PotVar0113080 | 102.27 |
| PotVar0112873 | 102.27 |
| PotVar0112981 | 102.27 |
| PotVar0112613 | 102.27 |
| PotVar0112532 | 102.27 |
| PotVar0112664 | 102.27 |
| PotVar0112736 | 102.27 |
| PotVar0112743 | 102.27 |
| PotVar0112967 | 102.27 |
| PotVar0112987 | 102.27 |
| PotVar0113261 | 102.27 |
| PotVar0113195 | 102.27 |
| Plocus_F35H_a2_LG11 | 102.37 |
| Plocus_F35H_c2_LG11 | 102.37 |
| Plocus_F35H_a1_LG11 | 102.37 |
| PotVar0112167 | 102.7 |
| PotVar0008128 | 102.7 |
| PotVar0112185 | 102.7 |
| PotVar0008113 | 102.7 |
| PotVar0112275 | 103.14 |
| PotVar0047372 | 103.18 |
| PotVar0112668 | 103.24 |
| PotVar0112779 | 103.24 |
| PotVar0113131 | 103.24 |
| PotVar0113193 | 103.24 |
| PotVar0112357 | 103.24 |
| PotVar0112455 | 103.24 |
| PotVar0113005 | 103.24 |
| PotVar0112971 | 103.24 |
| PotVar0112957 | 103.99 |

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| solcap_snp_c1_1323 | 104.06 |
| :--- | ---: |
| PotVar0113059 | 106.37 |
| PotVar0112205 | 106.43 |
| PotVar0112286 | 106.8 |
| PotVar0112207 | 106.88 |
| PotVar0008146 | 106.88 |
| PotVar0008149 | 106.88 |
| solcap_snp_c2_15388 | 106.88 |
| PotVar0008184 | 107.71 |
| PotVar0008553 | 107.85 |
| solcap_snp_c1_4947 | 108.14 |
| PotVar0008220 | 108.14 |
| PotVar0008239 | 108.14 |
| solcap_snp_c1_1271 | 108.21 |
| PotVar0112968 | 108.21 |
| solcap_snp_c2_56752 | 108.21 |
| PotVar0008243 | 109.68 |
| PotVar0112739 | 110.43 |
| PotVar0112531 | 110.43 |
| solcap_snp_c2_15268 | 111.66 |
| PotVar0008207 | 111.9 |
| solcap_snp_c2_22187 | 112.2 |
| solcap_snp_c1_6964 | 12.2 |


| solcap_snp_c2_15340 | 113.22 |
| :--- | ---: |
| PotVar0008494 | 113.66 |
| solcap_snp_c2_30298 | 113.66 |
| PotVar0008262 | 113.66 |
| PotVar0008237 | 114.96 |
| PotVar0008194 | 115.28 |
| solcap_snp_c2_15341 | 115.39 |
| PotVar0008636 | 115.47 |
| PotVar0008569 | 115.9 |
| PotVar0008903 | 116.75 |
| PotVar0008904 | 117.18 |
| PotVar0008281 | 117.91 |
| PotVar0008279 | 117.91 |
| PotVar0008293 | 117.91 |
| PotVar0130354 | 118.05 |
| PotVar0130423 | 118.48 |
| PotVar0124367 | 118.91 |
| solcap_snp_c2_34229 | 119.77 |
| PotVar0117920 | 120.63 |
| PotVar0117899 | 120.63 |
| solcap_snp_c2_34194 | 120.63 |
| solcap_snp_c2_31579 | 120.94 |
| PotVar0118016 | 121.09 |


| Chromosome 12 |  |
| :--- | ---: |
| Name | cM |
| PotVar0098059 | 0 |
| solcap_snp_c2_24595 | 0.63 |
| solcap_snp_c2_24536 | 4.31 |
| PotVar0098080 | 4.31 |
| PotVar0098277 | 4.31 |
| PotVar0097963 | 4.31 |
| PotVar0098047 | 4.31 |
| PotVar0098087 | 4.31 |
| PotVar0097922 | 5.28 |
| PotVar0097926 | 5.28 |
| PotVar0098023 | 5.28 |
| PotVar0098373 | 6.59 |
| PotVar0098367 | 7.03 |
| PotVar0098245 | 7.88 |
| PotVar0098172 | 10.75 |
| PotVar0098280 | 10.75 |
| PotVar0098129 | 10.75 |


| PotVar0098260 | 14.27 |
| :--- | ---: |
| PotVar0097929 | 14.27 |
| PotVar0098257 | 14.27 |
| PotVar0098049 | 14.27 |
| PotVar0098071 | 14.37 |
| PotVar0098029 | 14.37 |
| PotVar0053656 | 14.47 |
| PotVar0053573 | 15.59 |
| PotVar0022107 | 16.5 |
| PotVar0053636 | 16.96 |
| solcap_snp_c2_16182 | 17.41 |
| PotVar0053705 | 18.16 |
| PotVar0053701 | 18.44 |
| PotVar0068409 | 19.76 |
| solcap_snp_c2_31338 | 19.76 |
| solcap_snp_c1_8646 | 19.76 |
| solcap_snp_c2_31337 | 19.92 |
| PotVar0053907 | 19.92 |
| PotVar0053841 |  |


| solcap_snp_c2_34193 | 121.09 |
| :--- | ---: |
| solcap_snp_c2_34191 | 121.09 |
| solcap_snp_c2_34204 | 121.09 |
| PotVar0118308 | 121.54 |
| PotVar0118401 | 121.97 |
| PotVar0008554 | 122.79 |
| PotVar0117889 | 123.7 |
| solcap_snp_c2_30297 | 125.82 |
| PotVar0008637 | 126.3 |
| PotVar0008380 | 127.58 |
| PotVar0008447 | 128.44 |
| PotVar0008511 | 128.87 |
| PotVar0124374 | 130.26 |
| PotVar0008887 | 132.44 |
| PotVar0130497 | 132.44 |
| PotVar0130503 | 132.44 |
| PotVar0130324 | 133.72 |
| PotVar0008860 | 135.08 |
| solcap_snp_c2_43880 | 135.42 |
| PotVar0130323 |  |
| PotVar0118026 | 135 |
| PotVar0118303 | 1 |


| PotVar0031150 | 20.16 |
| :--- | :---: |
| PotVar0031559 | 20.16 |
| PotVar0031644 | 20.16 |
| PotVar0031118 | 20.16 |
| PotVar0031194 | 20.16 |
| PotVar0069242 | 20.16 |
| PotVar0031212 | 20.16 |
| PotVar0053629 | 20.62 |
| PotVar0053659 | 20.62 |
| solcap_snp_c2_39765 | 20.62 |
| PotVar0053855 | 20.62 |
| PotVar0068881 | 20.62 |
| PotVar0068893 | 20.62 |
| PotVar0068793 | 20.62 |
| PotVar0031174 | 20.81 |
| solcap_snp_c2_16204 | 21.24 |
| PotVar0053640 | 21.24 |
| PotVar0031093 | 21.25 |
| PotVar0031195 | 21.25 |

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| PotVar0031564 | 21.25 |
| :---: | :---: |
| PotVar0125939 | 21.68 |
| PotVar0053859 | 21.68 |
| PotVar0053790 | 21.68 |
| PotVar0053791 | 21.68 |
| PotVar0069011 | 21.68 |
| PotVar0068642 | 21.68 |
| PotVar0031023 | 21.68 |
| PotVar0031664 | 21.68 |
| PotVar0030968 | 21.68 |
| PotVar0031039 | 21.68 |
| PotVar0031117 | 21.68 |
| PotVar0031277 | 21.68 |
| PotVar0031560 | 21.68 |
| PotVar0068972 | 21.68 |
| PotVar0031645 | 21.68 |
| PotVar0031514 | 21.68 |
| PotVar0031207 | 21.68 |
| PotVar0030960 | 21.68 |
| PotVar0031147 | 21.68 |
| PotVar0031136 | 21.68 |
| PotVar0068822 | 21.68 |
| PotVar0068849 | 21.68 |
| PotVar0068584 | 21.68 |
| PotVar0069135 | 21.68 |
| PotVar0053739 | 21.68 |
| PotVar0031211 | 21.68 |
| PotVar0068890 | 21.68 |
| PotVar0069075 | 21.68 |
| PotVar0069136 | 21.68 |
| PotVar0030982 | 21.68 |
| PotVar0068587 | 21.68 |
| PotVar0031599 | 22.54 |
| PotVar0053857 | 23.68 |
| PotVar0053914 | 23.68 |
| PotVar0069155 | 23.84 |
| PotVar0069259 | 23.84 |
| PotVar0068428 | 23.84 |
| PotVar0068889 | 23.84 |
| solcap_snp_c1_8641 | 24.12 |
| PotVar0031486 | 24.58 |
| PotVar0031530 | 24.58 |
| PotVar0031589 | 24.58 |
| PotVar0068194 | 25.21 |
| PotVar0068187 | 25.41 |


| solcap_snp_c2_28012 | 25.6 |
| :---: | :---: |
| PotVar0132363 | 27.24 |
| PotVar0068383 | 27.24 |
| PotVar0069139 | 27.24 |
| PotVar0068447 | 27.24 |
| PotVar0068253 | 27.24 |
| PotVar0068388 | 27.77 |
| solcap_snp_c2_24645 | 28.91 |
| solcap_snp_c2_46296 | 29.14 |
| solcap_snp_c2_46289 | 30.32 |
| solcap_snp_c1_13767 | 30.32 |
| solcap_snp_c2_46285 | 31.3 |
| PotVar0068182 | 32.38 |
| PotVar0061979 | 33.41 |
| solcap_snp_c2_46299 | 33.49 |
| solcap_snp_c2_40699 | 33.6 |
| solcap_snp_c2_24650 | 34.09 |
| PotVar0061959 | 34.46 |
| PotVar0118812 | 34.96 |
| solcap_snp_c2_34789 | 35.52 |
| PotVar0061956 | 35.52 |
| PotVar0118838 | 36.4 |
| PotVar0118853 | 36.4 |
| solcap_snp_c2_34762 | 36.4 |
| PotVar0061934 | 36.4 |
| solcap_snp_c2_34780 | 36.65 |
| solcap_snp_c2_34806 | 37.94 |
| PotVar0027783 | 38.1 |
| PotVar0027729 | 38.1 |
| PotVar0061899 | 38.5 |
| PotVar0061906 | 38.6 |
| solcap_snp_c2_27379 | 38.6 |
| PotVar0027810 | 38.6 |
| PotVar0027811 | 38.74 |
| PotVar0027707 | 38.81 |
| PotVar0027746 | 38.81 |
| solcap_snp_c2_48900 | 38.81 |
| PotVar0027678 | 39.24 |
| PotVar0066128 | 40.1 |
| solcap_snp_c2_44932 | 40.1 |
| solcap_snp_c2_16286 | 40.1 |
| solcap_snp_c2_45743 | 40.1 |
| solcap_snp_c2_48391 | 40.1 |
| PotVar0082752 | 40.1 |
| solcap_snp_c2_57161 | 40.1 |


| solcap_snp_c2_4214 | 40.1 |
| :---: | :---: |
| PotVar0012947 | 40.1 |
| PotVar0013114 | 40.1 |
| PotVar0036483 | 40.1 |
| PotVar0036410 | 40.1 |
| solcap_snp_c1_10054 | 40.1 |
| PotVar0012951 | 40.82 |
| solcap_snp_c1_8914 | 40.82 |
| PotVar0066107 | 41 |
| solcap_snp_c2_44928 | 41 |
| solcap_snp_c2_44926 | 41 |
| PotVar0044799 | 41.16 |
| PotVar0118860 | 41.31 |
| solcap_snp_c2_57453 | 41.38 |
| solcap_snp_c2_48890 | 41.74 |
| solcap_snp_c2_16299 | 41.75 |
| PotVar0044792 | 41.75 |
| solcap_snp_c2_10055 | 41.75 |
| PotVar0014978 | 41.75 |
| solcap_snp_c2_27773 | 41.75 |
| PotVar0012912 | 41.75 |
| PotVar0036461 | 41.75 |
| solcap_snp_c2_27771 | 41.75 |
| PotVar0027702 | 42.08 |
| solcap_snp_c2_53383 | 42.08 |
| solcap_snp_c1_403 | 42.08 |
| PotVar0037501 | 42.1 |
| PotVar0037523 | 42.1 |
| solcap_snp_c2_54917 | 42.19 |
| solcap_snp_c2_3185 | 42.19 |
| PotVar0027759 | 42.19 |
| PotVar0019164 | 42.32 |
| PotVar0036430 | 42.32 |
| PotVar0087430 | 42.32 |
| PotVar0095247 | 42.32 |
| solcap_snp_c2_49334 | 42.32 |
| PotVar0019161 | 42.32 |
| solcap_snp_c2_48013 | 42.42 |
| solcap_snp_c1_14767 | 42.42 |
| solcap_snp_c1_8913 | 42.42 |
| solcap_snp_c1_13066 | 42.42 |
| PotVar0036521 | 42.42 |
| solcap_snp_c1_16695 | 42.42 |
| PotVar0027781 | 42.42 |
| PotVar0027766 | 42.42 |

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| solcap_snp_c1_10050 | 42.42 |
| :---: | :---: |
| PotVar0031913 | 42.42 |
| PotVar0031882 | 42.42 |
| PotVar0036535 | 42.42 |
| solcap_snp_c2_30296 | 42.42 |
| PotVar0036451 | 42.42 |
| PotVar0012999 | 42.52 |
| PotVar0012983 | 42.52 |
| PotVar0037640 | 43.44 |
| PotVar0037409 | 43.66 |
| PotVar0031836 | 44.28 |
| solcap_snp_c2_43152 | 45.7 |
| solcap_snp_c2_17613 | 46.55 |
| solcap_snp_c2_18788 | 47.65 |
| solcap_snp_c2_23308 | 48.74 |
| solcap_snp_c2_18816 | 48.74 |
| solcap_snp_c2_18836 | 49.33 |
| PotVar0109205 | 49.33 |
| solcap_snp_c2_18848 | 49.33 |
| PotVar0109143 | 50.22 |
| PotVar0109080 | 50.22 |
| PotVar0110871 | 51.13 |
| PotVar0110849 | 51.13 |
| PotVar0110868 | 51.64 |
| solcap_snp_c2_23284 | 53.6 |
| PotVar0110859 | 53.6 |
| PotVar0107187 | 53.6 |
| PotVar0110843 | 54 |
| solcap_snp_c1_11644 | 54.65 |
| PotVar0107214 | 54.65 |
| PotVar0107233 | 55.05 |
| PotVar0107181 | 55.15 |
| PotVar0107182 | 55.15 |


| PotVar0107202 | 55.15 |
| :---: | :---: |
| PotVar0104537 | 56.57 |
| solcap_snp_c2_32466 | 57 |
| solcap_snp_c2_48483 | 57.35 |
| PotVar0104542 | 58.49 |
| solcap_snp_c2_32467 | 58.49 |
| solcap_snp_c2_32519 | 58.49 |
| PotVar0107177 | 58.49 |
| PotVar0104553 | 58.49 |
| solcap_snp_c2_32082 | 60.02 |
| PotVar0104561 | 61.38 |
| solcap_snp_c2_6469 | 62.21 |
| PotVar0124993 | 62.25 |
| solcap_snp_c2_32482 | 62.25 |
| PotVar0124931 | 62.25 |
| solcap_snp_c1_2350 | 62.81 |
| solcap_snp_c2_32077 | 63.58 |
| solcap_snp_c2_6500 | 64.85 |
| solcap_snp_c2_6466 | 64.85 |
| PotVar0018635 | 66.17 |
| solcap_snp_c1_2366 | 66.85 |
| PotVar0018646 | 68.53 |
| PotVar0018524 | 68.69 |
| PotVar0018463 | 68.69 |
| PotVar0018476 | 68.84 |
| PotVar0018564 | 69.51 |
| PotVar0018569 | 69.52 |
| PotVar0018389 | 69.52 |
| PotVar0018377 | 69.52 |
| PotVar0018406 | 69.74 |
| PotVar0018214 | 69.8 |
| PotVar0018263 | 70.5 |
| PotVar0018140 | 70.67 |


| solcap_snp_c1_2689 | 71.4 |
| :---: | :---: |
| PotVar0018060 | 72.74 |
| solcap_snp_c2_7860 | 72.74 |
| PotVar0053309 | 72.76 |
| PotVar0018194 | 72.76 |
| PotVar0053463 | 72.98 |
| PotVar0053461 | 73.79 |
| PotVar0053387 | 73.79 |
| PotVar0052761 | 74.99 |
| solcap_snp_c1_13697 | 76.32 |
| PotVar0052987 | 76.32 |
| PotVar0052458 | 76.32 |
| PotVar0052776 | 76.32 |
| PotVar0052873 | 76.32 |
| solcap_snp_c2_5440 | 76.32 |
| solcap_snp_c2_5443 | 76.32 |
| PotVar0052756 | 77.2 |
| PotVar0052632 | 77.61 |
| PotVar0052628 | 77.61 |
| solcap_snp_c1_1954 | 78.3 |
| PotVar0052061 | 79.4 |
| solcap_snp_c1_1985 | 79.84 |
| PotVar0052399 | 80.15 |
| PotVar0052662 | 80.15 |
| solcap_snp_c2_5307 | 80.63 |
| PotVar0052083 | 80.97 |
| PotVar0052447 | 80.97 |
| PotVar0052284 | 81.03 |
| solcap_snp_c1_1944 | 81.31 |
| PotVar0052766 | 82.7 |
| PotVar0053344 | 83.13 |
| PotVar0053291 | 83.13 |

## Appendix 10: Updated physical positions in chromosome 3

In addition to the comparison the map positions with the physical positions, the physical positions themselves can be evaluated by such a comparison. In Programmes, Data and Assumptions, it was mentioned that during this thesis an updated version of the physical positions became available. In most cases this only involved an update of previously unknown physical positions, but one chromosome, chromosome 3, did undergo major revisions. In the region from 4 mbp to 5 mbp , the physical positions are inverted when the two versions are compared (Figure 32). This can be clearly seen in both parents while looking at the SxN markers. Although it appears that on three homologs the physical positions are in correspondence with the map positions, on one homolog this is not the case. It is therefore expected that the physical positions will likely change once again when a new update becomes available.


Figure 32. The comparison of the physical positions and $\operatorname{SxN}$ maps in the region of chromosome 3 where the physical positions were updated. In the region from 4 mbp to 5 mbp the physical positions were inverted.

# Appendix 11: Segregation distortion of markers on the integrated map 

According to literature, the self- incompatibility locus of potato is located on chromosome 1 (Gebhardt et al., 1991).The self- incompatibility caused skewed segregation in this region. To investigate if this is also true in this population, the skewedness of the markers on the integrated map were calculated. The SxN markers were tested for skewedness by using a Binomial test, while the other marker types were tested with a Chi-square test, with the null-hypothesis that markers followed the Mendelian segregation ratios (Table 1). From plotting the skewedness against the map positions and physical positions, the region of the self-incompatibility gene could not be found. It would be interesting to map the Segregation Distortion Loci (SDL) in a similar way as mapping a QTL (Vogl \& Xu, 2000), however both QTL and SDL mapping was beyond the scope of this thesis.

Figure 33, next page. Skewedness of the integrated chromosomes. The top left plot shows the $10 \log \mathrm{p}$-value for skewedness against the physical positions. The top right plot shows the $10 \log \mathrm{p}$-value for skewedness against the map positions. The bottom left plot shows the map positions against the physical positions. The bottom right shows a 3d plot of the three.





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Chromosome 9





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## Appendix 12: Summary r and LOD-estimators

Maximum likelihood (ML) is a statistical method for estimating parameters. By obtaining the maximum likelihood value, the estimate of the parameter will be good. To find the maximum likelihood, the likelihood function is differentiated and equated to zero. Since the log-likelihood is much easier to differentiate than the likelihood itself, this is in general done.

Here the exact ML-estimators of the recombination frequency for different marker segregation type combinations are given when this could be estimated by the maximum likelihood method (Table 20). Although many scientists have calculated the recombination frequencies of marker types, no paper has shown yet how they came to the ML estimator for the recombination frequency for the different marker segregation type pairs for tetraploids. Furthermore, the LOD-score, which is based on the likelihood ratio, is also given for those recombination frequency estimates. How the ML estimator and the LOD-score is obtained is explained in Figure 34 based on Van Ooijen \& Jansen (2013), after which the combinations of the marker segregation types follow.

Table 20. The maximum likelihood estimators or likelihood functions of the different marker type and phase combinations. The table is divided in two parts, following the exact analytical estimator and the iterative approach. The multinomial nominal coefficient and $1 / 2 \mathrm{~N}$ do not depend on r and are therefore abbreviated to MC and left out in equations. $x=$ dosage of marker $A ; y=$ dosage of maker $B ; \log =\log 10$.

| Exact approach |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Marker segregation type | Phase | Dosages | $n x y$ | ML estimator of ${ }^{\hat{r}}$ | LOD |
| Simplex x Nulliplex Simplex Nulliplex | Coupling | Aaaa x aaaa <br> Bbbb x bbbb | $\begin{aligned} & \mathrm{n} 10=1 / 2 \mathrm{r} \\ & \mathrm{n} 00=1 / 2(1-\mathrm{r}) \\ & \mathrm{n} 01=1 / 2 \mathrm{r} \\ & \mathrm{n} 11=1 / 2(1-\mathrm{r}) \end{aligned}$ | $\begin{aligned} & (\mathrm{n} 01+\mathrm{n} 10) / \\ & (\mathrm{n} 10+\mathrm{n} 01+\mathrm{n} 10+\mathrm{n} 11) \end{aligned}$ | $\begin{aligned} & \text { ntot*} \log (2 / n t o t)+(n 00+n 11) \log ( \\ & n 00+n 11)+(n 10+n 01) \log (n 10+n \\ & 01) \end{aligned}$ |
|  | Repulsion | Aaaa x aaaa bBbb x bbbb | $\begin{aligned} & \mathrm{n} 10=1 / 6+1 / 6(1-\mathrm{r}) \\ & \mathrm{n} 11=1 / 6+1 / 6 \mathrm{r} \\ & \mathrm{n} 01=1 / 6+1 / 6(1-\mathrm{r}) \\ & \mathrm{n} 00=1 / 6+1 / 6 \mathrm{r} \end{aligned}$ | $\begin{aligned} & (2(\mathrm{n} 00+\mathrm{n} 11)-(\mathrm{n} 10+\mathrm{n} 01)) / \\ & (\mathrm{n} 10+\mathrm{n} 01+\mathrm{n} 10+\mathrm{n} 11) \end{aligned}$ | $\begin{aligned} & \text { ntot*} \log (2 / \mathrm{ntot})+(\mathrm{n} 00+\mathrm{n} 11) \log ( \\ & \mathrm{n} 00+\mathrm{n} 11)+(\mathrm{n} 10+\mathrm{n} 01) \log (\mathrm{n} 10+\mathrm{n} \\ & 01) \end{aligned}$ |
|  | Repulsion under complete preferential pairing | Aaaa x aaaa bBbb x bbbb | $\begin{aligned} & \mathrm{n} 10=1 / 2(1-\mathrm{r}) \\ & \mathrm{n} 00=1 / 2 \mathrm{r} \\ & \mathrm{n} 01=1 / 2(1-\mathrm{r}) \\ & \mathrm{n} 11=1 / 2 \mathrm{r} \end{aligned}$ | $\begin{aligned} & (\mathrm{n} 11+\mathrm{n} 00) / \\ & (\mathrm{n} 10+\mathrm{n} 01+\mathrm{n} 10+\mathrm{n} 11) \end{aligned}$ | $\begin{aligned} & \text { ntot*} \log (2 / \mathrm{ntot})+(\mathrm{n} 00+\mathrm{n} 11) \log ( \\ & \mathrm{n} 00+\mathrm{n} 11)+(\mathrm{n} 10+\mathrm{n} 01) \log (\mathrm{n} 10+\mathrm{n} \\ & 01) \end{aligned}$ |
| Duplex x Nulliplex Simplex Nulliplex | Coupling | AAaa x aaaa Bbbb x bbbb | $\begin{aligned} & \mathrm{n} 10=1 / 6+1 / 6(1-\mathrm{r}) \\ & \mathrm{n} 11=1 / 6 \mathrm{r}+1 / 3 \\ & \mathrm{n} 21=1 / 6(1-\mathrm{r}) \\ & \mathrm{n} 00=1 / 6(1-\mathrm{r}) \\ & \mathrm{n} 20=1 / 3 \mathrm{r} \\ & \mathrm{n} 01=1 / 3 \mathrm{r} \end{aligned}$ | $\begin{aligned} & (\mathrm{n} 20+\mathrm{n} 01) / \\ & (\mathrm{n} 00+\mathrm{n} 21+\mathrm{n} 20+\mathrm{n} 01) \end{aligned}$ | $\begin{aligned} & (\mathrm{n} 00+\mathrm{n} 21+\mathrm{n} 20+\mathrm{n} 01) * \log (2)+(\mathrm{n} \\ & 00+\mathrm{n} 21) * \log (1- \\ & \mathrm{r})+(\mathrm{n} 20+\mathrm{n} 01) * \log (\mathrm{r}) \end{aligned}$ |

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|  | Repulsion | AAaa x aaaa bbBb x bbbb | $\begin{aligned} & \mathrm{n} 10=1 / 3 \\ & \mathrm{n} 11=1 / 3 \\ & \mathrm{n} 21=1 / 6 \mathrm{r} \\ & \mathrm{n} 00=1 / 6 \mathrm{r} \\ & \mathrm{n} 20=1 / 3 \\ & \mathrm{n} 01=1 / 6(1-\mathrm{r}) \end{aligned}$ | $\begin{aligned} & (\mathrm{n} 00+\mathrm{n} 21) / \\ & (\mathrm{n} 20+\mathrm{n} 01+\mathrm{n} 00+\mathrm{n} 21) \end{aligned}$ | $\begin{aligned} & (\mathrm{n} 00+\mathrm{n} 21+\mathrm{n} 20+\mathrm{n} 01) * \log (2)+(\mathrm{n} \\ & 00+\mathrm{n} 21) * \log (\mathrm{r})+(\mathrm{n} 20+\mathrm{n} 01) * \log \\ & (1-\mathrm{r}) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Simplex x Simplex Simplex Nulliplex | Coupling | Aaaa x Aaaa Bbbb x bbbb | $\begin{aligned} & \mathrm{n} 10=1 / 4 \\ & \mathrm{n} 00=1 / 4(1-\mathrm{r}) \\ & \mathrm{n} 01=1 / 4 \mathrm{r} \\ & \mathrm{n} 11=1 / 4 \\ & \mathrm{n} 21=1 / 4(1-\mathrm{r}) \\ & \mathrm{n} 20=1 / 4 \mathrm{r} \end{aligned}$ | $\begin{aligned} & (\mathrm{n} 01+\mathrm{n} 20) /(\mathrm{n} 21+\mathrm{n} 00+\mathrm{n} 01 \\ & +\mathrm{n} 20) \end{aligned}$ | $\begin{aligned} & (\mathrm{n} 21+\mathrm{n} 00+\mathrm{n} 01+\mathrm{n} 20) * \log (2 /(\mathrm{n} 2 \\ & 1+\mathrm{n} 00+\mathrm{n} 01+\mathrm{n} 20))+(\mathrm{n} 01+\mathrm{n} 20) * 1 \\ & \mathrm{og}(\mathrm{n} 01+\mathrm{n} 20)+ \\ & (\mathrm{n} 01+\mathrm{n} 20) * \log (\mathrm{n} 21+\mathrm{n} 00) \end{aligned}$ |
|  | Repulsion | Aaaa x Aaaa bBbb x bbbb | $\begin{aligned} & \mathrm{n} 10=1 / 4 \\ & \mathrm{n} 00=1 / 12+1 / 12 \mathrm{r} \\ & \mathrm{n} 01=1 / 12+1 / 12(1-\mathrm{r}) \\ & \mathrm{n} 11=1 / 4 \\ & \mathrm{n} 21=1 / 12+1 / 12 \mathrm{r} \\ & \mathrm{n} 20=1 / 12+1 / 12(1-\mathrm{r}) \end{aligned}$ | $\begin{aligned} & (2(\mathrm{n} 00+\mathrm{n} 21)-(\mathrm{n} 01+\mathrm{n} 20)) / \\ & (\mathrm{n} 01+\mathrm{n} 20+\mathrm{n} 00+\mathrm{n} 21) \end{aligned}$ | $\begin{aligned} & (\mathrm{n} 01+\mathrm{n} 20+\mathrm{n} 00+\mathrm{n} 21) * \log (2 /(\mathrm{n} 0 \\ & 1+\mathrm{n} 20+\mathrm{n} 00+\mathrm{n} 21))+(\mathrm{n} 01+\mathrm{n} 20) * 1 \\ & \mathrm{og}(\mathrm{n} 01+\mathrm{n} 20)+(\mathrm{n} 00+\mathrm{n} 21) * \log (\mathrm{n} \\ & 00+\mathrm{n} 21) \end{aligned}$ |
| Simplex x Triplex Simplex Nulliplex | Coupling | Aaaa x AAAa <br> Bbbb x bbbb | $\begin{aligned} & \mathrm{n} 31=1 / 4-1 / 4 \mathrm{r} \\ & \mathrm{n} 20=1 / 4 \\ & \mathrm{n} 30=1 / 4 \mathrm{r} \\ & \mathrm{n} 11=1 / 4 \mathrm{r} \\ & \mathrm{n} 21=1 / 4 \\ & \mathrm{n} 10=1 / 4-1 / 4 \mathrm{r} \end{aligned}$ | $\begin{aligned} & \mathrm{n} 30+\mathrm{n} 11 /(\mathrm{n} 30+\mathrm{n} 11+\mathrm{n} 31+ \\ & \mathrm{n} 10) \end{aligned}$ | $\begin{aligned} & \log ((1 / 4 *(\mathrm{n} 20+\mathrm{n} 11+\mathrm{n} 21+\mathrm{n} 10+\mathrm{n} \\ & 31+\mathrm{n} 30) *(1- \\ & \mathrm{r}) *(\mathrm{n} 11+\mathrm{n} 30) * \mathrm{r} *(\mathrm{n} 10+\mathrm{n} 31)) /(1 / \\ & 4 *(\mathrm{n} 20+\mathrm{n} 11+\mathrm{n} 21+\mathrm{n} 10+\mathrm{n} 31+\mathrm{n} 3 \\ & 0) *(1- \\ & 1 / 2) *(\mathrm{n} 11+\mathrm{n} 30) * 1 / 2 *(\mathrm{n} 10+\mathrm{n} 31) \\ & )) \end{aligned}$ |
|  | Repulsion | Aaaa x AAAa bBbb bbbb | $\begin{aligned} & \mathrm{n} 31=1 / 12+1 / 12 \mathrm{r} \\ & \mathrm{n} 20=1 / 4 \\ & \mathrm{n} 30=1 / 12+1 / 12 \mathrm{r} \\ & \mathrm{n} 21=1 / 4 \\ & \mathrm{n} 10=1 / 12+1 / 12 \mathrm{r} \\ & \mathrm{n} 11=1 / 6-1 / 12 \mathrm{r} \end{aligned}$ | $\begin{aligned} & \left(2^{*}(\mathrm{n} 10+\mathrm{n} 31)-\right. \\ & (\mathrm{n} 11+\mathrm{n} 30)) / \\ & (\mathrm{n} 11+\mathrm{n} 30+\mathrm{n} 10+\mathrm{n} 31) \end{aligned}$ | $\begin{aligned} & \log ((1 / 4 *(\mathrm{n} 21+\mathrm{n} 20) *(1 / 12+1 / 12 \\ & \left.{ }_{\mathrm{r}}\right) *(\mathrm{n} 10+\mathrm{n} 31) *(1 / 6- \\ & 1 / 12 * \mathrm{r}) *(\mathrm{n} 11+\mathrm{n} 30)) /(1 / 4 *(\mathrm{n} 21+ \\ & \mathrm{n} 20) *(1 / 12+1 / 12 * 1 / 2) *(\mathrm{n} 10+\mathrm{n} 3 \\ & 1) *(1 / 6-1 / 12 * 1 / 2) *(\mathrm{n} 11+\mathrm{n} 30)) \end{aligned}$ |
| Triplex x simplex Simplex x nulliplex | Coupling | AAAa x Aaaa <br> Bbbb x bbbb | $\begin{aligned} & \mathrm{n} 21=1 / 4 \\ & \mathrm{n} 10=1 / 6-1 / 12 \mathrm{r} \\ & \mathrm{n} 20=1 / 4 \\ & \mathrm{n} 11=1 / 12 \mathrm{r}+1 / 12 \\ & \mathrm{n} 31=1 / 6-1 / 12 \mathrm{r} \\ & \mathrm{n} 30=1 / 12 \mathrm{r}+1 / 12 \end{aligned}$ | $\begin{aligned} & \left(2^{*}(\mathrm{n} 10-\mathrm{n} 31)-\right. \\ & (\mathrm{n} 30+\mathrm{n} 11)) / \\ & (\mathrm{n} 10+\mathrm{n} 11+\mathrm{n} 31+\mathrm{n} 30) \end{aligned}$ | $\begin{aligned} & \log ((1 / 12 *(\mathrm{n} 21+\mathrm{n} 10+\mathrm{n} 20+\mathrm{n} 11+ \\ & \mathrm{n} 31+\mathrm{n} 30) *(2- \\ & \mathrm{r})^{*}(\mathrm{n} 31+\mathrm{n} 10)^{*}(1+\mathrm{r})^{*}(\mathrm{n} 11+\mathrm{n} 30) \\ & ) /(1 / 12 *(\mathrm{n} 21+\mathrm{n} 10+\mathrm{n} 20+\mathrm{n} 11+\mathrm{n} 3 \\ & 1+\mathrm{n} 30) *(2- \\ & 1 / 2)^{*}(\mathrm{n} 31+\mathrm{n} 10) *(1+1 / 2)^{*}(\mathrm{n} 11+ \\ & \mathrm{n} 30))) \end{aligned}$ |
|  | Repulsion | AAAa x Aaaa bbbB x bbbb | $\begin{aligned} & \mathrm{n} 20=1 / 4 \\ & \mathrm{n} 11=1 / 4-1 / 4 \mathrm{r} \\ & \mathrm{n} 21=1 / 4 \\ & \mathrm{n} 10=1 / 4 \mathrm{r} \\ & \mathrm{n} 31=1 / 4 \mathrm{r} \\ & \mathrm{n} 30=1 / 4-1 / 4 \mathrm{r} \end{aligned}$ | $\begin{aligned} & (\mathrm{n} 11+\mathrm{n} 30) /(\mathrm{n} 11+\mathrm{n} 30+\mathrm{n} 10 \\ & +\mathrm{n} 31) \end{aligned}$ | $\begin{aligned} & \log \left(\left(1 / 4^{(\mathrm{n} 20+\mathrm{n} 11+\mathrm{n} 21+\mathrm{n} 10+\mathrm{n} 31+\mathrm{n} 30)} *( \right.\right. \\ & 1-\mathrm{r})^{(\mathrm{n} 11+\mathrm{n} 30)} * \mathrm{r}^{(\mathrm{n} 10+\mathrm{n} 31)} \\ & ) /\left(1 / 4^{(\mathrm{n} 20+\mathrm{n} 11+\mathrm{n} 21+\mathrm{n} 10+\mathrm{n} 31+\mathrm{n} 30)} *(1-\right. \\ & \left.\mathrm{r})^{(\mathrm{n} 11+\mathrm{n} 30)} * \mathrm{r}^{(\mathrm{n} 10+\mathrm{n} 31)}\right) \end{aligned}$ |

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| Iterative approach |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Marker segregation type | Phase | Dosages | $n x y$ | Likelihood L(r) |
| Simplex x Simplex <br> Simplex Simplex | Coupling | Aaaa x Aaaa <br> Bbbb x Bbbb | $\begin{aligned} & \mathrm{n} 11=1 / 2 \mathrm{r} 2+1 / 2(1-\mathrm{r})^{2} \\ & \mathrm{n} 00=1 / 4(1-\mathrm{r})^{2} \\ & \mathrm{n} 01=1 / 2 \mathrm{r}(1-\mathrm{r}) \\ & \mathrm{n} 10=1 / 2 \mathrm{r}(1-\mathrm{r}) \\ & \mathrm{n} 21=1 / 2 \mathrm{r}(1-\mathrm{r}) \\ & \mathrm{n} 20=1 / 4 \mathrm{r}^{2} \\ & \mathrm{n} 22=1 / 4(1-\mathrm{r})^{2} \\ & \mathrm{n} 12=1 / 2 \mathrm{r}(1-\mathrm{r}) \\ & \mathrm{n} 02=1 / 4 \mathrm{r}^{2} \end{aligned}$ | $1 / 2^{(\mathrm{n} 11+\mathrm{n} 01+\mathrm{n} 10+\mathrm{n} 21+\mathrm{n} 12)} * 1 / 4^{\mathrm{n} 00+\mathrm{n} 20+\mathrm{n} 22+\mathrm{n} 02} *\left(\mathrm{r}^{2}\right)^{\mathrm{n} 02+\mathrm{n} 20} *((1-$ r) $\left.)^{2}\right)^{\mathrm{n} 00+\mathrm{n} 22} *(\mathrm{r} *(1-\mathrm{r}))^{\mathrm{n} 01+\mathrm{n} 10+\mathrm{n} 21+\mathrm{n} 12} *\left(\mathrm{r}^{2}+(1-\mathrm{r})^{2}\right)^{\mathrm{n} 11}$ |
|  | Mixed | Aaaa x Aaaa bBbb x Bbbb | $\begin{aligned} & \mathrm{n} 11=1 / 6+1 / 3 \mathrm{r}-1 / 3 \mathrm{r}^{2} \\ & \mathrm{n} 00=1 / 12\left(1-\mathrm{r}^{2}\right) \\ & \mathrm{n} 01=1 / 6-1 / 6 \mathrm{r}+1 / 6 \mathrm{r}^{2} \\ & \mathrm{n} 10=1 / 6-1 / 6 \mathrm{r}+1 / 6 \mathrm{r}^{2} \\ & \mathrm{n} 21=1 / 6-1 / 6 \mathrm{r}+1 / 6 \mathrm{r}^{2} \\ & \mathrm{n} 20=1 / 12\left(1-\mathrm{r}^{2}\right) \\ & \mathrm{n} 12=1 / 6-1 / 6 \mathrm{r}+1 / 6 \mathrm{r}^{2} \\ & \mathrm{n} 02=1 / 12 \mathrm{r}(2-\mathrm{r}) \end{aligned}$ | $1 / 12^{\mathrm{n00}} \mathrm{n}+\mathrm{nO1+n02+n10+n12+n10+n22*}\left(1-\mathrm{r}^{2}\right)^{\mathrm{n} 00+\mathrm{n} 22} *\left(2 \mathrm{r}^{2}-\right.$ $2 * \mathrm{r}+2)^{\mathrm{n} 01+\mathrm{n} 10+\mathrm{n} 21+\mathrm{n} 12} *\left(\mathrm{r}^{*}(2-\mathrm{r})\right)^{(\mathrm{n} 01+\mathrm{n} 20)} *\left(4 * r-4 * \mathrm{r}^{2}+2\right)^{\mathrm{n} 11}$ |
|  | Repulsion | Aaaa x Aaaa <br> bBbb x bBbb | $\begin{aligned} & \mathrm{n} 11=5 / 18-1 / 6 \mathrm{r}+1 / 9 \mathrm{r}^{2} \\ & \mathrm{n} 00=1 / 36+1 / 18 \mathrm{r}+1 / 36 \mathrm{r}^{2} \\ & \mathrm{n} 01=1 / 9+1 / 18 \mathrm{r}-1 / 18 \mathrm{r}^{2} \\ & \mathrm{n} 10=1 / 9+1 / 18 \mathrm{r}-1 / 18 \mathrm{r}^{2} \\ & \mathrm{n} 211 / 9+1 / 18 \mathrm{r}-1 / 18 \mathrm{r}^{2} \\ & \mathrm{n} 20=1 / 9-1 / 9 \mathrm{r}+1 / 36 \mathrm{r}^{2} \\ & \mathrm{n} 22)=1 / 36+1 / 18 \mathrm{r}+1 / 36 \mathrm{r}^{2} \\ & \mathrm{n} 12)=1 / 9+1 / 18 \mathrm{r}-1 / 18 \mathrm{r}^{2} \\ & \mathrm{n} 02=1 / 9-1 / 9 \mathrm{r}+1 / 36 \mathrm{r}^{2} \end{aligned}$ | $\begin{aligned} & \left(5 / 18-1 / 6 \mathrm{r}+1 / 9 \mathrm{r}^{2}\right)^{\mathrm{n} 11} *\left(1 / 36+1 / 18 \mathrm{r}+1 / 36 \mathrm{r}^{2}\right)^{(\mathrm{n} 00} \mathrm{+n22)} * \\ & \left(1 / 9+1 / 18 \mathrm{r}-1 / 18 \mathrm{r}^{2}\right)^{(\mathrm{n} 01+\mathrm{n} 10+\mathrm{n} 21+\mathrm{n} 12)} *\left(1 / 9-1 / 9 \mathrm{r}+1 / 36 \mathrm{r}^{2}\right)^{(\mathrm{n} 20+\mathrm{n} 02)} \end{aligned}$ |
| Duplex x Nulliplex <br> Duplex Nulliplex | Coupling | AAaa x aaaa BBbb x bbbb | $\begin{aligned} & \mathrm{n} 11=1 / 3+1 / 3(1-\mathrm{r})^{2}+1 / 3 \mathrm{r}^{2} \\ & \mathrm{n} 00=1 / 6(1-\mathrm{r})^{2} \\ & \mathrm{n} 01=1 / 3 \mathrm{r}(1-\mathrm{r}) \\ & \mathrm{n} 10=1 / 3 \mathrm{r}(1-\mathrm{r}) \\ & \mathrm{n} 21=1 / 3 \mathrm{r}(1-\mathrm{r}) \\ & \mathrm{n} 20=1 / 6 \mathrm{r}^{2} \\ & \mathrm{n} 22=1 / 6(1-\mathrm{r})^{2} \\ & \mathrm{n} 12=1 / 3 \mathrm{r}(1-\mathrm{r}) \\ & \mathrm{n} 02=1 / 6 \mathrm{r}^{2} \end{aligned}$ | $\left(1 / 3+1 / 3^{*}(1-r)^{2} * 1 / 3 r^{2}\right)^{n 11} *(1 / 6(1-$ <br> r) $)^{\mathrm{n} 22+\mathrm{n} 00} *\left(1 / 6 \mathrm{r}^{2}\right)^{\mathrm{n} 20+\mathrm{n} 02} *(1 / 3 \mathrm{r}(1-\mathrm{r}))^{\mathrm{n} 01+\mathrm{n} 10+\mathrm{n} 21+\mathrm{n} 12}$ |
|  | Repulsion | AAaa x aaaa bbBB x bbbb | $\begin{aligned} & \mathrm{n} 11=1 / 3+1 / 3 \mathrm{r} 2+1 / 3(1-\mathrm{r})^{2} \\ & \mathrm{n} 00=1 / 6 \mathrm{r}^{2} \\ & \mathrm{n} 01=1 / 3 \mathrm{r}(1-\mathrm{r}) \\ & \mathrm{n} 10=1 / 3 \mathrm{r}(1-\mathrm{r}) \\ & \mathrm{n} 21=1 / 3 \mathrm{r}(1-\mathrm{r}) \\ & \mathrm{n} 20=1 / 6(1-\mathrm{r})^{2} \\ & \mathrm{n} 22=1 / 6 \mathrm{r}^{2} \\ & \mathrm{n} 12=1 / 3 \mathrm{r}(1-\mathrm{r}) \\ & \mathrm{n} 02=1 / 6(1-\mathrm{r})^{2} \end{aligned}$ | $\left(1 / 3+1 / 3 *(1-r)^{2} * 1 / 3 r^{2}\right)^{n 11} *(1 / 6(1-$ <br> r) $\left.)^{2}\right)^{\mathrm{n} 20+\mathrm{n} 20}\left(\left(1 / 6 \mathrm{r}^{2}\right)^{\mathrm{n} 00+\mathrm{n} 22} * 1 / 3 \mathrm{r}(1-\mathrm{r})\right)^{\mathrm{n} 01+\mathrm{n} 10+\mathrm{n} 21+\mathrm{n} 12}$ |
|  | Mixed | AAaa x aaaa $\mathrm{BbBb} \times \mathrm{bbbb}$ | $\begin{aligned} & \hline \mathrm{n} 11=1 / 3+1 / 3(1-\mathrm{r}) \mathrm{r} \\ & \mathrm{n} 00=1 / 12 \mathrm{r}(1-\mathrm{r}) \end{aligned}$ | $\begin{aligned} & \left(1 / 3+1 / 3(1-\mathrm{r}) \mathrm{r}^{\mathrm{nII}} *(1 / 12 \mathrm{r}(1-\mathrm{r}))^{\mathrm{n} 20+\mathrm{n} 20+\mathrm{nOO}+\mathrm{n} 22} *(1 / 12+1 / 12(1-\right. \\ & \left.\mathrm{r})^{2}+1 / 12 \mathrm{r}^{2}\right)^{\mathrm{n} 01+\mathrm{n} 10+\mathrm{n} 21+\mathrm{n} 12} \end{aligned}$ |

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|  |  |  | $\begin{aligned} & \mathrm{n} 01=1 / 12+1 / 12(1-\mathrm{r})^{2}+1 / 12 \mathrm{r}^{2} \\ & \mathrm{n} 10=1 / 12+1 / 12(1-\mathrm{r})^{2}+1 / 12 \mathrm{r}^{2} \\ & \mathrm{n} 21=1 / 12+1 / 12(1-\mathrm{r})^{2}+1 / 12 \mathrm{r}^{2} \\ & \mathrm{n} 20=1 / 12 \mathrm{r}(1-\mathrm{r}) \\ & \mathrm{n} 22=1 / 12 \mathrm{r}(1-\mathrm{r}) \\ & \mathrm{n} 12=1 / 12+1 / 12(1-\mathrm{r})^{2}+1 / 12 \mathrm{r}^{2} \\ & \mathrm{n} 02=1 / 12 \mathrm{r}(1-\mathrm{r}) \end{aligned}$ |  |
| :---: | :---: | :---: | :---: | :---: |
| Duplex x Nulliplex <br> Simplex x Simplex | Coupling | AAaa x aaaa <br> Bbbb x Bbbb | $\begin{aligned} & \hline \mathrm{n} 11=1 / 3 \\ & \mathrm{n} 00=1 / 12-1 / 12 \mathrm{r} \\ & \mathrm{n} 01=1 / 12 \\ & \mathrm{n} 10=1 / 6 \\ & \mathrm{n} 21=1 / 12 \\ & \mathrm{n} 20=1 / 12 \mathrm{r} \\ & \mathrm{n} 12=1 / 6 \\ & \mathrm{n} 02=1 / 12 \mathrm{r} \\ & \mathrm{n} 22=1 / 12-1 / 12 \mathrm{r} \end{aligned}$ | $1 / 3^{\mathrm{nI1}} * 1 / 12^{\mathrm{n00}+\mathrm{no1} 1+\mathrm{n} 10+n 21+\mathrm{n} 20+\mathrm{n} 12+\mathrm{n} 02+\mathrm{n} 22} * 2^{\mathrm{n} 10+\mathrm{n} 12} *(1-$ <br> r) ${ }^{\mathrm{n} 0+\mathrm{n} 22} *_{\mathrm{r}}^{\mathrm{n} 20+\mathrm{n} 02}$ |
|  | Repulsion | AAaa x aaaa bbBb x Bbbb | $\begin{aligned} & \mathrm{n} 11=1 / 3 \\ & \mathrm{n} 00=1 / 12 \mathrm{r} \\ & \mathrm{n} 01=1 / 12 \\ & \mathrm{n} 10=1 / 6 \\ & \mathrm{n} 21=1 / 12 \\ & \mathrm{n} 20=1 / 12-1 / 12 \mathrm{r} \\ & \mathrm{n} 12=1 / 6 \\ & \mathrm{n} 02=1 / 12-1 / 12 \mathrm{r} \\ & \mathrm{n} 22=1 / 12 \mathrm{r} \end{aligned}$ | $\begin{aligned} & \mathrm{MC}^{*} 1 / 12^{\left(\mathrm{n000+n01+n10+n21+n20+n12+n02+n22} * 1 / 3^{\mathrm{nIT}} * \mathrm{r}^{(\mathrm{nn00+n22)}} * 2^{(\mathrm{nl0+}}\right.} \\ & \mathrm{n} 12) *(1-\mathrm{r})^{(\mathrm{n} 20+\mathrm{n} 02)} \end{aligned}$ |
| Simplex x Triplex <br> Duplex x Nulliplex | Coupling | Aaaa x AAAa <br> BBbb x bbbb | $\begin{aligned} & \hline \mathrm{n} 31=1 / 6 \\ & \mathrm{n} 21=1 / 3 \\ & \mathrm{n} 11=1 / 6 \\ & \mathrm{n} 32=1 / 12-1 / 12 \mathrm{r} \\ & \mathrm{n} 22=1 / 12 \\ & \mathrm{n} 12=1 / 12 \mathrm{r} \\ & \mathrm{n} 20=1 / 12 \\ & \mathrm{n} 10=1 / 12-1 / 12 \mathrm{r} \\ & \mathrm{n} 30=1 / 12 \mathrm{r} \end{aligned}$ | $\begin{aligned} & \left(1 / 12 * r^{(\mathrm{n} 30+\mathrm{n} 12)} *(1 / 6)^{(\mathrm{n} 31+\mathrm{n} 22+\mathrm{n} 20+\mathrm{nII})} *(1 / 12-\right. \\ & 1 / 12 * \mathrm{r})^{(\mathrm{n} 32+\mathrm{n} 10)} *(1 / 3)^{\mathrm{n} 21} \end{aligned}$ |
|  | Repulsion | Aaaa x AAAa <br> bBBb x bbbb | $\begin{aligned} & \mathrm{n} 31=1 / 6 \\ & \mathrm{n} 21=1 / 3 \\ & \mathrm{n} 11=1 / 6 \\ & \mathrm{n} 32=1 / 12 \mathrm{r} \\ & \mathrm{n} 22=1 / 12 \\ & \mathrm{n} 12=1 / 12-1 / 12 * \mathrm{r} \\ & \mathrm{n} 20=1 / 12 \\ & \mathrm{n} 10=1 / 12 * \mathrm{r} \\ & \mathrm{n} 30=1 / 12-1 / 12 * \mathrm{r} \end{aligned}$ | $\begin{aligned} & (1 / 12-1 / 12 * \mathrm{r})^{(\mathrm{n} 30+\mathrm{n} 12)} * 1 / 6^{(\mathrm{n} 31+\mathrm{n} 22+\mathrm{n} 20+\mathrm{n} 11)} * \\ & (1 / 12 * \mathrm{r})^{(\mathrm{n} 32+\mathrm{n} 10)} * 1 / 3^{\mathrm{n} 21} \end{aligned}$ |
| Simplex x Triplex <br> Simplex x Simplex | Coupling | Aaaa x AAAa <br> Bbbb Bbbb | $\begin{aligned} & \mathrm{n} 32=1 / 6-1 / 4 \mathrm{r}+1 / 12 \mathrm{r}^{2} \\ & \mathrm{n} 22=1 / 12+1 / 6 \mathrm{r}-1 / 6 \mathrm{r}^{2} \end{aligned}$ | $\left(1 / 12 * \mathrm{r}+1 / 12{ }^{*} \mathrm{r}^{2}\right)^{(\mathrm{n} 30+\mathrm{n} 2)} *\left(1 / 12+1 / 6 * \mathrm{r}-1 / 6 * \mathrm{r}^{2}\right)$ ${ }^{(\mathrm{n} 31+\mathrm{n} 22+\mathrm{n} 20+\mathrm{nl1})} *\left(1 / 6-1 / 4 * \mathrm{r}+1 / 12 *{ }^{2}\right)^{2} \mathrm{n}^{(\mathrm{n} 2+\mathrm{n} 10)} *(1 / 3-$ |

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|  |  | bBbb x BBbB | $\begin{aligned} & \mathrm{n} 22=5 / 18-1 / 9 \mathrm{r}+1 / 9 \mathrm{r}^{2} \\ & \mathrm{n} 11=1 / 36+1 / 18 \mathrm{r}+1 / 36 \mathrm{r}^{2} \\ & \mathrm{n} 31=1 / 9-1 / 9 \mathrm{r}+1 / 36 \mathrm{r}^{2} \\ & \mathrm{n} 13=1 / 9-1 / 9 \mathrm{r}+1 / 36 \mathrm{r}^{2} \\ & \mathrm{n} 32=1 / 9+1 / 18 \mathrm{r}-1 / 18 \mathrm{r}^{2} \\ & \mathrm{n} 21=1 / 9+1 / 18 \mathrm{r}-1 / 18 \mathrm{r}^{2} \\ & \mathrm{n} 23=1 / 9+1 / 18 \mathrm{r}-1 / 18 \mathrm{r}^{2} \\ & \mathrm{n} 12=1 / 9+1 / 18 \mathrm{r}-1 / 18 \mathrm{r}^{2} \end{aligned}$ | $\begin{aligned} & \left.1 / 18 * \mathrm{r}^{2}\right)^{(\mathrm{n} 23+\mathrm{n} 32+\mathrm{n} 12+\mathrm{n} 21)} *\left(1 / 36+1 / 18 * \mathrm{r}+1 / 36 * \mathrm{r}^{2}\right)^{(\mathrm{n} 33+\mathrm{nII})} *(5 / 18 \\ & \left.-1 / 9 * \mathrm{r}+1 / 9 * \mathrm{r}^{2}\right)^{\mathrm{n} 22} \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: |
|  | Mixed 1 | Aaaa x AAAa <br> bBbb x BBBb | $\begin{aligned} & \mathrm{n} 33=1 / 12-1 / 12 \mathrm{r}^{2} \\ & \mathrm{n} 22=1 / 6+1 / 3 \mathrm{r}-1 / 3 \mathrm{r}^{2} \\ & \mathrm{n} 11=1 / 12-1 / 12 \mathrm{r}^{2} \\ & \mathrm{n} 31=1 / 6 \mathrm{r}-1 / 12 \mathrm{r}^{2} \\ & \mathrm{n} 13=1 / 6 \mathrm{r}-1 / 12 \mathrm{r}^{2} \\ & \mathrm{n} 32=1 / 6-1 / 6 \mathrm{r}+1 / 6 \mathrm{r}^{2} \\ & \mathrm{n} 21=1 / 6-1 / 6 \mathrm{r}+1 / 6 \mathrm{r}^{2} \\ & \mathrm{n} 23=1 / 6-1 / 6 \mathrm{r}+1 / 6 \mathrm{r}^{2} \\ & \mathrm{n} 12=1 / 6-1 / 6 \mathrm{r}+1 / 6 \mathrm{r}^{2} \end{aligned}$ | $\begin{aligned} & \left(1 / 6 * \mathrm{r}-1 / 12 * \mathrm{r}^{2}\right)^{(\mathrm{n} 13+\mathrm{n} 31)} *(1 / 6- \\ & \left.1 / 6 * \mathrm{r}+1 / 6 * \mathrm{r}^{2}\right)^{(\mathrm{n} 23+\mathrm{n} 32+\mathrm{n} 12+\mathrm{n} 21)} *(1 / 12- \\ & \left.1 / 12 * \mathrm{r}^{2}\right)^{(\mathrm{n} 33+\mathrm{n} 11)} *\left(1 / 6+1 / 3 * \mathrm{r}-1 / 3 * \mathrm{r}^{2}\right)^{\mathrm{n} 22} \end{aligned}$ |
|  | Mixed 2 | Aaaa x AAAa <br> Bbbb x BBbB | $\begin{aligned} & \mathrm{n} 33=1 / 12-1 / 12 \mathrm{r}^{2} \\ & \mathrm{n} 22=1 / 6+1 / 3 \mathrm{r}-1 / 3 \mathrm{r}^{2} \\ & \mathrm{n} 11=1 / 12-1 / 12 \mathrm{r}^{2} \\ & \mathrm{n} 31=1 / 6 \mathrm{r}-1 / 12 \mathrm{r}^{2} \\ & \mathrm{n} 13=1 / 6 \mathrm{r}-1 / 12 \mathrm{r}^{2} \\ & \mathrm{n} 32=1 / 6-1 / 6 \mathrm{r}+1 / 6 \mathrm{r}^{2} \\ & \mathrm{n} 21=1 / 6-1 / 6 \mathrm{r}+1 / 6 \mathrm{r}^{2} \\ & \mathrm{n} 23=1 / 6-1 / 6 \mathrm{r}+1 / 6 \mathrm{r}^{2} \\ & \mathrm{n} 12=1 / 6-1 / 6 \mathrm{r}+1 / 6 \mathrm{r}^{2} \end{aligned}$ | $\begin{aligned} & \left(1 / 6 * \mathrm{r}-1 / 12 * \mathrm{r}^{2}\right)^{(\mathrm{n} 13+\mathrm{n} 31)} *(1 / 6- \\ & \left.1 / 6 * \mathrm{r}+1 / 6 * \mathrm{r}^{2}\right)^{(\mathrm{n} 23+\mathrm{n} 32+\mathrm{n} 12+\mathrm{n} 21)} *(1 / 12- \\ & \left.1 / 12 * \mathrm{r}^{2}\right)^{(\mathrm{n} 33+\mathrm{n} 11)} *\left(1 / 6+1 / 3 * \mathrm{r}-1 / 3 *{ }^{2}\right)^{\mathrm{n} 22} \end{aligned}$ |



Figure 34. Procedure of calculating the recombination frequencies of the different marker type and phase combinations. This procedure is described in more detail in (Van Ooijen \& Jansen, 2013).

## Appendix 13: Map comparison with other populations and Solanum species

In Chapter 7 and the Discussion, the integrated map was compared with maps of other potato populations and Solanum species. The statistics of some of those maps and mapping population are shown here (Table 21).

Table 21. Map statistics of different potato and Solanum maps. The maps vary in the population size used.
The map statistics include the number of markers, map length per chromosome, coverage, and number of markers with a specific marker type.

| Potatoes |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Thesis |  |  |  |  |  |  |  |  |
| Chromosome | N markers | cM | Coverage <br> N/cM | Coverage N/MB | SN | DN | SS | TS |
| 1 | 624 | 141.7 | 4.403669725 | 9.984 | 338 | 95 | 129 | 62 |
| 2 | 544 | 118.9 | 4.575273339 | 12.65116279 | 359 | 46 | 118 | 21 |
| 3 | 459 | 125.57 | 3.655331688 | 18 | 262 | 95 | 65 | 37 |
| 4 | 478 | 151.26 | 3.160121645 | 9.192307692 | 267 | 74 | 103 | 34 |
| 5 | 545 | 101.75 | 5.356265356 | 15.13888889 | 353 | 93 | 55 | 44 |
| 6 | 352 | 121.2 | 2.904290429 | 8.8 | 219 | 45 | 78 | 10 |
| 7 | 447 | 94.78 | 4.716184849 | 14.19047619 | 227 | 93 | 91 | 36 |
| 8 | 450 | 102.85 | 4.375303841 | 16.36363636 | 228 | 46 | 78 | 38 |
| 9 | 369 | 119.06 | 3.099277675 | 12.09836066 | 197 | 72 | 72 | 28 |
| 10 | 213 | 109.83 | 1.93936083 | 5.195121951 | 110 | 48 | 38 | 17 |
| 11 | 396 | 136.1 | 2.909625276 | 12.375 | 229 | 57 | 66 | 44 |
| 12 | 288 | 83.13 | 3.464453266 | 7.384615385 | 165 | 64 | 39 | 20 |
| Total (sum or average) | 5165 | 1406.13 | 3.71326316 | 11.78113083 | 2954 | 828 | 932 | 391 |
| Tetraploid potato (Hackett et al., 2013) |  |  |  |  |  |  |  |  |
| Chromosome | N markers | cM | Coverage <br> N/cM | Coverage <br> N/MB | SN | DN | SS | TS |
| 1 | 142 | 115.3 | 1.231569818 | 2.272 | 43 |  |  |  |
| 2 | 120 | 91.9 | 1.305767138 | 2.790697674 | 27 |  |  |  |
| 3 | 74 | 91.5 | 0.808743169 | 2.901960784 | 29 |  |  |  |
| 4 | 152 | 95.8 | 1.586638831 | 2.923076923 | 46 |  |  |  |
| 5 | 119 | 73.1 | 1.627906977 | 3.305555556 | 34 |  |  |  |
| 6 | 122 | 90.8 | 1.343612335 | 3.05 | 32 |  |  |  |
| 7 | 89 | 90 | 0.9888888889 | 2.825396825 | 47 |  |  |  |
| 8 | 85 | 62.3 | 1.364365971 | 3.090909091 | 22 |  |  |  |
| 9 | 91 | 121.6 | 0.748355263 | 2.983606557 | 37 |  |  |  |


| 10 | 104 | 71.9 | 1.446453408 | 2.536585366 | 26 |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 11 | 85 | 96.2 | 0.883575884 | 2.65625 | 35 |  |  |  |
| 12 | 118 | 87.1 | 1.354764638 | 3.025641026 | 32 |  |  |  |
| Total | 1301 | 1087.5 | 1.224220193 | 2.863473317 | 410 |  |  |  |

Diploid potato (Prashar et al., 2014)

| Chromosome | N markers | cM | Coverage N/cM | Coverage N/MB | SN | DN | SS | TS |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 170 | 85.4 | 1.990632319 | 2.72 |  |  |  |  |
| 2 | 119 | 52.9 | 2.24952741 | 2.76744186 |  |  |  |  |
| 3 | 120 | 66.9 | 1.793721973 | 4.705882353 |  |  |  |  |
| 4 | 151 | 69.2 | 2.182080925 | 2.903846154 |  |  |  |  |
| 5 | 77 | 58.4 | 1.318493151 | 2.138888889 |  |  |  |  |
| 6 | 91 | 55.6 | 1.636690647 | 2.275 |  |  |  |  |
| 7 | 157 | 64.3 | 2.441679627 | 4.984126984 |  |  |  |  |
| 8 | 111 | 53.4 | 2.078651685 | 4.036363636 |  |  |  |  |
| 9 | 115 | 67.5 | 1.703703704 | 3.770491803 |  |  |  |  |
| 10 | 78 | 57 | 1.368421053 | 1.902439024 |  |  |  |  |
| 11 | 106 | 59.8 | 1.772575251 | 3.3125 |  |  |  |  |
| 12 | 60 | 63.4 | 0.94637224 | 1.538461538 |  |  |  |  |
| Total | 1355 | 753.8 | 1.790212499 | 3.08795352 |  |  |  |  |

Other Solanum species
Tomato (EXPEN2000 population of a S. lycopersicum $x$ S. pennellii cross) (Sim et al., 2012)

| Chromosome | N markers | cM | Coverage N/cM | Coverage <br> N/MB | SN | DN | SS | TS |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 252 | 201.8 | 1.24876115 | 2.795961389 |  |  |  |  |
| 2 | 416 | 165.5 | 2.513595166 | 8.407437348 |  |  |  |  |
| 3 | 286 | 121.7 | 2.350041085 | 4.420401855 |  |  |  |  |
| 4 | 385 | 159.5 | 2.413793103 | 6.014685205 |  |  |  |  |
| 5 | 363 | 154.3 | 2.352559948 | 5.59235865 |  |  |  |  |
| 6 | 374 | 111.3 | 3.360287511 | 8.151700087 |  |  |  |  |
| 7 | 224 | 108.2 | 2.070240296 | 3.447214528 |  |  |  |  |
| 8 | 289 | 124.4 | 2.323151125 | 4.589487057 |  |  |  |  |
| 9 | 218 | 144.2 | 1.511789182 | 3.220088626 |  |  |  |  |
| 10 | 167 | 122.8 | 1.359934853 | 2.579548965 |  |  |  |  |
| 11 | 466 | 114.4 | 4.073426573 | 8.746246246 |  |  |  |  |
| 12 | 163 | 141.9 | 1.148696265 | 2.476450927 |  |  |  |  |
| Total | 3603 | 1670 | 2.227189688 | 5.036798407 |  |  |  |  |
| Eggplant (Gramazio et al., 2014) |  |  |  |  |  |  |  |  |
| Chromosome | N | cM | Coverage | Coverage | SN | DN | SS | TS |

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|  | markers |  | N/cM | N/MB |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 23 | 132.9 | 0.173062453 |  |  |  |  |  |
| 2 | 18 | 78.7 | 0.228716645 |  |  |  |  |  |
| 3 | 21 | 94.3 | 0.222693531 |  |  |  |  |  |
| 4 | 16 | 76 | 0.210526316 |  |  |  |  |  |
| 5 | 18 | 58.6 | 0.307167235 |  |  |  |  |  |
| 6 | 27 | 111.9 | 0.241286863 |  |  |  |  |  |
| 7 | 21 | 101.7 | 0.206489676 |  |  |  |  |  |
| 8 | 20 | 78.3 | 0.255427842 |  |  |  |  |  |
| 9 | 22 | 96.1 | 0.2289282 |  |  |  |  |  |
| 10 | 19 | 96.7 | 0.196483971 |  |  |  |  |  |
| 11 | 19 | 79.7 | 0.238393977 |  |  |  |  |  |
| 12 | 19 | 80.1 | 0.237203496 |  |  |  |  |  |
| Total | 243 | 1085 | 0.228865017 |  |  |  |  |  |
| Solanum bulbocastanum (Iorizzo et al., 2014) |  |  |  |  |  |  |  |  |
| Chromosome | N markers | cM | Coverage N/cM | Coverage <br> N/MB | SN | DN | SS | TS |
| 1 | 49 | 49.1 | 0.99796334 |  |  |  |  |  |
| 2 | 53 | 48.3 | 1.097308489 |  |  |  |  |  |
| 3 | 49 | 36.5 | 1.342465753 |  |  |  |  |  |
| 4 | 67 | 83.7 | 0.800477897 |  |  |  |  |  |
| 5 | 20 | 40.7 | 0.491400491 |  |  |  |  |  |
| 6 | 40 | 45.6 | 0.877192982 |  |  |  |  |  |
| 7 | 30 | 58.4 | 0.51369863 |  |  |  |  |  |
| 8 | 19 | 51.4 | 0.369649805 |  |  |  |  |  |
| 9 | 25 | 60.4 | 0.413907285 |  |  |  |  |  |
| 10 | 9 | 61.5 | 0.146341463 |  |  |  |  |  |
| 11 | 22 | 40.2 | 0.547263682 |  |  |  |  |  |
| 12 | 26 | 69.1 | 0.376266281 |  |  |  |  |  |
| Total | 409 | 644.9 | 0.664494675 |  |  |  |  |  |

## Appendix 14: Map integration of two rose populations

A mapping population of rose was used to validate the integration procedure described in Chapter 7. Two maps (maternal and paternal) of one chromosome were used for integration. The maps were first put in right orientation based on the Pearson correlation of the common markers. Thereafter, the maps were integrated twice. The first time, the maternal map had a mapping error since one of the chromosome arms was inverted (Figure 35), while the second time, the maps had no structural errors (Figure 36). In the latter, the integration went well, while the integration with an inverted arm went not well.


Figure 35. Integration of the maternal map (Map 2) with an inverted arm and the paternal map (Map 1). The top left plot shows the map positions of the common markers. The top left plot shows the integrated map distances based on the two underlying maps. The bottom right plot shows the comparison of map positions between the paternal map and the integrated map. The bottom middle plot shows the comparison of map positions between the maternal map and the integrated map. The bottom right plot shows the comparison of the map position of the common markers.


Figure 36. Integration of the maternal map (Map 2) with the correct ordering and the paternal map (Map
1). The top left plot shows the map positions of the common markers. The top left plot shows the integrated map distances based on the two underlying maps. The bottom right plot shows the comparison of map positions between the paternal map and the integrated map. The bottom middle plot shows the comparison of map positions between the maternal map and the integrated map. The bottom right plot shows the comparison of the map position of the common markers.

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## Appendix 15: Alstroemeria

During this thesis, the method for the determination of the mode of inheritance and calculation of recombination frequencies of SxN markers was used for an Alstroemeria population. First, the recombination frequencies were calculated under the assumption of tetrasomic inheritance (Figure 37). However, the coupling and repulsion phase were too much overlapping for linkage group assignment. Therefore, only SxN markers with less than 5\% missing values were used (Figure 38). In addition, the recombination frequency calculation allowing for preferential pairing was also calculated (Figure 39). What the effect of preferential pairing is on the linkage group and homolog assignment is currently not known.


Figure 37. Recombination frequencies plotted against the LOD-score for SxN markers of Alstroemeria. All SxN markers were used.


Figure 38. Recombination frequencies plotted against the LOD-score for SxN markers of Alstroemeria. Only SxN markers with less than $5 \%$ missing values were used. This already gave a clear distinction between Coupling and Repulsion phase.


Figure 39. Recombination frequencies plotted against the LOD-score for SxN markers of Alstroemeria.
Only SxN markers with less than 5\% missing values were used. The recombination frequency calculation also allowed for repulsion phase under preferential pairing. There were $S x N$ markers that tested positively for preferential pairing, which could indicate preferential pairing on one or more of the chromosomes.

## Appendix 16: Integrated map against homolog maps

In Chapter 7, all the homologs were integrated into one consensus map per chromosome. In this chapter the map positions of the markers on the homolog maps of chromosome 11 were plotted against the map positions of markers on the integrated chromosome. In Figure 40 this was done for all chromosomes.

Figure 40. Comparison of the map positions of the markers on the homolog maps with the map positions on the integrated map for all the chromosomes. The homolog maps per parent are shown. The homolog maps are the maps used for the integration procedure.


Chromosome 2


Chromosome 3



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Chromosome 6


Chromosome 7


## Chromosome 8



Chromosome 9

> P1 Homolog 1
> P1 Homolog 3


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| Chromosome 12 <br> P1 Homolog 1 | P1 Homolog 3 | P2 Homolog 1 | P2 Homolog 3 |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
| P1 Homolog 2 | P1 Homolog 4 | P2 Homolog 2 | P2 Homolog 4 |
|  |  |  |  |

## Appendix 17: Gaps

In Chapter 7, the homolog maps were integrated into one integrated map per chromosome. Table 11 showed the number of gaps on the integrated linkage maps. Here, some plots are presented to further investigate the distribution and the size of the gaps. Figure 41 shows that every chromosome contains gaps of different sizes. Gap sizes of a length of 1 cM are most abundant as is expected, while larger gaps are less often present. Figure 42 shows that the gaps are randomly distributed over the integrated linkage maps. This shows that all chromosomal regions are equally well represented by markers.

Chromosome 1


Chromosome 2


Chromosome 3


Chromosome 4


Chromosome 5


Chromosome 6


Chromosome 7


Chromosome 8


Chromosome 9


Chromosome 10


Chromosome 11


Chromosome 12


Figure 41. The frequency of gap size per integrated map. The 12 integrated maps all contain gaps of different sizes.


Figure 42. The distribution of gaps on the integrated linkage maps. The gap size in cM is plotted against the starting position of the gap in cM for all the 12 integrated chromosomes.


[^0]:    * Two clustering methods are compared with the Rand Index, a is the number of pairs that ended up in the same cluster by both clustering methods, b is the number of pairs that ended up in different clusters by both clustering methods, c is the number of pairs that are in the same clusters by the first clustering method but are in different clusters by the second clustering method, d is the number of pairs that are in different clusters by the first clustering method but are in the same clusters by the second clustering method.

[^1]:    * $\mathrm{L}(\mathrm{r})$ is the likelihood of $\mathrm{r}, \mathrm{r} 1$ is the estimate of the recombination frequency of two DxN markers in coupling phase, r 2 is the estimate of the recombination frequency of two DxN markers in repulsion phase, r3 is the estimate of the recombination frequency of two DxN markers in mixed phase, n01 is the number of markers that have genotype aaaa and Bbbb, n10 is the number of markers that have genotype Aaaa and bbbb, n00 is the number of markers that have genotype aaaa and bbbb, n 11 is the number of markers that have genotype Aaaa and Bbbb, the A's (for example Aaaa) and B's (for example Bbbb) are not position dependent.

[^2]:    * LOD is the logarithm of odds ratio, rl is the estimate of the recombination frequency of a SxT marker and a SxN marker in coupling phase, r 2 is the estimate of the recombination frequency of SxT marker and a SxN marker in repulsion phase, n 11 is the number of markers that have genotype Aaaa and Bbbb, $n 30$ is the number of markers that have genotype AAAa and bbbb, n10 is the number of markers that have genotype Aaaa and bbbb, n31 is the number of markers that have genotype AAAa and Bbbb, the A's (for example Aaaa) and B's (for example Bbbb) are not position dependent.

[^3]:    *With $\mathrm{d}_{\mathrm{xy}}$ being the observed distance (based on recombination frequency) between marker x and marker $\mathrm{y}, \delta_{\mathrm{xy}}$ being the expected distance between marker x and y based on the model and $\mathrm{e}_{\mathrm{xy}}$ the error corresponding to the distance between marker x and y

[^4]:    bp

